



中山大學
SUN YAT-SEN UNIVERSITY



*STCF*实验下研究双粲偶素 $\eta_c J/\psi$ 的产生

Study for the double charmonium $\eta_c J/\psi$ production at STCF

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超级陶粲装置研讨会

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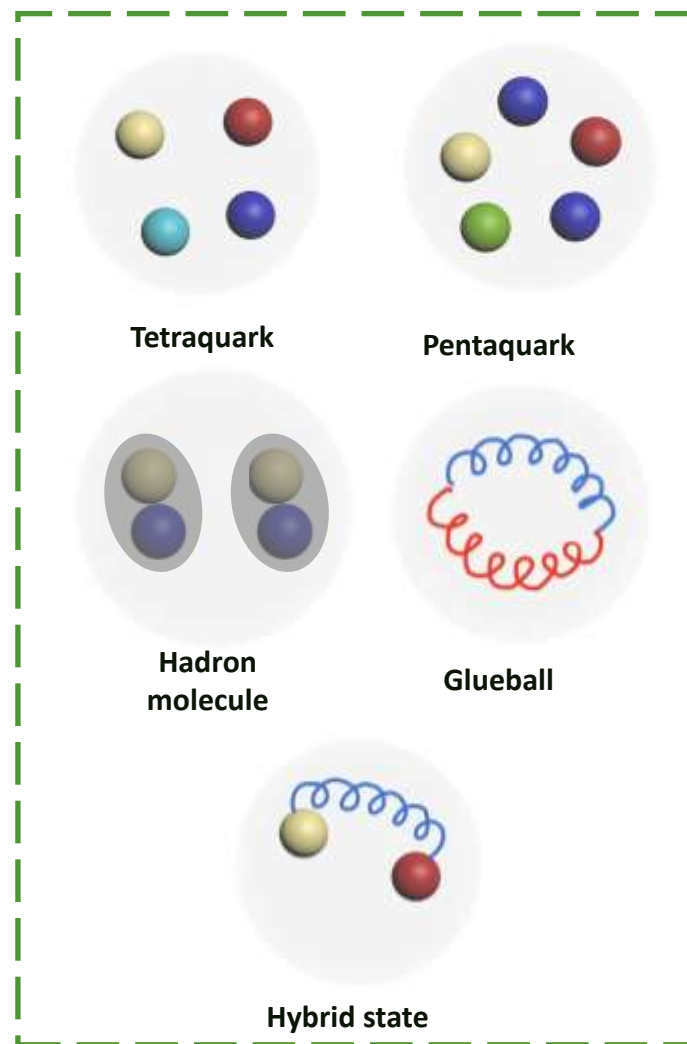
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Background analysis

