Electromagnetic Calorimeter Software for Super Tau-Charm Facility

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超级陶粲装置研讨会

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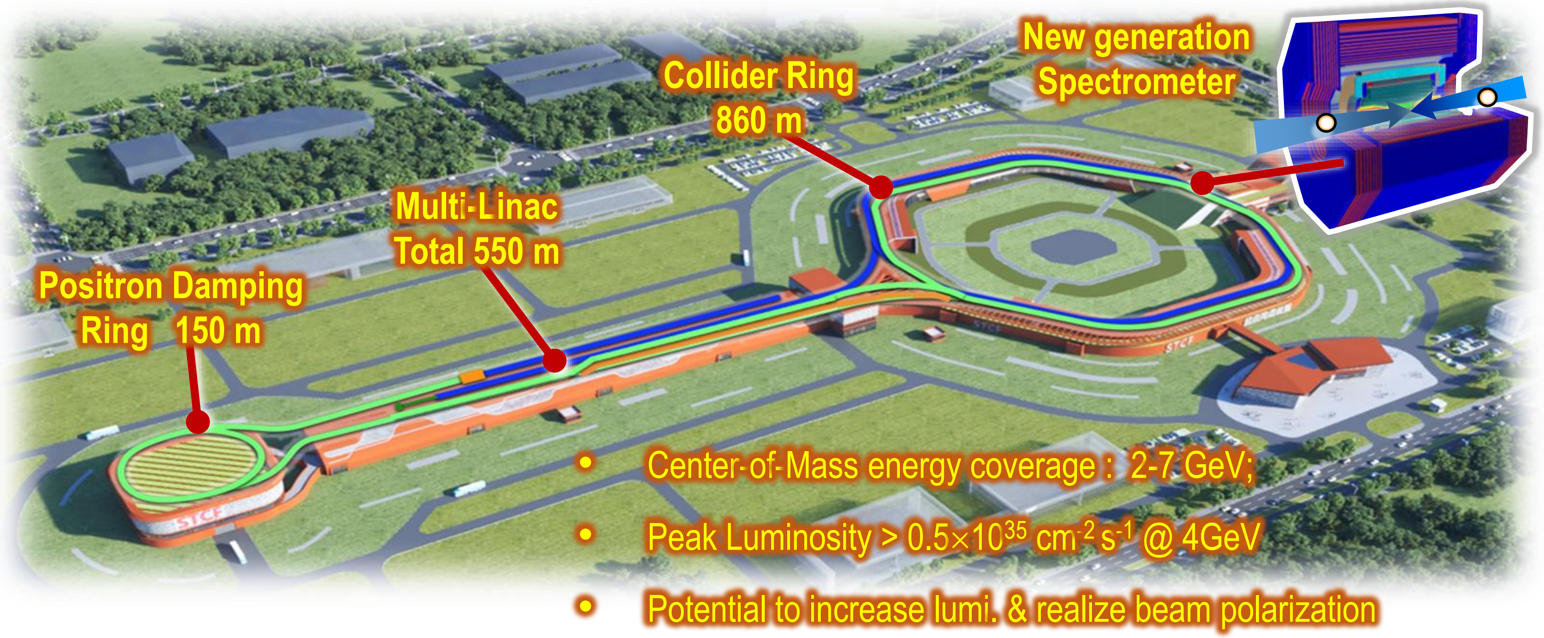
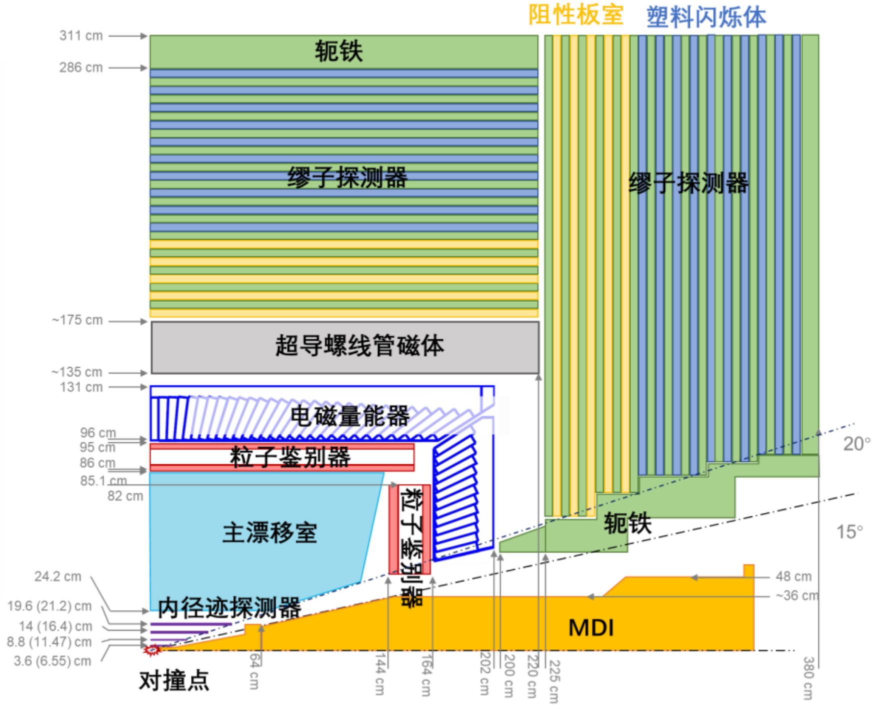
Super Tau-Charm Facility

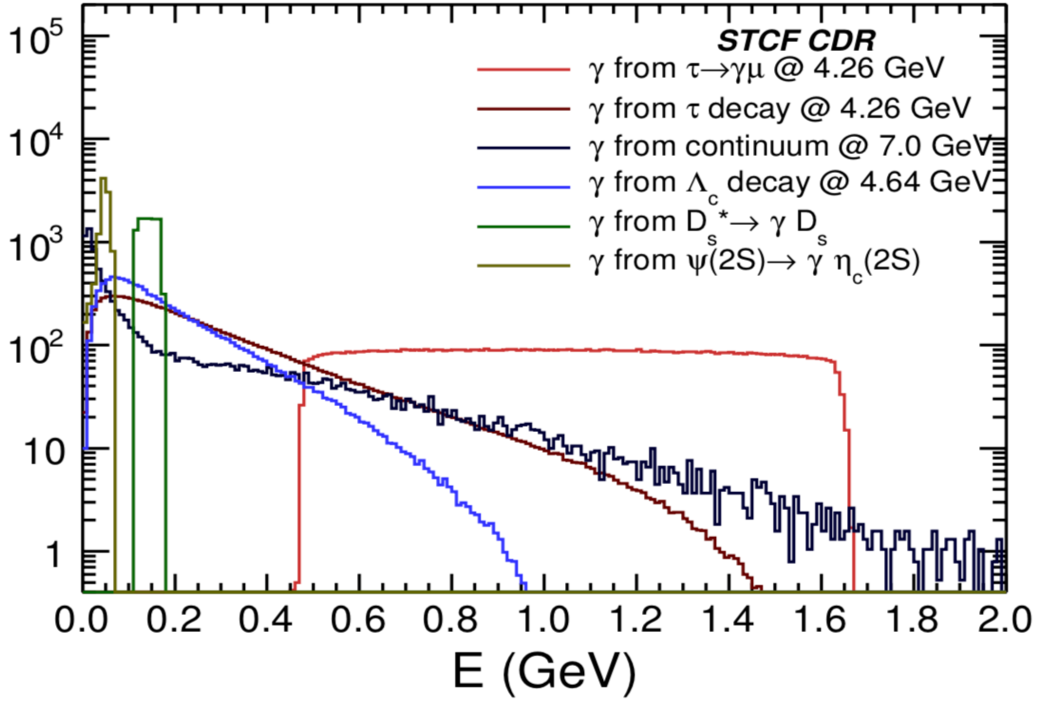
- Electron-positron collider experiment
- High luminosity： beyond $0.5 \times 10^{35}\ cm^{-2} \cdot s^{-1}$ @ 4GeV
- Wide energy region： center-of-mass energy range of 2~7 GeV





Requirements for ECAL

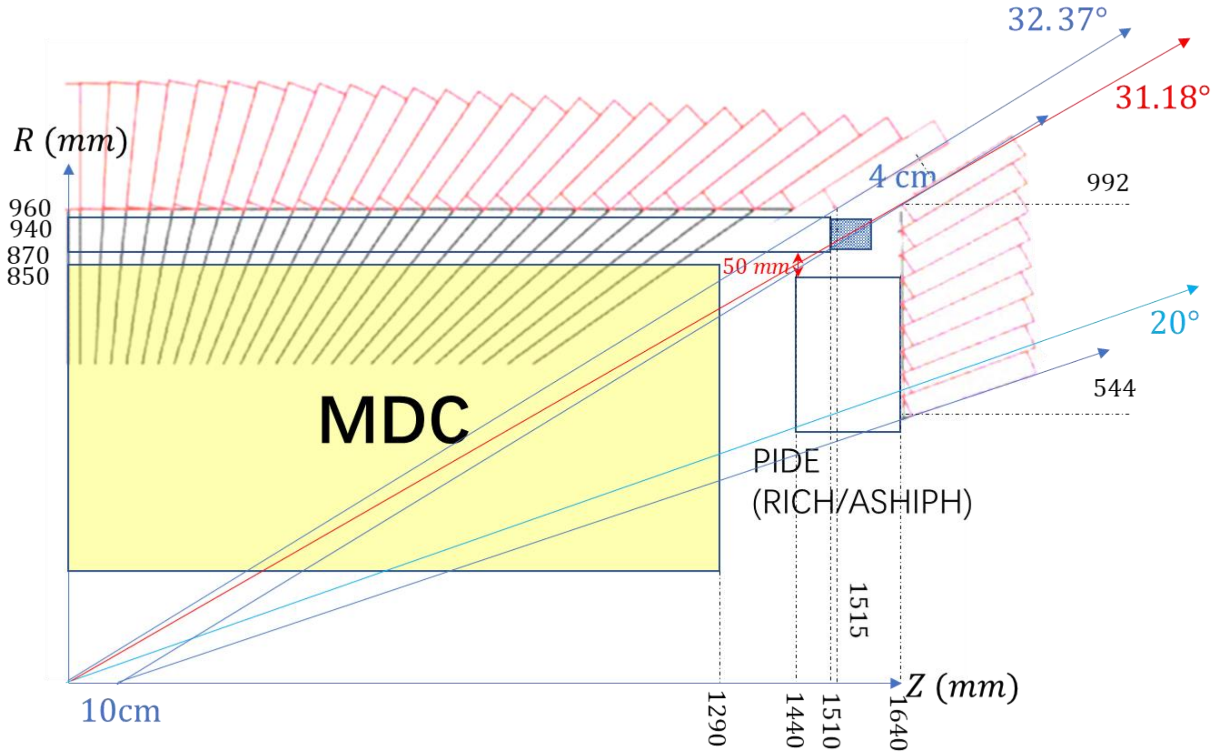
- **Fast response**
  - Challenge of high Luminosity
    - High count rate
    - Extremely high background
- **High precision**
  - Energy resolution
    - Better than 2.5% @1GeV
  - Position resolution
    - Approximately 5mm @1GeV
  - Time resolution
    - Better than 300ps @1GeV

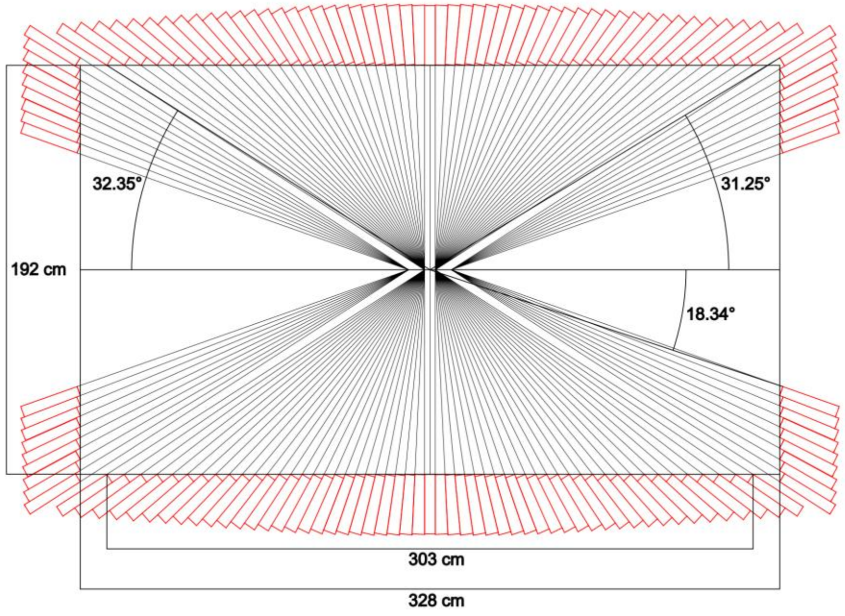


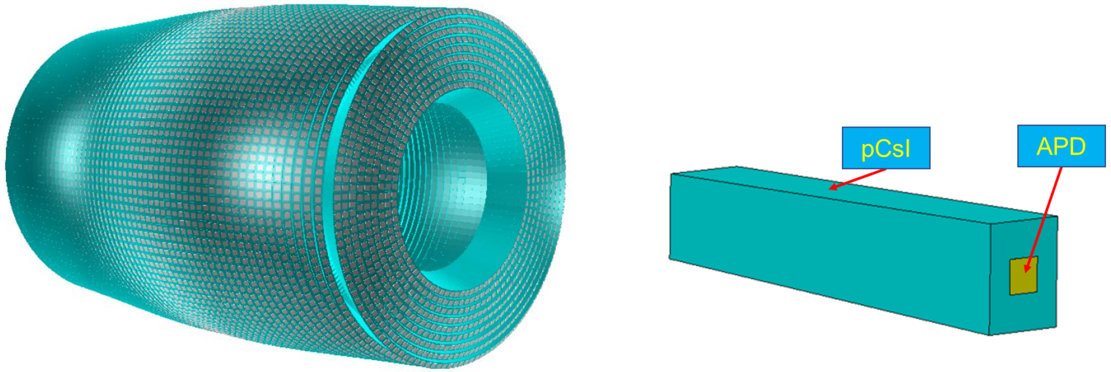
Energy distribution for photons

ECAL Geometry Optimization

- Total absorption calorimeter
  - Barrel: $(51 \rightarrow 53) \times 132 = 6996$
  - Endcap: $3 \times (85 + 105 + 130) \times 2 = 1920$
  - 11% volume reduction

