

SMASH: development and applications

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December 11th, 2025

Introduction

Simulating Many Accelerated Strongly-interacting Hadrons



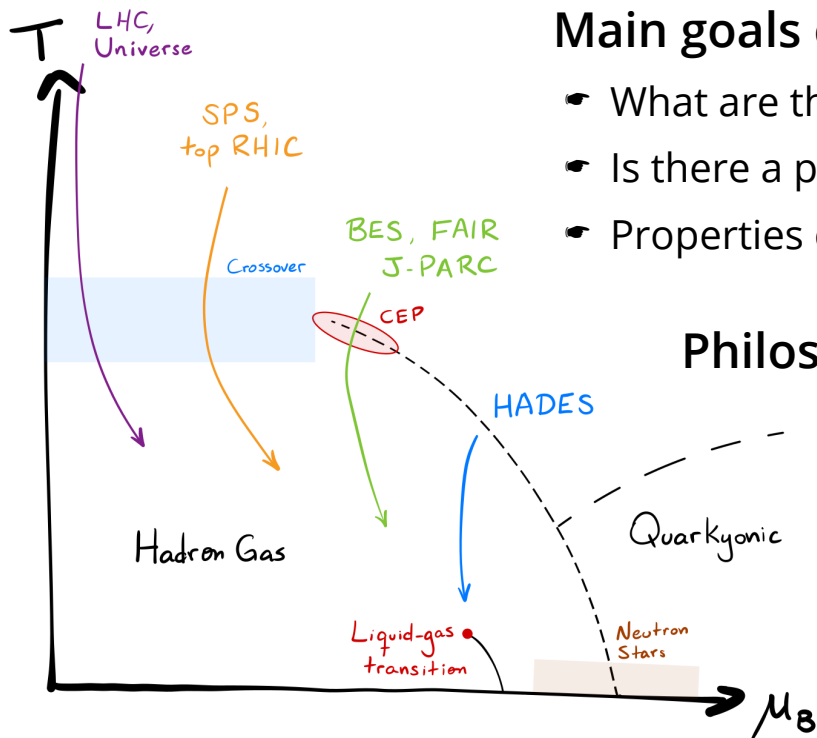
Main goals of our field:

- What are the relevant degrees of freedom at high densities?
- Is there a phase transition, critical endpoint?
- Properties of neutron star and their mergers?

Philosophy: to learn *new Physics*, we need a good baseline

SMASH: General purpose BUU hadronic transport, with underlying relativistic Boltzmann equation

$$p^\mu \frac{\partial f_i(x, p)}{\partial x^\mu} + m_i \frac{\partial [K^\mu f_i(x, p)]}{\partial p^\mu} = C_i^{\text{coll}}$$



Outline



- Basics of the SMASH approach
- Mean-field and studying the equation of state
- Beyond transport: coupling to hydrodynamics
- How rescattering affects fluctuation observables
- Dynamics of light nuclei production
- Beyond hadrons: hard and EM probes
- Clean code strategy

Basic ingredients

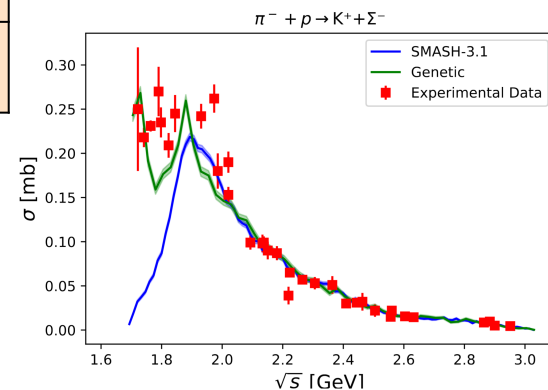
Degrees of freedom



Baryons						
N		Δ	Λ		Σ	Ξ
N ₉₃₈	N ₁₈₇₅	Δ_{1232}	Λ_{1116}	Λ_{1810}	Σ_{1189}	Ξ_{1321}
N ₁₄₄₀	N ₁₉₀₀	Δ_{1620}	Λ_{1405}	Λ_{1820}	Σ_{1385}	Ξ_{1530}
N ₁₅₂₀	N ₁₉₉₀	Δ_{1700}	Λ_{1520}	Λ_{1830}	Σ_{1660}	Ξ_{1690}
N ₁₅₃₅	N ₂₀₆₀	Δ_{1900}	Λ_{1600}	Λ_{1890}	Σ_{1670}	Ξ_{1820}
N ₁₆₅₀	N ₂₀₈₀	Δ_{1905}	Λ_{1670}	Λ_{2100}	Σ_{1750}	Ξ_{1950}
N ₁₆₇₅	N ₂₁₀₀	Δ_{1910}	Λ_{1690}	Λ_{2110}	Σ_{1775}	Ξ_{2030}
N ₁₆₈₀	N ₂₁₂₀	Δ_{1920}	Λ_{1800}	Λ_{2350}	Σ_{1915}	Ω
N ₁₇₀₀	N ₂₁₉₀	Δ_{1930}			Σ_{1940}	Ω_{1672}
N ₁₇₁₀	N ₂₁₉₀	Δ_{1950}			Σ_{2030}	Ω_{2250}
N ₁₇₂₀	N ₂₂₂₀				Σ_{2250}	

Mesons						
Light					Strange	
π_{138}	$\pi_{1(1600)}$	$a_0(980)$	σ_{800}	$f_2'(1525)$	K_{494}	$K_2^*(1430)$
$\pi_{(1300)}$	$\pi_{2(1670)}$	$a_{1(1260)}$	$f_0(980)$	$f_0(1710)$	K_{892}^*	$K_{(1680)}^*$
$\pi_{1(1400)}$	$\pi_{(1800)}$	$a_2(1320)$	$f_2(1275)$	$f_2(1950)$	$K_{1(1270)}$	$K_2(1770)$
η_{548}	$\eta_{(1405)}$	$a_0(1450)$	$f_1(1285)$	$f_2(2010)$	$K_{1(1400)}$	$K_3^*(1780)$
η'_{958}	$\eta_{(1475)}$	$a_4(2040)$	$f_0(1370)$	$f_4(2050)$	$K_{(1410)}^*$	$K_2(1820)$
$\eta_{(1295)}$	$\eta_{2(1645)}$	ϕ_{1019}	$f_1(1420)$	$f_2(2300)$	$K_0^*(1430)$	$K_4^*(2045)$
ρ_{778}	$\rho_{3(1690)}$	$\phi_{(1680)}$	$f_0(1500)$	$f_2(2340)$	<div><div>$\pi^- +$</div></div>	
$\rho_{(1450)}$	$\rho_{(1700)}$	$\phi_{3(1850)}$	ω_{783}	$\omega_{(1650)}$		
	$b_1(1235)$	$h_1(1170)$	$\omega_{(1420)}$	$\omega_{3(1670)}$		

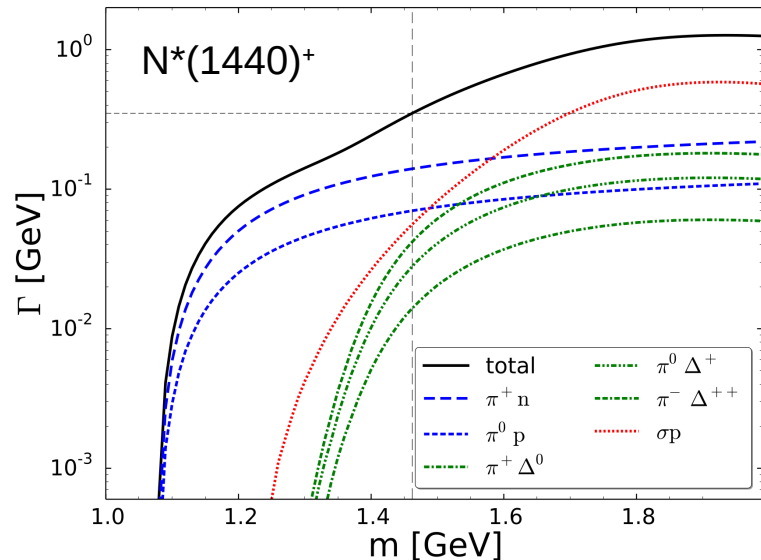
- Hadrons with 3 or 4-star rating from Particle Data Group
- Isospin symmetry assumed $\rightarrow m_{\pi^0} = m_{\pi^\pm} = 138$ MeV
- N* and Δ^* properties (mass and BR) recently tuned to strangeness production via a genetic algorithm



CB Rosenkvist, H Elfner (2025) PRC 112

5

Spectral functions & decay widths



- Threshold ~ masses of decay products
- Δ baryon much narrower than σ meson
- Isospin symmetry determines BR in a multiplet:

$$1 \otimes \frac{3}{2} \rightarrow \frac{1}{2} \Rightarrow \Gamma_{\pi^+ \Delta^0} : \Gamma_{\pi^0 \Delta^+} : \Gamma_{\pi^- \Delta^{++}} = 2 : 3 : 6$$

- Philosophy: vacuum properties

$$\mathcal{A}^{\text{vac}}(m) = \frac{2\mathcal{N}}{\pi} \frac{m^2 \Gamma^{\text{dec}}(m)}{(m^2 - M_0^2)^2 + m^2 \Gamma^{\text{dec}}(m)^2} \quad \text{Breit-Wigner distribution}$$

- Resonance lifetimes ~ inverse width

$$P_{\text{dec}}(t) = 1 - e^{-\Gamma^{\text{dec}}(m)t}$$

$$\Gamma_R^{\text{dec}}(m) = \sum_{\{ab\}} \Gamma_{R \rightarrow ab}(m)$$

- Mass-dependence a la Manley-Saleski

$$\Gamma_{R \rightarrow ab}(m) = \text{BR}(R \rightarrow ab) \Gamma_0 \frac{\rho_{ab}(m)}{\rho_{ab}(M_0)}$$

$$\rho_{ab}(\sqrt{s}) = \int dm_a dm_b \mathcal{A}_a^{\text{vac}}(m_a) \mathcal{A}_b^{\text{vac}}(m_b) \frac{|\mathbf{p}_{\text{cm}}|}{\sqrt{s}} B_L^2(|\mathbf{p}_{\text{cm}}|) \mathcal{F}_{ab}^2(\sqrt{s})$$

Available phase space

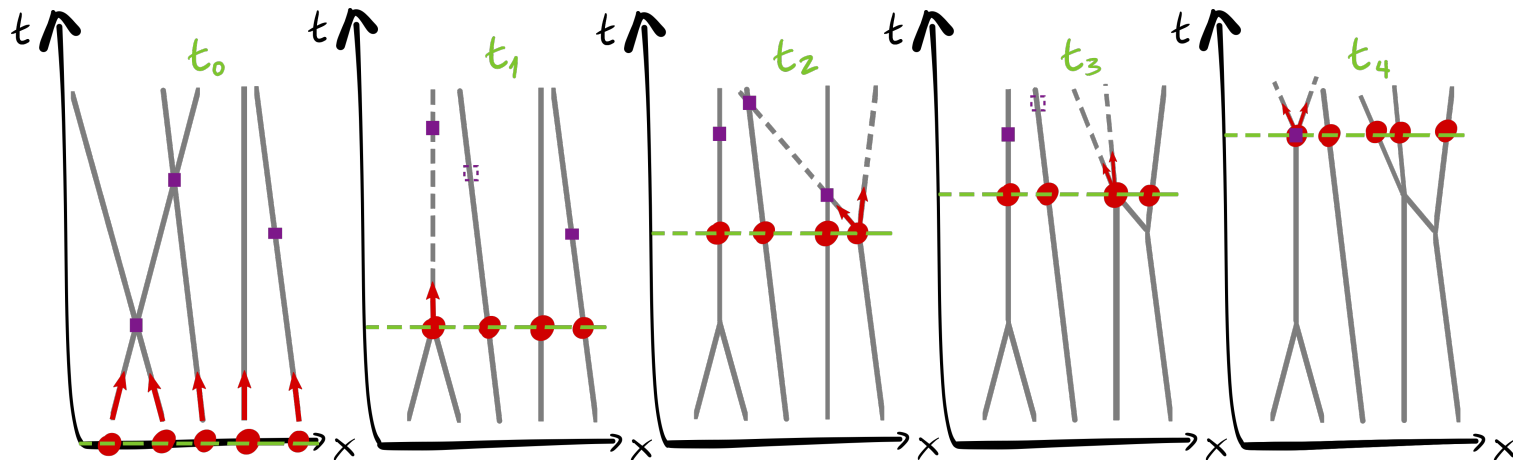
Actions & cascade

$$p^\mu \frac{\partial f_i(x, p)}{\partial x^\mu} + m_i \frac{\partial [K^\mu f_i(x, p)]}{\partial p^\mu} = C_i^{\text{coll}}$$

0



Without mean-field, trajectories between interactions are straight lines!



Action: Generic *possible* interaction in collision term

SMASH searches for upcoming **actions** between **particles** and propagates, performing them according to a given criterion and **time-ordering**, ignoring now-invalid actions

Collision criteria



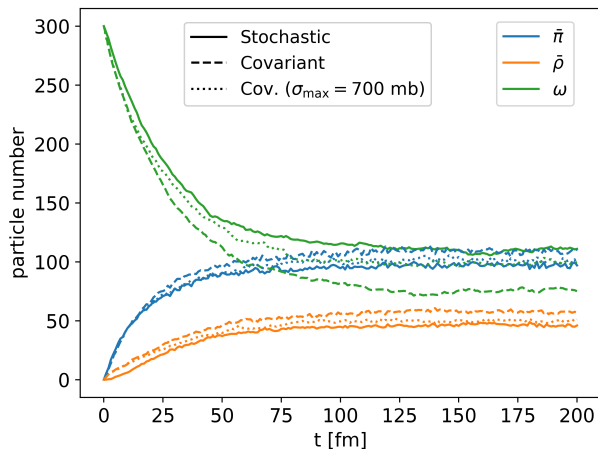
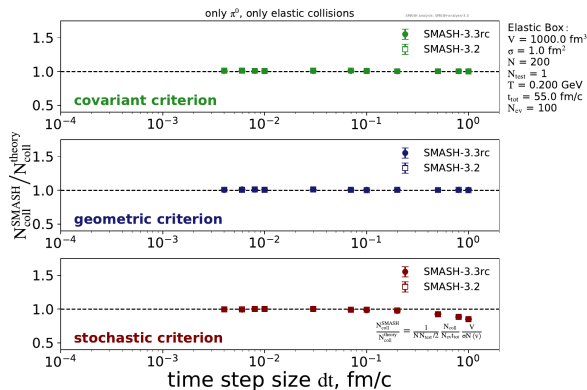
Geometric → covariant $\pi d_{\perp}^2 \leq \sigma_{ab}$

$$d_{\perp}^2 = |\vec{x}|^2 - \frac{(\vec{x} \cdot \vec{p})^2}{|\vec{p}|^2} \longrightarrow d_{\perp}^2 = -x^2 - \frac{p_a^2(p_b \cdot x)^2 + p_b^2(p_a \cdot x)^2 - 2(p_a \cdot x)(p_b \cdot x)(p_a \cdot p_b)}{(p_a \cdot p_b)^2 - p_a^2 p_b^2}$$

