



中国科学技术大学
University of Science and Technology of China



STCF上超子半轻衰变过程 $\Xi^- \rightarrow \Lambda e^- \bar{\nu}_e$ 研究

韩许
中国科学技术大学

2025.9.21

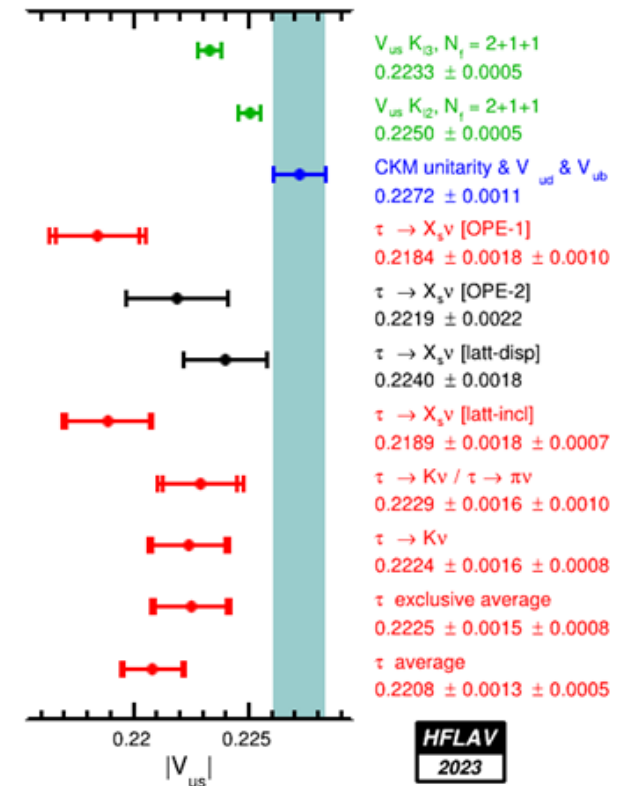
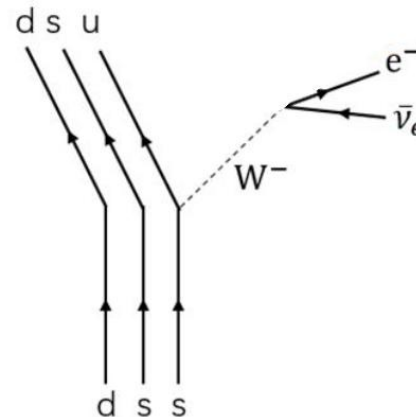
- Motivation
- Simulated data sets
- Analysis strategy
- Single tag analysis
- Double tag analysis
- Summary

- Determination of CKM matrix element V_{us} or Cabibbo-angle θ_c . In fact, different previous measurements of θ_c , have **poor mutual agreement** which is so-called “Cabibbo-angle anomaly”.
- $\Xi^- \rightarrow \Lambda e^- \bar{\nu}_e$ can provide a complementary method to **determine the Cabibbo angle θ_c** and to test the Unitarity of the CKM matrix.

- ✓ Determine the branching fraction
- ✓ Determine the form factors

$$\Gamma_{e,SM} \simeq \frac{G_F^2 |V_{us} f_1(0)|^2 \Delta^5}{60\pi^3} \left[\left(1 - \frac{3}{2}\delta\right) + 3 \left(1 - \frac{3}{2}\delta\right) \frac{g_1(0)^2}{f_1(0)^2} - 4\delta \frac{g_2(0)}{f_1(0)} \frac{g_1(0)}{f_1(0)} \right]$$

[PRL 114, 161802 \(2015\)](#)



■ Study of SU3 breaking effects.

- ✓ $g_1(0)/f_1(0)$ has intriguingly **small SU3 breaking effects**. Lots of phenomenology models are waiting for more experiments.
- ✓ g_2 is 0 or not. Could be the first observation of a second-class weak-interaction current.

■ Proton spin content

- ✓ Provide complementarity to polarized deep inelastic scattering experiments for the determination of the proton spin content.

● 实验：深度非弹性轻子-核子散射过程

$$\int_0^1 dx g_1^p(x, Q^2) = \left(\frac{1}{12} g_A^{(3)} + \frac{1}{36} g_A^{(8)} \right) \left\{ 1 + \sum_{\ell \geq 1} c_{\text{NS}\ell} \alpha_s^\ell(Q) \right\} \\ + \frac{1}{9} g_A^{(0)}|_{\text{inv}} \left\{ 1 + \sum_{\ell \geq 1} c_{\text{S}\ell} \alpha_s^\ell(Q) \right\} + \mathcal{O}\left(\frac{1}{Q^2}\right) - \beta_1(Q^2) \frac{Q^2}{4M^2}.$$

