



中国科学院大学  
University of Chinese Academy of Sciences



ICTP-AP  
International Centre  
for Theoretical Physics Asia-Pacific  
国际理论物理中心-亚太地区

# Topological Solitons, Phase Transitions and Gravitational Waves

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4.25, 2025



# Outline

- Why do we want to study solitons?
- Magnetic Monopoles
- Gravitational waves from cosmic phase transitions and Cosmic strings
- How to detect their gravitational waves?

Motivated by the desire to explore the new tool: gravitational waves

# Hulse–Taylor Binary

## The Nobel Prize in Physics 1993



Photo from the Nobel  
Foundation archive.

Russell A. Hulse

Prize share: 1/2



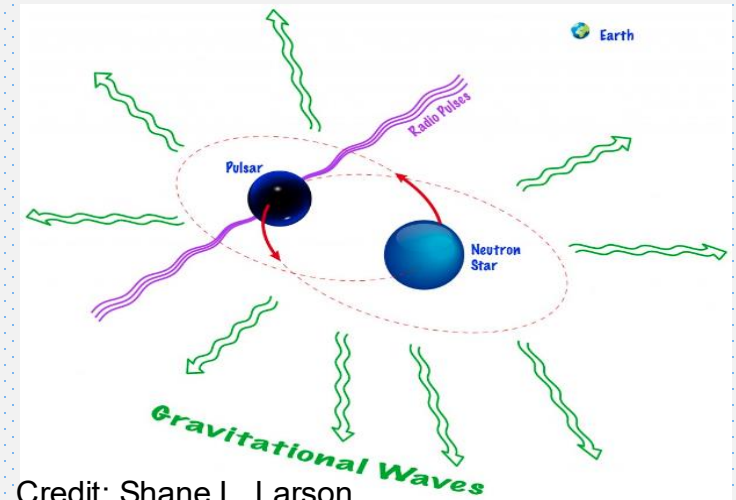
Photo from the Nobel  
Foundation archive.

Joseph H. Taylor Jr.

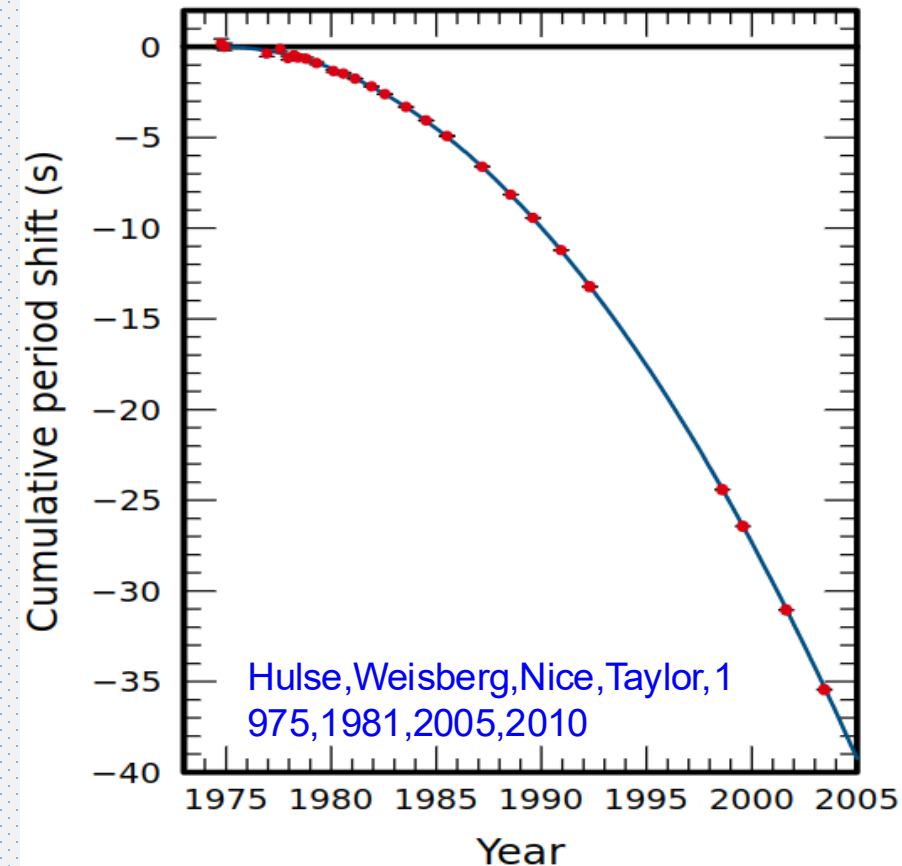
Prize share: 1/2

[www.nobelprize.org](http://www.nobelprize.org)

The Nobel Prize in Physics 1993 was awarded jointly to Russell A. Hulse and Joseph H. Taylor Jr. "for the discovery of a new type of pulsar, a discovery that has opened up new possibilities for the study of gravitation"



Credit: Shane L. Larson



# The Gravitational Wave Spectrum

Sources

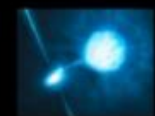
Detectors



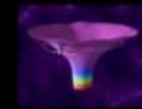
Big Bang



Supermassive Black Hole Binary Merger



Compact Binary Inspiral & Merger



Extreme Mass-Ratio Inspirals



Pulsars, Supernovae



age of the universe

Wave Period

years

hours

seconds

milliseconds

$10^{-16}$

$10^{-14}$

$10^{-12}$

$10^{-10}$

$10^{-8}$

$10^{-6}$

$10^{-4}$

$10^{-2}$

1

$10^2$

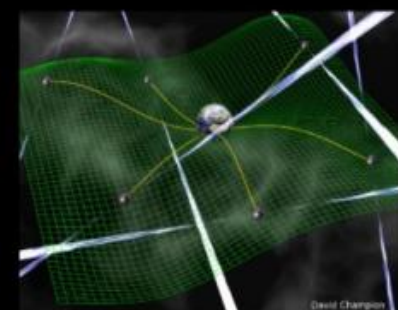
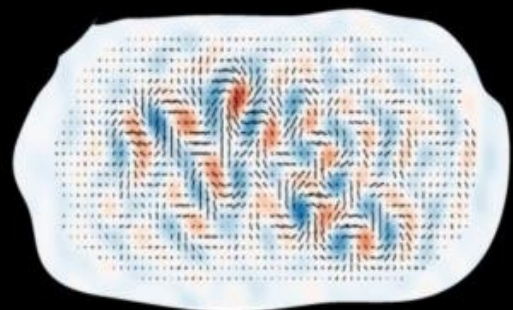
Wave Frequency