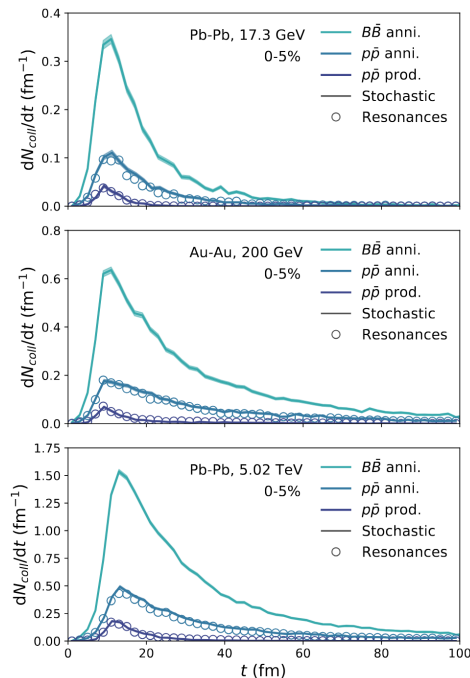
$$t_c = -\frac{\vec{x} \cdot \vec{v}}{|\vec{v}|^2} \longrightarrow t_c = \frac{1}{2} \frac{(P \cdot x)(P \cdot p) - P^2(p \cdot x)}{(p_a \cdot p)(P \cdot p_b) - (p_b \cdot p)(P \cdot p_a)}$$

Stochastic $P_{ab \rightarrow X} = \frac{\Delta t}{\Delta^3 x} v_{\text{rel}} \sigma_{ab \rightarrow X}$

Geometric criterions misbehave in edge cases (resonances away from pole mass)



Consistent reaction rates in $p\bar{p} \leftrightarrow 5\pi$



Interaction cross sections



- **Total cross section:** built from partial processes or parametrized from data
- **Resonances** for low energies
- **PYTHIA strings** for high interaction energies + formation time for leading hadrons
- **Elastic** (BB and MB) and **Binary inelastic** (NN and NK) scattering parametrized
- **AQM rescaling** for colliding resonances

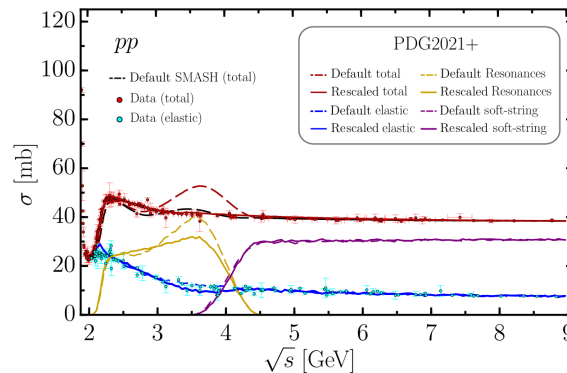
BottomUp

TopDown

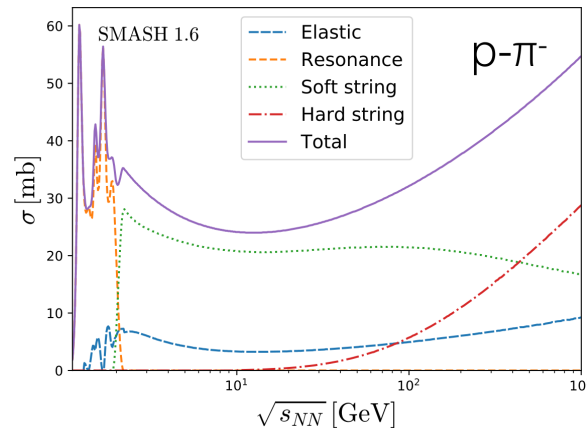
Detailed balance

$$\sigma_{ab \rightarrow R}(\sqrt{s}) = \frac{g_R}{g_a g_b} (\delta_b^a + 1) \frac{2\pi^2}{p_{\text{cm}}^2} \Gamma_{ab \rightarrow R}(\sqrt{s}) \mathcal{A}_R(\sqrt{s})$$

$$\sigma_{AB} = \sigma_{pp} \frac{n_q^A}{3} \frac{n_q^B}{3} (1 - 0.4x_s^A) (1 - 0.4x_s^B)$$



J.S.S. Martin, RGH, et al.
[arXiv:2309.01737]



J. Mohs, S. Ryu and H. Elfner,
J.Phys.G 47 (2020)

Mean-field potentials & Equation of state

Numerical algorithm

$$f(\mathbf{r}, \mathbf{p}) = \frac{1}{N_{\text{test}}} \sum_j^{N_{\text{test}}} G(\mathbf{r} - \mathbf{r}_i) \delta^3(\mathbf{p} - \mathbf{p}_i)$$

Testparticle ansatz



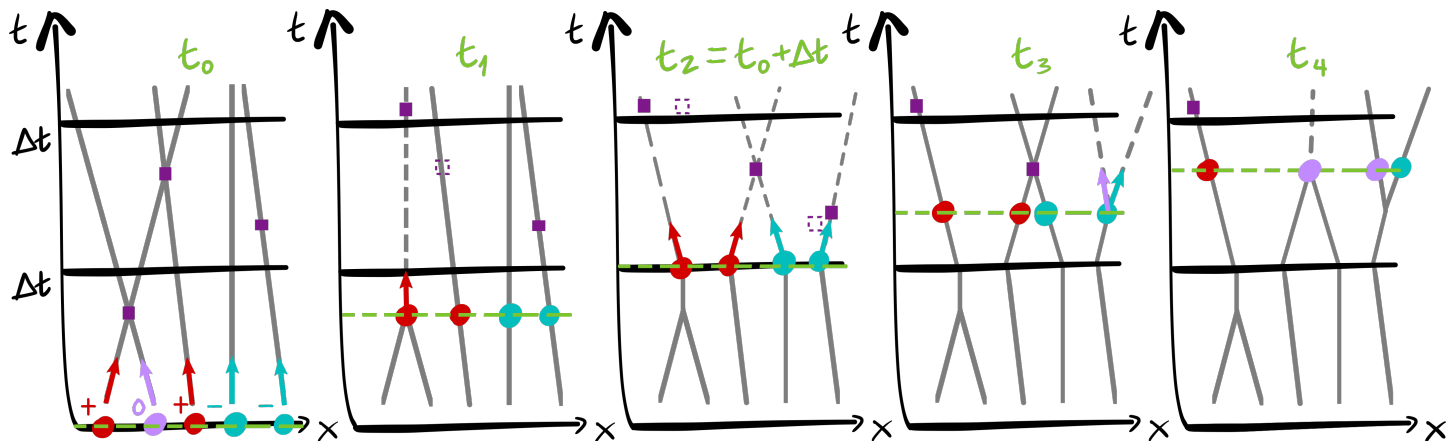
Equations of motion

$$\dot{\mathbf{r}}_i = \frac{\mathbf{p}_i}{\sqrt{p_i^2 + m^2}} + \nabla_{\mathbf{p}} U$$

$$\dot{\mathbf{p}}_i = -\nabla_{\mathbf{r}} E_i \longrightarrow \text{Divide spacetime in 4D lattice cells}$$

$$E = \sqrt{p^2 + m^2} + U(\rho_B, \mathbf{p}) \quad \text{Evaluated in LRF}$$

At each timestep, \mathbf{r} and \mathbf{p} are updated (Euler). Inbetween, particles propagate and actions are performed as in cascade.



Available potentials



- NN potential: **Skyrme + Symmetry**

$$U_{\text{Skyrme}} = A \left(\frac{\rho_B}{\rho_0} \right) + B \left(\frac{\rho_B}{\rho_0} \right)^\tau$$

$$U_{\text{sym}} = \pm S_{\text{pot}} \left(\frac{\rho_{I_3}}{\rho_0} \right) \quad \text{Only for baryons}$$

- Alternative: fully relativistic **VDF**

$$A^\mu = \sum_{i=1}^N C_i \left(\frac{\rho}{\rho_0} \right)^{b_i-2} \frac{j^\mu}{\rho_0}$$

A. Sorensen, V. Koch (2021) PRC 104 3

- **Coulomb** (magnetostatic)

$$\mathbf{E}(\mathbf{r}_j) = \sum_{i \neq j} \frac{\rho(\mathbf{r}_i)(\mathbf{r}_j - \mathbf{r}_i)}{|\mathbf{r}_j - \mathbf{r}_i|^3} \Delta V$$

$$\mathbf{B}(\mathbf{r}_j) = \sum_{i \neq j} \mathbf{j}(\mathbf{r}_i) \times \frac{\mathbf{r}_j - \mathbf{r}_i}{|\mathbf{r}_j - \mathbf{r}_i|^3} \Delta V$$

Without nuclear potential,

Gold
Time: 0 fm



Fermi Motion + Potentials



Only Fermi Motion



it potentially goes nuclear!

Momentum dependence

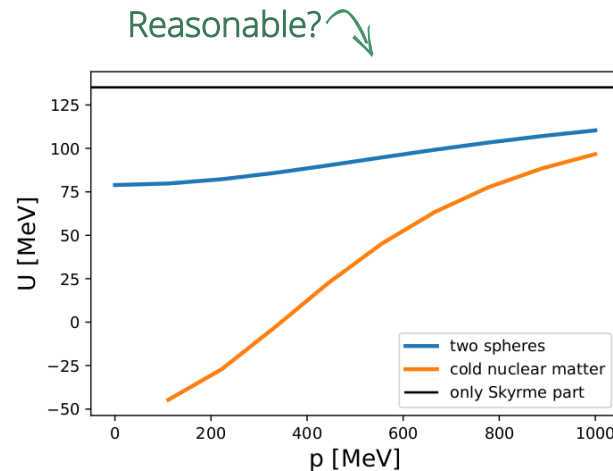
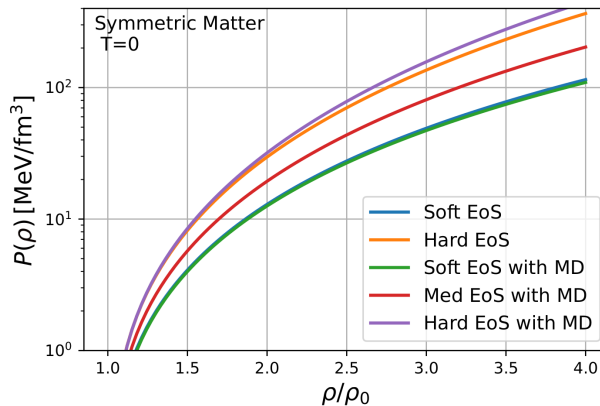
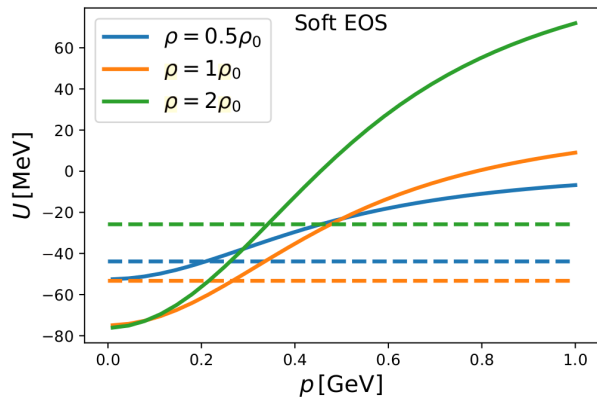


Optical model: experimental data depends on kinetic energy of probe

$$U_{\text{MD}} = \frac{2C}{\rho_0} g \int \frac{d^3 p'}{(2\pi)^3} \frac{f(\mathbf{r}, \mathbf{p}')}{1 + \left(\frac{\mathbf{p} - \mathbf{p}'}{\Lambda}\right)^2}$$

G. M. Welke et al. (1988) Phys.Rev.C 38
Used in GiBUU: O. Buss et al. (2012) Phys.Rept. 512

Analytical solution by assuming cold nuclear matter $f(\vec{r}, \vec{p}) = \Theta(p_F - p)$

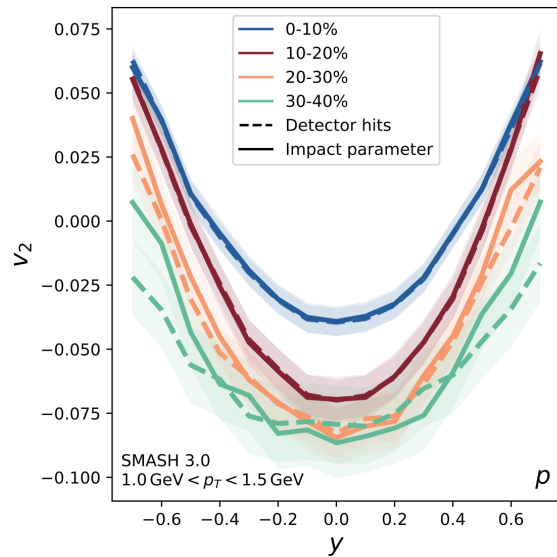


J. Mohs (2025) PhD thesis

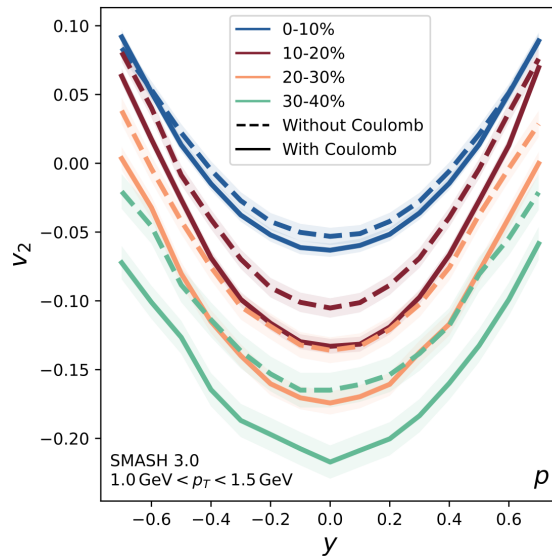
13

Bayesian analysis

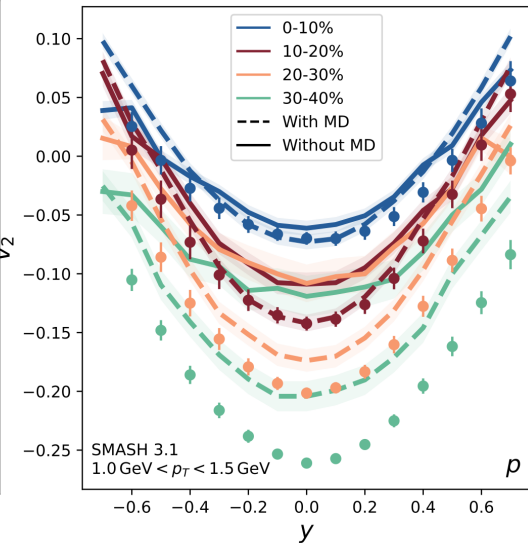
- SMASH with different mean field settings vs. HADES flow data for protons and deuterons in 4 centrality classes
- Many events required to calculate flow coefficients → Gaussian process