Decay	Scale	$f_1(0)$	$g_1(0)$	g_1/f_1	f_2/f_1
$n \rightarrow pe^- \bar{\nu}$	V_{ud}	1	$D+F$	$F+D$	$\frac{M_n}{M_p} \frac{(\mu_p - \mu_n)}{2} = 1.855$
$\Xi^- \rightarrow \Xi^0 e^- \bar{\nu}$	V_{ud}	-1	$D-F$	$F-D$	$\frac{M_{\Xi^-}}{M_p} \frac{(\mu_p + 2\mu_n)}{2} = -1.432$
$\Sigma^\pm \rightarrow \Lambda e^\pm \nu$	V_{ud}	0 ^b	$\sqrt{\frac{2}{3}} D$	$\sqrt{\frac{2}{3}} D$	$-\frac{M_{\Sigma^\pm}}{M_p} \sqrt{\frac{3}{2}} \frac{\mu_n}{2} = 1.490$
$\Sigma^- \rightarrow \Sigma^0 e^- \bar{\nu}$	V_{ud}	$\sqrt{2}$	$\sqrt{2} F$	F	$\frac{M_{\Sigma^-}}{M_p} \frac{(2\mu_p + \mu_n)}{4} = 0.534$
$\Sigma^0 \rightarrow \Sigma^+ e^- \bar{\nu}$	V_{ud}	$\sqrt{2}$	$-\sqrt{2} F$	$-F$	$\frac{M_{\Sigma^0}}{M_p} \frac{(2\mu_p + \mu_n)}{4} = 0.531$
$\Xi^0 \rightarrow \Sigma^+ e^- \bar{\nu}$	V_{us}	1	$D+F$	$F+D$	$\frac{M_{\Xi^0}}{M_p} \frac{(\mu_p - \mu_n)}{2} = 2.597$
$\Xi^- \rightarrow \Sigma^0 e^- \bar{\nu}$	V_{us}	$\frac{1}{\sqrt{2}}$	$\frac{1}{\sqrt{2}}(D+F)$	$F+D$	$\frac{M_{\Xi^-}}{M_p} \frac{(\mu_p - \mu_n)}{2} = 2.609$
$\Sigma^- \rightarrow ne^- \bar{\nu}$	V_{us}	-1	$D-F$	$F-D$	$\frac{M_{\Sigma^-}}{M_p} \frac{(\mu_p + 2\mu_n)}{2} = -1.297$
$\Sigma^0 \rightarrow pe^- \bar{\nu}$	V_{us}	$\frac{-1}{\sqrt{2}}$	$\frac{1}{\sqrt{2}}(D-F)$	$F-D$	$\frac{M_{\Sigma^0}}{M_p} \frac{(\mu_p + 2\mu_n)}{2} = -1.292$
$\Lambda \rightarrow pe^- \bar{\nu}$	V_{us}	$-\sqrt{\frac{3}{2}}$	$-\frac{1}{\sqrt{6}}(D+3F)$	$F+D/3$	$\frac{M_\Lambda}{M_p} \frac{\mu_p}{2} = 1.066$
$\Xi^- \rightarrow \Lambda e^- \bar{\nu}$	V_{us}	$\sqrt{\frac{3}{2}}$	$-\frac{1}{\sqrt{6}}(D-3F)$	$F-D/3$	$-\frac{M_{\Xi^-}}{M_p} \frac{(\mu_p + \mu_n)}{2} = 0.085$

Annu. Rev. Nucl. Part. Sci. 2003.

■ Searching for new physics

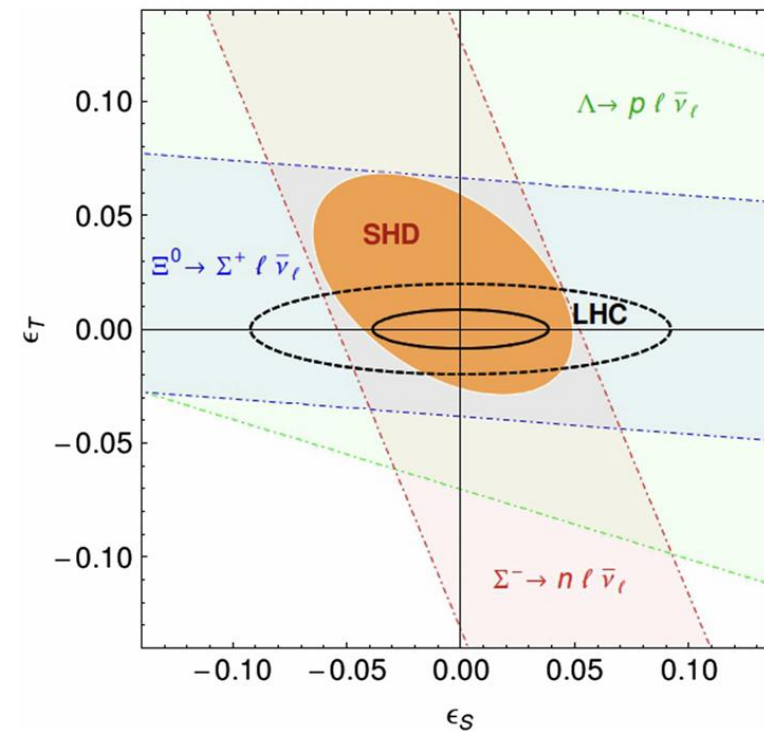
[PRL 114, 161802 \(2015\)](#)

- ✓ Provide extremely stringent constraints on the Wilson coefficients (ϵ_S, ϵ_T) of new physics.
- ✓ Complement the search for new physics at high-energy experiments such as the LHC.

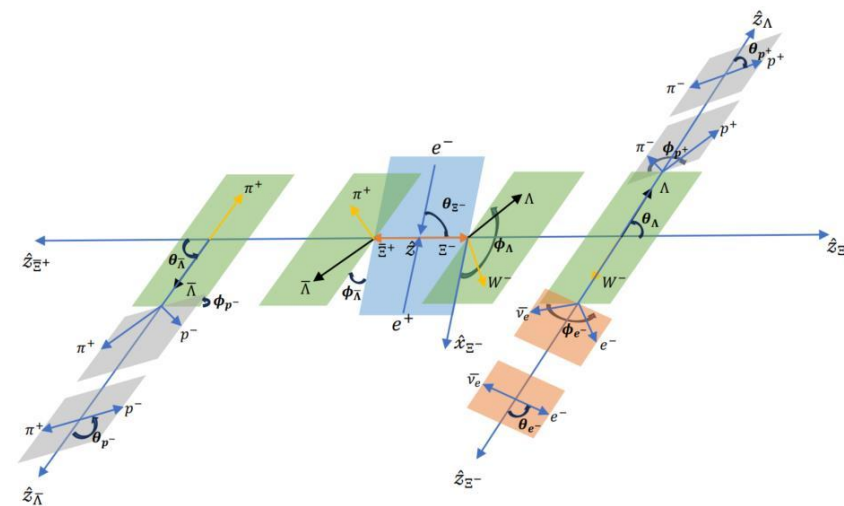
$$R^{\mu e} = \frac{\Gamma(B_1 \rightarrow B_2 \mu^- \bar{\nu}_\mu)}{\Gamma(B_1 \rightarrow B_2 e^- \bar{\nu}_e)}, \quad R_{\text{SM}}^{\mu e} = \sqrt{1 - \frac{m_\mu^2}{\Delta^2} \left(1 - \frac{9m_\mu^2}{2\Delta^2} - 4\frac{m_\mu^4}{\Delta^4} \right)} + \frac{15m_\mu^4}{2\Delta^4} \arctan h \left(\sqrt{1 - \frac{m_\mu^2}{\Delta^2}} \right).$$