CMB Polarization

Radio Pulsar Timing Arrays

Space-based interferometers

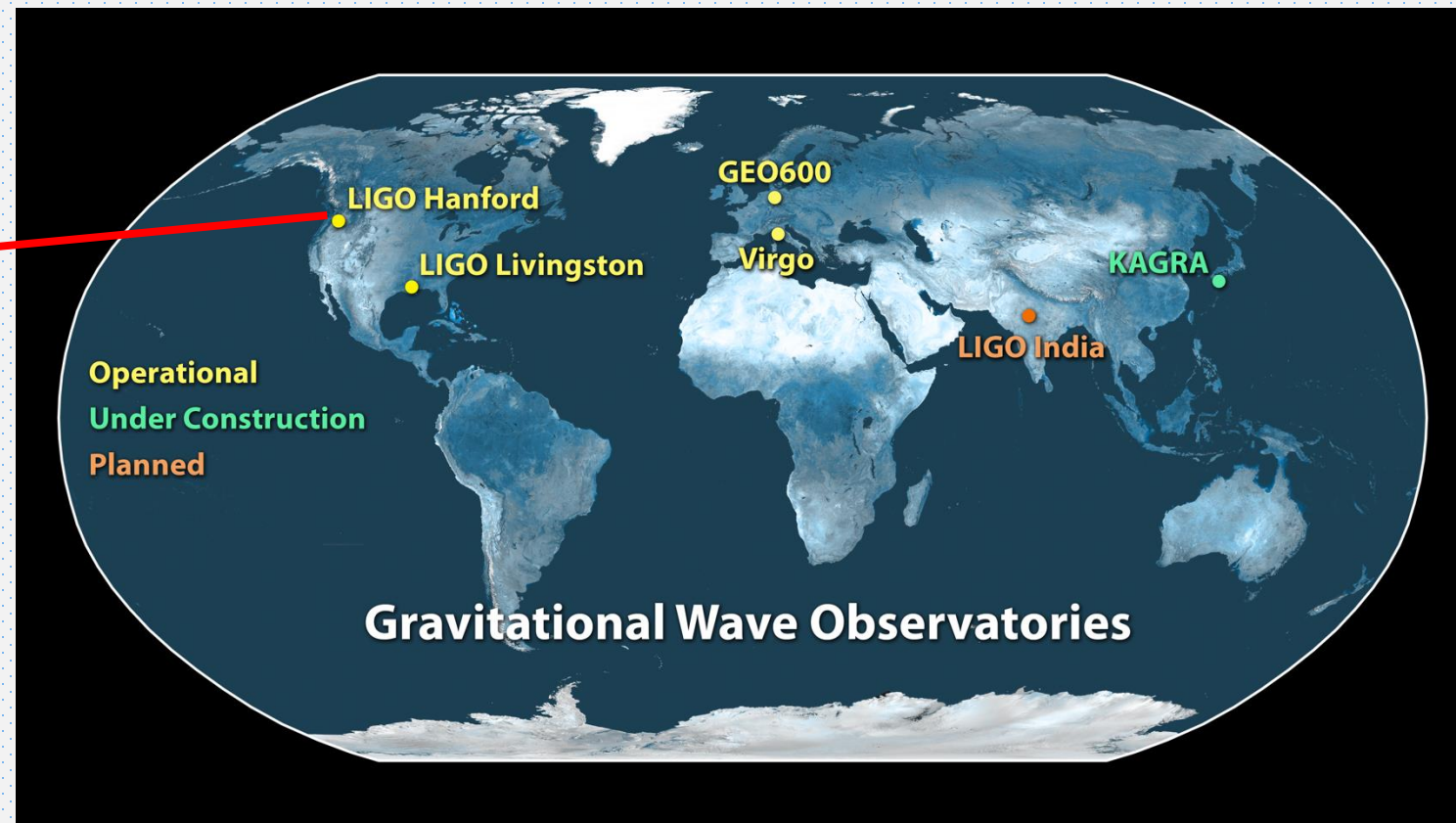
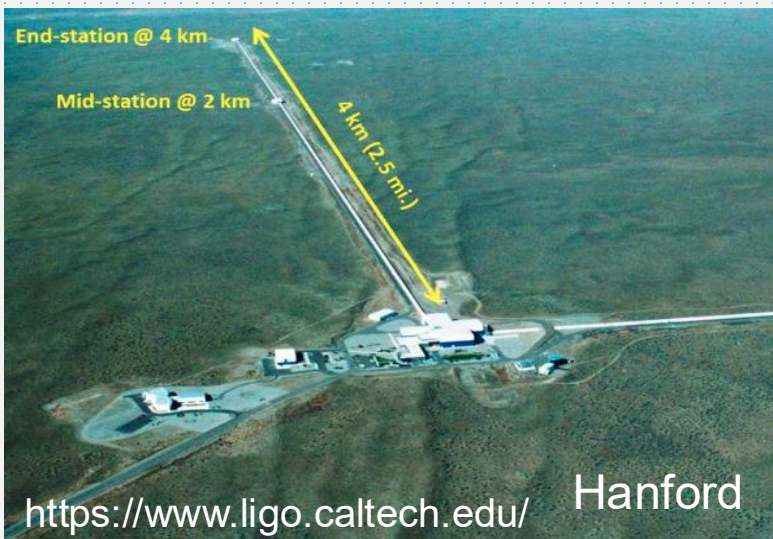
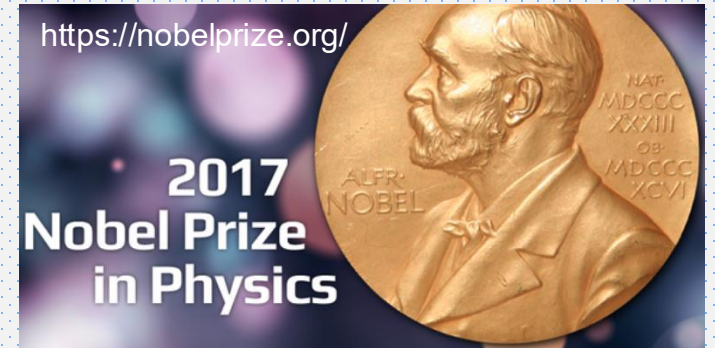
Terrestrial interferometers