Centrality selection does not matter at midrapidity



Coulomb potential important and included



Momentum dependence crucial for elliptic flow strength

Maximum posterior parameters



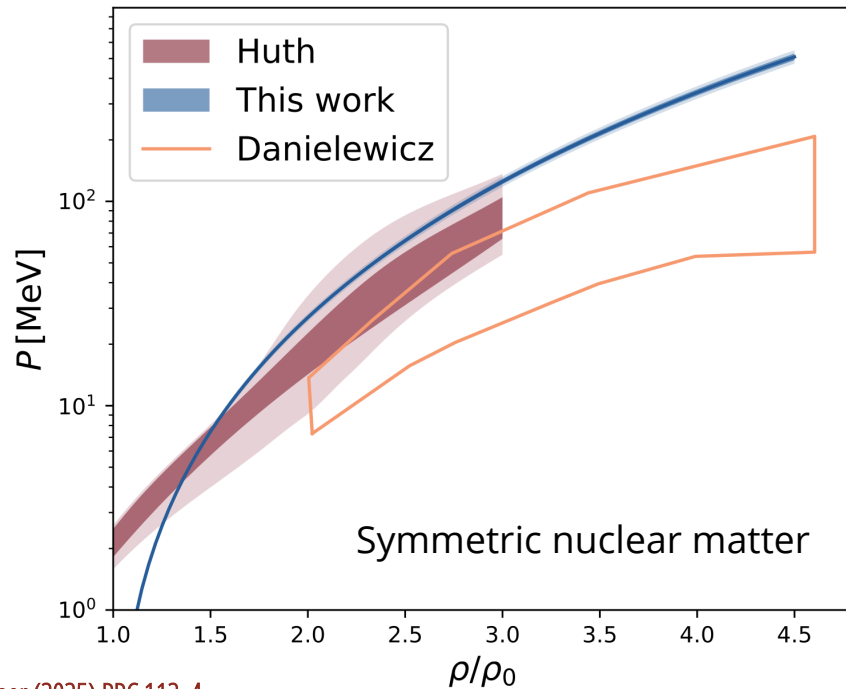
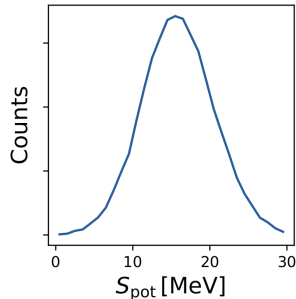
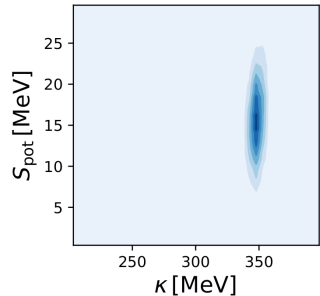
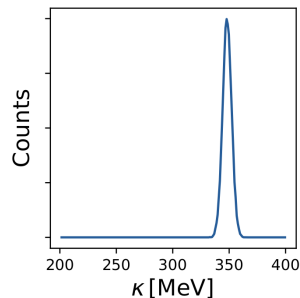
68.3% confidence:

$$\kappa = 348.2^{+4.0}_{-3.9} \text{ MeV}$$

Relatively stiff

$$S_{\text{Pot}} = 15.8^{+4.7}_{-4.6} \text{ MeV}$$

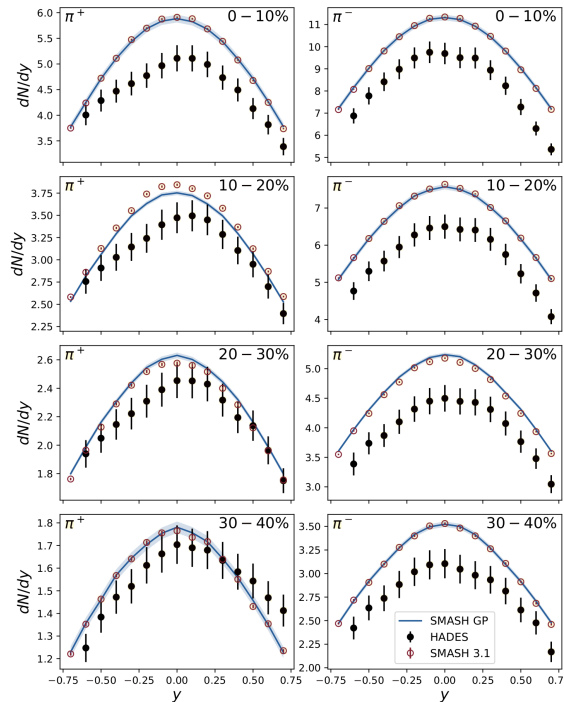
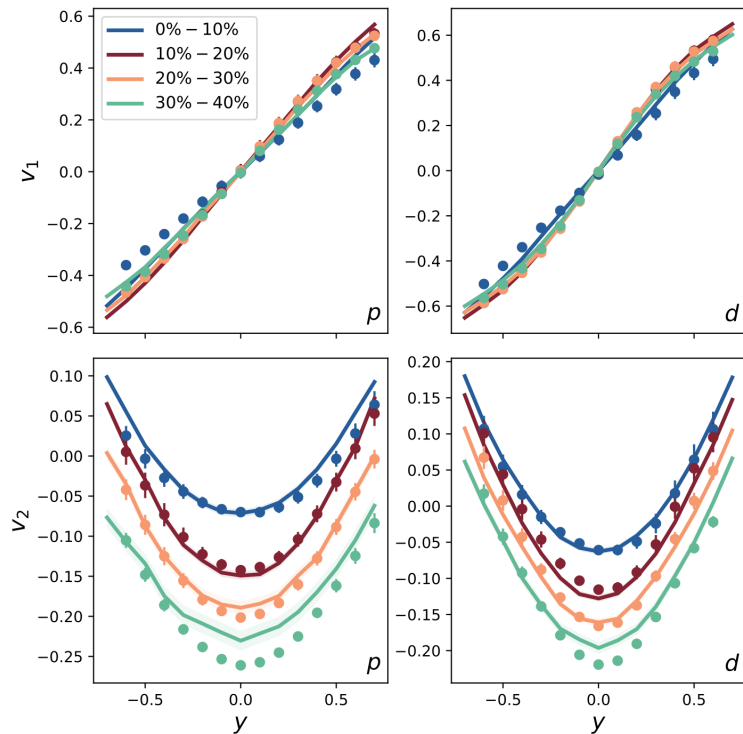
Consistent with previous studies but not so sensitive



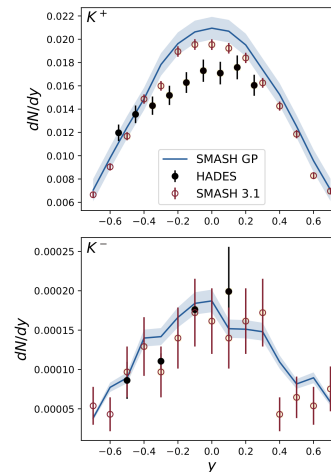
J. Mohs, S. Spies, H. Elfner (2025) PRC 112 4

15

Comparison to data



J. Mohs (2025) PhD thesis



Good agreement for baryons, but not meson spectra

Symmetry potential for all hadrons?

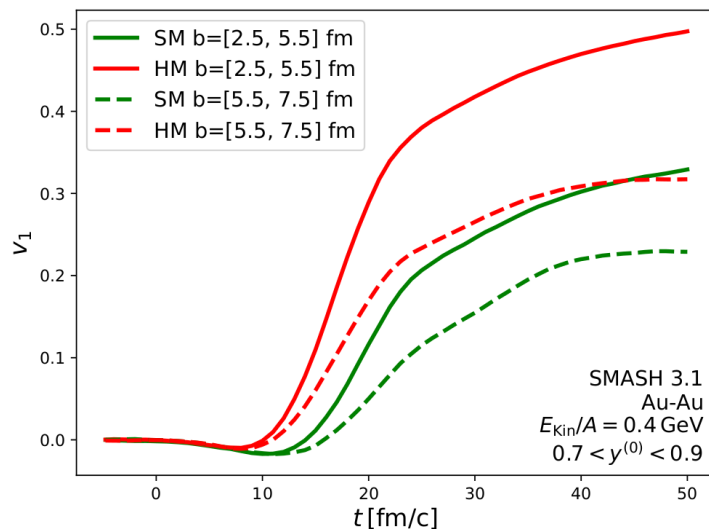
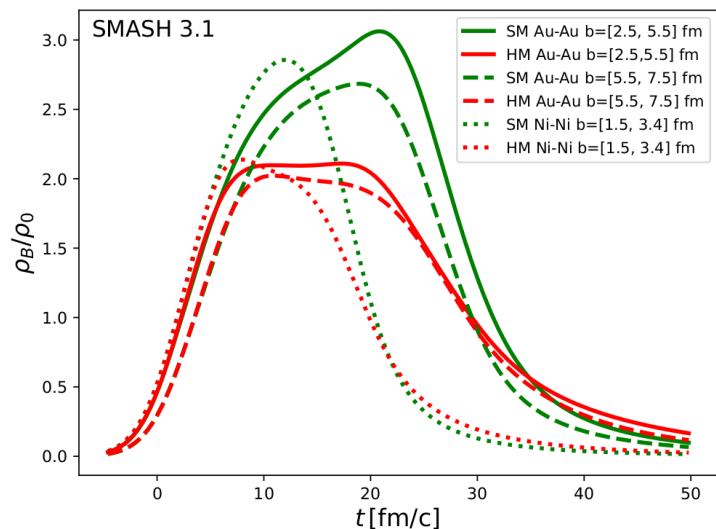
J. Mohs, S. Spies, H. Elfner (2025) PRC 112 4

16

Evolution of the medium Without Coulomb!



- Densities, medium lifetime, and consequently directed flow scale with system size as expected
- Soft EoS allows for more compression → weaker bounce-off



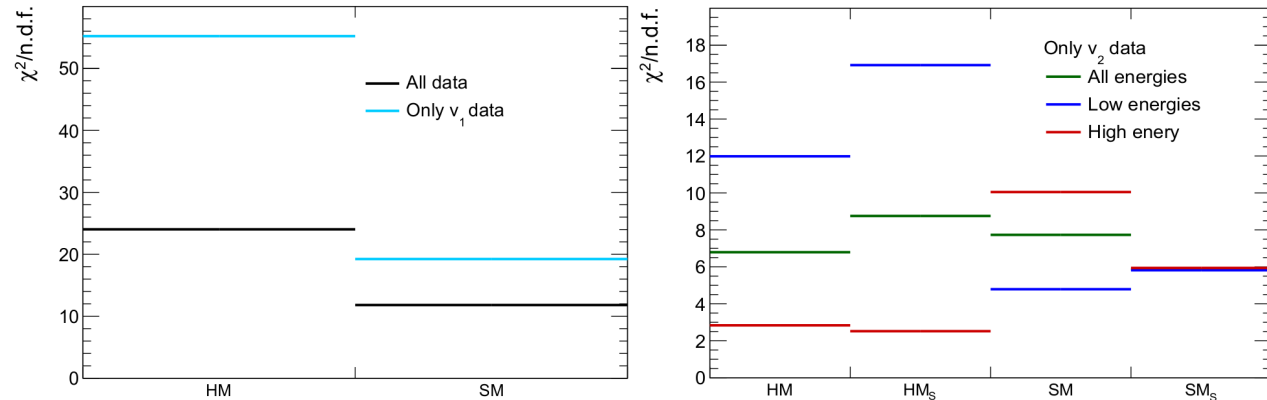
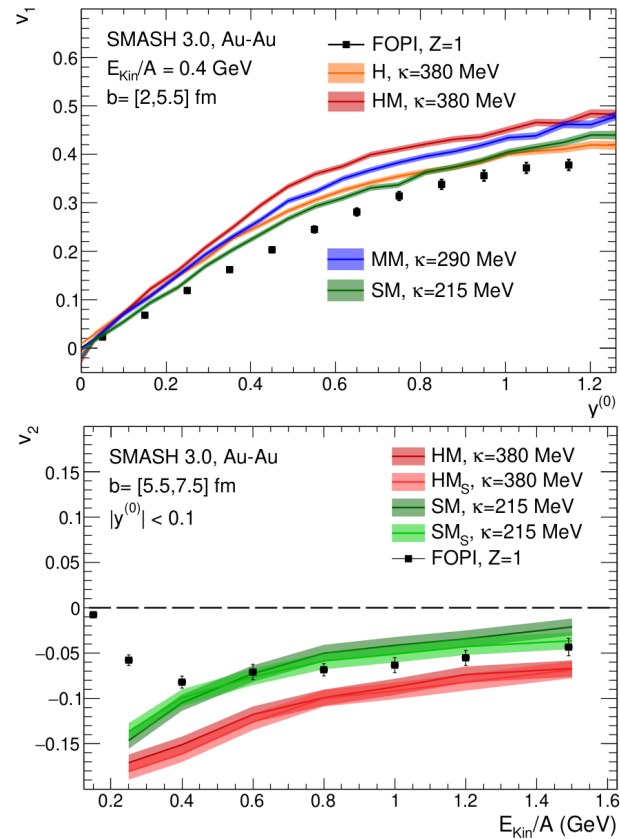
L. Tarasovicova, J. Mohs, A. Andronic, H. Elfner and K.-H. Kampert EPJA 60 (2024), FAIR-NRW network

Comparison to FOPI

Without Coulomb!