$$\frac{R^{\mu e}}{R_{\text{SM}}^{\mu e}} = 1 + r_S \epsilon_S + r_T \epsilon_T,$$

	$\Lambda \rightarrow p$	$\Sigma^- \rightarrow n$	$\Xi^0 \rightarrow \Sigma^+$	$\Xi^- \rightarrow \Lambda$
$g_1(0)/f_1(0)$	0.718(15)	-0.340(17)	1.210(50)	0.250(50)
$f_S(0)/f_1(0)$	1.90(10)	2.80(14)	1.36(7)	2.25(11)
$f_T(0)/f_1(0)$	0.72	-0.28	1.22	0.22
r_S	1.60	4.1	0.56	3.7
r_T	5.2	1.7	7.2	1.1



- ✓ OSCAR version: 2.6.2
 - ✓ CDR $J/\psi: 3.4 \times 10^{12}$
 - ✓ Simulated signal MC and dominant BKG sample: 5.0×10^5
 - ✓ Signal MC : $e^+e^- \rightarrow J/\psi \rightarrow \bar{\Xi}^+\Xi^-$, $\bar{\Xi}^+ \rightarrow \bar{\Lambda}\pi^+$, $\Xi^- \rightarrow \Lambda e^- \bar{\nu}_e$, $\bar{\Lambda} \rightarrow \bar{p}\pi^+$, $\Lambda \rightarrow p\pi^-$
 - ✓ Background MC: $e^+e^- \rightarrow J/\psi \rightarrow \bar{\Xi}^+\Xi^-$, $\bar{\Xi}^+ \rightarrow \bar{\Lambda}\pi^+$, $\Xi^- \rightarrow \Lambda\pi^-$, $\bar{\Lambda} \rightarrow \bar{p}\pi^+$, $\Lambda \rightarrow p\pi^-$
- ST-MC: $J/\psi \rightarrow \bar{\Xi}^+(\bar{\Lambda}\pi^+(\bar{\Lambda} \rightarrow \bar{p}\pi^+))\Xi^-(anything)$
 - DT-MC: $J/\psi \rightarrow \bar{\Xi}^+(\bar{p}\pi^+\pi^+)\Xi^-(\Lambda e^- \bar{\nu}_e(\Lambda \rightarrow p\pi^-))$



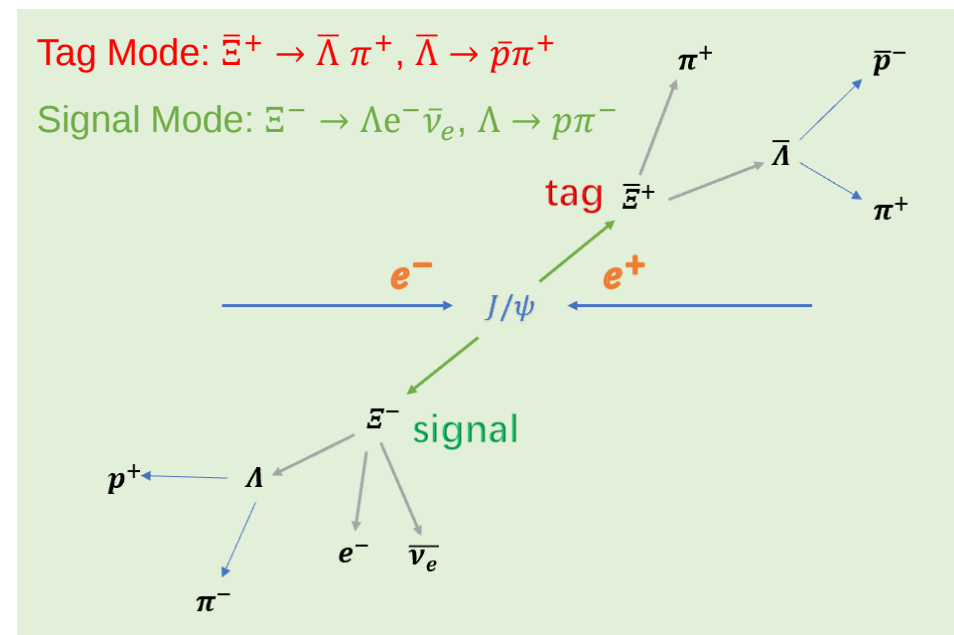
✓ Double Tag Method:

Double tag method can reduce several terms of systematic uncertainty.