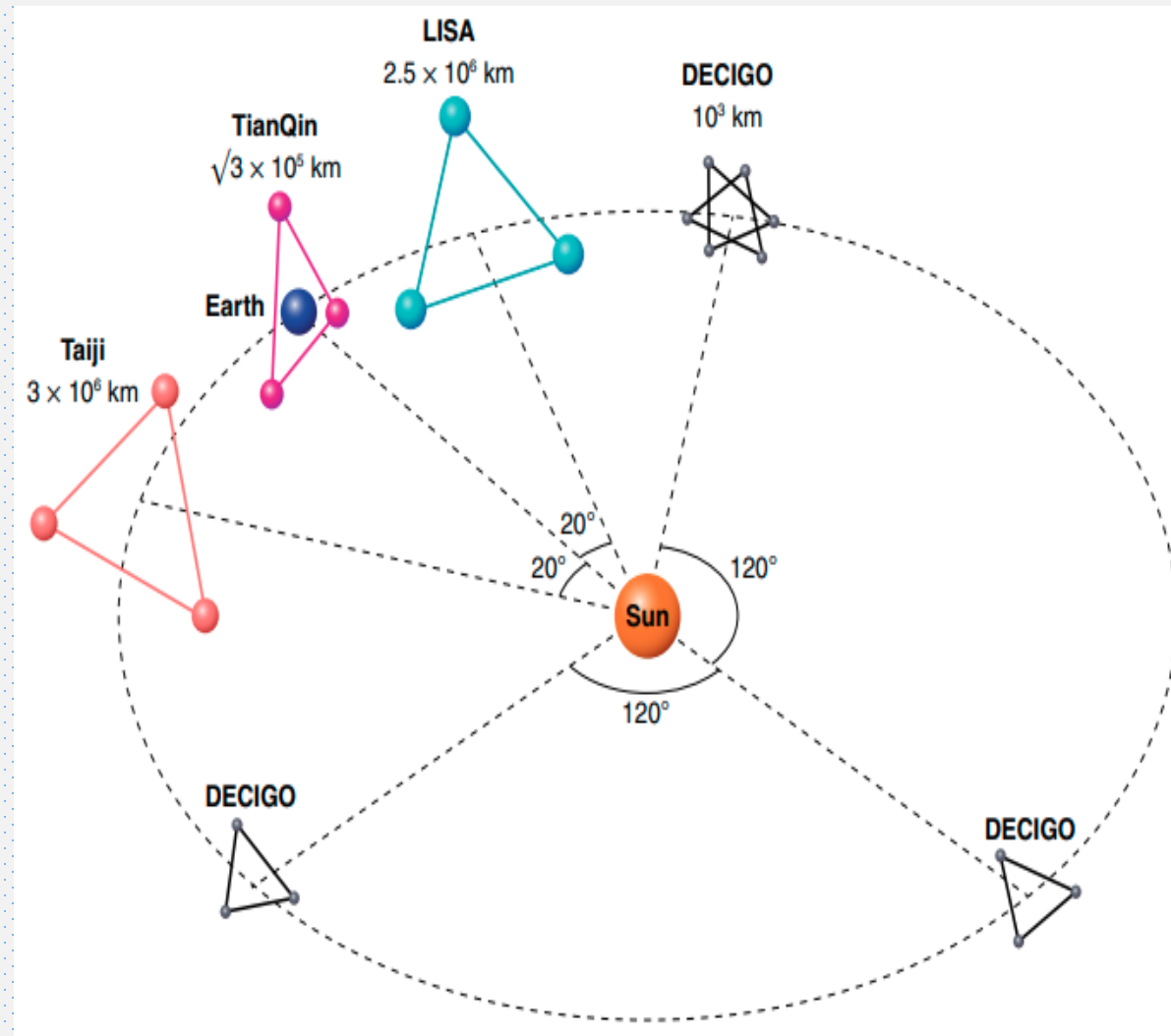




# LIGO

First direct detection of gravitational waves.  
A new era for astronomy, and fundamental physics





Nature Astronomy, Gong, Luo, Wang (2021)



中国科学院牵头成立了我国空间探测工作组，并首次在ELISA联盟会议上，提出了中国空间引力波探测计划

正式对外公布“太极计划”，明确了“单星、双星、三星”三步走的发展战略

“三步走”的第一步（单星工程任务）正式启动实施

2019年8月31日，“太极一号”成功发射

“太极一号”通过在轨实验，验证了关键技术路线的可行性，完成了我国空间引力波探测的第一步，成功入选2019年的“中国十大科技进展新闻”和中国科学院年度科技创新亮点成果

太极二号、太极三号



白春礼院长在开学典礼上通报发射成功的喜讯

任务团队在酒泉卫星发射中心合影留念

2019年



~2035年

2018年

2017年

小提示

2016年

2015年

小提示

2015年9月14日，激光干涉引力波天文台（LIGO）首次直接探测到引力波

2017年10月3日，诺贝尔物理学奖授予三名美国科学家雷纳·韦斯（Rainer Weiss）、巴里·巴里什（Barry C. Barish）和基普·索恩（Kip S. Thorne），以表彰他们为LIGO项目和发现引力波所作的贡献