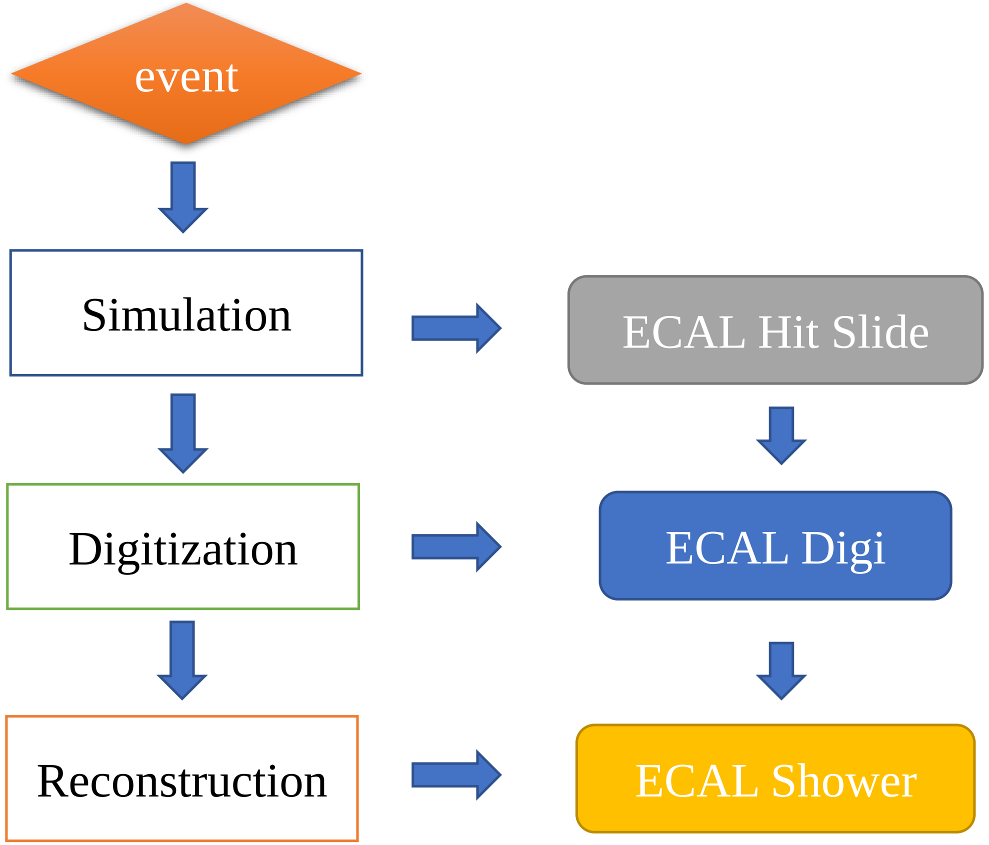






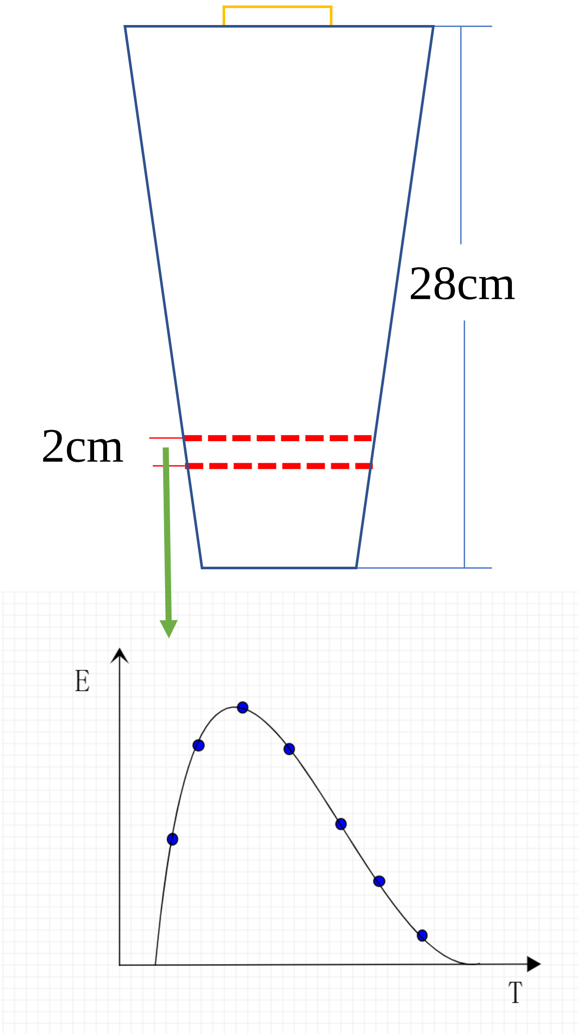
ECAL Full Chain

- Simulation
  - Geant4 based
  - Vertical Layered Crystal Data Structure
- Digitization
  - Waveform shaping
  - Waveform fitting
    - Peaking finding method
    - Template fit method
    - Pipeline fit method
- Reconstruction
  - Classical cluster reconstruction method
  - 4D Cluster reconstruction



Simulation Algorithm

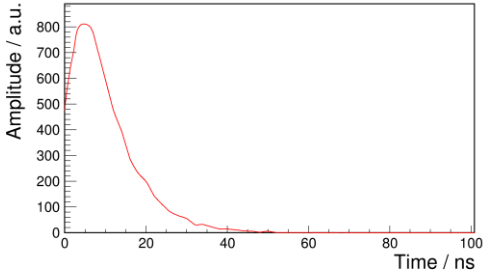
- Based on Geant4 Simulation
  - Process the information for each Geant4 step
- Data Model (layer as a unit)
  - Thickness 2cm as a layer unit
  - Each unit with a energy-time distribution: points with (E,T)
  - Bin width 500ps for energy-time distribution



- ✓ Save storage space
- ✓ Minimal loss of information
- ✓ Facilitate the Digitization

Digitization Algorithm

Waveform shaping



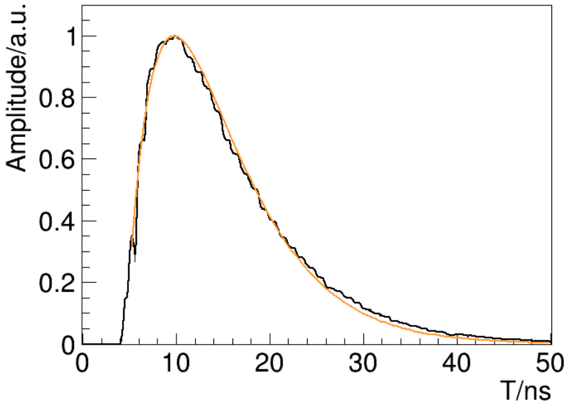
Geant4 optical simulation for each layer unit (standalone)

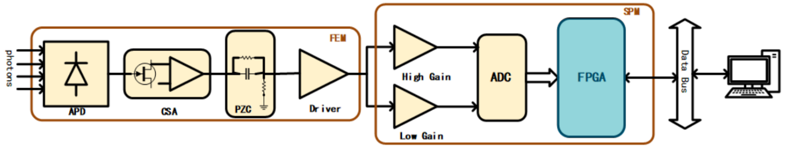
Sampling

Points (E-T) in each layer unit

Fluorescence transfer parameterized simulation

Light output nonuniformity

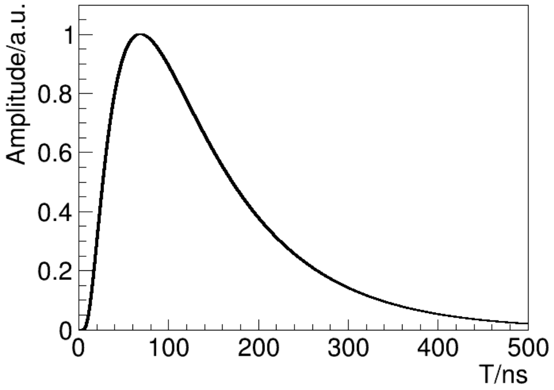




convolution

Scintillation process

Electronics response function



Electronic noise

ADC (12.5ns)

Output waveform

Strategy 0

Digitization Algorithm

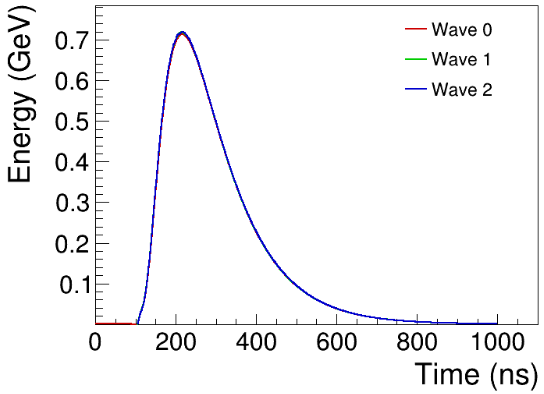
Waveform shaping

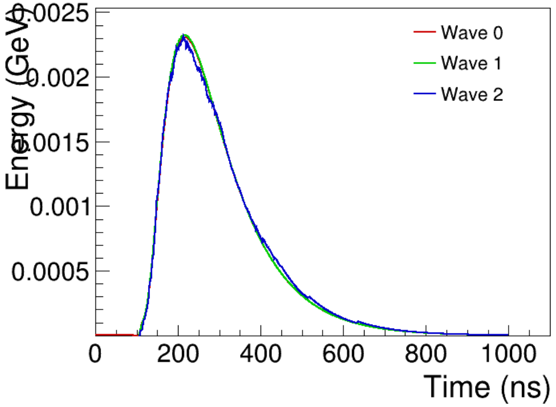
Strategy 1

Time: 15s→ 10s per event

convolution

Points (E-T) in each layer unit → Fluorescence transfer parameterized simulation / Scintillation process / Electronics response function → ADC (12.5ns)





Strategy 2

Time: Comparable

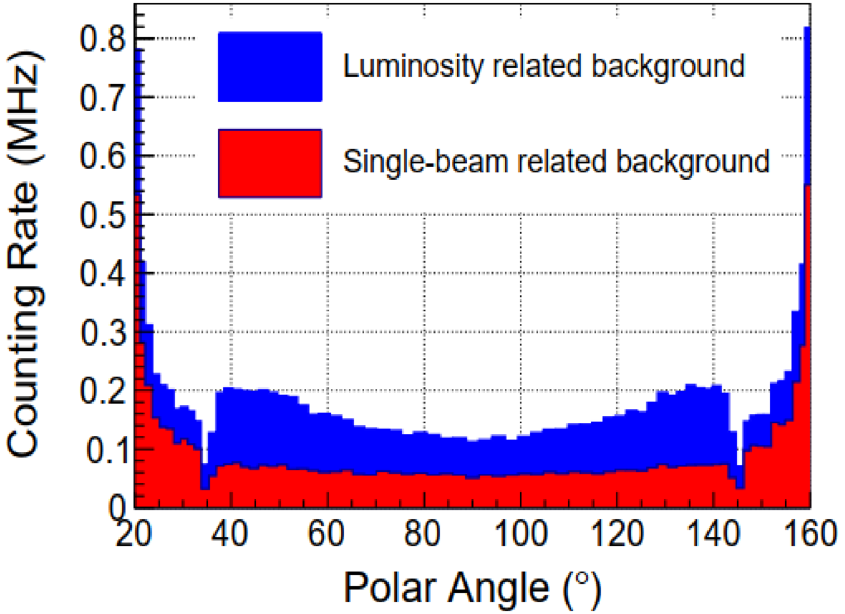
Sampling

convolution

Points (E-T) in each layer unit → Fluorescence transfer parameterized simulation / Scintillation process → Electronics response function → ADC (12.5ns)

Challenges of high background

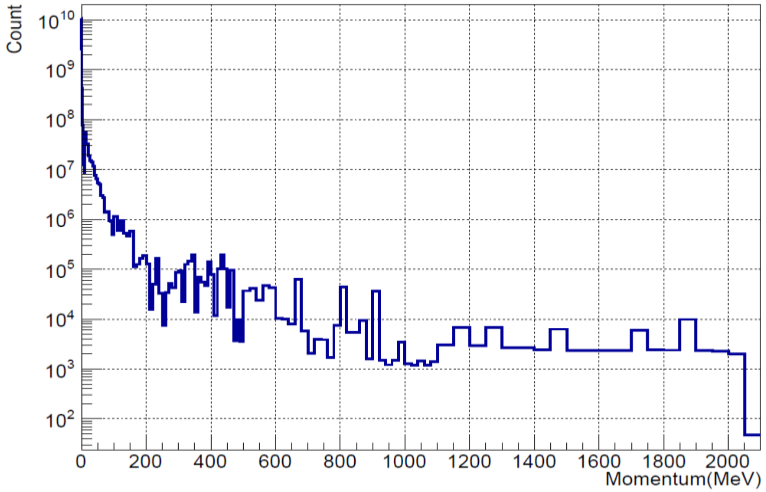
- **Luminosity-related Background**
  - Radiative BhaBha Scattering (RBB)
  - Two Photon Process



Variation of the background counting rate with polar angle

Counting rate reaches the order of MHz

- **Single-beam related Background**
  - Thouschek Effect
  - Coulomb Scattering
  - Bremsstrahlung



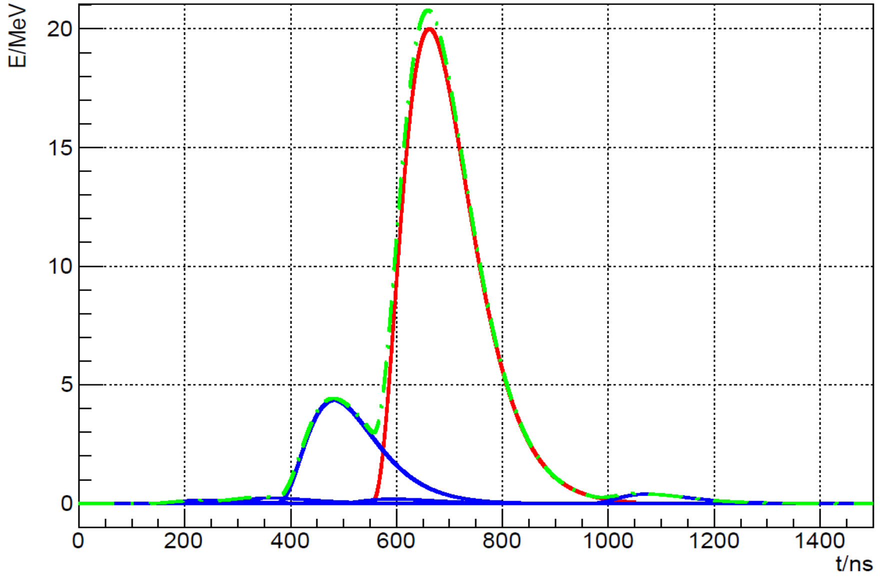
Momentum distribution of background particles

Most background particles concentrate in the low momentum region

Digitization Algorithm

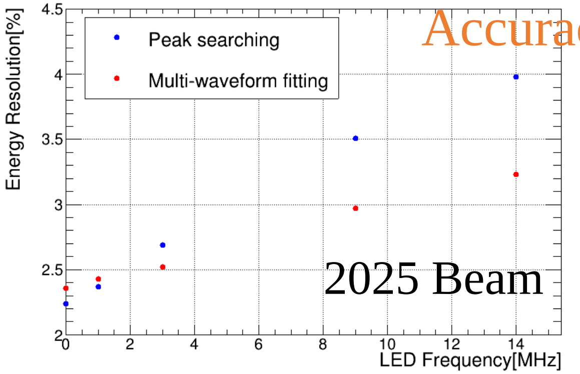
Pile-up recovery

- Pile-up is superimposed on the signal waveform
  - Inaccurate fit results of amplitude and time
  - Larger resolution of energy and time



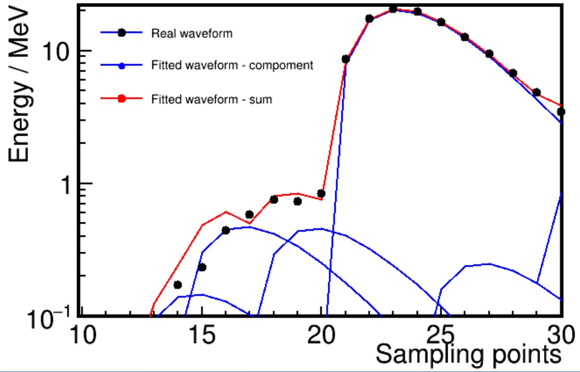
The amplitude of signal is distorted

- Pipeline fitting method



Accuracy unsatisfactory!