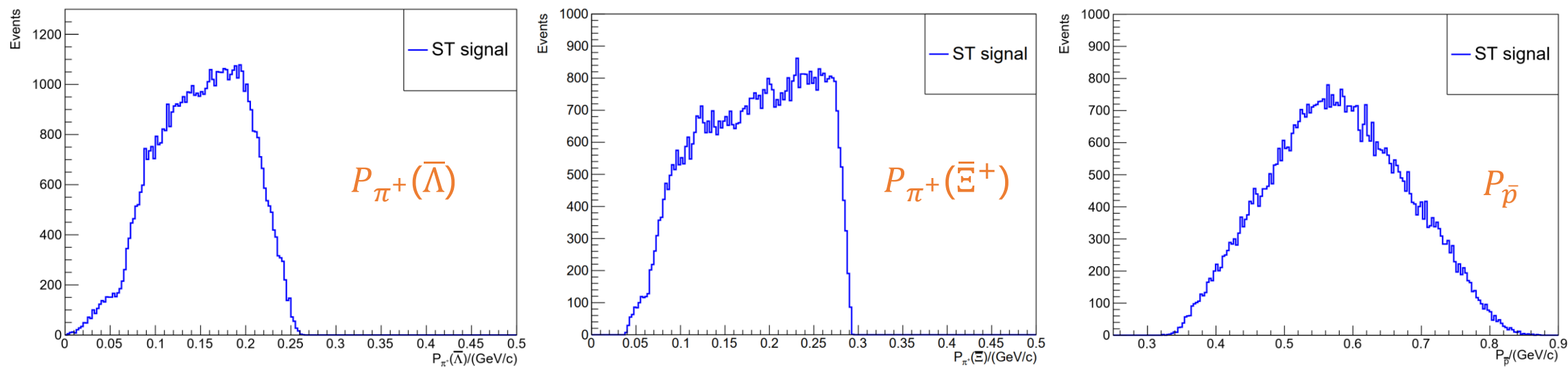
- ST-MC: $J/\psi \rightarrow \bar{\Xi}^+ (\bar{\Lambda} \pi^+ (\bar{\Lambda} \rightarrow \bar{p} \pi^+)) \Xi^- (\text{anything})$
- DT-MC: $J/\psi \rightarrow \bar{\Xi}^+ (\bar{p} \pi^+ \pi^+) \Xi^- (\Lambda e^- \bar{\nu}_e (\Lambda \rightarrow p \pi^-))$

Yield of each side:

- $N_{ST} = N_{J/\psi} \times \text{Br}_{J/\psi \rightarrow \bar{\Xi}^+ \Xi^-} \times \text{Br}_{\bar{\Xi}^+ \rightarrow \bar{\Lambda} \pi^+} \times \text{Br}_{\bar{\Lambda} \rightarrow \bar{p} \pi^+} \times \epsilon_{ST}$
- $N_{DT} = N_{J/\psi} \times \text{Br}_{J/\psi \rightarrow \bar{\Xi}^+ \Xi^-} \times \text{Br}_{\bar{\Xi}^+ \rightarrow \bar{\Lambda} \pi^+} \times \text{Br}_{\bar{\Lambda} \rightarrow \bar{p} \pi^+} \times \text{Br}_{\Xi^- \rightarrow \Lambda e^- \bar{\nu}_e} \times \text{Br}_{\Lambda \rightarrow p \pi^-} \times \epsilon_{DT}$
- $Br_{\Xi^- \rightarrow \Lambda e^- \bar{\nu}_e} = \frac{N_{DT}}{N_{ST}} \times \frac{\epsilon_{ST}}{\epsilon_{DT}} \times \frac{1}{Br_{\Lambda \rightarrow p \pi^-}}$



➤ ST signal MC truth information(final state particles):



- ST-MC: $J/\psi \rightarrow \bar{\Xi}^+(\bar{\Lambda} \pi^+(\bar{\Lambda} \rightarrow \bar{p}\pi^+))\Xi^-(anything)$

➤ ST Event Selection

Tag Mode: $\bar{\Xi}^+ \rightarrow \bar{\Lambda} \pi^+$, $\bar{\Lambda} \rightarrow \bar{p} \pi^+$

✓ **Good charged track**: No Vertex requirement; $|\cos \theta| < 0.93$, $N_{charge^+} \geq 2$; $N_{charge^-} \geq 1$

✓ **Particle ID**: For proton: $p_{\bar{p}} > 0.32 \text{ GeV}/c$; $N_{\bar{p}} \geq 1$;
For pion: $p_{\pi^+} < 0.30 \text{ GeV}/c$; $N_{\pi^+} \geq 2$;