- Overall data (spectra and flow) favors soft momentum dependent EoS, v_1 alone as well
- v_2 at high energies asks for hard MD EoS, but soft MD is not very far off



L. Tarasovicova, J. Mohs, A. Andronic, H. Elfner and K.-H. Kampert EPJA 60 (2024), FAIR-NRW network

18

Interlude: kaon flow & KN potential

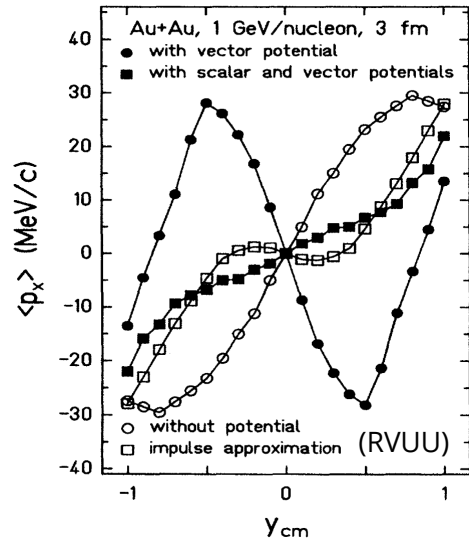


FOPI and E895 data consistent with **repulsive vector + attractive scalar** KN potential

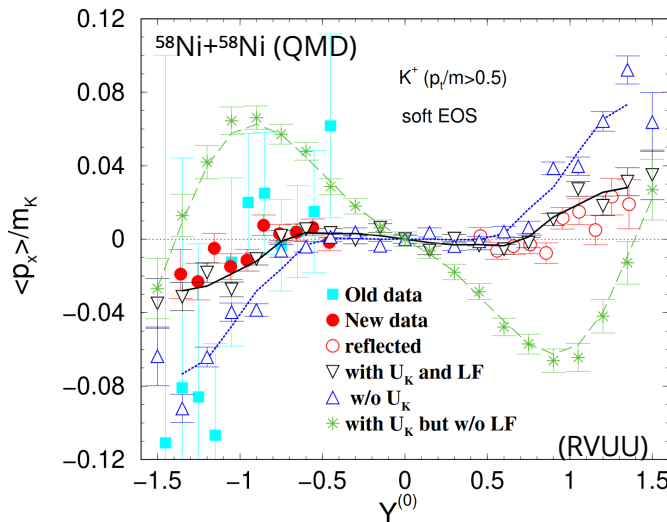
$$U(\rho, \mathbf{k}) = \omega(\rho, \mathbf{k}) - \omega_0(\mathbf{k})$$

$$= \sqrt{\mathbf{k}^2 + m_K^2 - \frac{\Sigma_{KN}}{f_\pi^2} \rho_s + V_0^2} \pm V_0 - \sqrt{\mathbf{k}^2 + m_K^2}$$

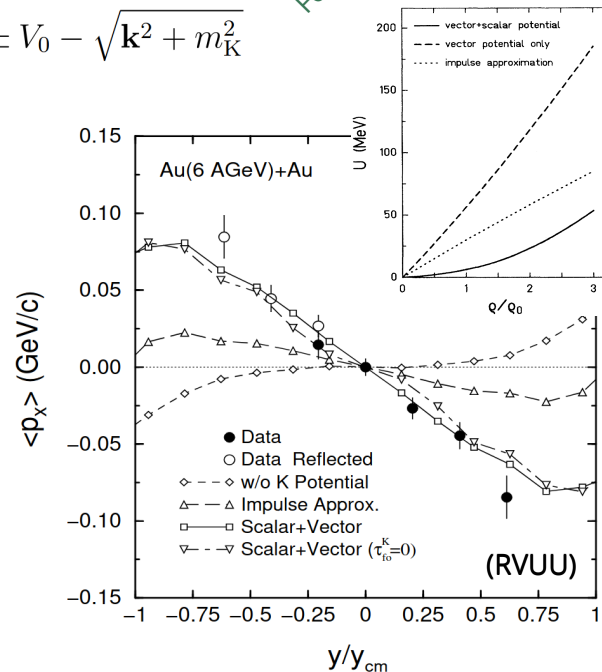
+Lorentz Force



G. Q. Li, C. M. Ko, and Bao-An Li (1995) PRL 74(2)



Y.M. Zheng, C. Fuchs, A. Faessler, and Y.P. Yan (2004) PRC 69

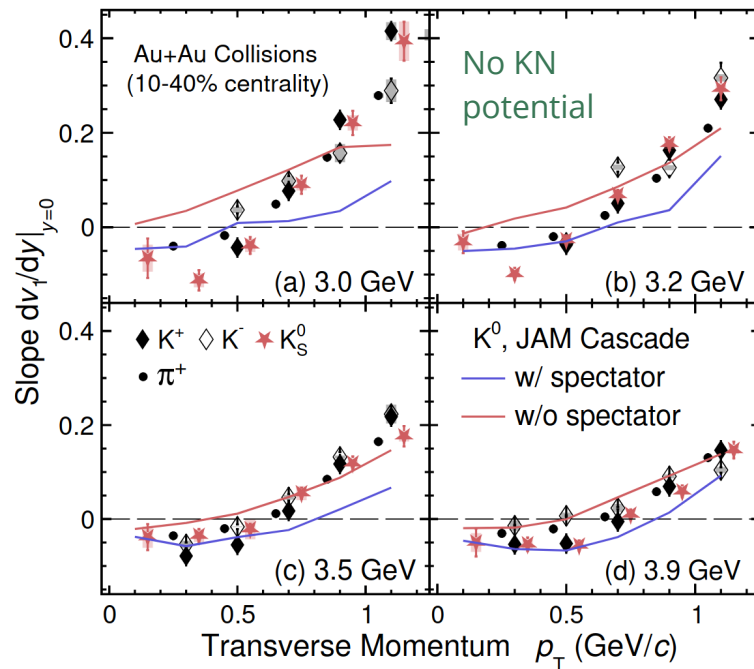


S. Pal, C. M. Ko, Z. Lin, B. Zhang (2000) Phys.Rev.C62

Interlude: kaon flow & KN potential



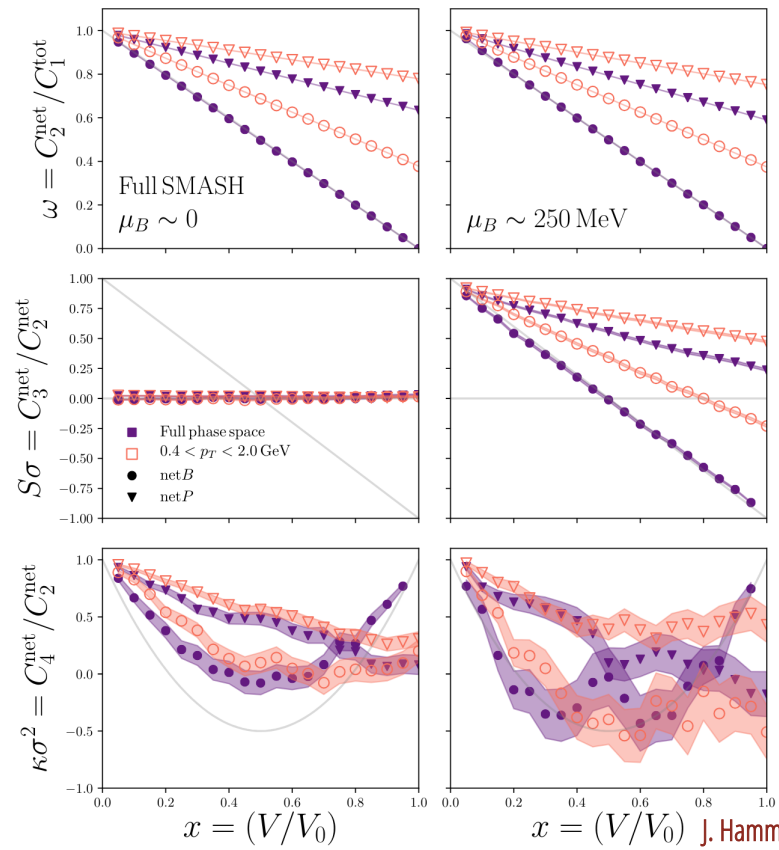
But! STAR analysis from this year says it might due spectator shadowing



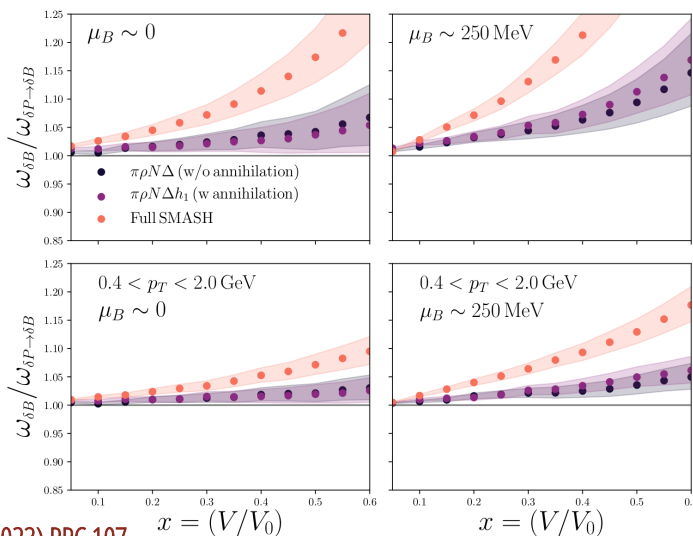
STAR Collaboration, 2503.23665 [nucl-ex]

**Fluctuation
observables**

Effect of conservation laws



- Charges are conserved in every interaction
- Are net-proton fluctuations good proxies for net-baryon?
- Dependence on phase space volume available



J. Hammelmann et al. (2023) PRC 107

Survival of critical fluctuations



Critical fluctuations of σ field contribute to the net/total particle number cumulant

$$\langle(\delta\sigma)^n\rangle_c = \left(\frac{T}{VH_0}\right)^{n-1} \frac{\partial^{n-1}M}{\partial h^{n-1}} \Big|_r$$

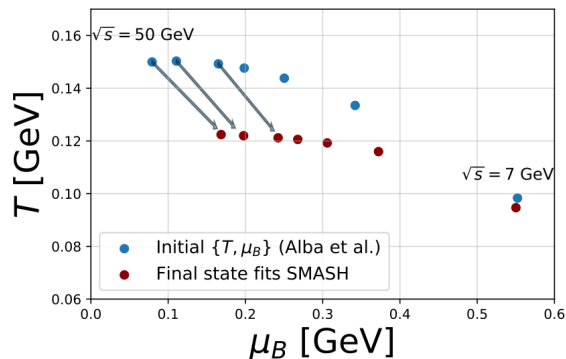
Taken from Ising mapping
M. Bluhm et al. (2017) EPJC 77, 210

$$\kappa_n^{\text{net}} = \kappa_n^p + (-1)^n \kappa_n^{\bar{p}} + (-1)^n \langle(V\delta\sigma)^n\rangle_c (I_p - I_{\bar{p}})^n$$

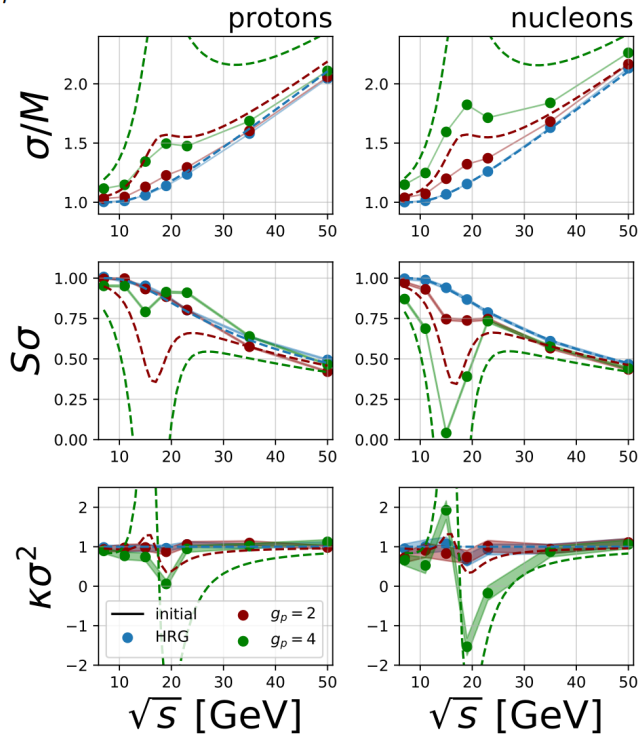
$$\kappa_n^{\text{tot}} = \kappa_n^p + \kappa_n^{\bar{p}} + (-1)^n \langle(V\delta\sigma)^n\rangle_c (I_p + I_{\bar{p}})^n$$

$$I_i = \frac{g_i d_i}{T} \int \frac{d^3k}{(2\pi\hbar)^3} \frac{f_{i,k}^0}{\gamma_{i,k}}$$

Generate distributions with above cumulants and plug into expanding sphere, using full SMASH hadronic dynamics



Signal can survive only if coupling is strong enough



J. Hammelmann et al. (2024) PRC 110

23

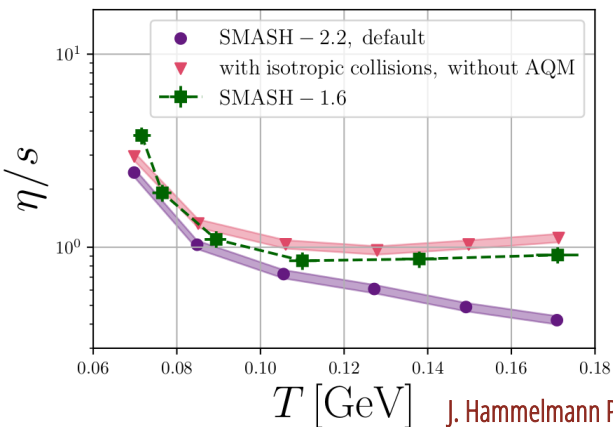
Transport coefficients

Shear viscosity and conductivities for conserved charges (B,Q,S) as functions of temperature

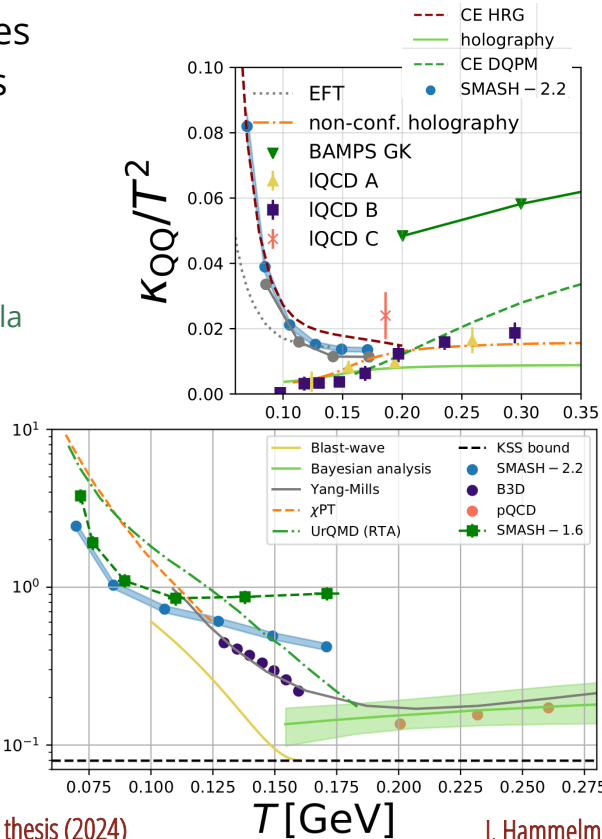
$$\eta = \frac{V}{T} \int \langle T^{ij}(t) T^{ij}(0) \rangle dt$$

$$\kappa_{ij} = \frac{V}{3} \int \langle \vec{J}_i(t) \vec{J}_j(0) \rangle dt.$$

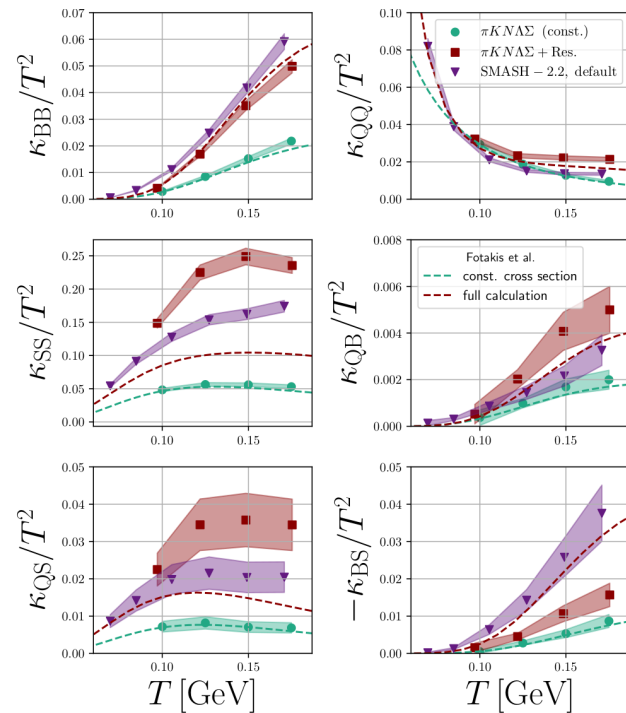
Kubo formula



J. Hammelmann PhD thesis (2024)



J. Hammelmann, J. Staudenmaier and H. Elfner (2025), PRC 111



24

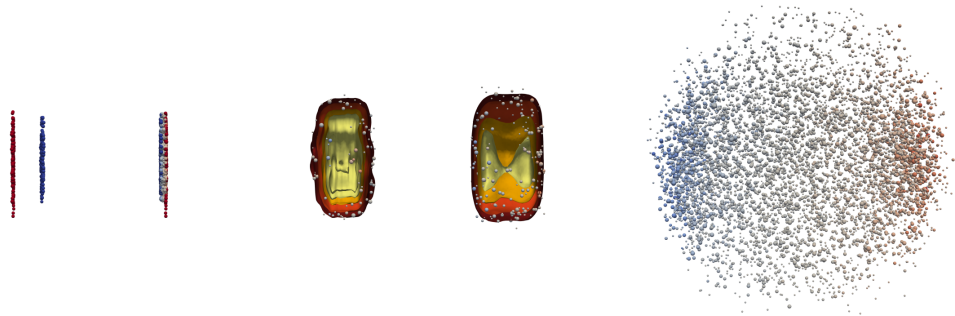
Coupling to hydrodynamics

Hybrid approach

<https://github.com/smash-transport/smash-vhll-hybrid>



SMASH-vHLL-Hybrid



IC & Initial Propagation

QGP & Hydrodynamic Expansion

Hadronic Rescattering

- Modular hybrid approach for high and intermediate energy HICs
- Hybrid-handler: Framework for testing and integration of modules
- Fully open source and public