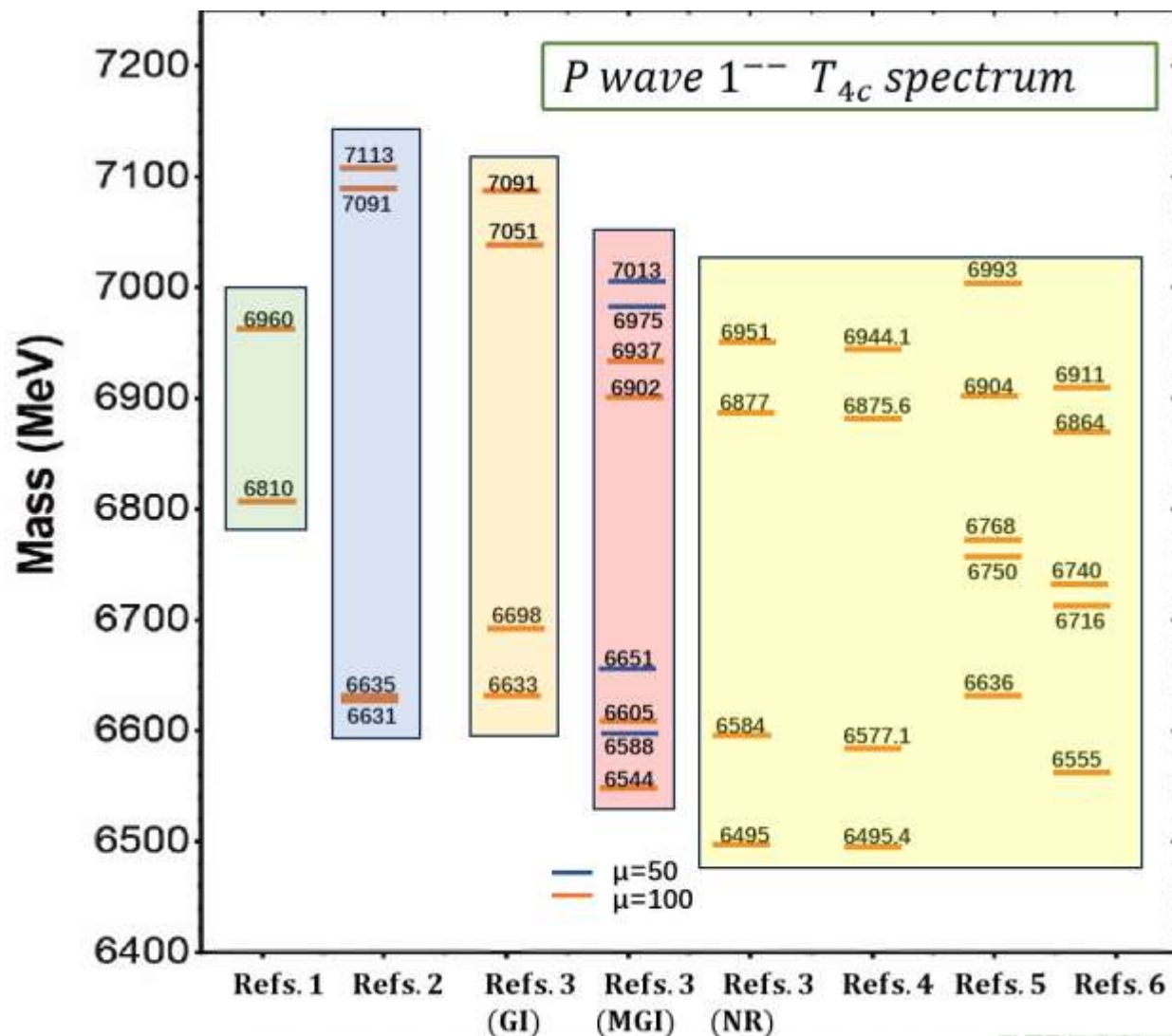
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- 2003年以前，人们认为粲偶素是粲夸克和反粲夸克的束缚态，应该用非相对论的势能夸克模型来描述。然而，自2003年 Belle 发现 X(3872) 以来，通过各种实验包括 BESIII、BaBar、Belle、CDF、DO、ATLAS、CMS 和 LHCb，在粲偶素质量区观测到大量新的共振态结构，这些共振态称为奇特态，即 XYZ 粒子。
- 奇特强子态包括强子分子态、四夸克态、五夸克态以及混杂态等。
- 双粲偶素也称全粲四夸克态，夸克组成为 $\bar{c}\bar{c}cc$ 。