- Multi-template fit
  - Has been used to study the capability for pile-up recovery



Digitization Algorithm

Pipeline fit

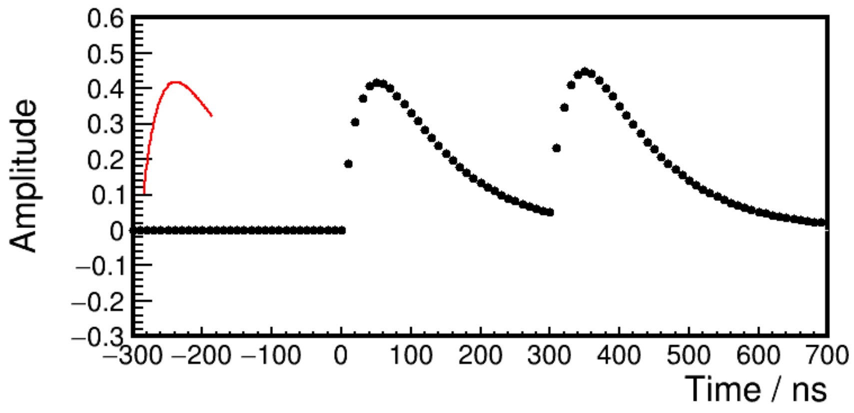
- Interpolation fitting
  - Real-time online processing
  - Template fit once for each fitting
    - Each fitting begin with different ADC point
    - Add one more fitting between two ADC points
  - Fit successful
    - $A > E_{thr}$
    - $\triangle T < 12.5/2$
    - $\chi^2/ndf < 3$:

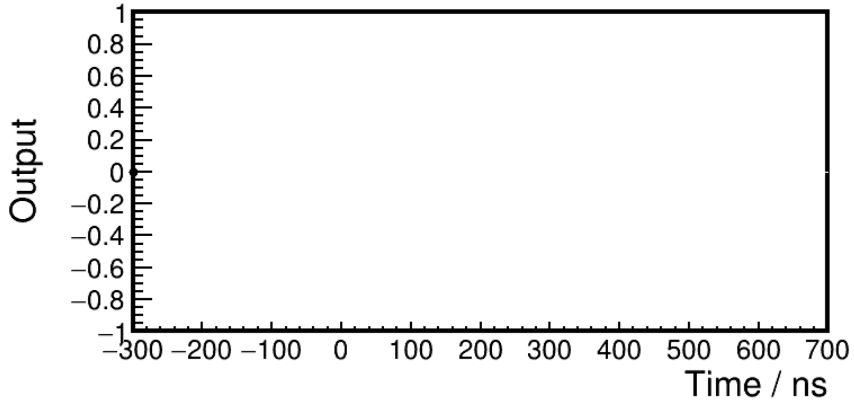
$$\chi^2/ndf = [\sum_{i,j}(y_i - A \cdot f(t_i - \tau) - p) \cdot S_{ij}^{-1} \cdot (y_j - A \cdot f(t_j - \tau) - p)] / ((n-2) \cdot (\sigma_{nos}^2 + (A \cdot 0.01)^2))$$

→ Cache and compared with next fit

→ Remove template

→ Ongoing processing



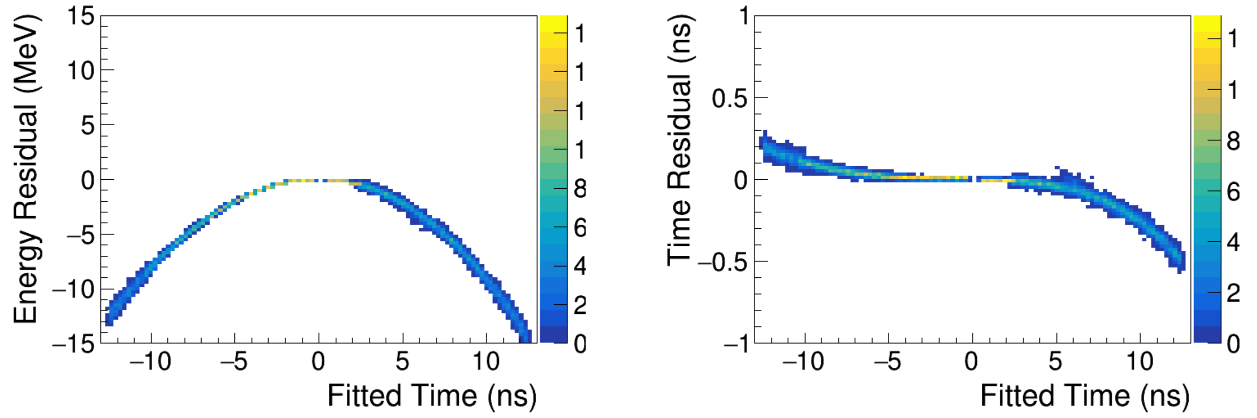


Digitization Algorithm

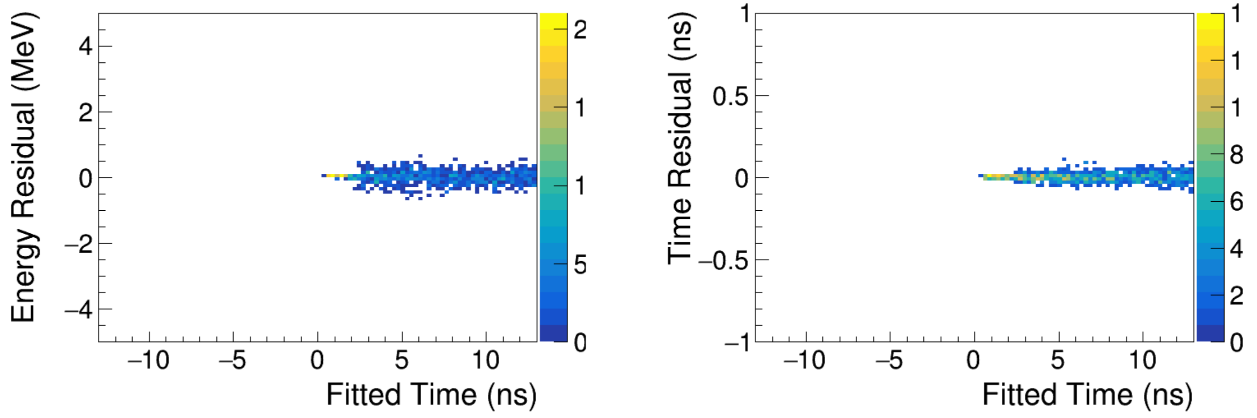
Pipeline fit

- A-T correction
  - Real-time online processing
  - Template fit once for each fitting
  - Fit successful
    - $A > E_{thr}$
    - $\triangle T < 12.5$
  - Correction with control sample
    - $\triangle T \sim (E_{pipe} - E_{single})$
    - $\triangle T \sim (T_{pipe} - T_{single})$

Before Correction



After Correction

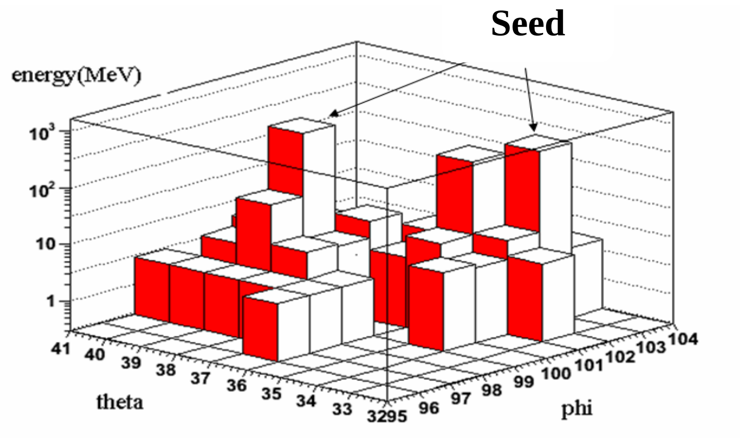


Reconstruction Algorithm

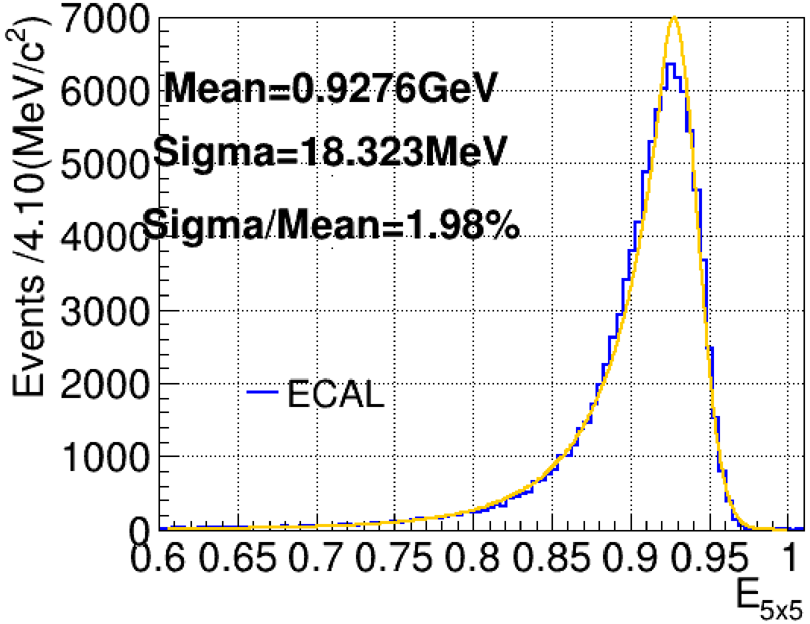
- A complete reconstruction algorithm of ECAL is developed

ECALRecAlg

Cluster search → **Seed search** → **Clusters split into Showers** → **Calculation and correction of shower energy and position**



π^0 Cluster (two photons)



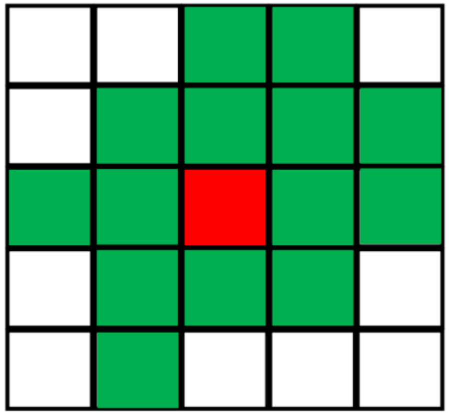
Energy distribution of 1GeV γ with background

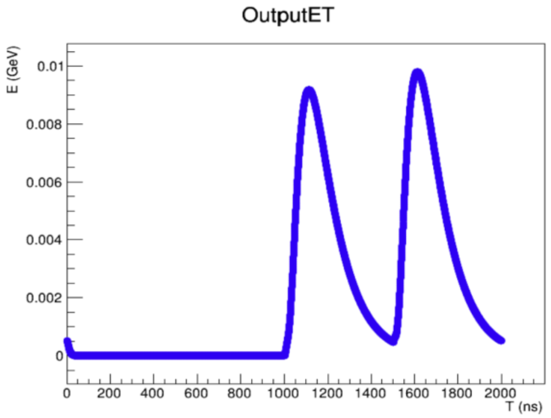
- Fitted by Crystal Ball function
- Energy resolution defined by