SMASH

- Woods-Saxon nuclei
- Fluid formed at nuclear passing time τ_0

P. Huovinen et al.: EPJA 48 (2012)
Iu. Karpenko et al.: CPC 185 (2014)

vHLL

- (3+1)D Israel-Stewart
- Cornelius routine for hypersurface finding

smash-hadron-sampler

- Cooper-Frye particlization
- Viscous corrections

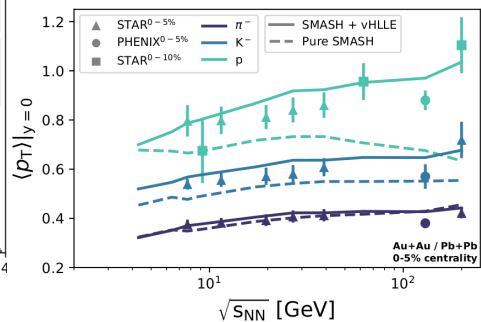
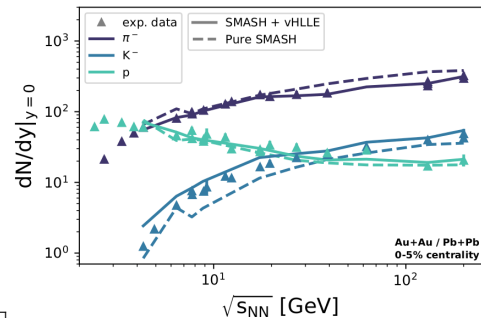
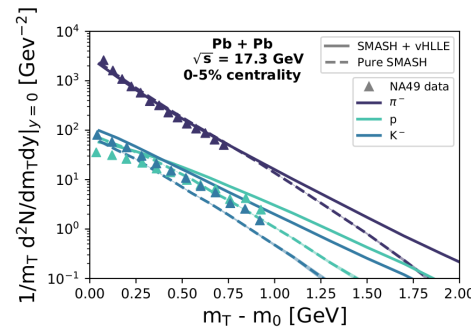
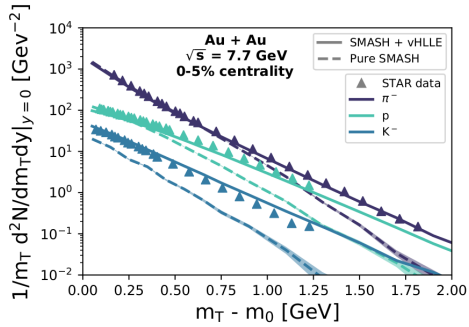
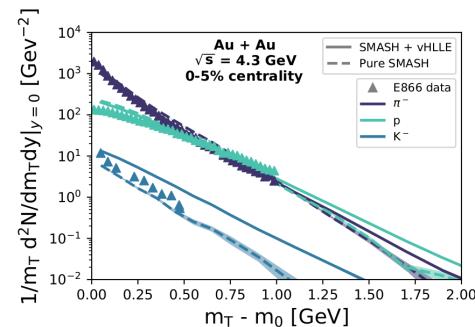
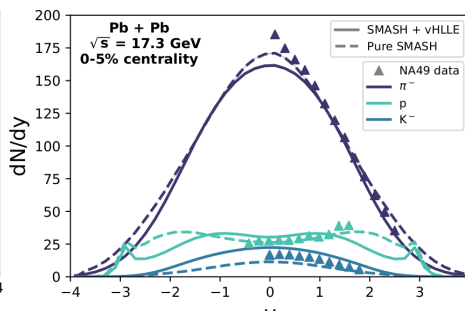
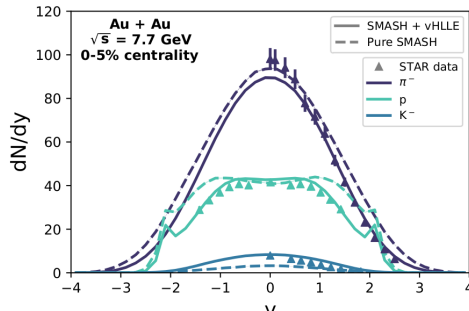
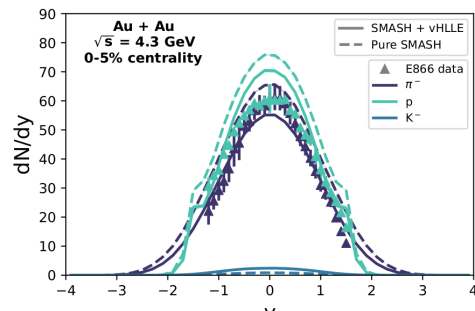
Iu. Karpenko et al.: PRC 91, 064901 (2015)
A. Schäfer et al., EPJA 58 (2022)

SMASH

- Hadronic rescattering until freezeout

Spectra and excitation functions

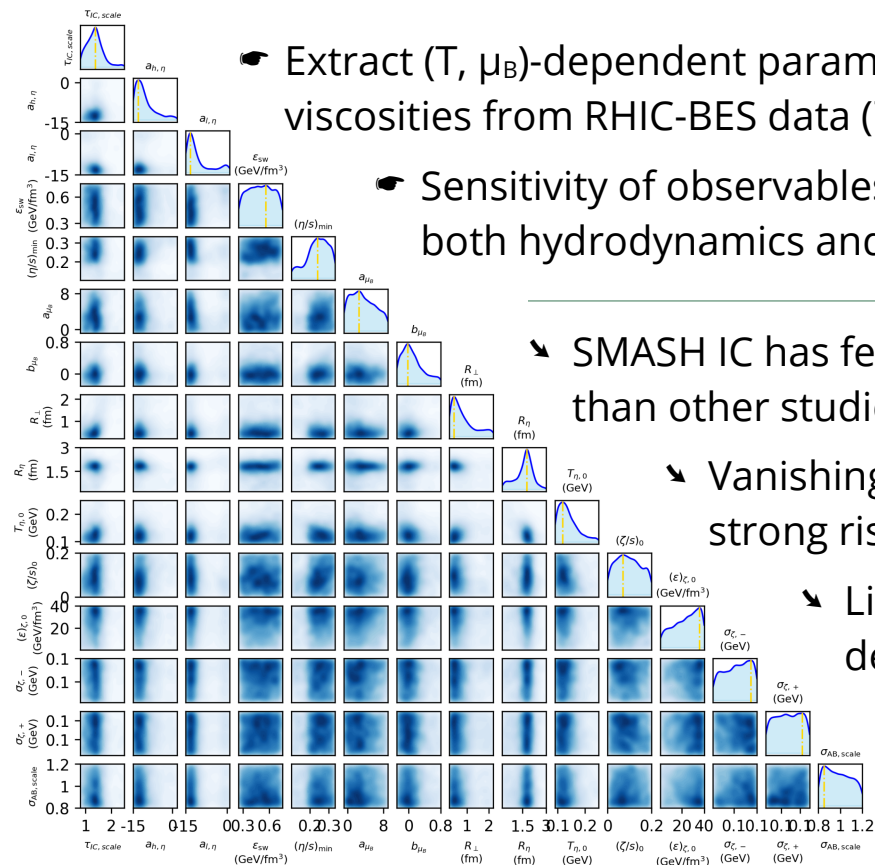
- Hybrid approach in decent agreement with measurements
- Midrapidity yields and m_T spectra well described over large range of beam energies by hybrid ($\langle p_T \rangle$ too small in pure SMASH)



Smearing/viscosity was tuned for each energy individually and kept constant

A. Schäfer, Iu. Karpenko, X-Y Wu, J. Hammelmann, H. Elfner (2022) EPJA 58

Bayesian analysis



Extract (T, μ_B) -dependent parameterizations of viscosities from RHIC-BES data (7.7, 19.6, 200 GeV)

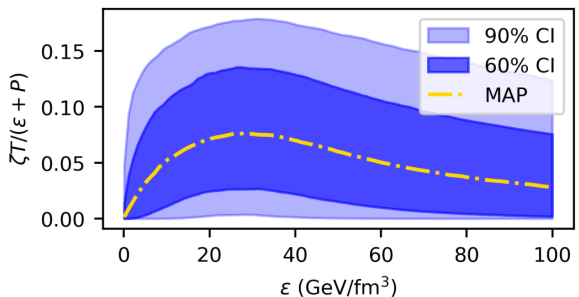
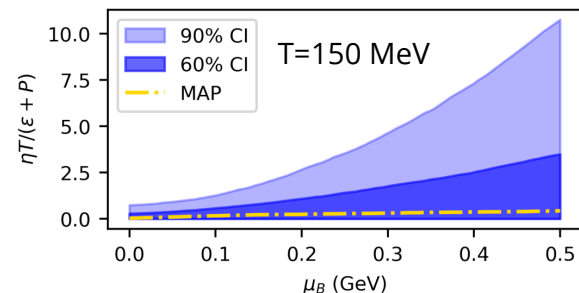
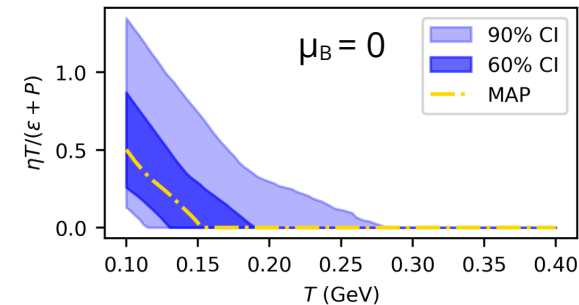
Sensitivity of observables on parameters from both hydrodynamics and hadronic transport

SMASH IC has fewer free parameters than other studies in literature

Vanishing shear viscosity and strong rise in hadronic regime

Little constraints on μ_B dependence

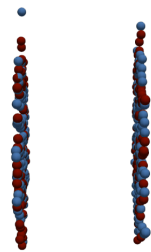
Finite bulk viscosity required



N. Götz, Iu. Karpenko, and H. Elfner. (2025) PRC 112
Earlier analysis on similar data: Shun et al. (2024) PRL 132

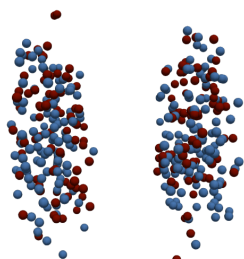
Hydro at lower energies?

$$\sqrt{s_{NN}} = 200 \text{ GeV}$$



$$\gamma = 106$$

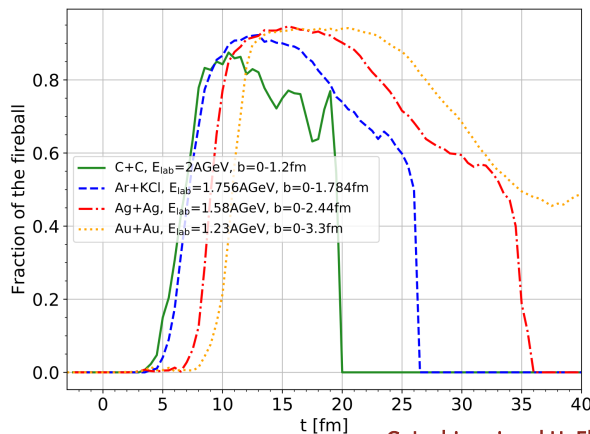
$$\sqrt{s_{NN}} = 5 \text{ GeV}$$



$$\gamma = 2.7$$

Coarse-grained SMASH

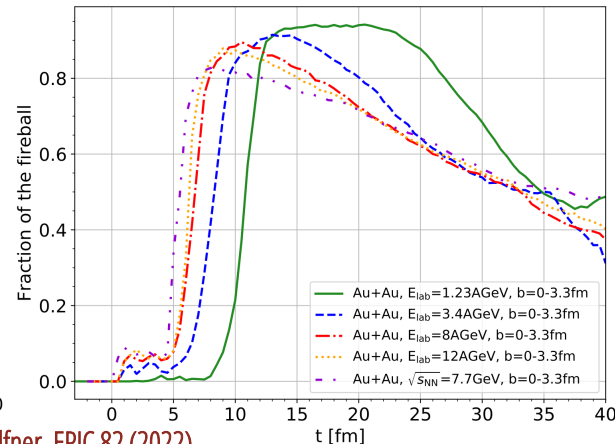
Fraction of the fireball close to local equilibrium (X, Y < 0.3)



G. Inghirami and H. Elfner, EPJC 82 (2022)

X: pressure anisotropy

Y: off-diagonality in $T^{\mu\nu}$



- Hadronic medium is partially “thermalized” even at low energies
- **IF** we use hydrodynamics, the initial conditions cannot be isochronous