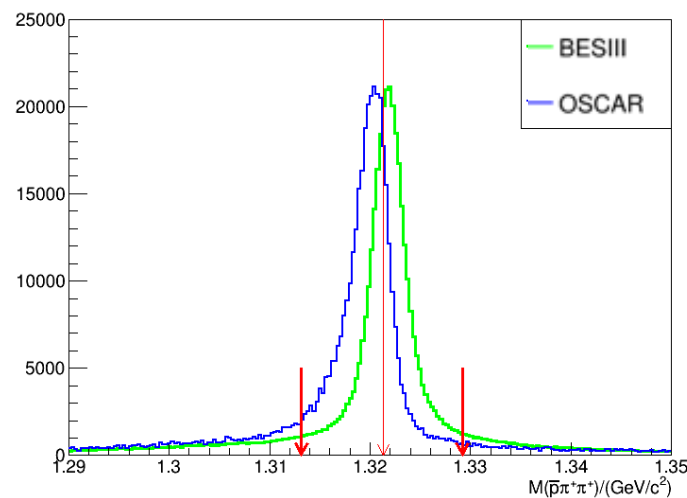
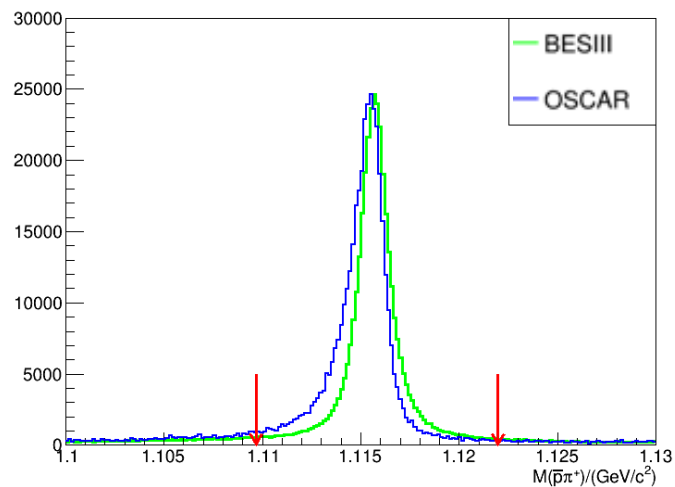
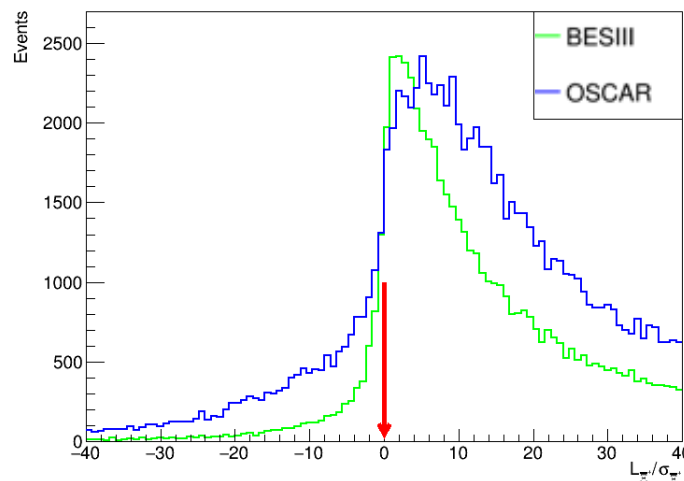
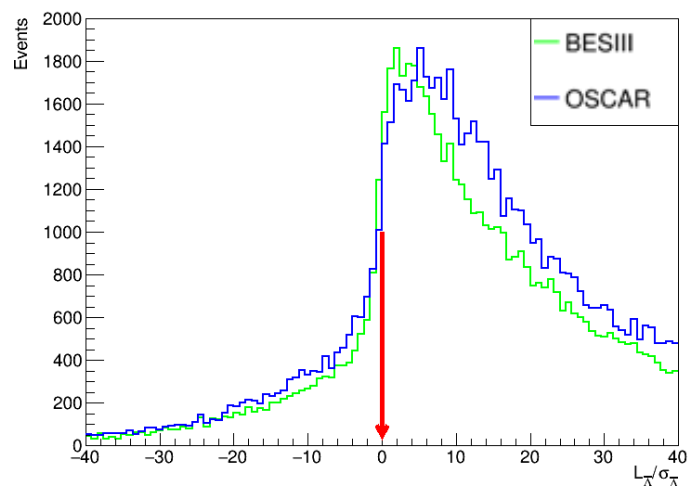
✓ **Vertex fit for $\bar{\Lambda}$, $\bar{\Xi}^+$** : Primary vertex fit: $\bar{p} \pi^+$ for $\bar{\Lambda}$, $\bar{\Lambda} \pi^+$ for $\bar{\Xi}^+$
Secondary vertex fit: $\bar{\Lambda} \pi^+$ and $\bar{\Xi}^+$, $\bar{\Xi}^+$ and initial vertex

Loop all the combinations, select the minimum $\chi^2 = \frac{(M_{\bar{p} \pi^+} - M_{\bar{\Lambda} PDG})^2}{\sigma_{\bar{\Lambda}}^2} + \frac{(M_{\bar{p} \pi^+ \pi^+} - M_{\bar{p} \pi^+} + M_{\bar{\Lambda} PDG} - M_{\bar{\Xi}^+ PDG})^2}{\sigma_{\bar{\Xi}^+}^2}$

✓ **Decay length**: $L_{\bar{\Lambda}}/\sigma_{L_{\bar{\Lambda}}} > 0$ && $L_{\bar{\Xi}^+}/\sigma_{L_{\bar{\Xi}^+}} > 0$

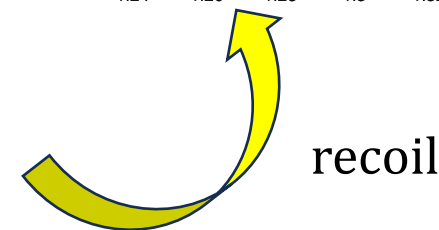
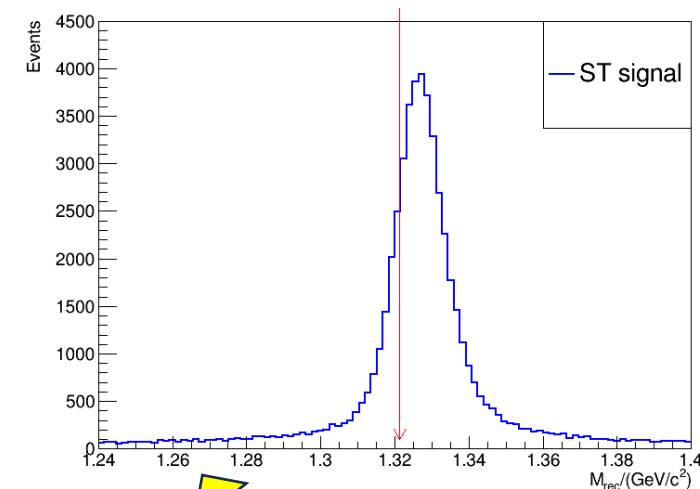
✓ **Mass distribution**: $|M_{\bar{\Lambda}} - M_{\bar{\Lambda} PDG}| < 0.006 \text{ GeV}$; $|M_{\bar{p} \pi^+ \pi^+} - M_{\bar{p} \pi^+} + M_{\bar{\Lambda} PDG} - M_{\bar{\Xi}^+ PDG}| < 0.008 \text{ GeV}$
 $1.273 \text{ GeV} < M_{recoil} < 1.363 \text{ GeV}$