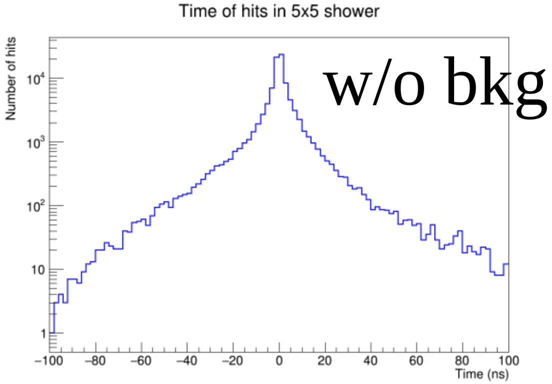
$$\sigma_E = \frac{FWHM}{2.355}$$

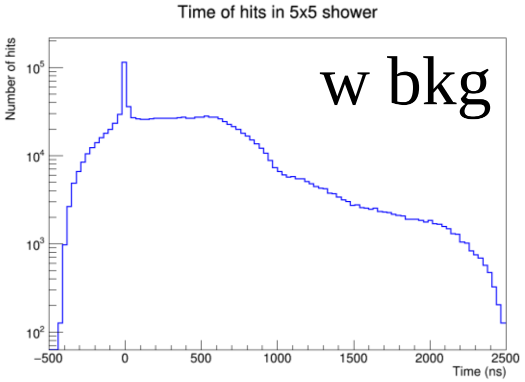
Reconstruction Algorithm

- No Time information





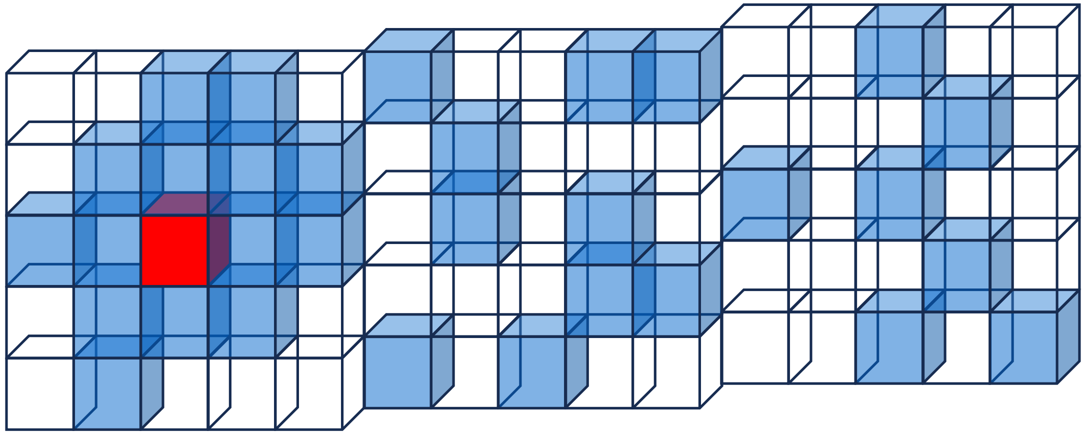


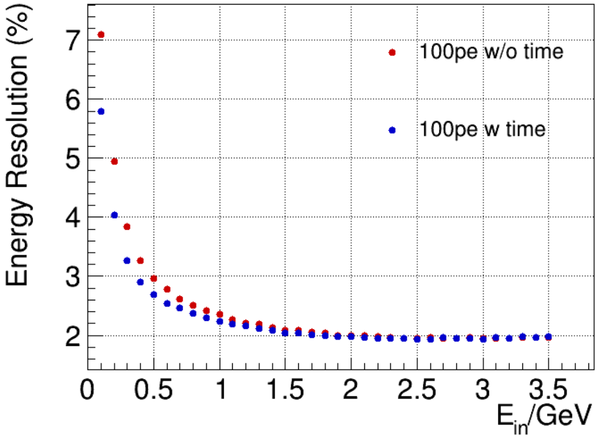


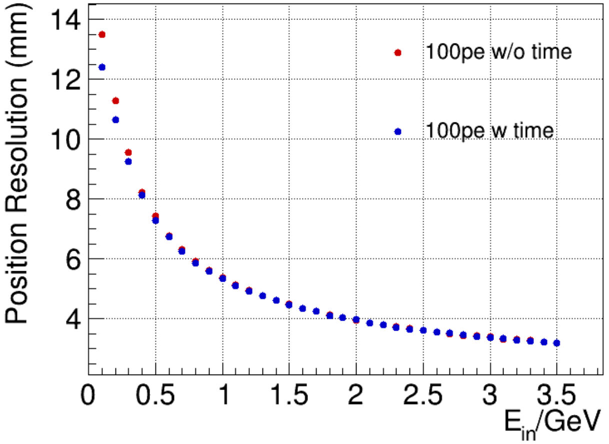
- Digi→Hit
  - The Digi with max energy will be chosen as the Hit to reconstruct the shower
- Hit→Cluster
  - The connected ignited crystals will be treated as a Cluster
- Background
  - Affects signal resolution
  - A large number of fake photons
  - Affects π^0 mass resolution

Reconstruction Algorithm

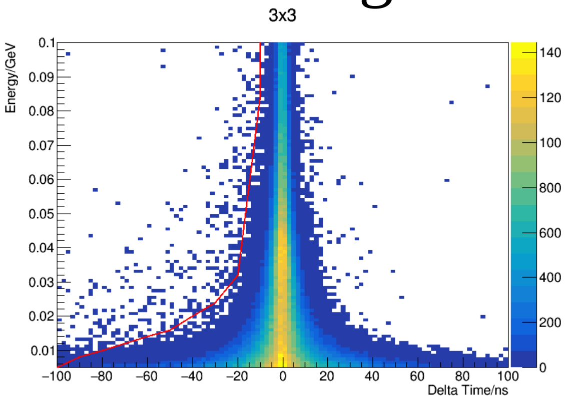
- 4D Reconstruction
  - Seed finding in 3D space with timing information
  - Add time selection while reconstructing Cluster



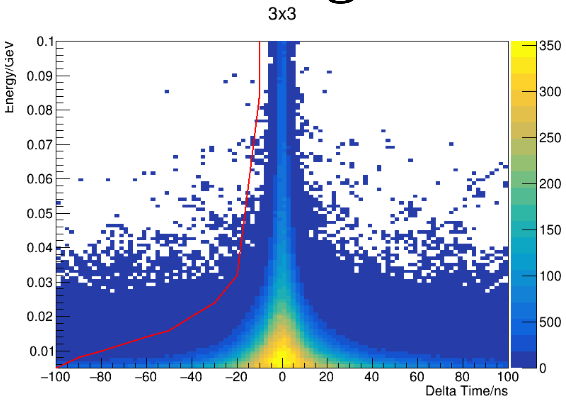




w/o bkg

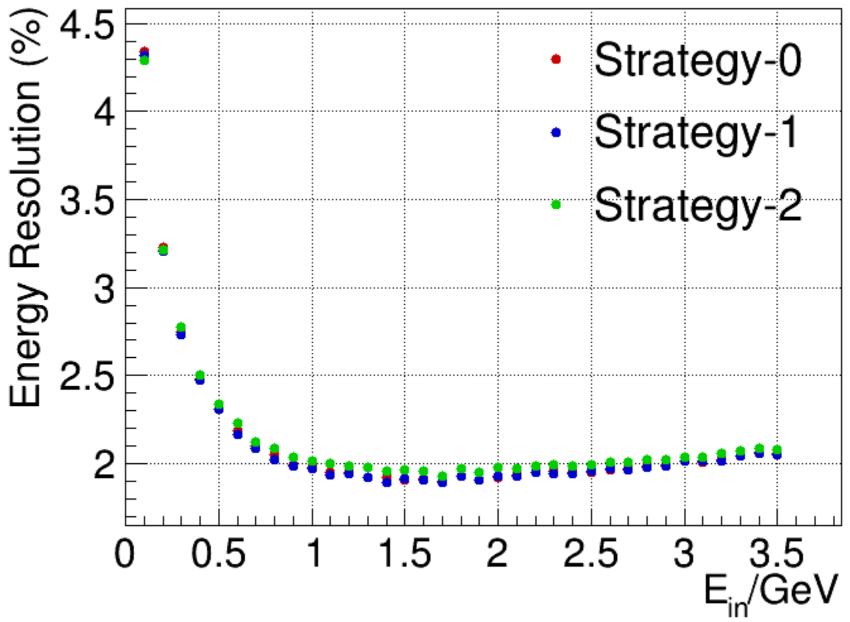


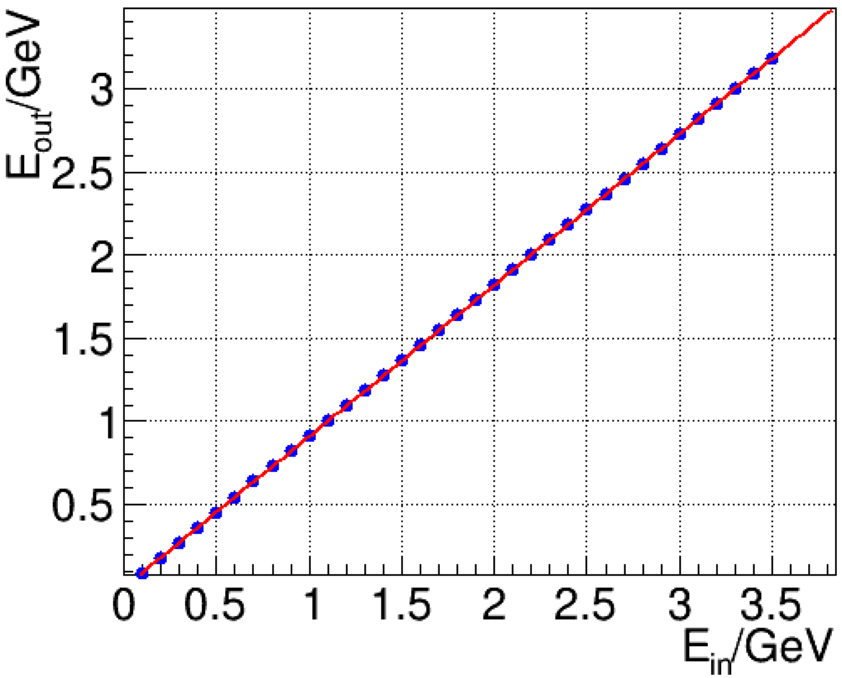
w bkg



Reconstruction Performance

Energy Reconstruction



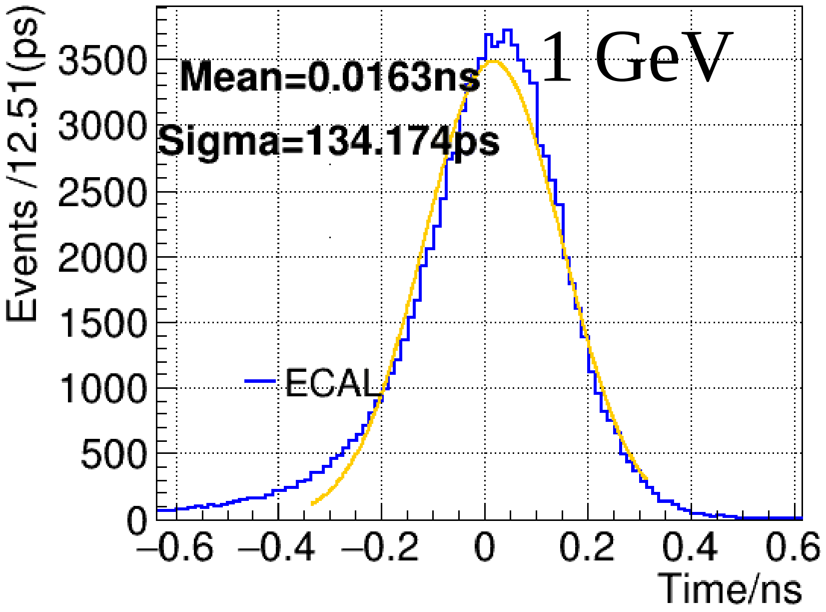


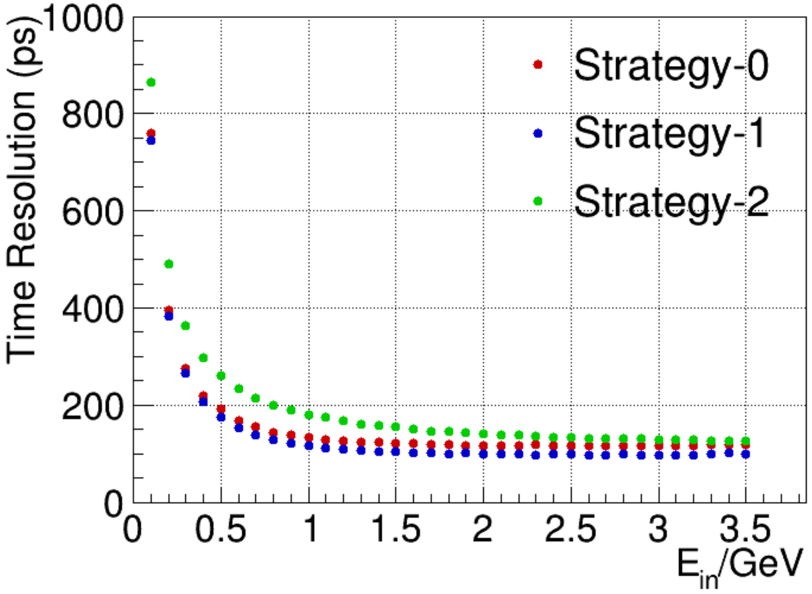
- ✓ $\sigma_E = 1.98\%$ @ 1 GeV
- ✓ $\sigma_E = 4.34\%$ @ 0.1 GeV
- ✓ With background
- ✓ Meet the requirement

- ✓ Good energy linearity in the energy range of 100 MeV ~ 3.5 GeV

Reconstruction Performance

Time Reconstruction





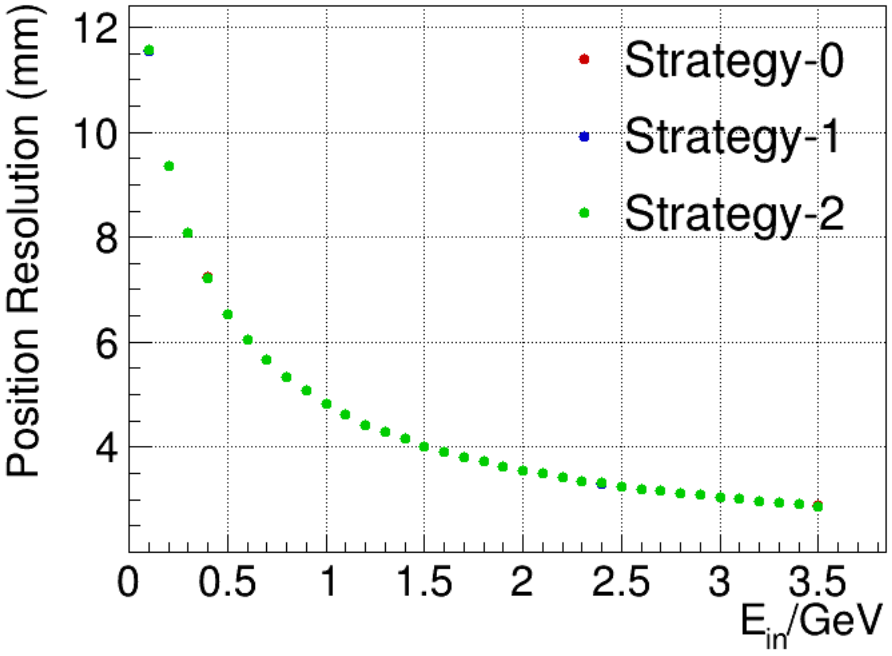
- ✓ σ_T = 134 ps @ 1 GeV
- ✓ Fitted with Gaussian function
- ✓ With background
- ✓ Meet the requirement

Reconstruction Performance

Position Reconstruction

- Splitting algorithms (used by BESIII and Panda)
  - $a_{ik} = \frac{E_k \times \exp(c \times \frac{r_{ik}}{R_M})}{\sum_{j=1}^{m} E_j \times \exp(c \times \frac{r_{ij}}{R_M})}$
- Barycenter method
  - $X_c = \sum_j^N W_j(E_j) \cdot X_j / \sum_j^N W_j(E_j)$