作为太极实验室的挂靠单位，国际理论物理中心（亚太地区）正式启动运行

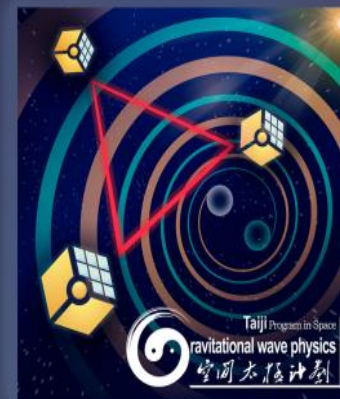
重大意义

中国首颗空间引力波探测技术实验卫星

中国首次在轨无拖曳控制技术试验

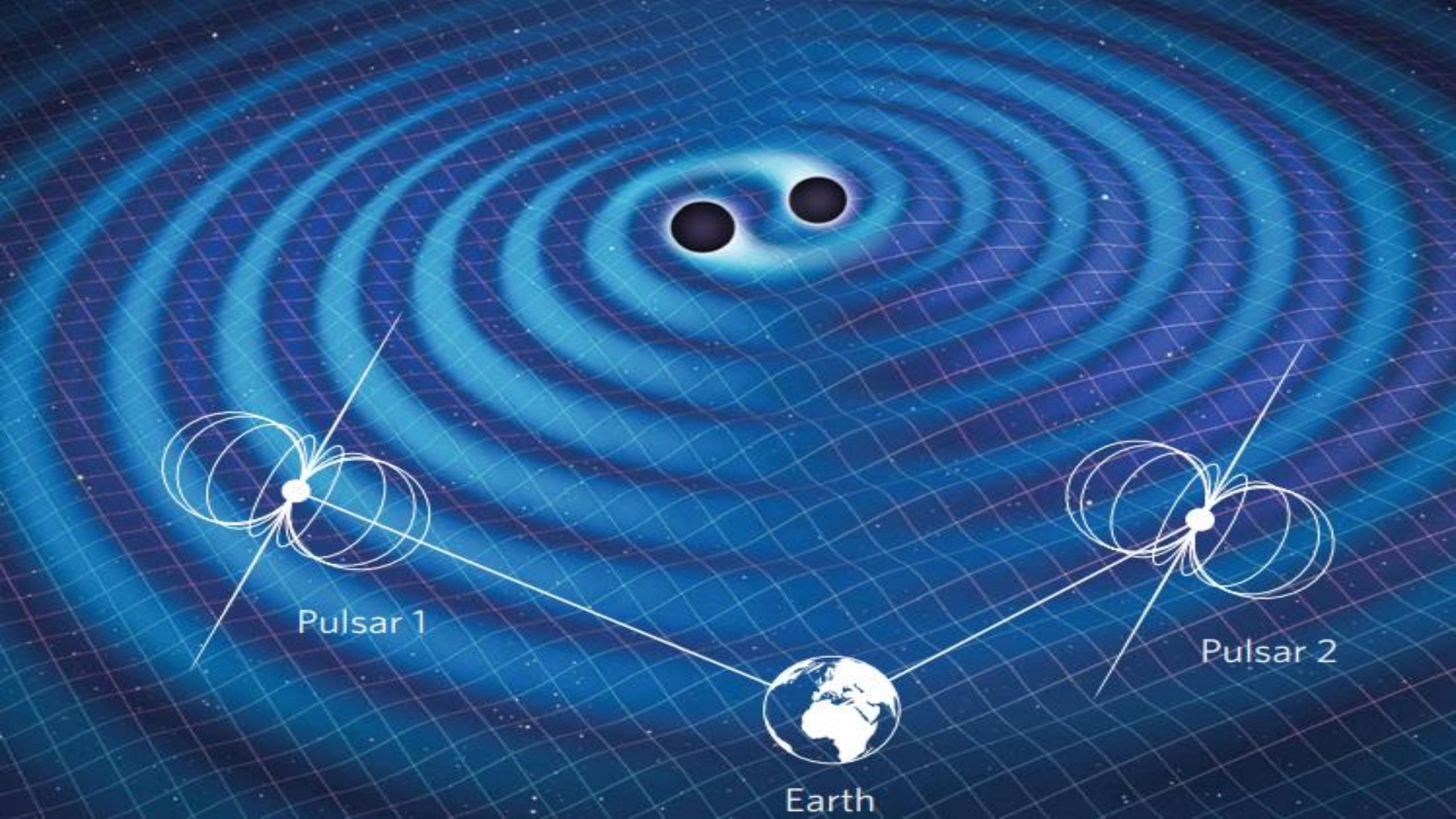
中国最高精度的空间激光干涉测量

国际上首次在轨验证微牛级射频离子和双模霍尔电推进技术



2012年



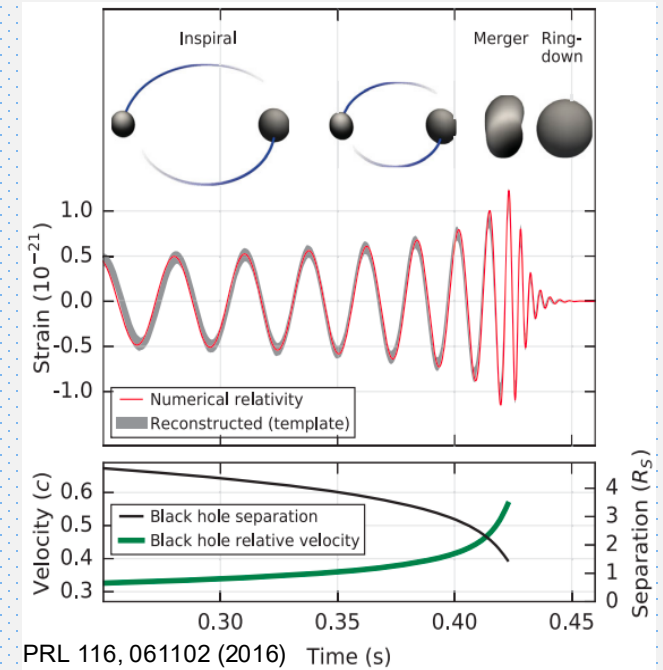




# Why Solitons?

GW generation requires **macroscopic mass/energy**

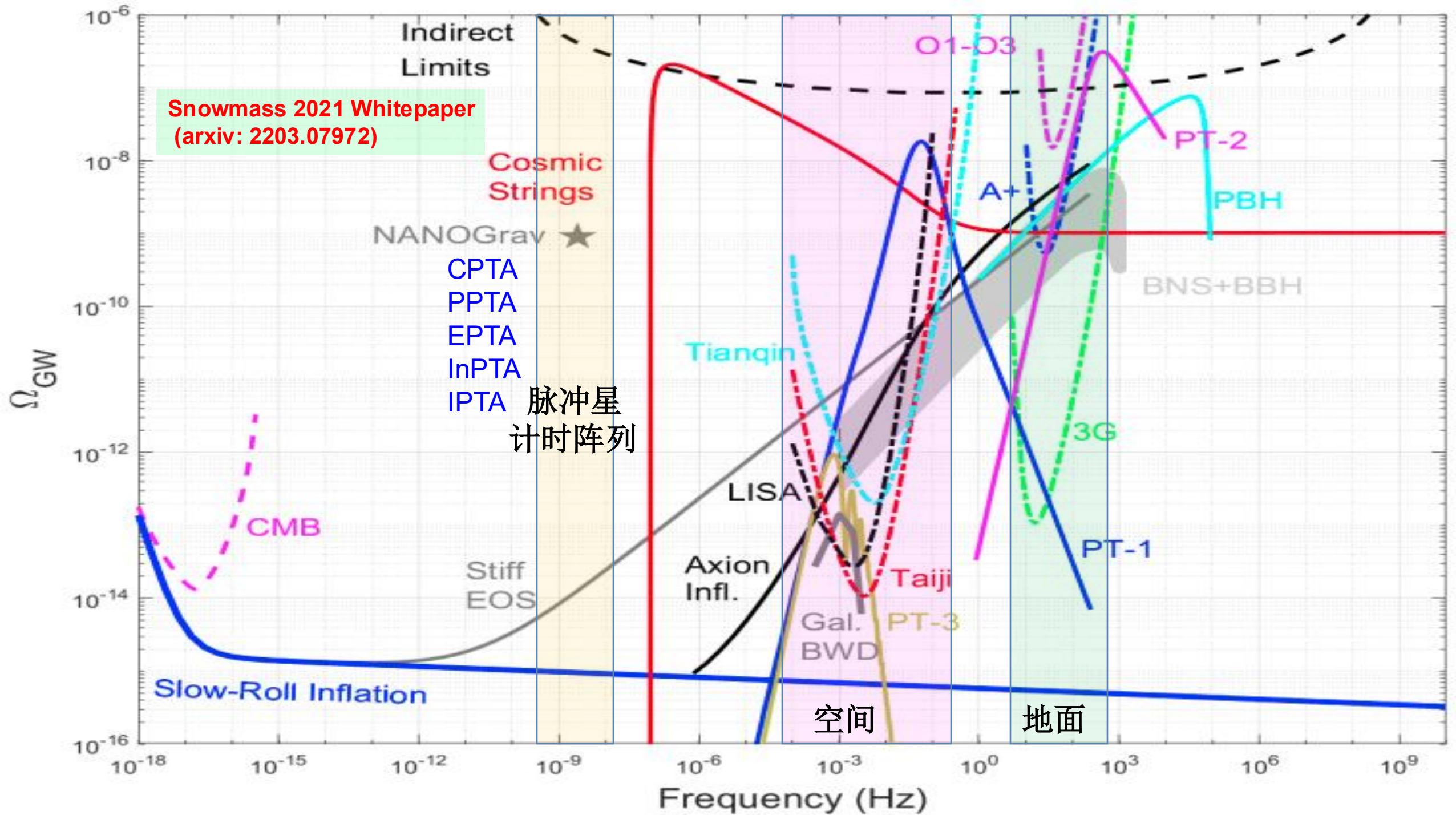