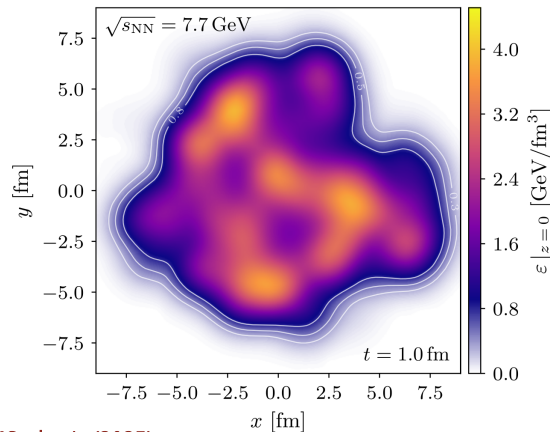
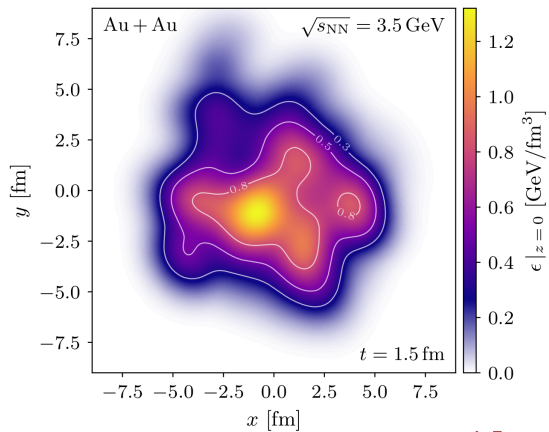
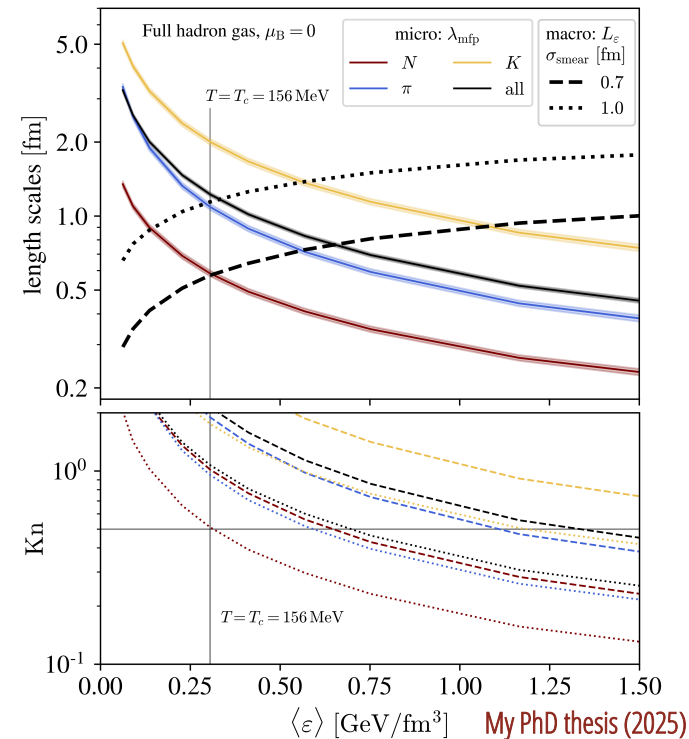
Local equilibration



Box calculation

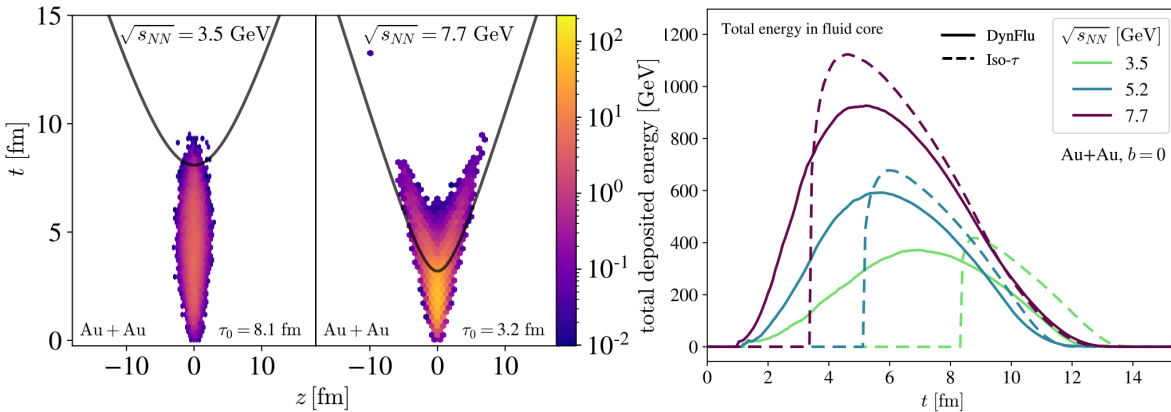
$$\frac{1}{L_\varepsilon}(t, x) \equiv \left| \frac{\nabla \varepsilon(t, x)}{\varepsilon(t, x)} \right|$$

- Mean free path and Knudsen number decrease with temperature, thus with local energy density
- We can use this to decide dynamically which regions of spacetime should become fluid
- Stricter threshold \rightarrow less fluid
- Automatic core-corona separation



J. Egger MSc thesis (2025)

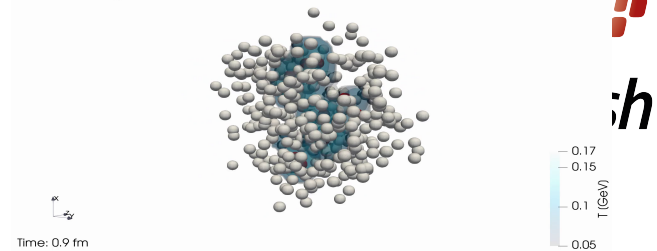
Dynamic fluidization



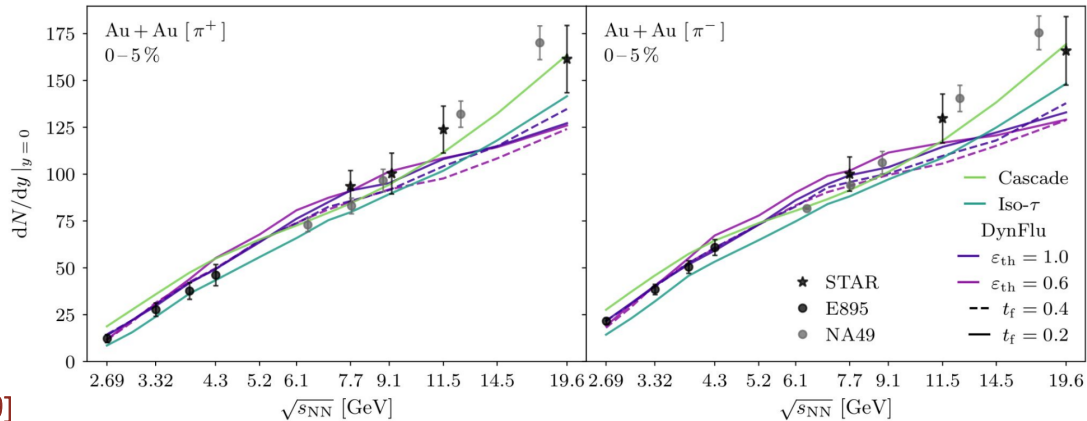
- Spacetime fluidization converges towards iso- τ at higher energies
- Much smoother deposition of hot matter in the fluid
- Results without retuning parameters
- Effective extension of hybrid model to lower energies

R. G-H. et al. (2025) [2507.19389]

SMASH-vHLL- τ -Hybrid
Au-Au at $\sqrt{s_{NN}} = 5.2$ GeV



Core particles kept in IC to contribute to calculation of $T^{\mu\nu}$



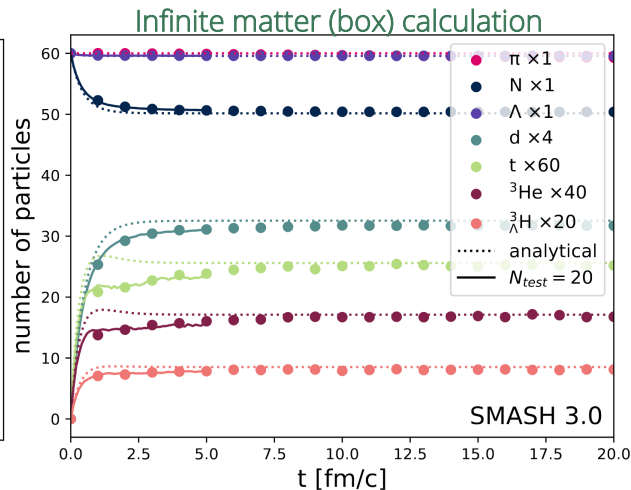
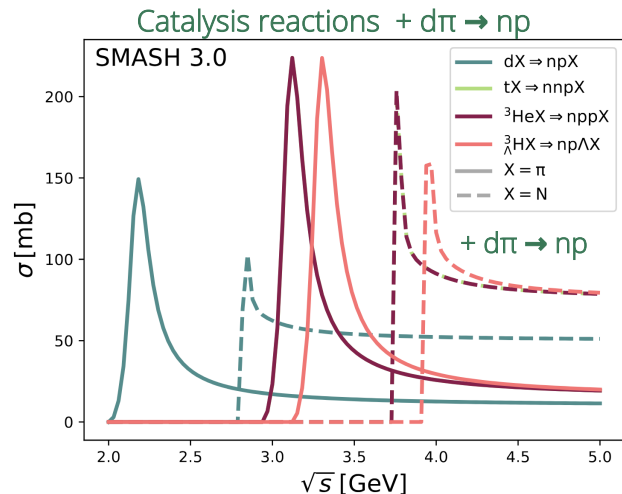
Production of light nuclei

Setup & rate equations



Using hypersurface from hydro:

- ▶ Sample particles directly (similar to statistical hadronization model)
- ▶ Run through SMASH as afterburner and apply coalescence afterwards
- ▶ Run SMASH with dynamic reactions for light nuclei

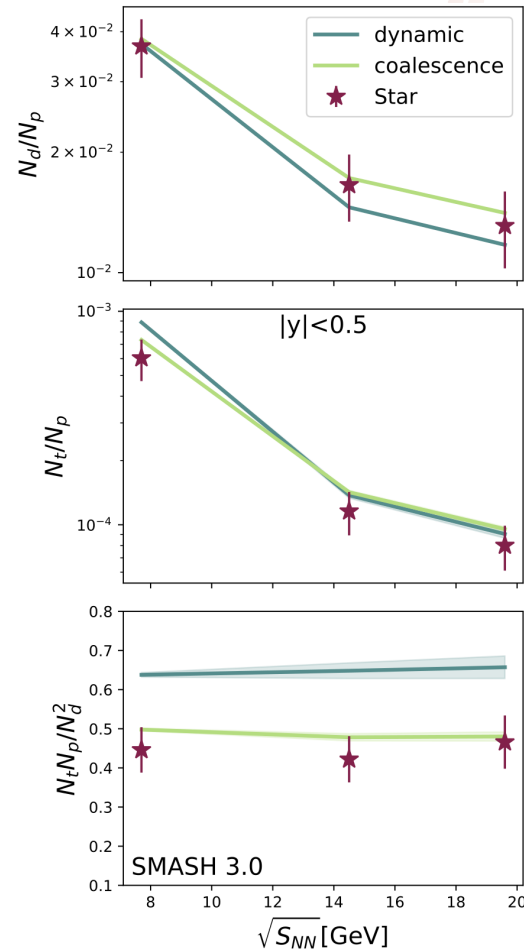


- ▶ The stochastic collision criterion allows for multi-particle reactions
- ▶ Equilibrium yields in very good agreement
- ▶ Thermalization process is faster than analytic solution
- ▶ 10 testparticles are sufficient

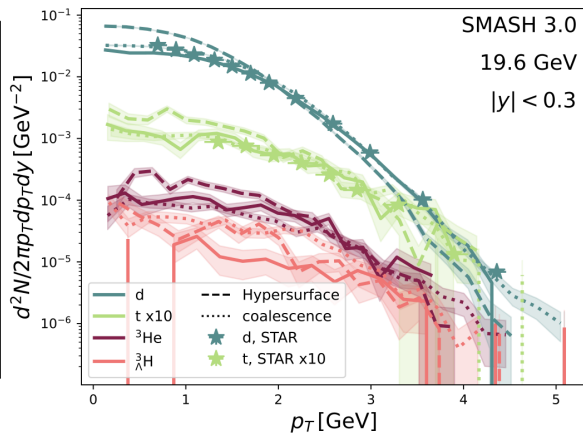
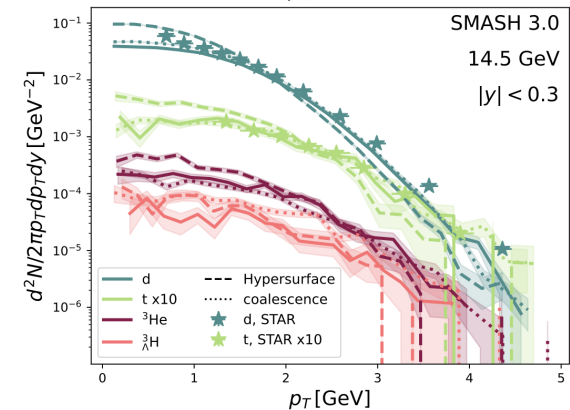
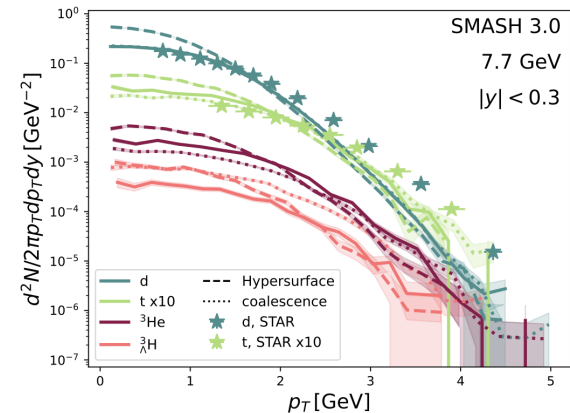
M. Ege, J. Mohs, J. Staudenmaier and H. Elfner (2025) PRC 112 5

Particle ratios & pT spectra

- Rescattering necessary to describe shape of the low momentum spectra
- Small differences between coalescence and dynamic processes
- Single ratios well described, while double ratio slightly deviates

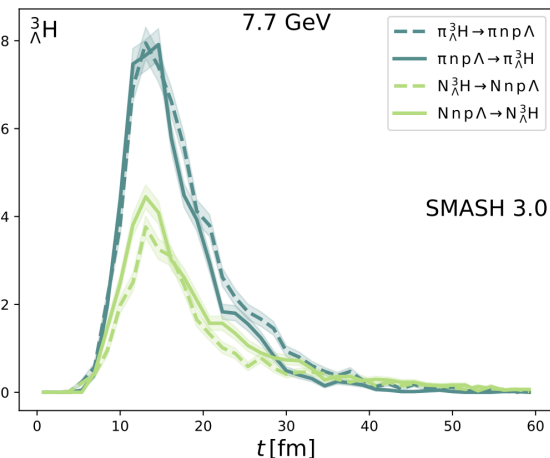
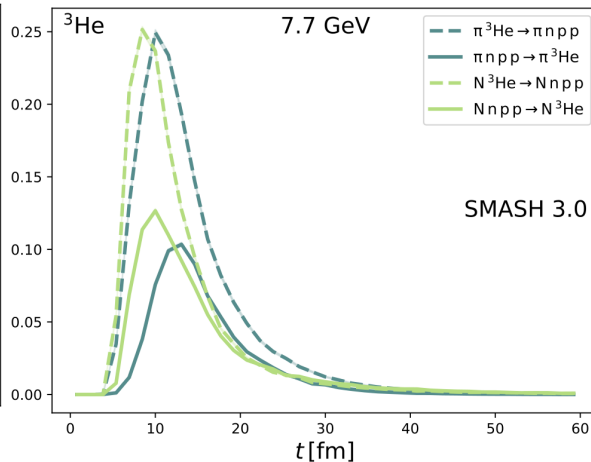
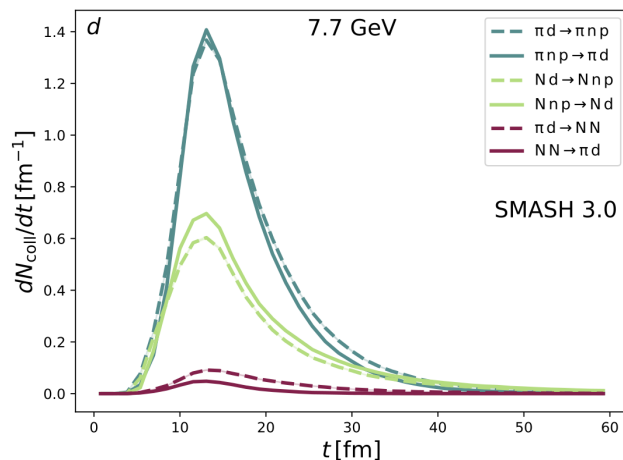
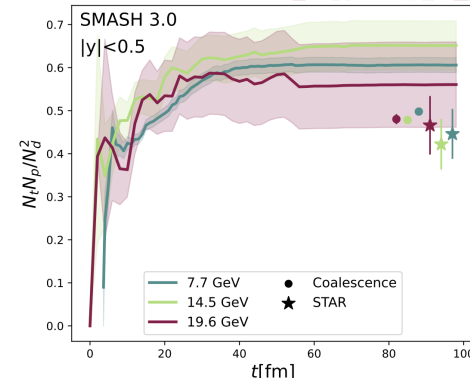
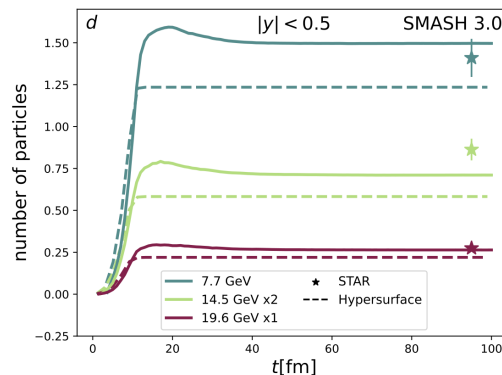