  Where $W_j(E_j) = \max\{0, a + \ln(E_j / \sum_j^N E_j)\}$

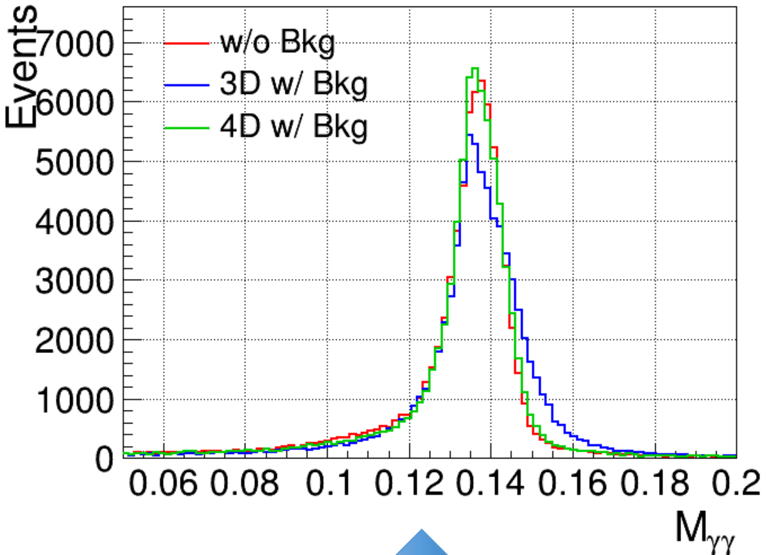


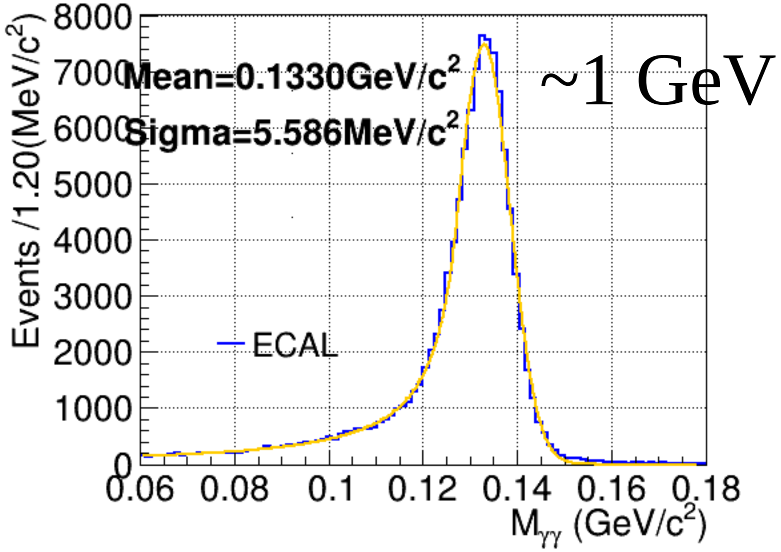
- ✓ σ_{pos} = 4.8 mm @ 1 GeV
- ✓ With background
- ✓ Meet the requirement

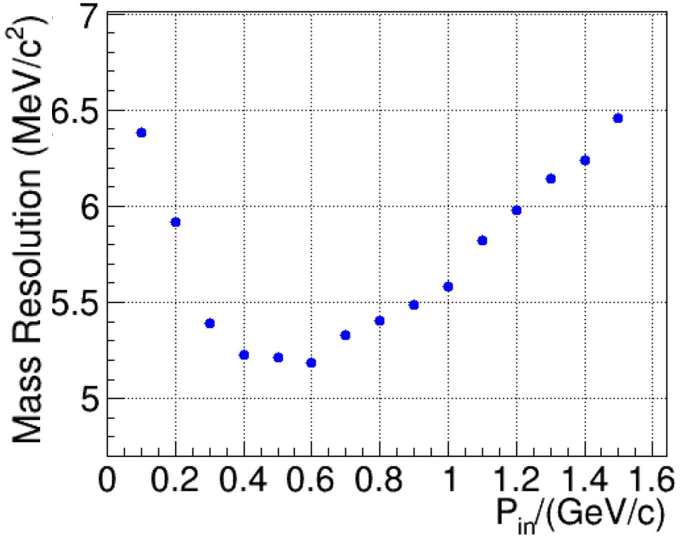
Reconstruction Performance

π^0 Reconstruction

$$m_{\pi^0} = \sqrt{2E_1E_2(1-cos\alpha)}$$







$-10ns < T_{seed} < 10ns$

π^0 with the minimum ΔM

Truth matched π^0

- ✓ $J/\psi \to \rho\pi$ sample
- ✓ σ_{π^0} = 5.6 MeV/c² @ 1 GeV
- ✓ With background

Summary

- The software of ECAL has been established based on OSCAR
- The simulated performance of ECAL meets requirements with the background concerned
  - ✓ Energy measurement with 2.03% @ 1 GeV
  - ✓ Time measurement with 130 ps @ 1 GeV
  - ✓ Position measurement with 5.3 mm @ 1 GeV
  - ✓ π^0 mass measurement with 5.6 MeV/c^2 @ ~1GeV

Prospect:

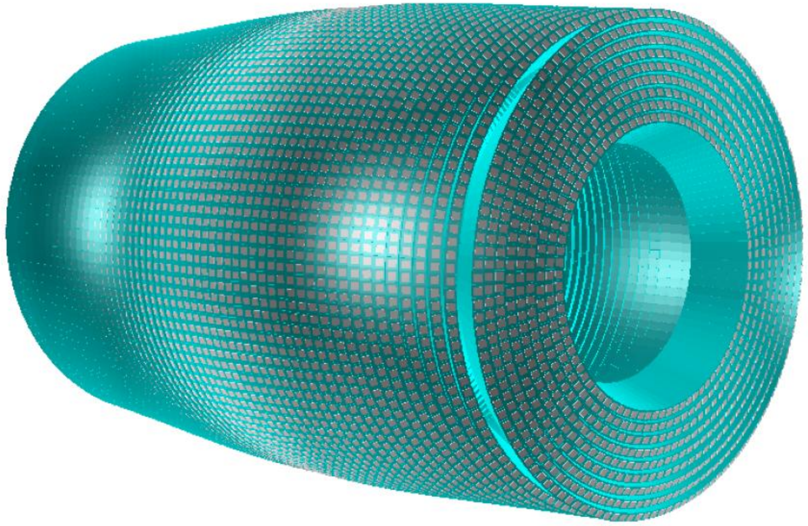
- Verify and update digitization to align with beam test data
- dE/dx for simulation to describe hardon waveform

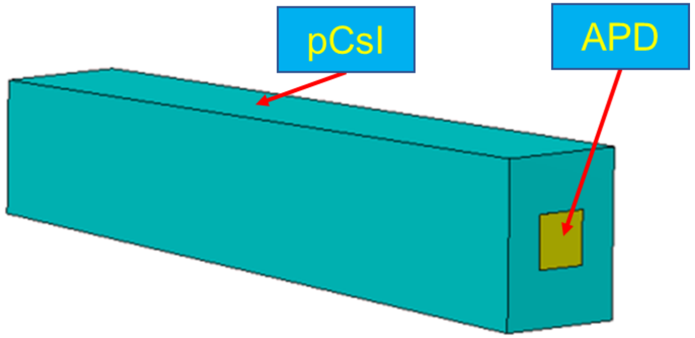
Thanks for your listening!

Back up

ECAL Design

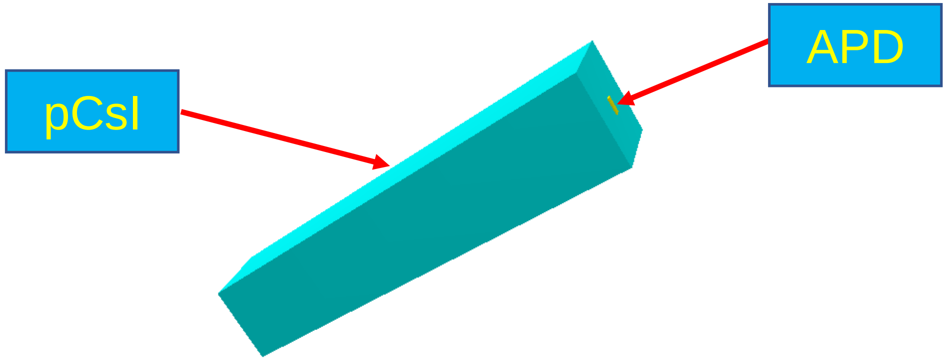
- Total absorption calorimeter
  - Barrel: $53 \times 132 = 6996$
  - Endcap: $3 \times (85 + 105 + 130) \times 2 = 1920$
  - Crystal Size:
    - $5 \times 5 \times 28(15X_0)\ \mathrm{cm}^3$
- Sensitive Unit
  - Pure CsI (pCsI) crystal
    - Fast decay time (~30ns)
    - Good radiation hardness
    - Low light yield
  - Avalanche photodiode (APD)
    - Short wavelength type
    - Large area $(10 \times 10\ mm^2 \times 4)$





ECAL Design —— Sensitive Unit

- **Pure CsI crystal + APD photo-device**
  - Pure CsI (pCsI) crystal
    - ✓ Fast decay time
    - ✓ Good radiation hardness
    - ✓ Low light yield
  - Crystal Size:
    - ✓ Total radiation length
      $15\ X_0$ (28 cm)
    - ✓ End face size
      front end: $\sim 5 \times 5\ cm^2$
      back end: $\sim 6.5 \times 6.5\ cm^2$
  - Avalanche photodiode (APD)
    - ✓ Short wavelength type
    - ✓ Large area ($10 \times 10\ mm^2 \times 4$)

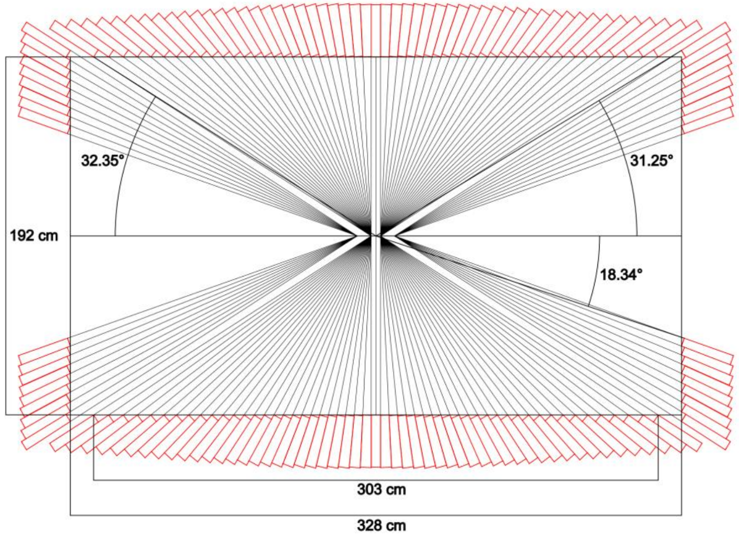


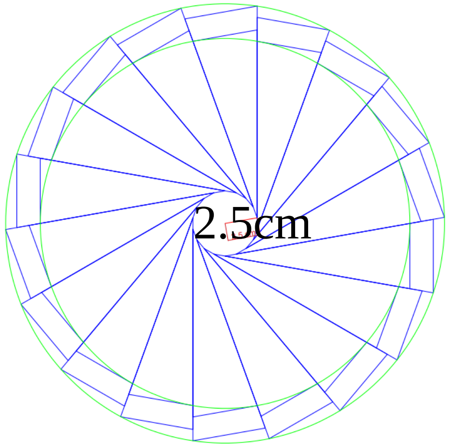
ECAL pCsI crystal unit

Crystal	Pure CsI
Density (g/cm^3)	4.51
Melting Point (°C)	621
Radiation Length (cm)	1.86
Moliere Radius (cm)	3.57
Refractive index	1.95
Hygroscopicity	Slight
Luminescence (nm)	310
Decay time (ns)	30 6
Light yield (%)	3.6 1.1
Dose rate dependent	No
D(LY)/dT (%/°C)	-1.4
Experiment	KTeV Mu2e

ECAL Setup

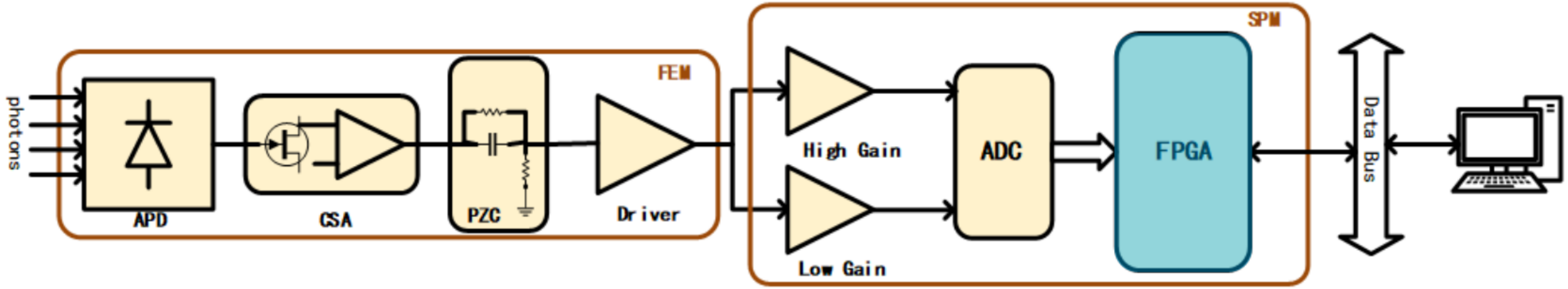
- "Dead Material"
  - 150-μm Teflon reflective film
  - 75-μm polyethylene insulating film
  - 75-μm Al electrostatic shielding film
  - No supporting material
- Light Yield: 300 p.e./MeV
- Light Collection Non-uniformity
  - collection efficiency: $\epsilon(l) = 95\% + l/L \times 5\%$
- $\sigma_{noise} = 0.4$ MeV
- $E_{hit\_thres} = 2.0$ MeV
- Secondary Particles Hit APD