$$\square^2 h_{\mu\nu} = -16\pi G \overset{\text{matter}}{S_{\mu\nu}} \rightarrow \text{matter}$$



$$h \sim 10^{-22} \frac{\boxed{M/M_{\odot}}}{\boxed{r/100\text{Mpc}}} \left(\frac{v}{c}\right)^2 \rightarrow \text{huge mass/energy}$$

How to study particle physics with GWs?

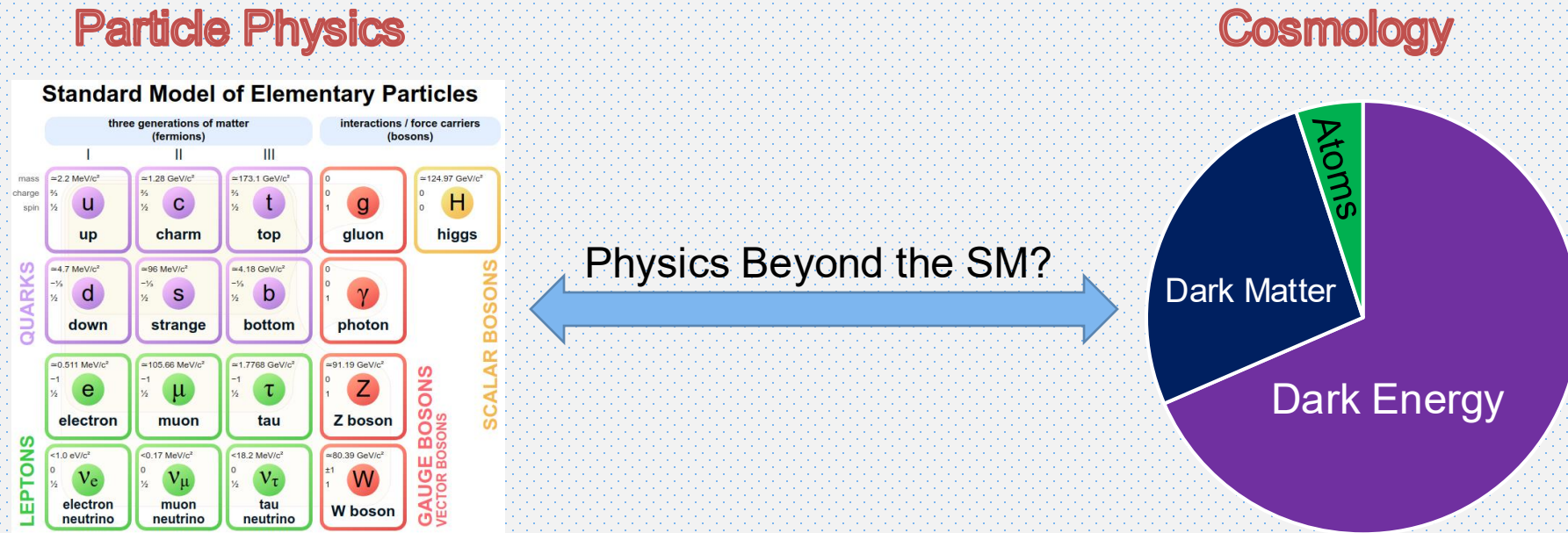
Answer: make it much bigger





# New Perspectives?

How to reconcile the two standard models?