➤ ST Event Selection



$$1.273\text{GeV} < M_{\text{rec}} < 1.363\text{GeV}$$

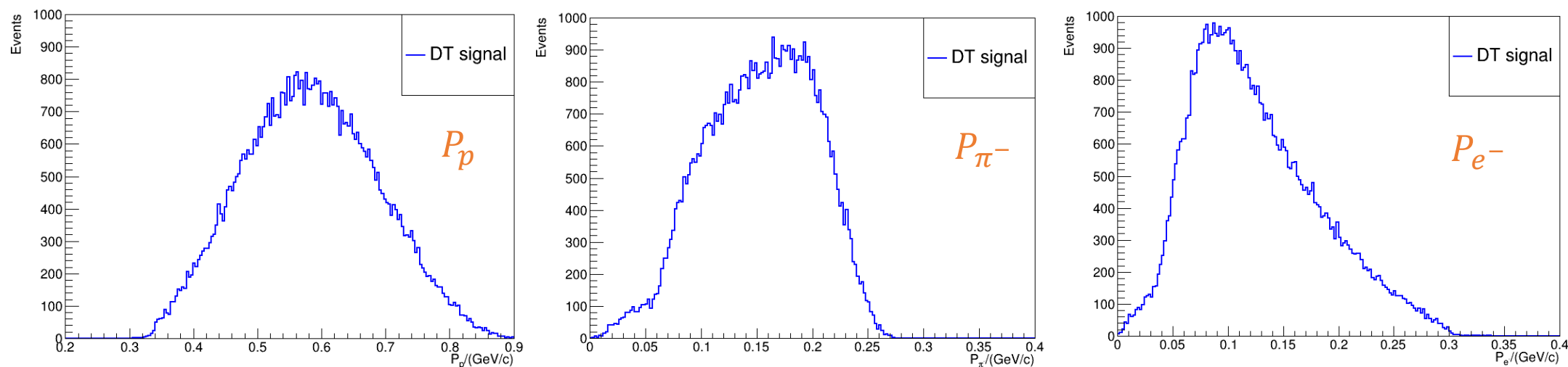
$$M_{\text{recoil}} = (ecms - P_{\bar{E}^+}) \cdot M();$$



➤ Cut flow

Selection Criteria	Event number	OSCAR		BESIII	
		Absolute Efficiency(%)	Relative Efficiency(%)	Absolute Efficiency(%)	Relative Efficiency(%)
Total Number	500000	100	-----	100	-----
Good charged track	489759	97.95	97.95	92.81	92.81
$N_{\bar{p}} \geq 1$	452302	90.46	92.35	80.53	86.77
$N_{\pi^+} \geq 2$	357857	71.57	79.12	54.27	67.39
$\bar{E}^+$ Vertex	291457	58.29	73.20	48.01	88.47
Further cut	179939	36.00	61.76	27.27	56.80

➤ DT signal MC truth information(final state particles):



- DT-MC: $J/\psi \rightarrow \bar{E}^+(\bar{p}\pi^+\pi^+)E^-(\Lambda e^-\bar{\nu}_e(\Lambda \rightarrow p\pi^-))$

➤ DT Event Selection

Signal Mode: $\Xi^- \rightarrow \Lambda e^- \bar{\nu}_e$, $\Lambda \rightarrow p \pi^-$

✓ **Particle ID:** Proton: $p_p > 0.32 \text{ GeV}/c$; $N_p \geq 1$;

Pion or electron: $p/\pi^- < 0.30 \text{ GeV}/c$; $N \geq 2$

✓ **Vertex fit for simulated decay $\Xi^- \rightarrow \Lambda \pi^-$ candidate:**

Primary vertex fit : $p\pi^-$ for Λ , $\Lambda\pi^-$ for Ξ^-

Secondary vertex fit : $\Lambda\pi^-$ and Ξ^- , Ξ^- and Primary Vertex

Loop all the pairs, select the minimum chisquare

✓ **Vertex fit for signal candidate :**

Primary vertex fit : $p\pi^-$ for Λ , Λe^- for Ξ^- .