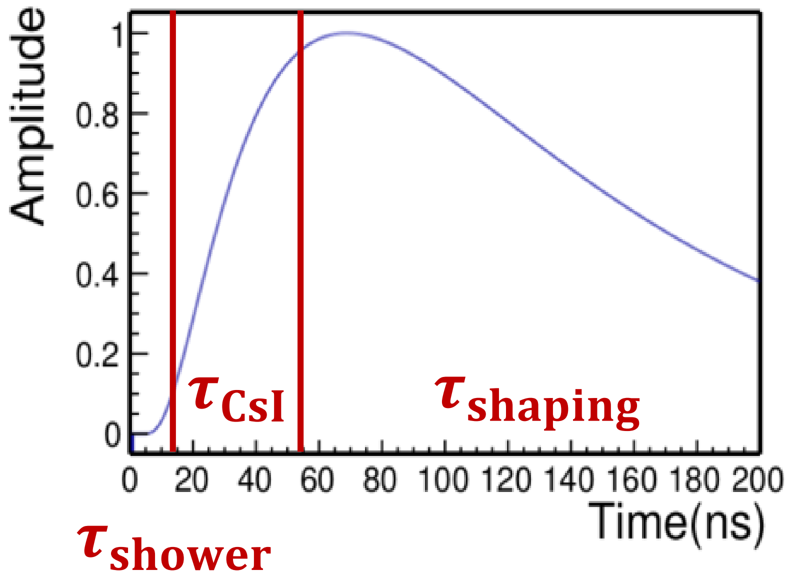
ECAL Electronics

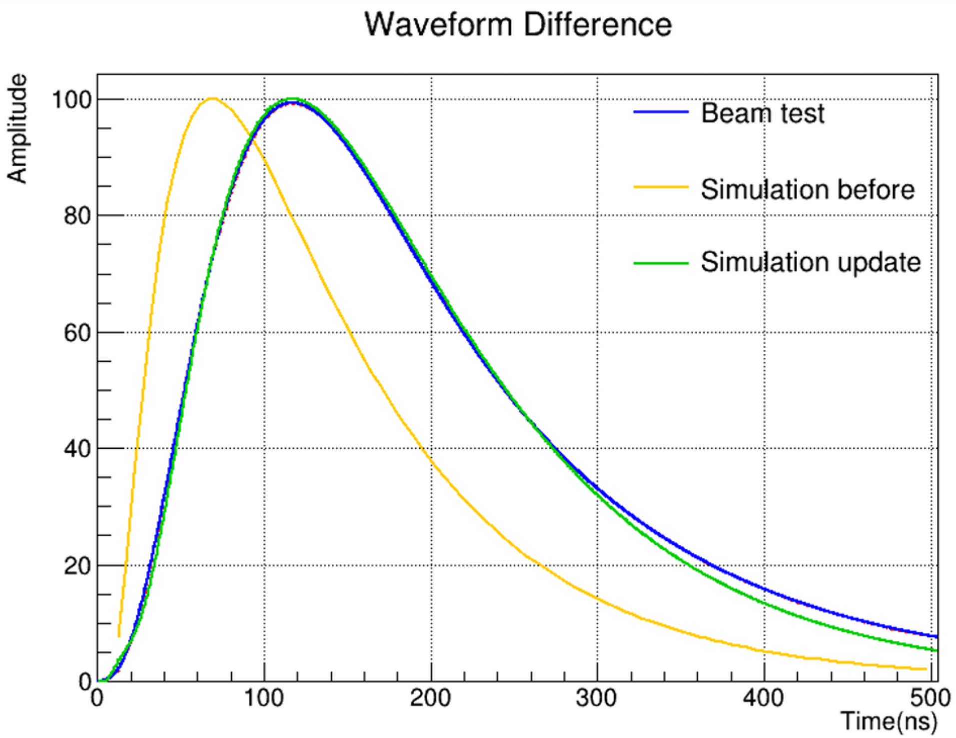
- Charge sensitive amplifier and pole-zero cancellation with shaping time 100 ns
- High and Low Gain (300 MeV/3000MeV)
- 16-bit ADC (~16000 channels) with 80 MHz sampling rate



Digitization Algorithm

Waveform check





- $\tau_{\text{shaping}} = 100$ ns
- $\tau_{\text{CsI}} = 30$ ns
- $\sigma_{\text{noise}} < 1.0$ MeV
- L.Y. > 100 p.e./MeV

→

- $\tau_{\text{shaping}} = 100$ ns
- $\tau_{\text{CsI}} \approx 30$ ns + 85ns
- $\sigma_{\text{noise}} <$ **0.4** MeV
- L.Y. > **300** p.e./MeV

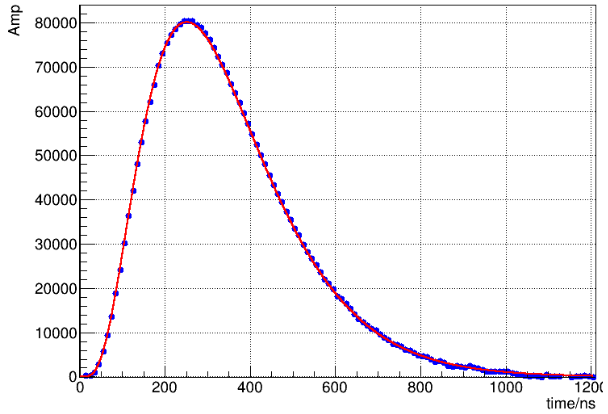
Digitization Algorithm

Waveform fitting

- Template fit to extract Amplitude and Time
  - Find the points around amplitude peak to do the template fitting
  - Template shape function: $f(t) = A \times f(t-\tau) + p$
  - $\chi^2 = \sum_{i,j}(y_i - A \cdot f(t_i - \tau) - p) \cdot S_{ij}^{-1} \cdot \left(y_j - A \cdot f\left(t_j - \tau\right) - p\right)$
  - Apply $\frac{\partial \chi^2}{\partial A} = 0, \frac{\partial \chi^2}{\partial \tau} = 0$

  Where y_i and t_i are from readout waveform; the electronics foundation p in digitization is $p = 0$; A and τ are the amplitude and time from fitting result; S_{ij} is the noise covariance matrix.

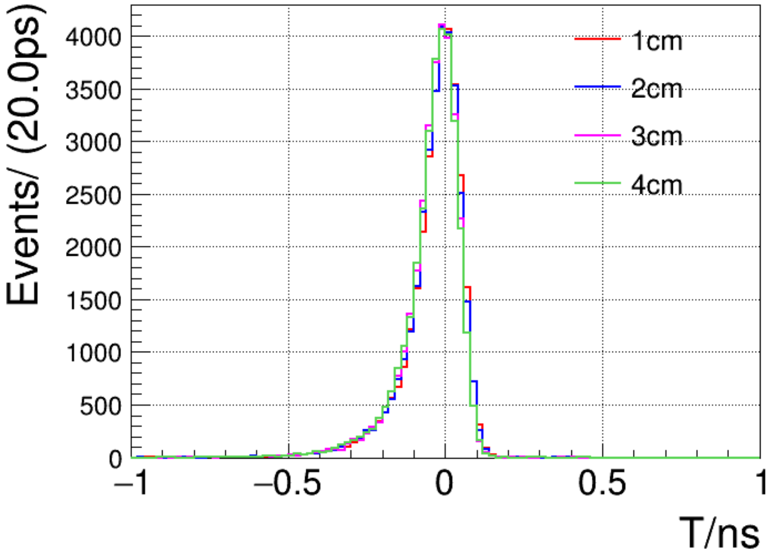
- Pipeline fit for pile-up recovery

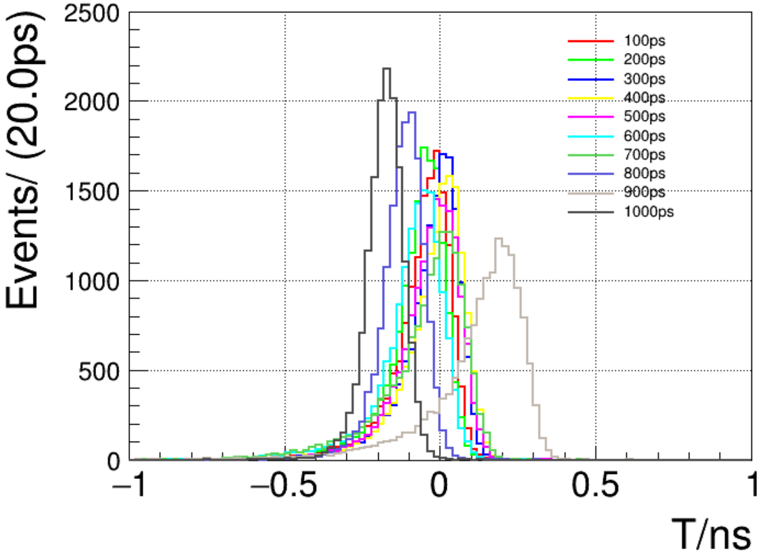


Simulation Algorithm

Data Model

- Sizes of thickness and time bin width have been optimized
  - No large difference of time distribution for different thickness
    - Consider the non-uniformity may vary in the future : 2cm
  - Different time bin width with different time resolution and central value
    - Difference in central value approximately equivalent to a shift of the template
    - Consider the resolution and the similarity to the template: 500ps