## REVIEW

<https://doi.org/10.1038/s41586-019-1129-z>

### The new frontier of gravitational waves

M. Coleman Miller<sup>1,2\*</sup> & Nicolás Yunes<sup>3\*</sup>

What is dark matter? (solitons)

Why more matter than anti-matter? (phase transitions, solitons)

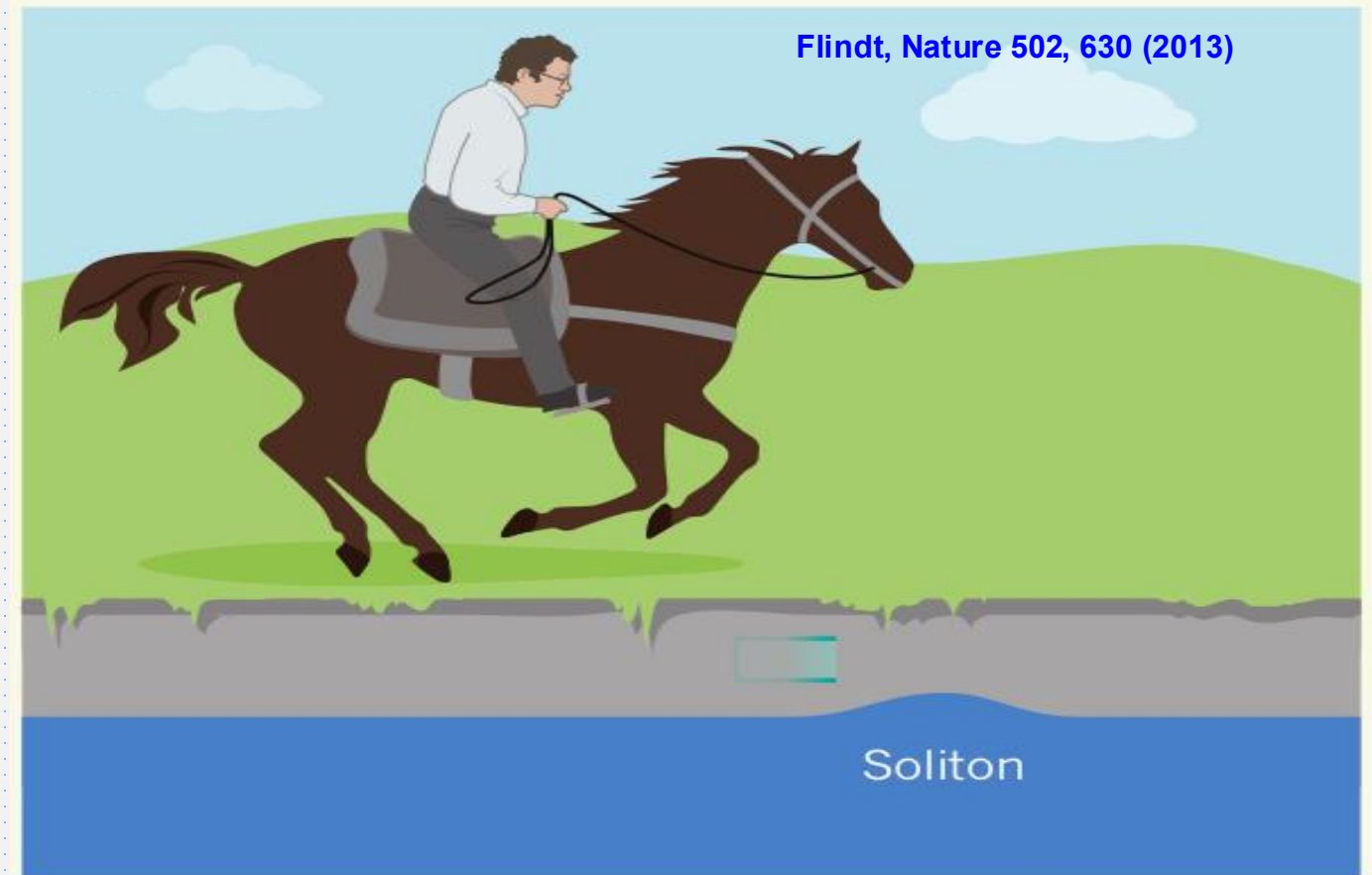
# Solitons

- Localized
- Associated with nonlinear problem

Found in:

- ✓ Optics
- ✓ Hydrodynamics
- ✓ Condensed matter systems
- ✓ Quantum field theory (this talk)

...