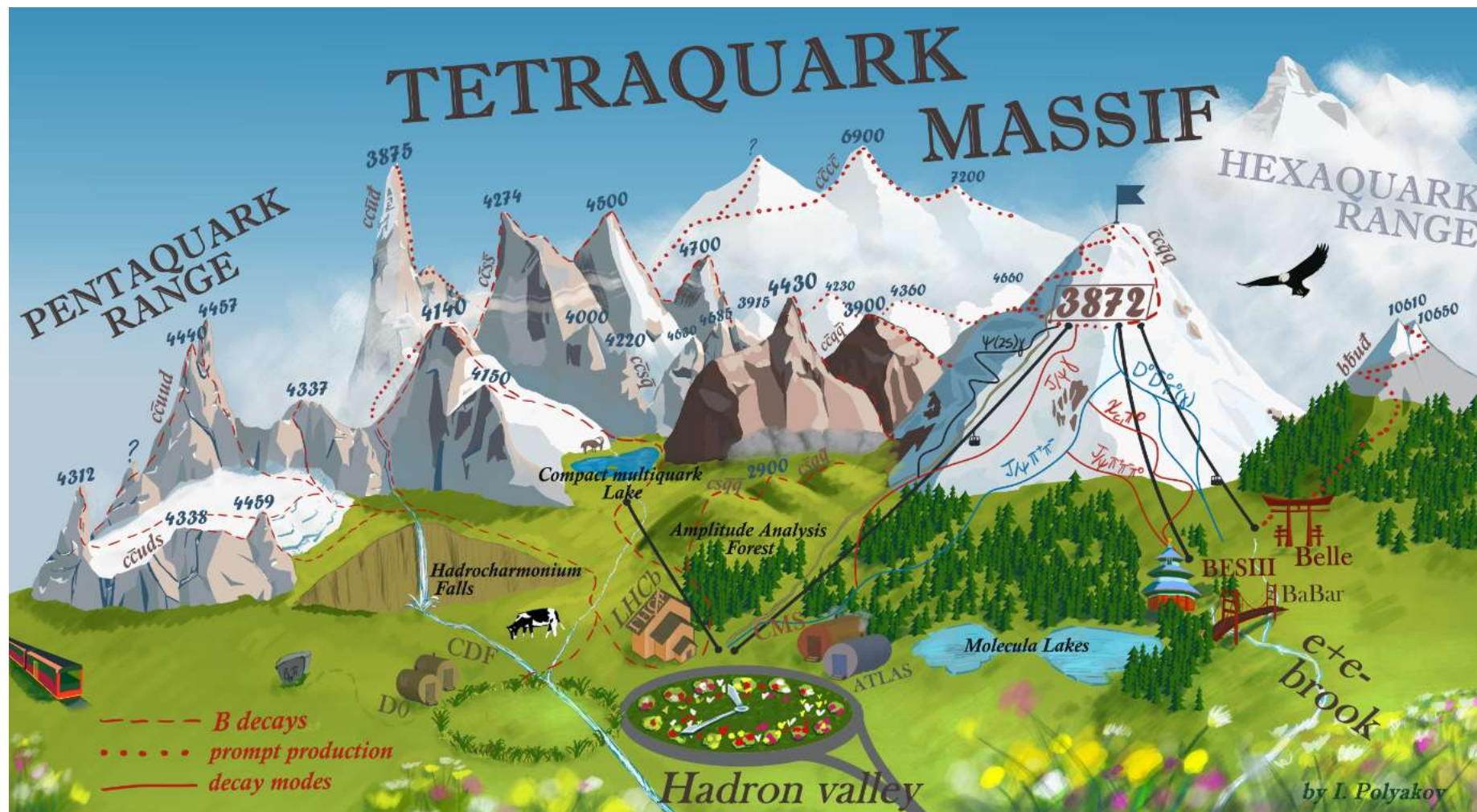
➤ 目前与全粲四夸克态相关的五个理论模型理论研究调研结果



- QCD Sum Rules
- Relativistic Quark Model
- Godfrey-Isgur relativized diquark model
- The modified Godfrey-Isgur relativized diquark model with the color screening effects
- Nonrelativistic Quark Model

➤ 量子数为 1^{--} 的全粲四夸克态的质量理论预言范围在：**6.495~7.113 GeV**

➤ 目前奇特强子态的实验研究成果

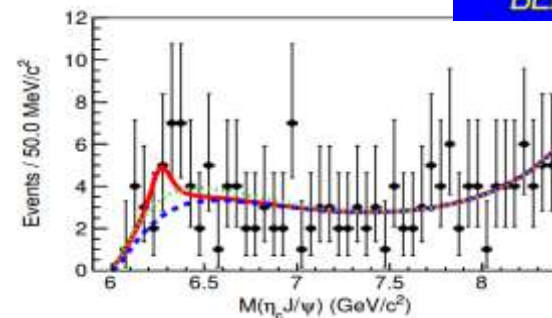


★ Hüsken N, Norella E S, Polyakov I. A Brief Guide to Exotic Hadrons[J]. arXiv:2410.06923, 2024.

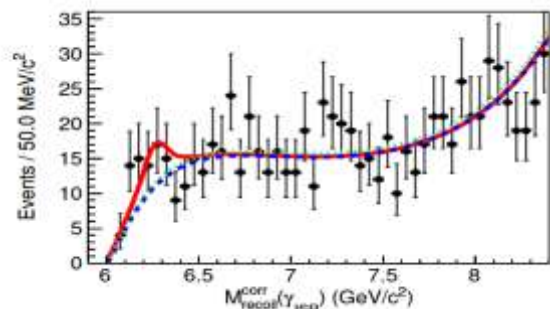


➤ Search for the double-charmonium state with $\eta_c J/\psi$ @ Belle

- 产生过程: $e^+e^- \rightarrow (\gamma_{ISR})\eta_c J/\psi$
- 能区: 10.52GeV
- 衰变模型:
 - J/ψ : $e^+e^-, \mu^+\mu^-$
 - η_c : $p\bar{p}, p\bar{p}\pi^0, K_0^S K^\pm \pi^\mp, K^+ K^- \pi^0, K^+ K^- K^+ K^-, 2(\pi^+ \pi^- \pi^0)$
- 积分亮度: 980fb^{-1}
- 质量: $6267 \pm 43\text{MeV}/c^2$
- 衰变宽度: $121 \pm 72\text{MeV}$
- 显著度结果: 2.1σ (阈值附近)



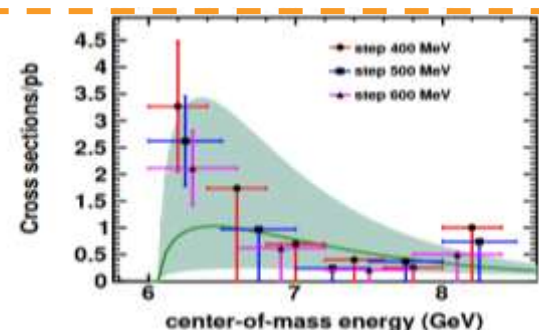
图A



- $\eta_c J/\psi$ 质量区间: $[6.0, 6.6]\text{GeV}/c^2$
- 截面结果: $2.1 \pm 0.7 \pm 0.2\text{pb}$