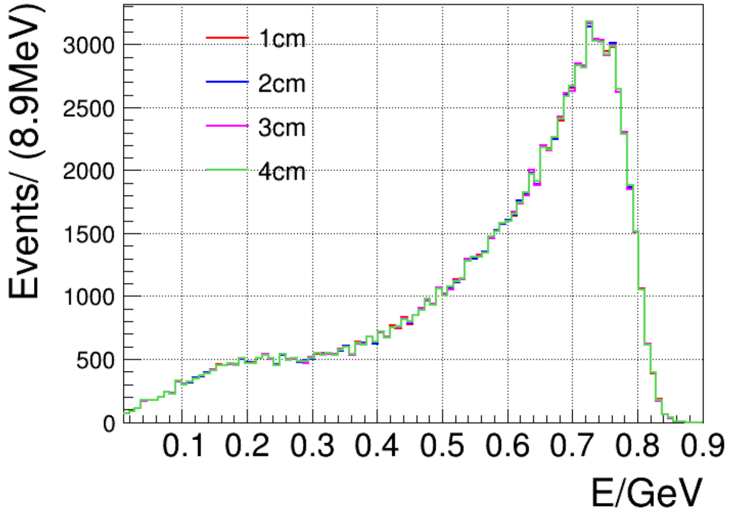


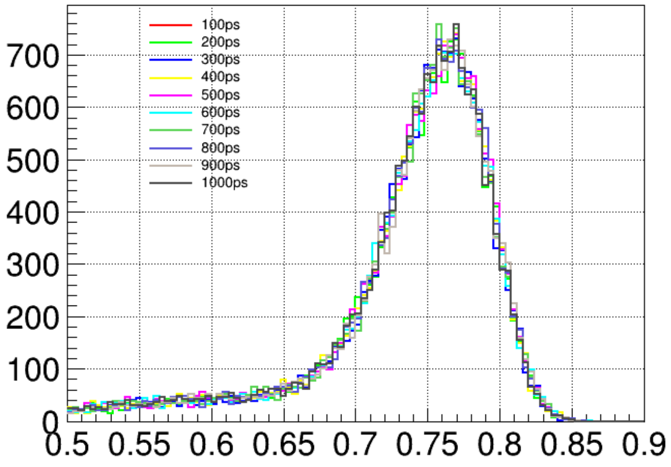


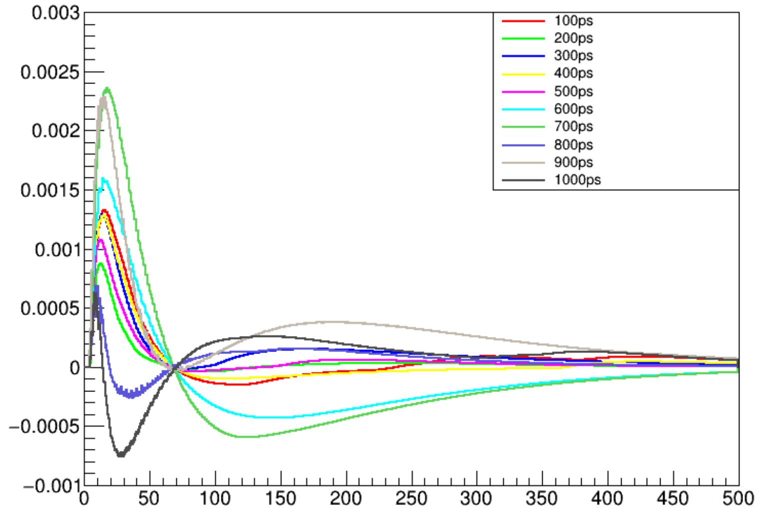
Simulation Algorithm

Data Model

- Energy distribution and comparison with template

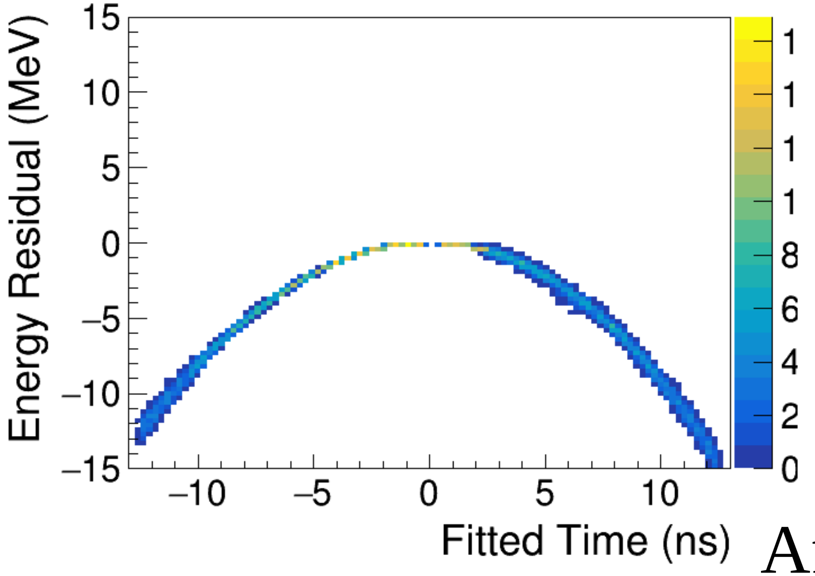


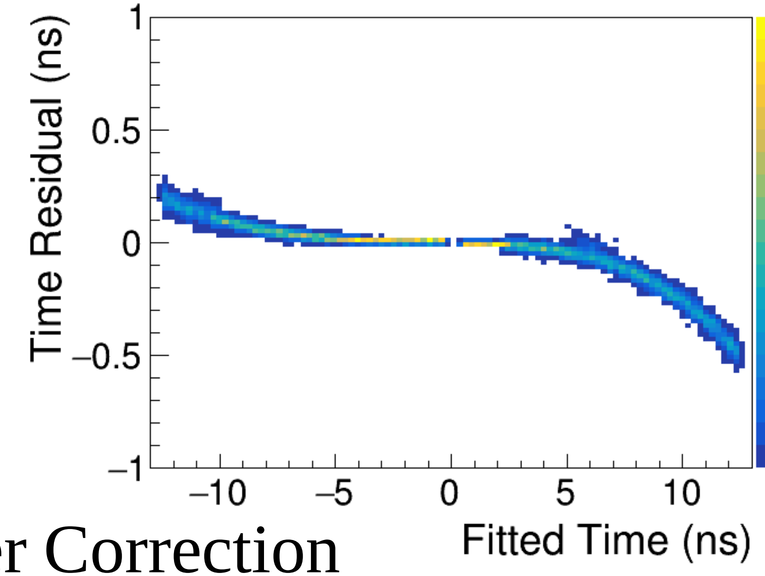




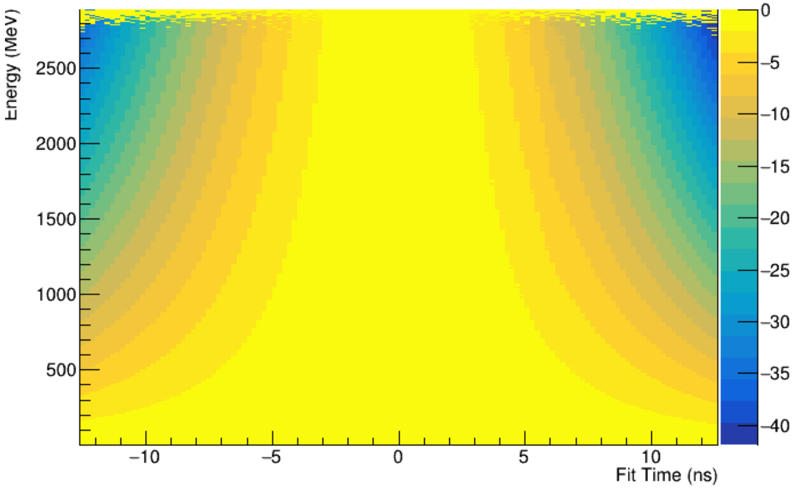
A-T Correction

Before Correction

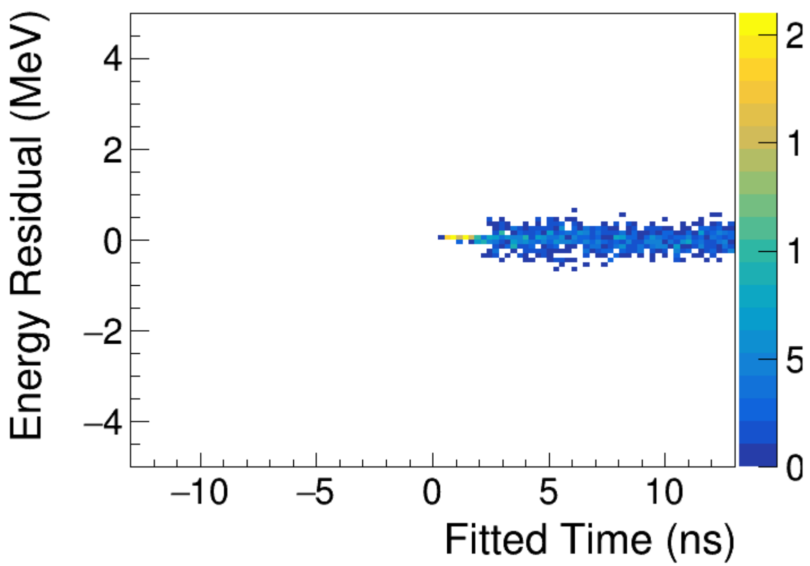


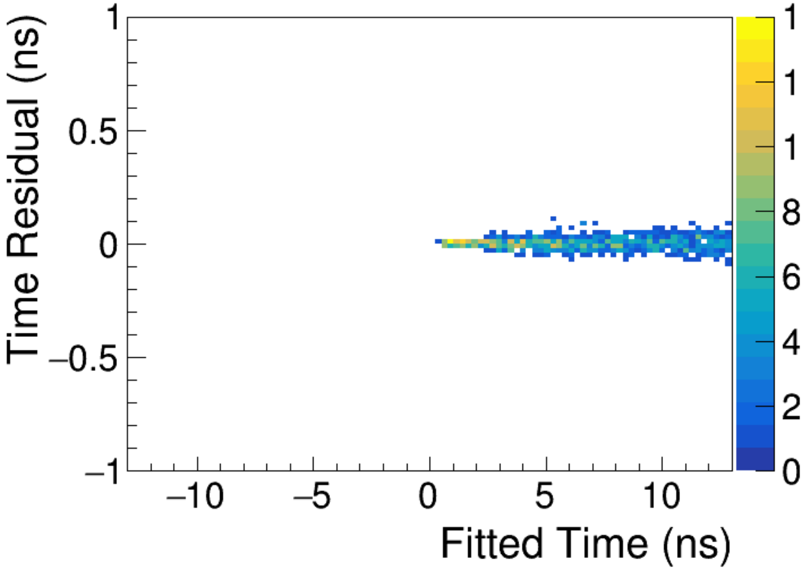


E Correction

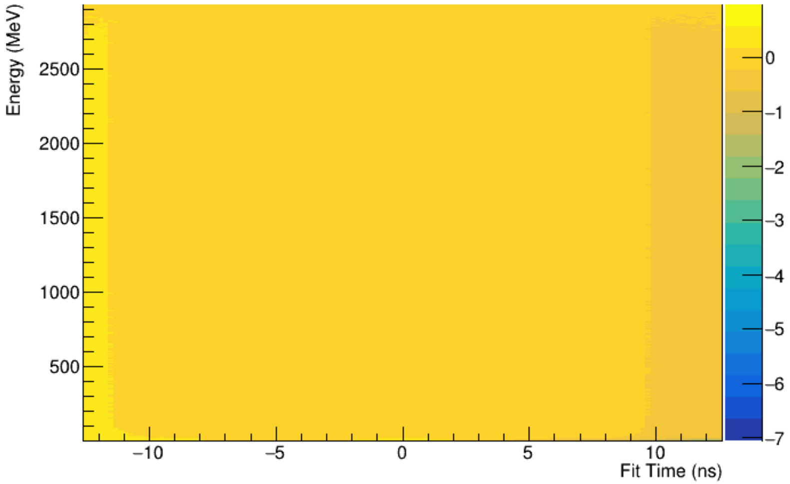


After Correction





T Correction



Template Fitting

- Template shape function： $f(t) = A \times f(t-\tau) + p$
- $\chi^2 = \sum_{i,j}(y_i - A \cdot f(t_i - \tau) - p) \cdot S_{ij}^{-1} \cdot \left(y_j - A \cdot f\left(t_j - \tau\right) - p\right)$
- Apply $\frac{\partial \chi^2}{\partial A} = 0, \frac{\partial \chi^2}{\partial \tau} = 0, \frac{\partial \chi^2}{\partial p} = 0$:

$$\begin{cases} \sum_{i,j} f_{ki} \cdot S_{ij}^{-1} \cdot \left(y_j - Af_{kj} - Bf'_{kj} - p\right) = 0 \\ \sum_{i,j} f'_{ki} \cdot S_{ij}^{-1} \cdot \left(y_j - Af_{kj} - Bf'_{kj} - p\right) = 0 \\ \sum_{i,j} 1 \cdot S_{ij}^{-1} \cdot \left(y_j - Af_{kj} - Bf'_{kj} - p\right) = 0 \end{cases}$$

$$\begin{pmatrix} \boldsymbol{F}_k \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{F}_k^T & \boldsymbol{F}_k \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{F}_k'^T & \boldsymbol{F}_k \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{I} \\ \boldsymbol{F}'_k \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{F}_k^T & \boldsymbol{F}'_k \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{F}_k'^T & \boldsymbol{F}'_k \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{I} \\ \boldsymbol{I} \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{F}_k^T & \boldsymbol{I} \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{F}_k'^T & \boldsymbol{I} \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{I} \end{pmatrix} \cdot \begin{pmatrix} A \\ B \\ p \end{pmatrix} = \begin{pmatrix} \boldsymbol{F}_k \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{Y} \\ \boldsymbol{F}'_k \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{Y} \\ \boldsymbol{I} \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{Y} \end{pmatrix}$$

$$\begin{pmatrix} A \\ B \\ p \end{pmatrix} = \begin{pmatrix} \boldsymbol{F}_k \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{F}_k^T & \boldsymbol{F}_k \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{F}_k'^T & \boldsymbol{F}_k \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{I} \\ \boldsymbol{F}'_k \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{F}_k^T & \boldsymbol{F}'_k \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{F}_k'^T & \boldsymbol{F}'_k \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{I} \\ \boldsymbol{I} \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{F}_k^T & \boldsymbol{I} \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{F}_k'^T & \boldsymbol{I} \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{I} \end{pmatrix}^{-1} \cdot \begin{pmatrix} \boldsymbol{F}_k \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{Y} \\ \boldsymbol{F}'_k \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{Y} \\ \boldsymbol{I} \cdot \boldsymbol{S}^{-1} \cdot \boldsymbol{Y} \end{pmatrix}$$

Nonnegative Least Square (NNLS)

Convention:

- b: A real pulse with m points
- x: fitted amplitudes for n pulses
- A: the ith column of A represents the template for the ith pulse and of course each template has m points
- P: passive set – currently not fixed amps
- R: active set – currently fixed amplitudes

Algorithm *fnnls* **:**

Input: $\mathbf{A} \in \mathbf{R}^{m \times n}$, $\mathbf{b} \in \mathbf{R}^m$
Output: $\mathbf{x}^* \geq 0$ such that $\mathbf{x}^* = \arg\min \|\mathbf{Ax} - \mathbf{b}\|^2$.
Initialization: $P = \varnothing, R = \{1, 2, \cdots, n\}, \mathbf{x} = \mathbf{0}, \mathbf{w} = \mathbf{A}^T\mathbf{b} - (\mathbf{A}^T\mathbf{A})\mathbf{x}$
repeat

1. Proceed if $R \neq \varnothing \wedge [\max_{i \in R}(w_i) > \textit{tolerance}]$
2. $j = \arg\max_{i \in R}(w_i)$
3. Include the index j in P and remove it from R
4. $\mathbf{s}^P = [(\mathbf{A}^T\mathbf{A})^P]^{-1}(\mathbf{A}^T\mathbf{b})^P$
   4.1. Proceed if $\min(\mathbf{s}^P) \leq 0$
   4.2. $\alpha = -\min_{i \in P}[x_i/(x_i - s_i)]$
   4.3. $\mathbf{x} := \mathbf{x} + \alpha(\mathbf{s} - \mathbf{x})$
   4.4. Update R and P
   4.5. $\mathbf{s}^P = [(\mathbf{A}^T\mathbf{A})^P]^{-1}(\mathbf{A}^T\mathbf{b})^P$
   4.6. $\mathbf{s}^R = \mathbf{0}$
5. $\mathbf{x} = \mathbf{s}$
6. $\mathbf{w} = \mathbf{A}^T(\mathbf{b} - \mathbf{Ax})$

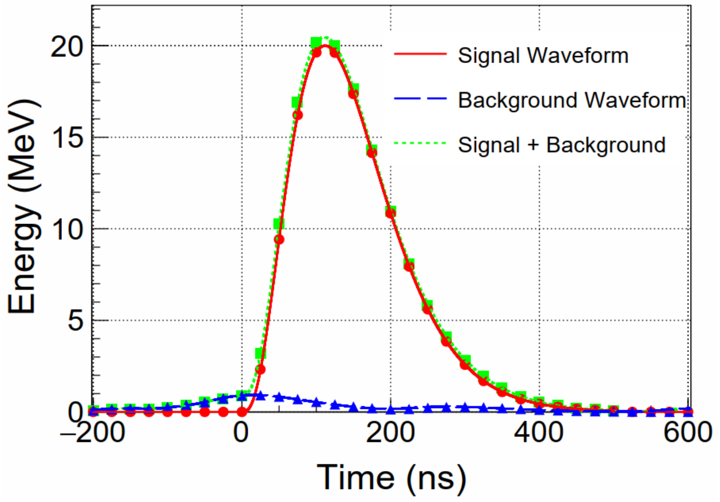
Pile-up Recovery

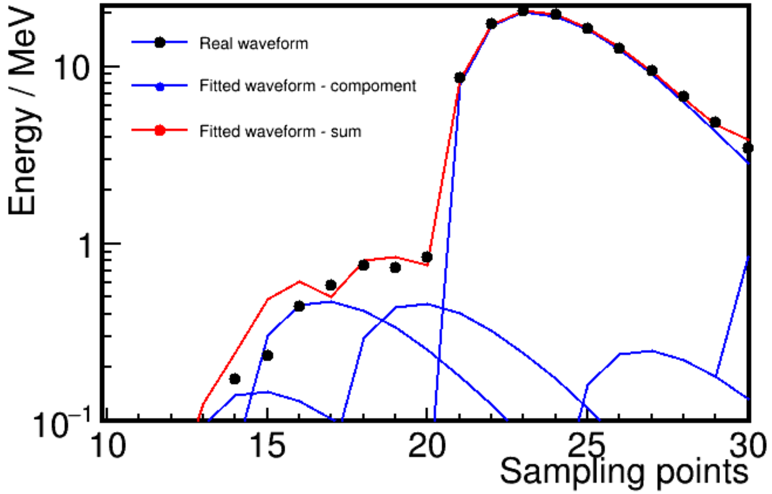
Multi-template fit

- Fit all the potential waveforms with template
- Isolate signals by time
- The fit minimizes the χ^2 defined as:

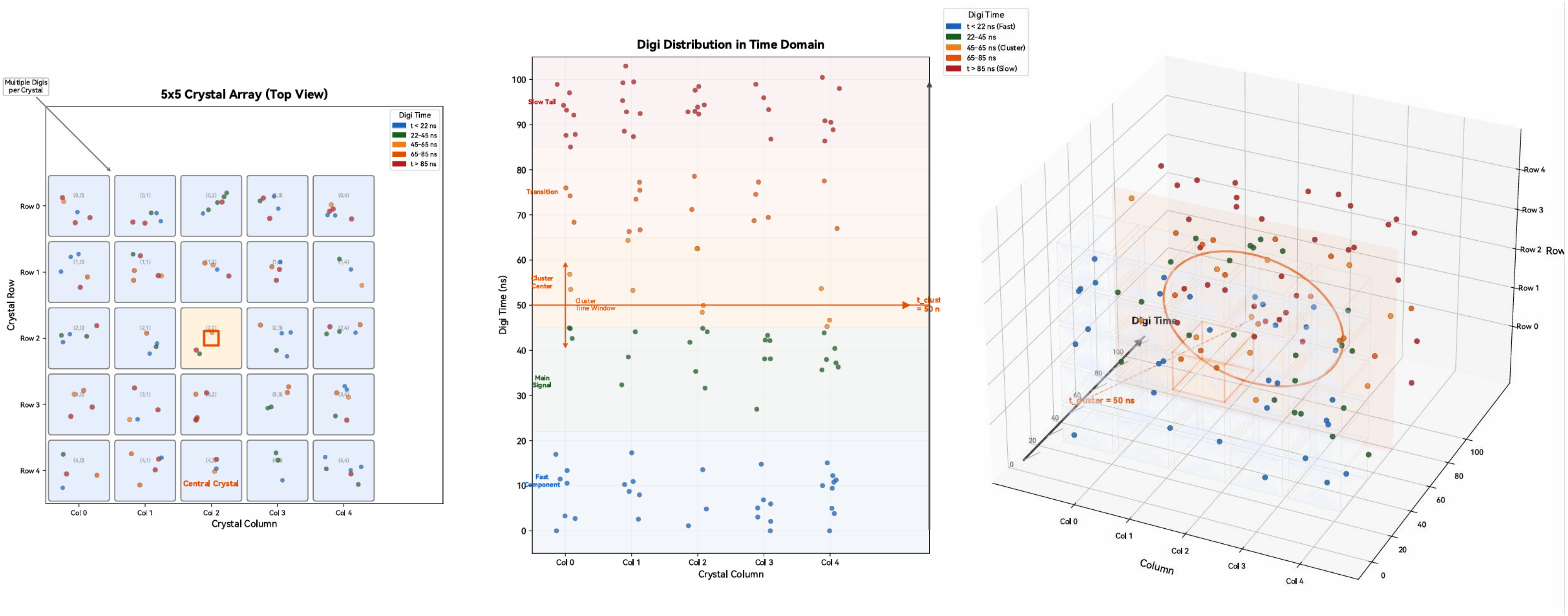
$$\chi^2 = \left(\sum_{j=1}^{N} A_j\overrightarrow{p_j} - \vec{S}\right)^T C^{-1}\left(\sum_{j=1}^{N} A_j\overrightarrow{p_j} - \vec{S}\right)$$

Where:
N is the number of templates;
vector $\vec{S}$ comprise the readout samples;
vector $\overrightarrow{p_j}$ is the waveform template;
A_j are the amplitudes, which are obtained by the fit;
C is the noise covariance matrix.