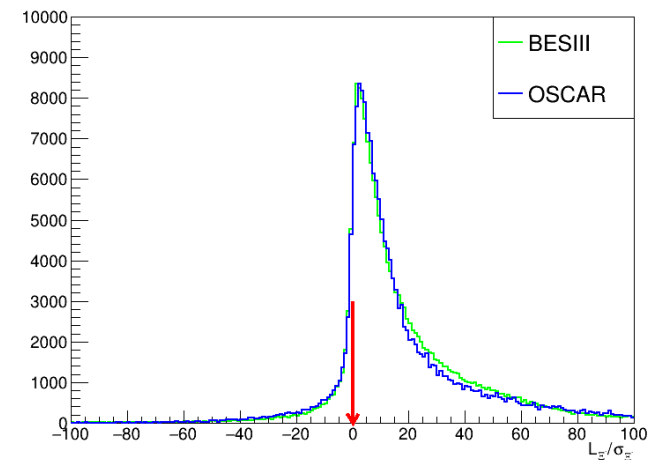
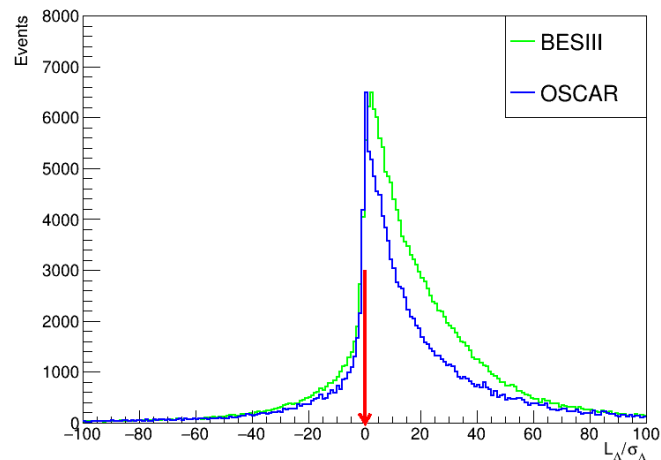
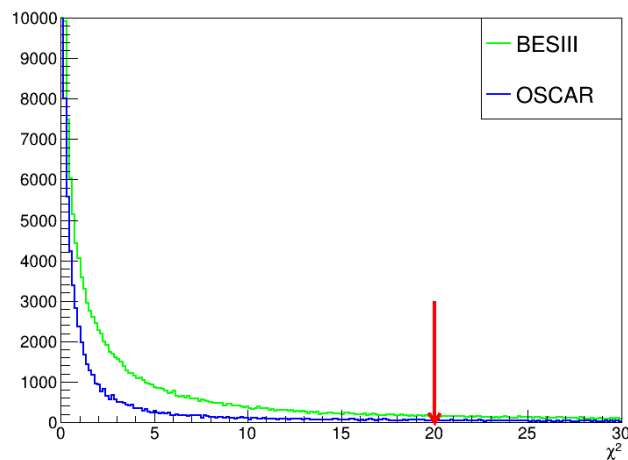
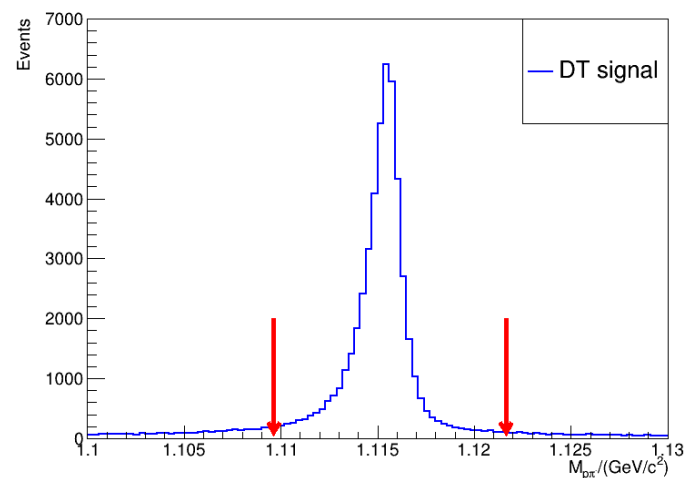
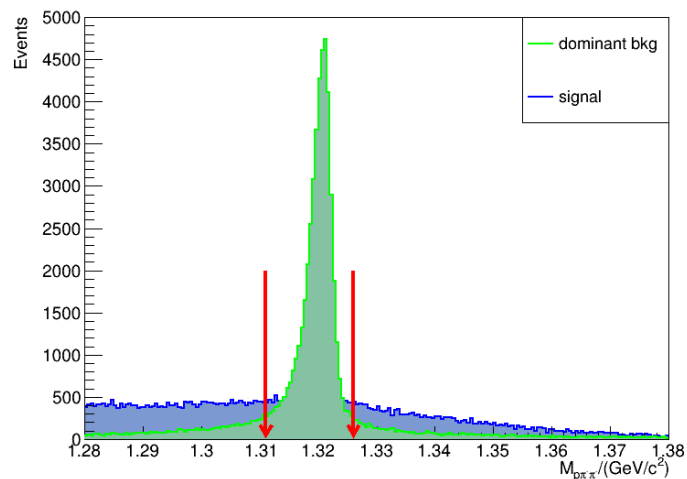
Secondary vertex fit : Λ and Ξ^- , Ξ^- and Primary Vertex.

Loop all the pairs, select combination by minimizing $|M_{p\pi^-} - M_{\Lambda_{PDG}}|$ and then minimizing primary vertex fit χ^2 of Ξ^-

✓ **Mass distribution:** Veto $|M_{p\pi^-\pi^-} - M_{p\pi^-} + M_{\Lambda_{PDG}} - M_{\Xi_{PDG}^-}| < 0.006 \text{ GeV}$
 $|M_{\Lambda} - M_{\Lambda_{PDG}}| < 0.006 \text{ GeV}$

✓ **Further cut:** $L_{\Lambda}/\sigma_{L_{\Lambda}} > 0$ && $L_{\Xi}/\sigma_{L_{\Xi}} > 0$; $\chi^2 < 20$