# Solitons in Quantum Field Theory

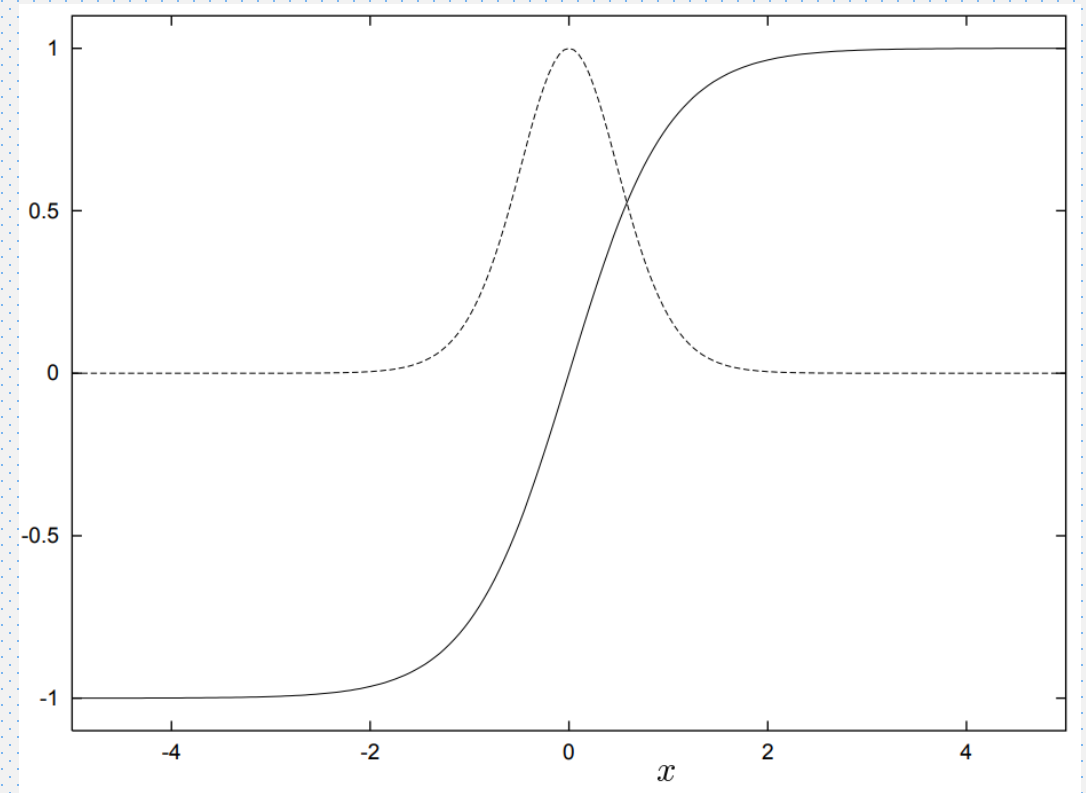
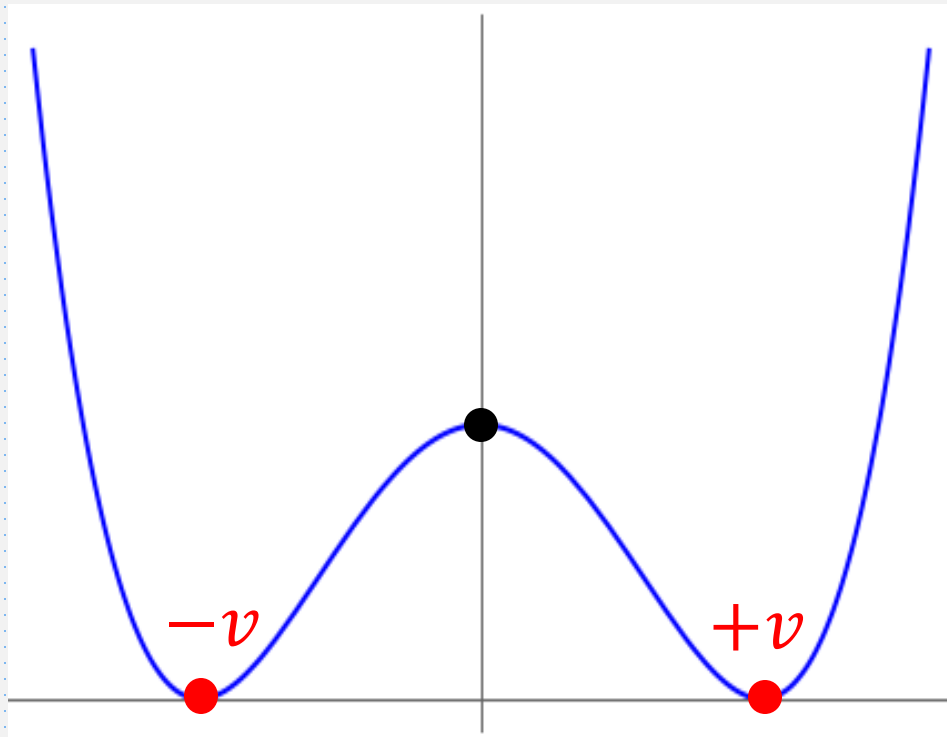
- Both are **solitonic** solutions to **classical** field equations
- Differ in the nature, context, and how they are stabilized

	Topological Solitons	Non-Topological Solitons
Definition	<p>Static Solution (Theory with Spontaneously Broken Symmetry)</p> <ul style="list-style-type: none"> <li>● Global symmetry (Skyrmion, Cosmic String)</li> <li>● Discrete symmetry (<b>Domain wall</b>)</li> <li>● Local symmetry (<b>Monopole</b>, <b>Cosmic String</b> or Vortex line...)</li> <li>● Pure gauge theory (Instanton)</li> </ul>	<p>Bose-Einstein Condensate of Ultralight particles (DM)</p> <ul style="list-style-type: none"> <li>● Galactic scale (DM Halo)</li> <li>● Stellar scale (<b>Boson stars</b>)</li> </ul>
Boundary	Non-Trivial (needs degenerate vacuum states)	Trivial vacuum state
Stabilized by	Topology (boundary field values)	<p>Conserved Charge, and Balancing</p> <ul style="list-style-type: none"> <li>● quantum pressure</li> <li>● gravity (or not, Q-balls etc)</li> <li>● self-interactions (or not)</li> </ul>

# Kinks/Domain Wall

$$\pi_0(\mathcal{M})$$

$$\mathcal{L} = \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - \lambda (v^2 - \phi^2)^2$$