34



Dynamical evolution

- Non-trivial time evolution cancels in double ratio
- Many late stage collisions happen
- Production and destruction of light nuclei may balance each other



M. Ege, J. Mohs, J. Staudenmaier and H. Elfner (2025) PRC 112 5

Electromagnetic and hard probes

Dileptons in SMASH



- Dileptons produced perturbatively by the hadrons
- Resonances: time-integration/shining method
- No in-medium modification \rightarrow only dynamically generated broadening of spectral functions
- To match data, some resonances need coarse graining + in-medium rates

Continuously perform dilepton radiation and weight them by taking the decay probability into account

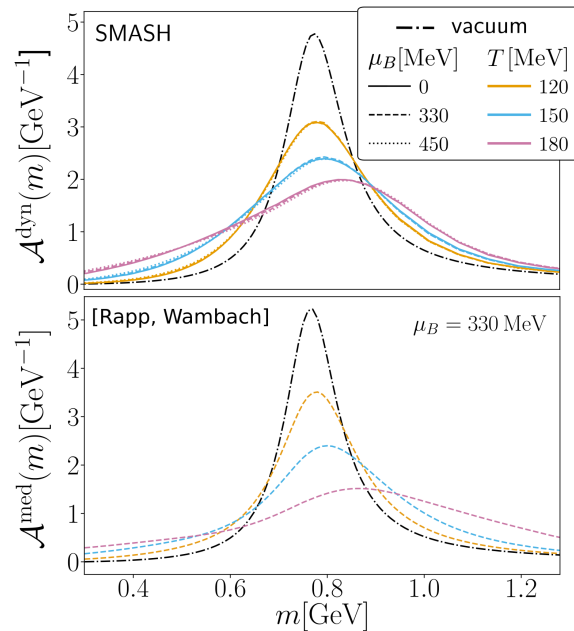
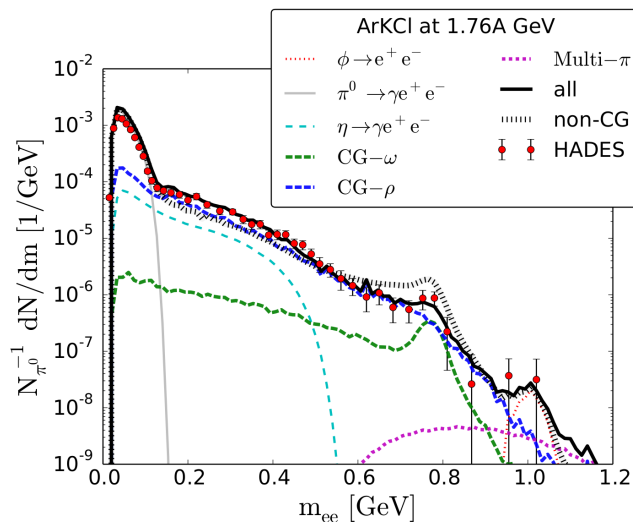
Dalitz

Direct

$$\begin{aligned}
 \pi &\rightarrow e^+e^-\gamma \\
 \eta &\rightarrow e^+e^-\gamma \\
 \eta' &\rightarrow e^+e^-\gamma \\
 \omega &\rightarrow e^+e^-\pi^0 \\
 \phi &\rightarrow e^+e^-\pi^0 \\
 \Delta^+ &\rightarrow e^+e^-p \\
 \Delta^0 &\rightarrow e^+e^-n^0
 \end{aligned}$$

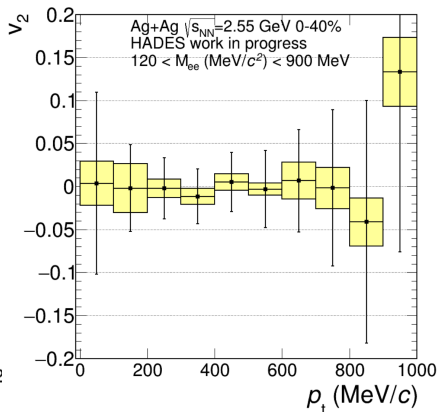
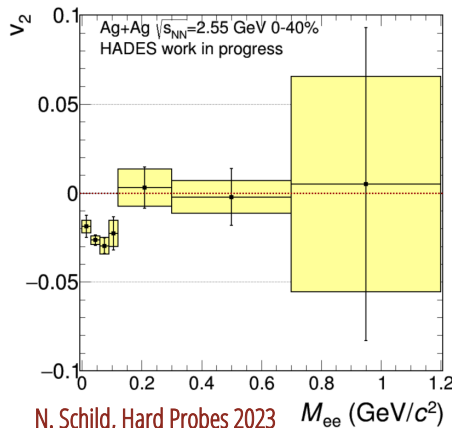
$$\begin{aligned}
 \rho &\rightarrow e^+e^- \\
 \omega &\rightarrow e^+e^- \\
 \phi &\rightarrow e^+e^-
 \end{aligned}$$

J. Staudenmaier et al., PRC 98 (2018)
R.G.-H. et al. (2023) PRC 107(2)

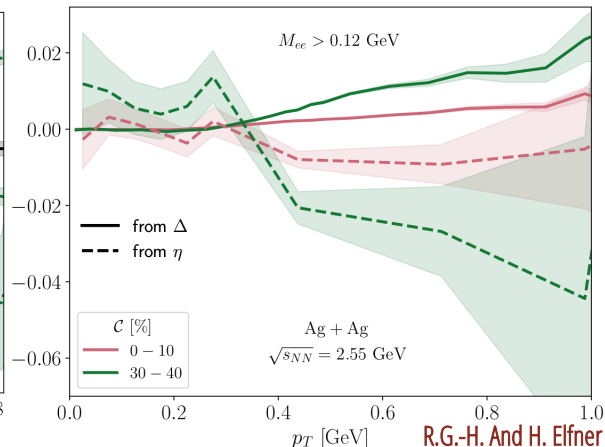
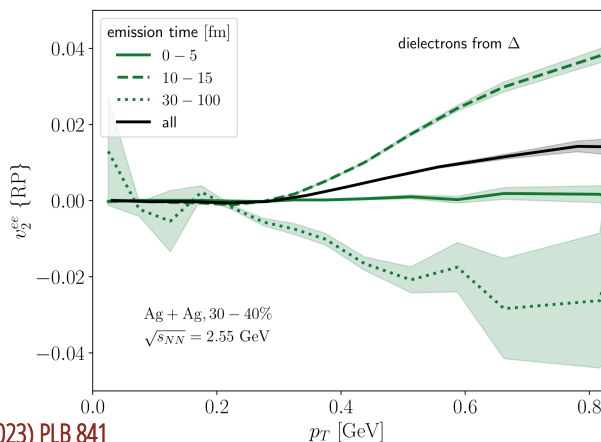
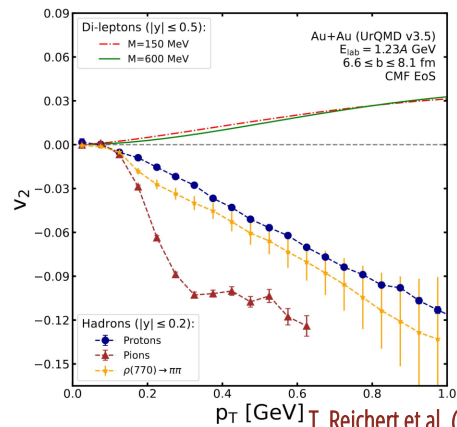


37

Flow of dielectrons



- HADES measures dielectron flow in AgAg@1.76 AGeV collisions
- “Zero” flow in resonance region
- Actually caused by cancellation between in- (early) and out-of-plane (late) contributions



Flow of dielectrons

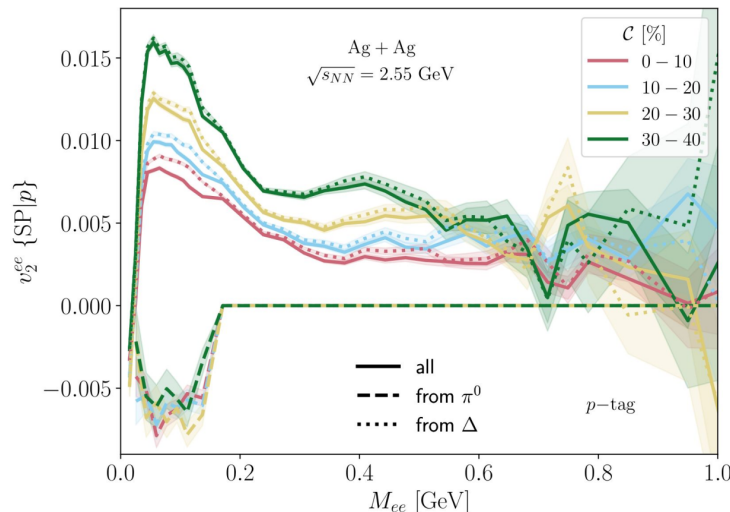
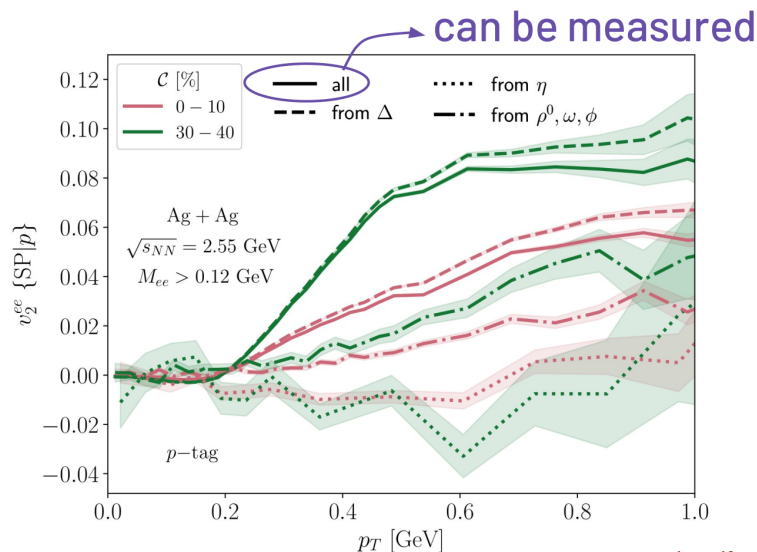


By **tagging** the dielectrons with a specific selection of hadrons, we can experimentally track the resonances

Event flow vector

$$\mathbf{q}_n^X(\Omega) = \frac{1}{N_X(\Omega)} \sum_{k \in \Omega} e^{in\phi_k}$$

$$v_{ll}\{\text{SP}|h\}(\Omega) \equiv \frac{\text{Cov}[\mathbf{q}_{ll}(\Omega), \mathbf{q}_h]}{\sqrt{\langle |q_h|^2 \rangle}}$$



R.G.-H. and H. Elfner (2024) PRC 110

39

Dielectrons in the hybrid

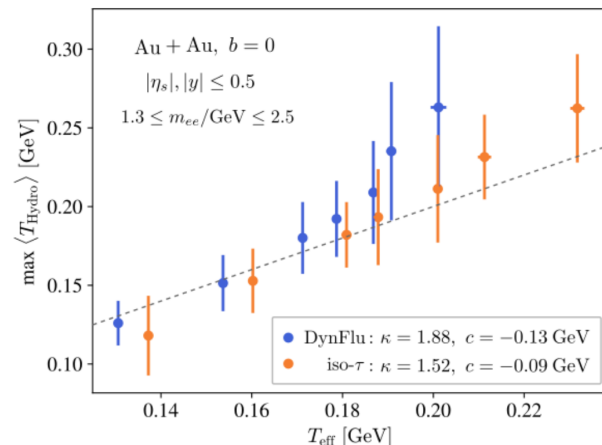
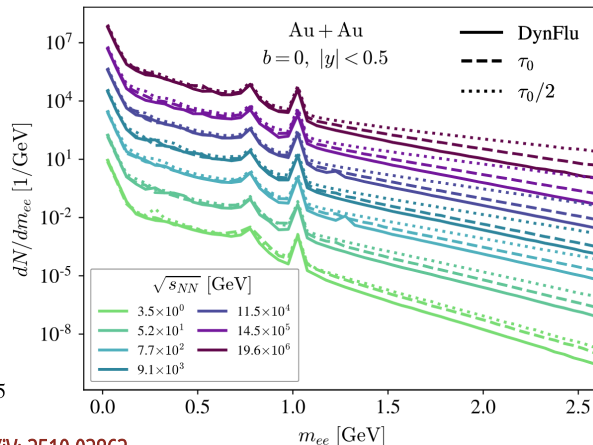
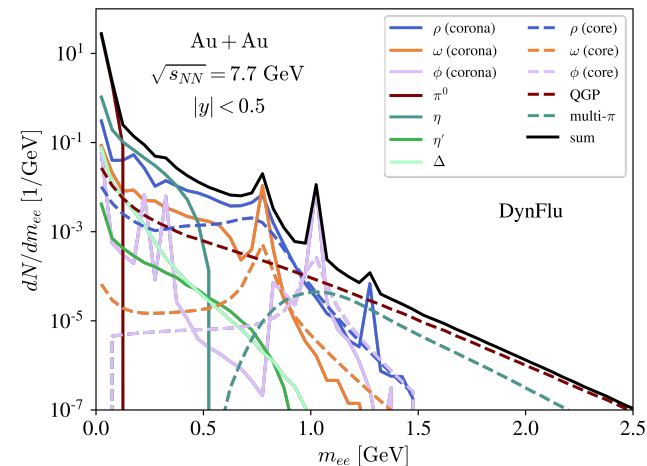
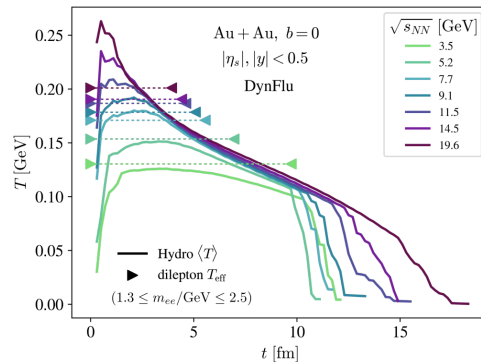
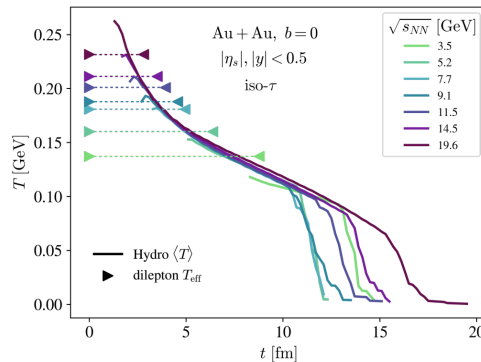
$$\frac{dN}{dm_{ee}} \propto m_{ee}^{3/2} \exp\left(-\frac{m_{ee}}{T}\right)$$