➤ DT Event Selection



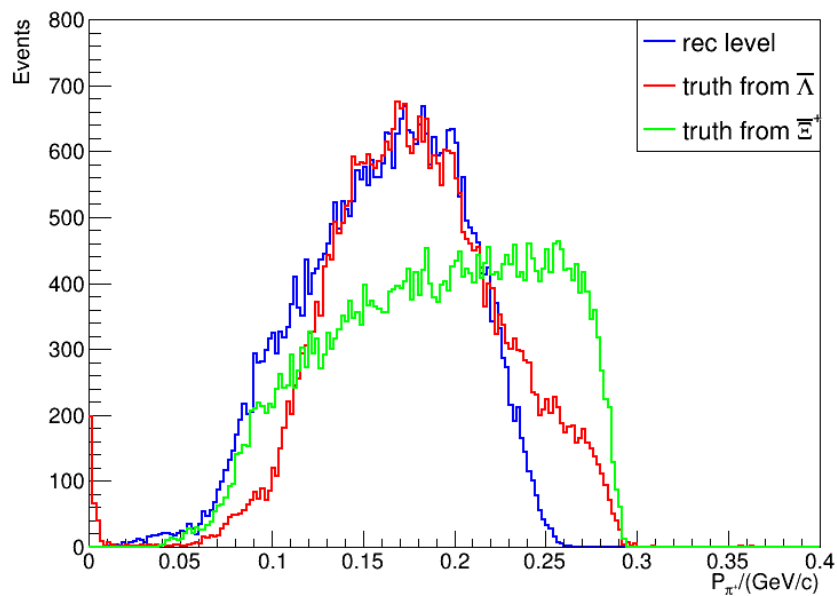
➤ Cut flow

Selection Criteria	OSCAR			BESIII		
	Absolute Efficiency(%) signal	Relative Efficiency(%) signal	Absolute Efficiency(%) dominant bkg	Absolute Efficiency(%) signal	Relative Efficiency(%) signal	Absolute Efficiency(%) dominant bkg
After DT Vertex fit	19.38	49.05	21.83	13.58	49.80	15.69
veto dominant bkg	15.87	81.88	5.02	11.99	88.29	2.97
$\frac{L_{\Lambda}}{\sigma_{L_{\Lambda}}} > 0$	12.74	80.15	2.14	9.98	83.24	2.39
$\frac{L_{\Xi^-}}{\sigma_{L_{\Xi^-}}} > 0$	9.69	75.87	1.01	8.60	86.17	1.26
$\chi^2 < 20$	8.99	93.01	0.57	6.77	78.72	0.422
$ M_{p^+\pi^-} - M_{\Lambda}^{\text{PDG}} < 6\text{MeV}$	8.63	95.85	0.42	6.50	96.01	0.417

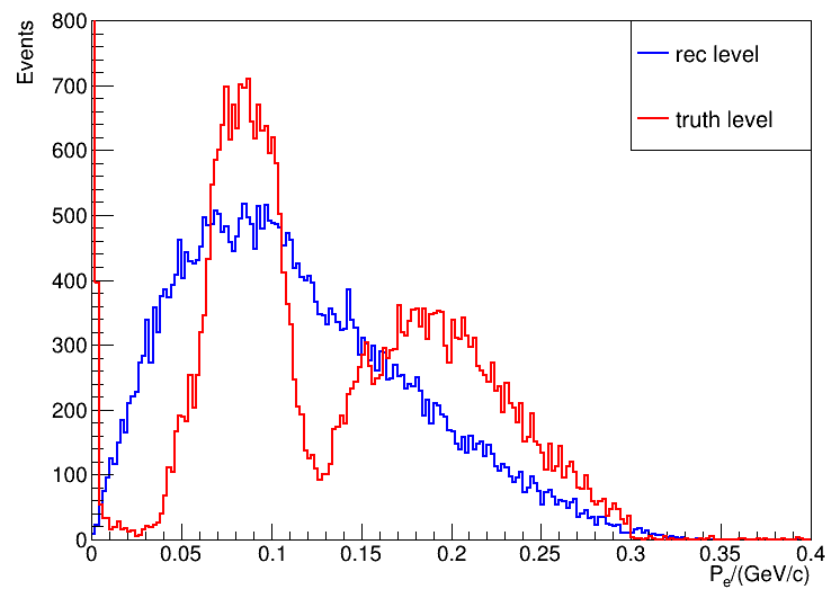
$$\text{OSCAR} : \frac{S}{\sqrt{S+B}} \approx 27.10$$

$$\text{BESIII} : \frac{S}{\sqrt{S+B}} \approx 1.12$$

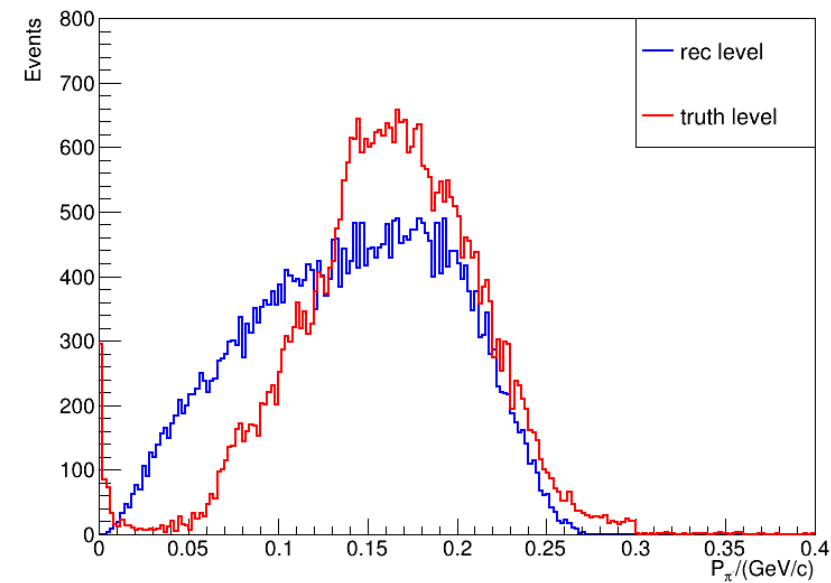
Truth VS Rec level(after GlobalPID)



P_{π^+}



P_{e^-}



P_{π^-}

- This work is now ready to study at the STCF under the OSCAR framework.
- Efficiency and signal-to-noise ratio have both been significantly improved compared to BESIII before GlobalPID. However, we hope to further improve GlobalPID in future studies.
- Understanding the reasons for the deviations in the central values and the asymmetry in the distribution of the numerous reconstructed mass spectra, and make further corrections.
- Improving efficiency, especially in electronic identification.

Thanks!