Topological Solitons, Manton, Sutcliffe



# Cosmic String/Vortex Line

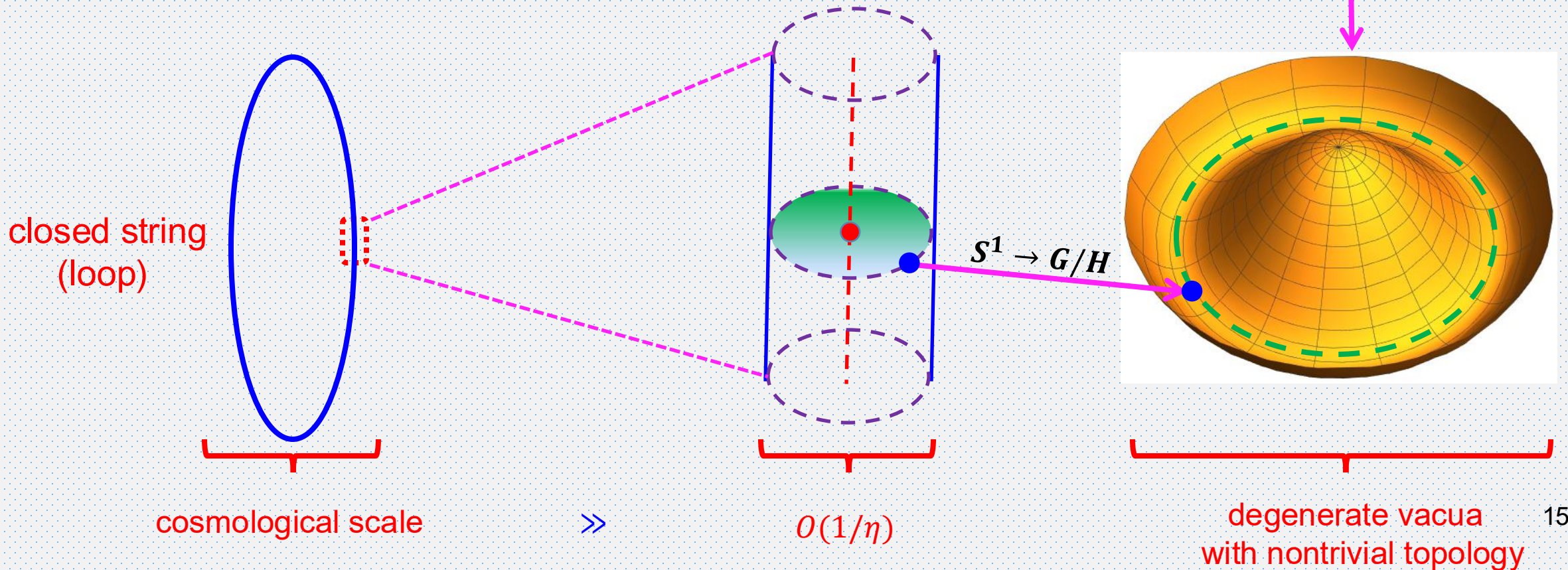
$$\pi_1(\mathcal{M})$$

$$G\mu \sim \left( \frac{\eta}{10^{19} \text{GeV}} \right)^2$$

$\mu$ : line mass density

## Example: the Abelian Higgs Model

$$\mathcal{L} = |(\partial_\mu - igA_\mu)\Phi|^2 - \frac{1}{4}\lambda(|\Phi|^2 - \eta^2)^2 - \frac{1}{4}F_{\mu\nu}F^{\mu\nu}$$



# Topological Solitons in the Early Universe

- Firstly proposed to form in the early universe (Kibble, 1976)  
(None observed)
- Later proposed to form in condensed matter systems (Zurek, 1985)  
(already observed)

Name variant:  
Topological Defects

## Topology of cosmic domains and strings

T W B Kibble

[J.Phys.A 9 \(1976\) 1387-1398](#)

Blackett Laboratory, Imperial College, Prince Consort Road, London

Received 11 March 1976

[www.theguardian.com](http://www.theguardian.com)



## The Cosmological Kibble Mechanism in the Laboratory: String Formation in Liquid Crystals

[Science, 263 \(1994\)](#)

Mark J. Bowick,\* L. Chandar, E. A. Schiff, Ajit M. Srivastava





Radius of the Visible Universe

Quantum  
Fluctuations

Inflation

Inflation Ends

Protons Formed

Nuclear Fusion Begins

Nuclear Fusion Ends

Cosmic Microwave Background

Dark Ages

First Stars & Galaxies Form

Modern Universe

Today

0

$10^{-32}$

$1 \mu\text{s}$

0.01 s

3 min

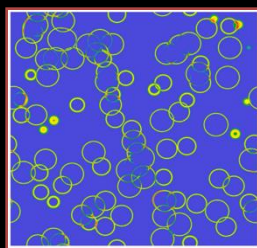
380,000 yrs

200 Million yrs

13.8 Billion yrs

Age of the Universe

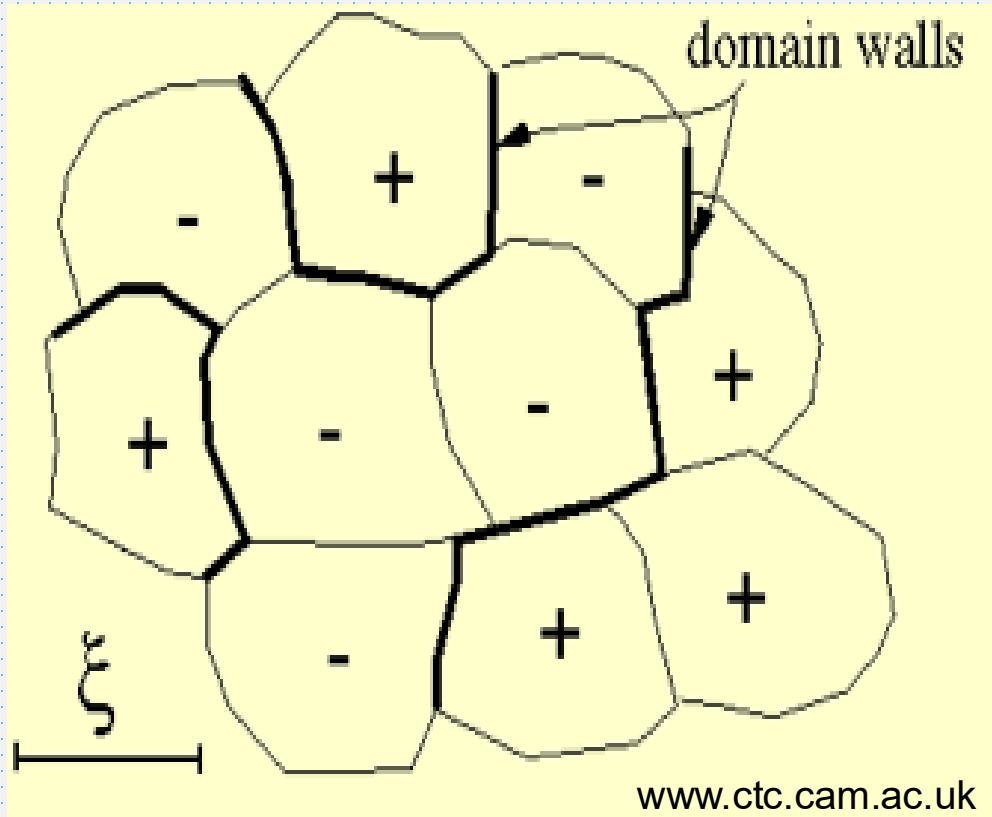
first order PT, cosmological defects (cosmic string)





# Topological Solitons in the Early Universe

$$V(\phi) = \frac{1}{4}(\phi^2 - v^2)^2$$



$$V(\Phi) = \frac{1}{4}(|\Phi|^2 - \eta^2)^2$$