SMASH corona: shining method

vHLL core: thermal rates (same as in CG)

• Compare the different initializations

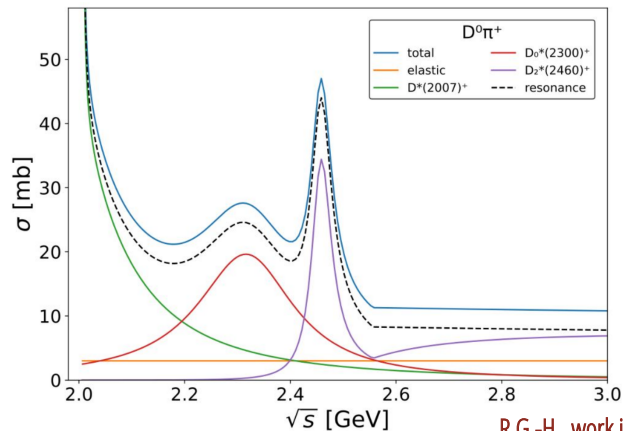


R.G.-H. et al. (2025) arXiv: 2510.02862

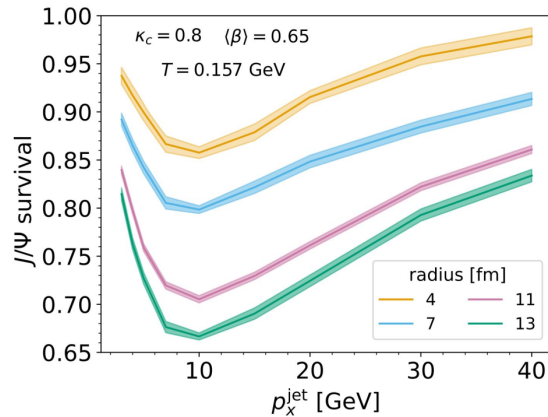
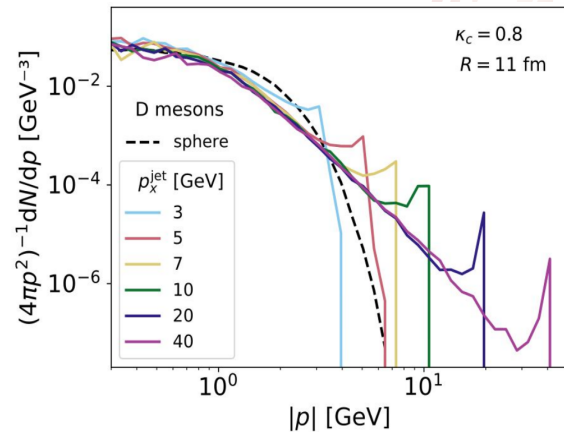
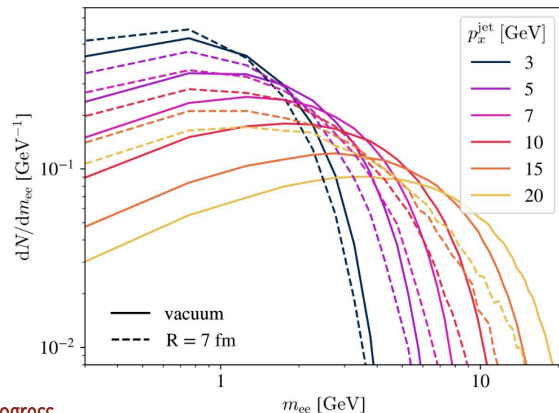
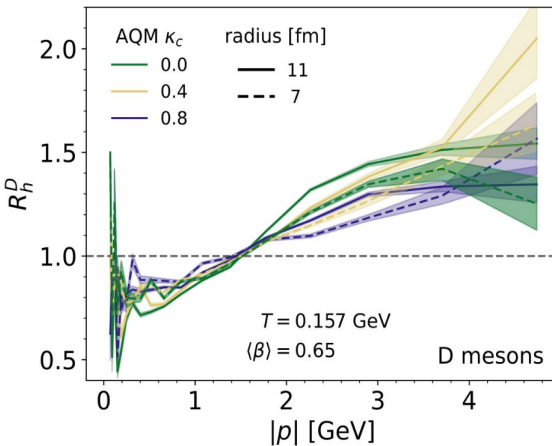
Heavy flavor rescattering

Toy model setup:

- Sphere of thermalized hadron gas (T, V, μ_B from SHM)
- Jet-like particles from the origin
- PDG resonances, AQM σ_{elastic}



R.G.H., work in progress



Software development

The SMASH team

In Frankfurt

- Hannah Elfner
- Alessandro Sciarra
- Renan Góes-Hirayama
- Carl Rosenkvist
- Lucas Constantin
- Shi-Lei Tao sup. by Ben-Wei Zhang
- Qian-Ru Lin sup. by Long-Gang Pang
- Sebastian Ostrowski
- Jakob Lohr
- Nils Sass
- Robin Sattler
- Antonio Bozic
- Vinzent Pott
- Manou Engel
- Luis Velez

In USA/Spain/Slovakia

- Agnieszka Sorensen
- Hendrik Roch
- Oscar García-Montero
- Zuzana Paulinyová



Bouldering with group in November

Clean coding

<https://smash-transport.github.io/>



Version 3.3 out last week !

Strict rules for software development

- Each newly implemented feature goes through internal review (pull requests)
- ~100 unit and functional tests catch bugs before merging to development branch
- Specific error handling prevent wrong usage
- Enforced documentation and user guide
- Completely open source codebase

```
WARN      DecayModes      : Branching ratios of 53 hadrons were renormalized by more than 1% to have sum 1.
INFO      Main            : Config hash: e57de317391abb160fd7de1154bbd8e8d169a69439245152f6e85bd6ba9f20fd
INFO      Collider        : Fermi motion is ON.
INFO      Experiment      : End time: 50 fm
                        -- Collider Modus:
                        sqrt(S) (nucleus-nucleus) = 154.489 GeV
                        sqrt(S) (nucleon-nucleon) = 2.41389 GeV
                        Projectile:
                        #particles  #testparticles  mass [GeV]  radius [fm]  diffusiveness [fm]
                        64          640            60.032     4.265        0.54
                        Target:
                        #particles  #testparticles  mass [GeV]  radius [fm]  diffusiveness [fm]
                        64          640            60.032     4.265        0.54
INFO      Experiment      : Using 10 testparticles per particle.
INFO      Experiment      : Using 20 parallel ensembles.
INFO      FindScatter     : Evaluating total cross sections from parametrizations only for measured processes.
INFO      Experiment      : Pauli blocking is ON.
INFO      Experiment      : Added output Particles of format Oscar2013
INFO      Experiment      : Potentials are ON. Timestep is 0.1
FATAL     Main            : SMASH failed with the following error:
                        Can't use Skyrme and VDF potentials at the same time!
```

Collision term

The Collision_Term section in the input file can be used to configure SMASH interactions. Before describing each possible key in detail, it is useful to give some taste with a couple of examples.

A real life example

The following section in the input file configures SMASH to include all but strangeness exchange involving $2 \leftrightarrow 2$ scatterings, to treat $N + Nbar$ processes as resonance formations and to not force decays at the end of the simulation. The elastic cross section is globally set to 30 mbarn and the \sqrt{s} cutoff for elastic nucleon + nucleon collisions is 1.93 GeV. All collisions are performed isotropically and $2 \leftrightarrow 1$ processes are forbidden.

```
Collision_Term:
  Included_2to2: ["Elastic", "NN_to_NR", "NN_to_DR", "KN_to_KN"]
  Two_to_One: true
  Force_Decays_At_End: false
  NNbar_Treatment: "resonances"
  Elastic_Cross_Section: 30.0
  Elastic_NN_Cutoff_Sqrts: 1.93
  Isotropic: true
```

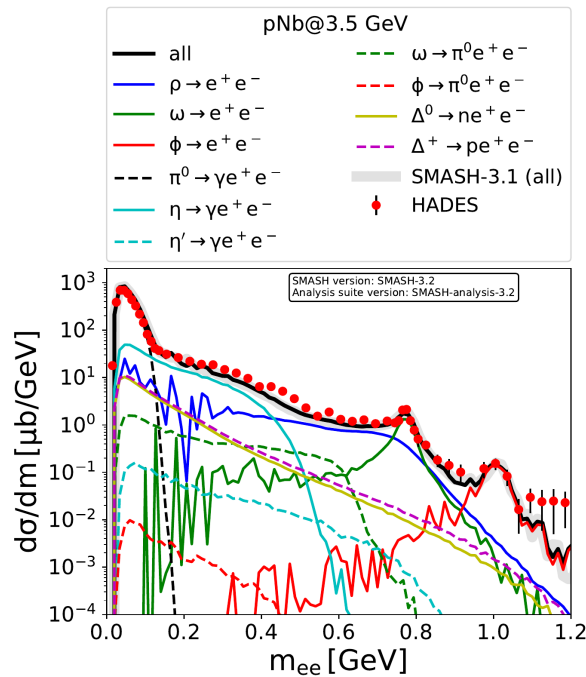
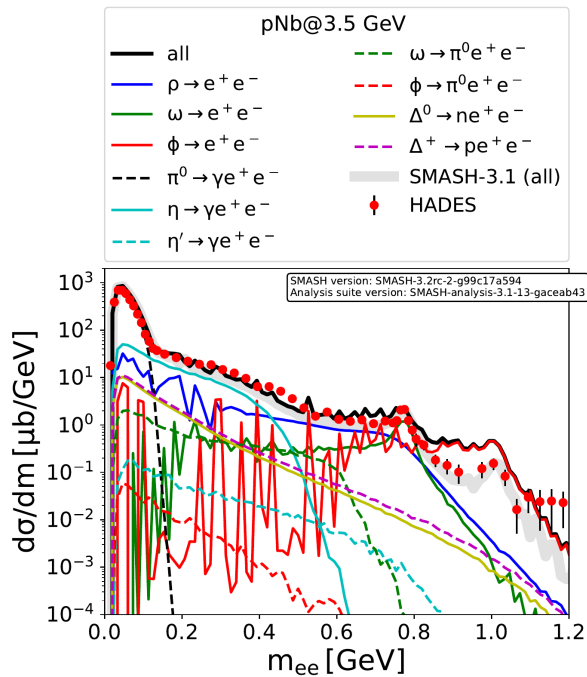
Analysis suite

http://theory.gsi.de/~smash/analysis_suite/current/



Collection of basic physics results to compare the new changes to the model, which also helps to catch bugs undetectable via tests

When changing resonance properties to improve strangeness production, Carl did not initially constrain the $BR(N^* \rightarrow N\Phi)$



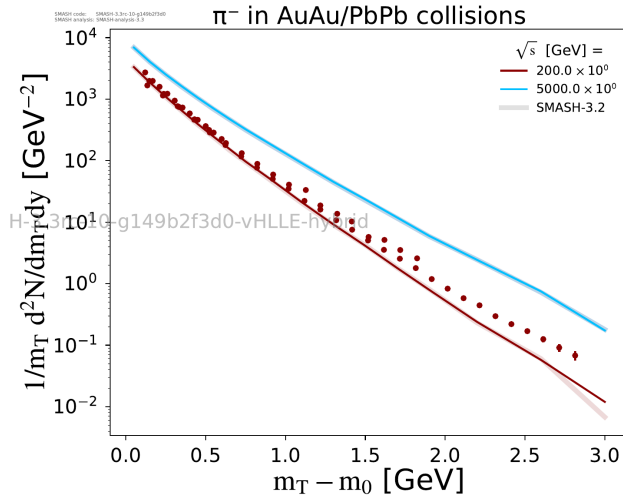
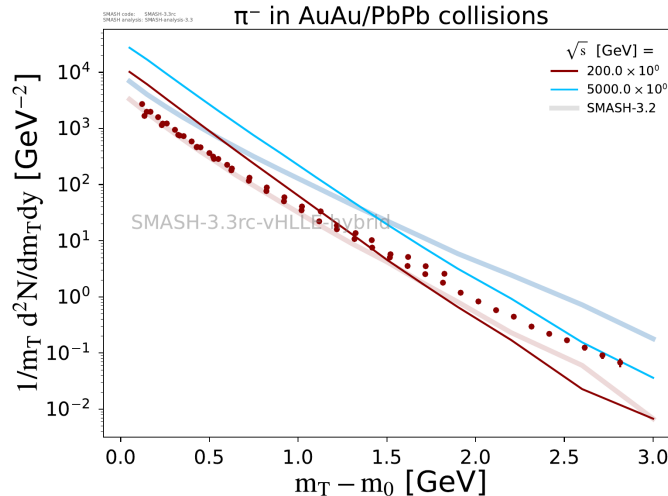
Analysis suite

http://theory.gsi.de/~smash/analysis_suite/current/



Collection of basic physics results to compare the new changes to the model, which also helps to catch bugs undetectable via tests

When adding infrastructure of a custom input for the afterburner calculations, I forgot to set the formation time of entering particles



Visualization

<https://smash-transport.github.io/movies.html>



- Useful tool for science communication [Paraview tutorial](#)
- Identify potential issues in the model when something looks wrong or unphysical

The SMASH-hadron sampler was not adjusted to vHLLC providing spacetime four vectors in Cartesian coordinates (needed for DynFlu)

smash-vhllc-hybrid

Au-Au @ $\sqrt{s_{NN}} = 17.3$ GeV, $b = 0$ fm



Summary



SMASH and **SMASH-vHLE hybrid** approaches are available to the public and we support you with your calculations

- Bulk observables are in reasonable agreement with experimental data
- Momentum dependent nuclear potentials compared to FOPI and HADES flow data, suggesting constraints for equation of state
- Fluctuation observables survive rescattering for a strong enough σ -field coupling
- Bayesian analysis for transport coefficients as a function of (T, μ_B)
- Hybrid model extended to lower energies with a dynamic core-corona separation
- Light nuclei can be created and destroyed dynamically via multiparticle scatterings, similar but distinct results to coalescence approach
- Dilepton flow carries interesting information on resonance contributions
- Heavy flavor hadrons now included in the degrees of freedom