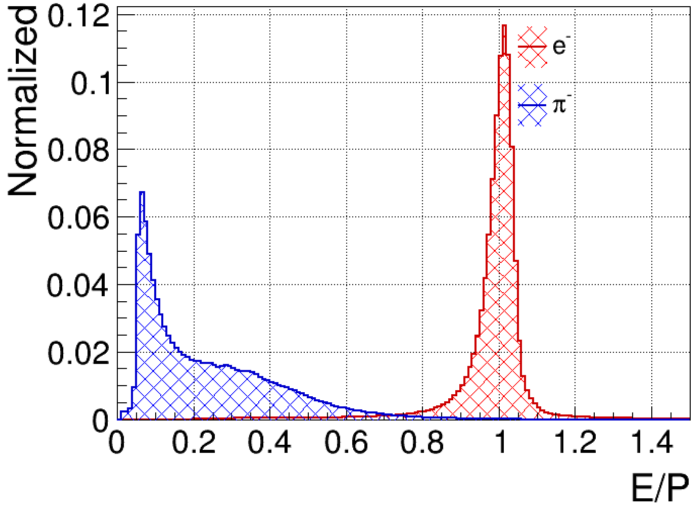


4D Reconstruction Algorithm

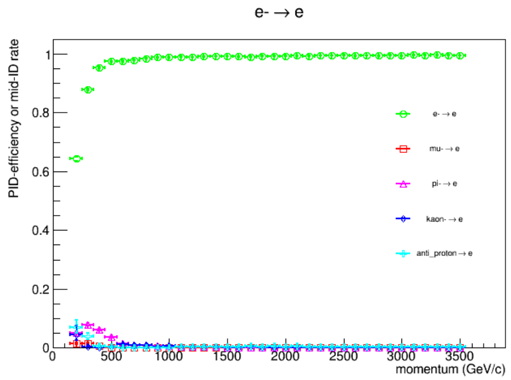


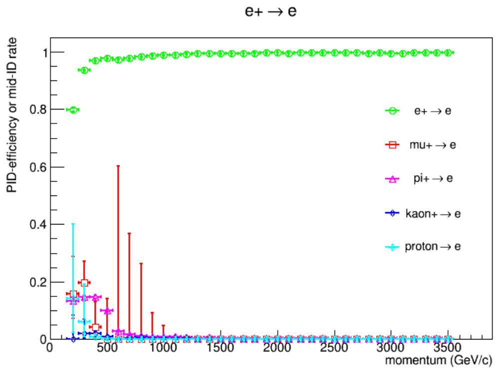
Electron PID Algorithm

- E/P ratio
  - E: Energy of ECAL Shower
  - P: Momentum from Track
  - $L_e = \ln(e) + 0.001; L_{other} = \ln(other) + 0.001$
  - Poor performance in low-momentum

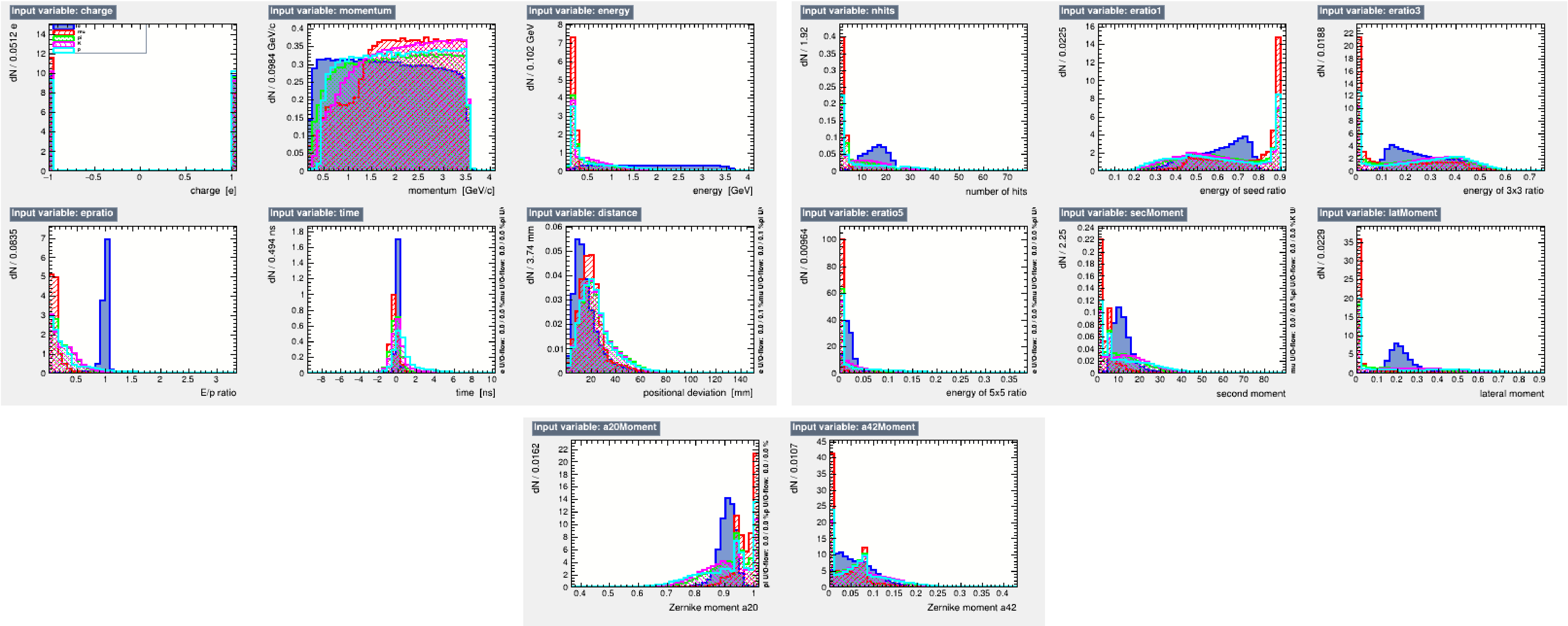


- BDT Method
  - Input variables: charge, P_{track}, E_{shower}, E/P, T_{seed}, $|R_{ext} - R_{shower}|$, N_{hits}, E_{seed}/E_{shower}, $(E_{3x3} - E_{seed})/E_{shower}$, $(E_{5x5} - E_{3x3})/E_{shower}$, second moment, lateral moment, A_{20} moment, A_{42} moment
  - Distinguishing electrons from other charged hadrons (or muon)
  - BDT Method used



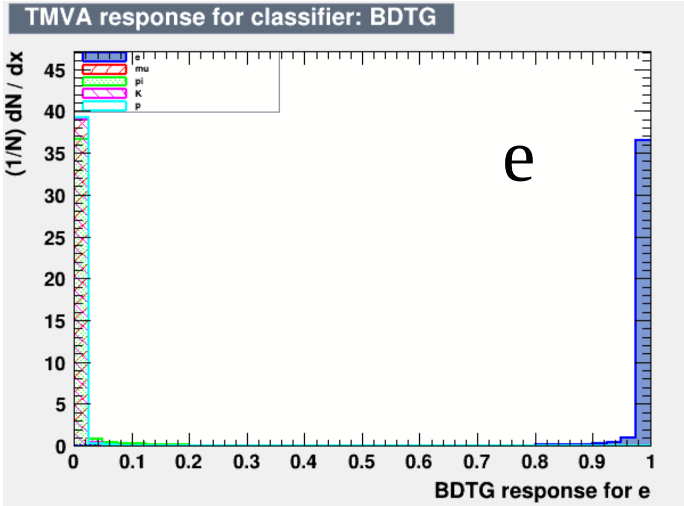


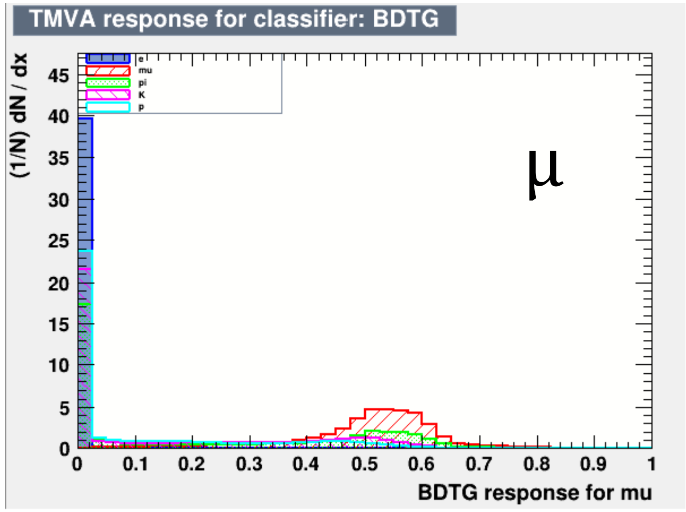
BDT Input

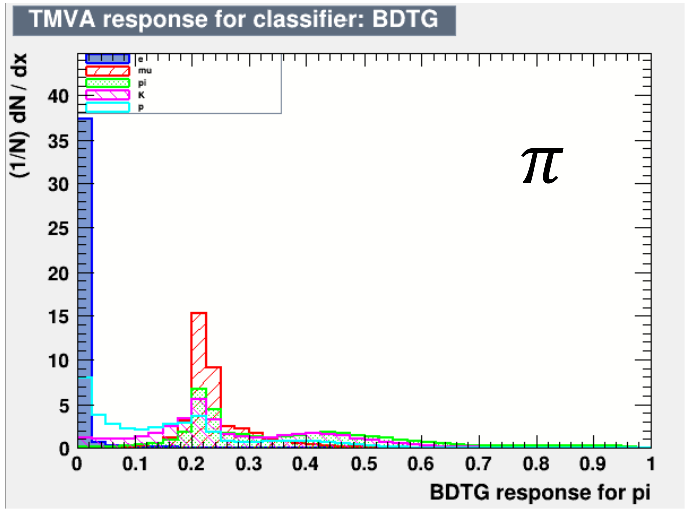


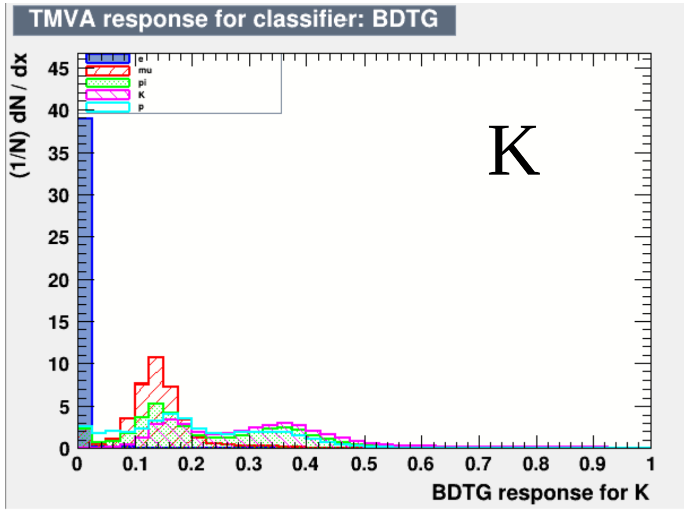
Input variable: charge
dN / 0.0512 e
charge [e]
Input variable: momentum
dN / 0.0984 GeV/c
momentum [GeV/c]
Input variable: energy
dN / 0.102 GeV
energy [GeV]
Input variable: nhits
dN / 1.92
number of hits
Input variable: eratio1
dN / 0.0225
energy of seed ratio
Input variable: eratio3
dN / 0.0188
energy of 3x3 ratio
Input variable: epratio
dN / 0.0835
E/p ratio
Input variable: time
dN / 0.494 ns
time [ns]
Input variable: distance
dN / 3.74 mm
positional deviation [mm]
Input variable: eratio5
dN / 0.00964
energy of 5x5 ratio
Input variable: secMoment
dN / 2.25
second moment
Input variable: latMoment
dN / 0.0229
lateral moment
Input variable: a20Moment
dN / 0.0162
Zernike moment a20
Input variable: a42Moment
dN / 0.0107
Zernike moment a42

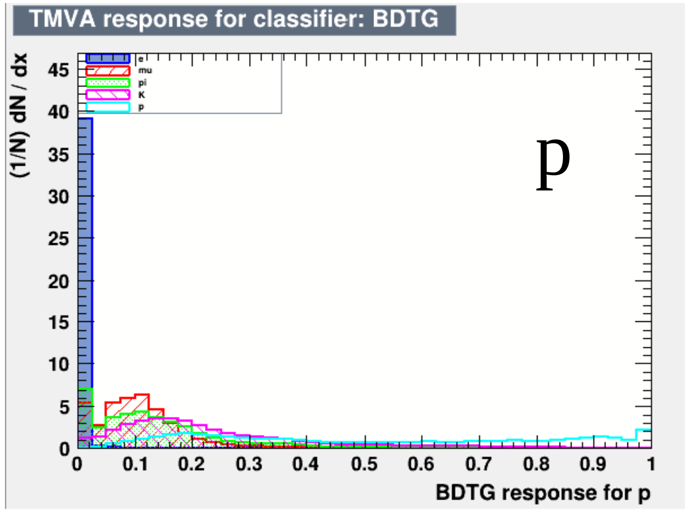
BDT Output


TMVA response for classifier: BDTG
(1/N) dN / dx
e
mu
pi
K
p
BDTG response for e
e


TMVA response for classifier: BDTG
(1/N) dN / dx
e
mu
pi
K
p
BDTG response for mu
μ


TMVA response for classifier: BDTG
(1/N) dN / dx
e
mu
pi
K
p
BDTG response for pi
π


TMVA response for classifier: BDTG
(1/N) dN / dx
e
mu
pi
K
p
BDTG response for K
K


TMVA response for classifier: BDTG
(1/N) dN / dx
e
mu
pi
K
p
BDTG response for p
p

- 桶部角分布相同
  - 共53圈（左右各加一圈）
- 端盖重新排列
  - 最外层与桶部最外层平行
  - 间距4cm
  - 散焦点10cm
  - 尺寸变小
  - 共8→9圈
- 端盖边界1640mm
- 体积 6.47 m^3
- 节约 11%