- Continuum产生截面拟合函数: $\sigma = A \frac{\sqrt{2\mu\Delta M}}{\left(\frac{s}{s_0}\right)^n}$

$$\Delta M = \sqrt{s} - m(\eta_c) - m(J/\psi)$$



图B

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Exclusive MC production under OSCAR 2.6.2

产生子: ConExc

$\sqrt{S}$: 6.73GeV

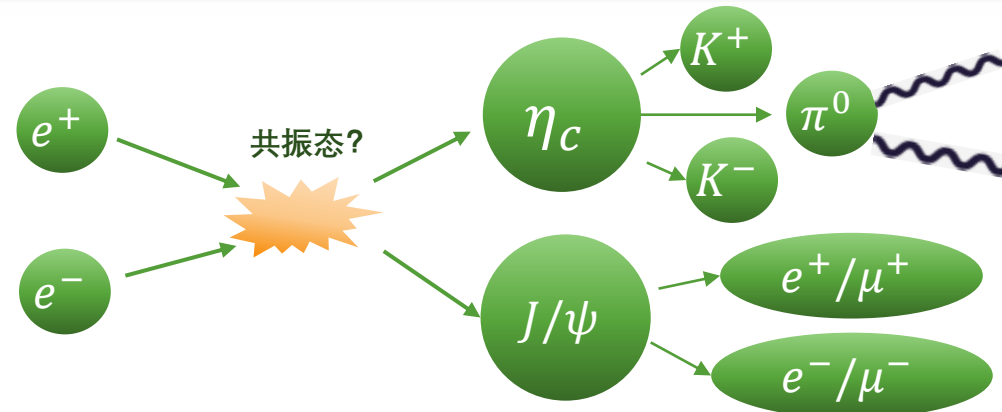
事例数: 100000

信号道: $e^+e^- \rightarrow T_{4c} \rightarrow \eta_c J/\psi$,

- $\eta_c \rightarrow K^+ K^- \pi^0$, $\pi^0 \rightarrow \gamma\gamma$
- $J/\psi \rightarrow \mu^+ \mu^-$ and $e^+ e^-$

衰变卡

```
Particle vpho 6.7300 0.0
Decay vpho
1.0000 gamma gamma* ConExc -2 443 441;
Enddecay
#
Decay gamma*
1.0000 eta_c J/psi PHSP;
Enddecay
#
Decay J/psi
1.0000 e+ e- PHOTOS VLL;
Enddecay
#
Decay eta_c
1.0000 pi0 K+ K- PHSP;
Enddecay
#
Decay pi0
1.0000 gamma gamma PHSP;
Enddecay
End
```



- 利用Breit-Wigner公式获得输入截面分布模拟共振态

- 公式: $\sigma(e^+e^- \rightarrow T_{4c}) = \mathcal{B}_{T_{4c} \rightarrow e^+e^-} \mathcal{B}_{T_{4c} \rightarrow \eta_c J/\psi} \frac{12\pi\Gamma_0^2}{(s-m_{T_{4c}}^2)^2 + m_{T_{4c}}^2 \Gamma_0^2}$

6.72000	1.74915	0.0
6.72500	2.48728	0.0
6.73000	3.80113	0.0
6.73500	6.45682	0.0
6.74000	12.90311	0.0
6.74500	32.23149	0.0
6.75000	64.43911	0.0
6.75500	32.20762	0.0
6.76000	12.87256	0.0
6.76500	6.43104	0.0
6.77000	3.77999	0.0
6.77500	2.46962	0.0
6.78000	1.73409	0.0
6.78500	1.28226	0.0
6.79000	0.98561	0.0

选择带电径迹:

- $|d_0| \leq 1.0\text{cm}, |d_z| \leq 10.0\text{cm};$

选择光子:

- 桶部: $|\cos\theta| \leq 0.8325, E_{ecal} \geq 25\text{MeV},$
- 端盖: $0.8325 \leq |\cos\theta| \leq 0.9445, E_{ecal} \geq 50\text{MeV};$
- 飞行时间: $0 \leq |T_0| \leq 50\text{ns}$

选择 Kaon:

- Global PID : $\text{prob}(K) \geq \text{prob}(\pi) \& \& \text{prob}(K) \geq \text{prob}(\mu) \& \& \text{prob}(K) \geq \text{prob}(e)$

选择缪子:

- $0.1 \leq E_{ecal} \leq 0.3, |p_\mu| \geq 0.9\text{GeV}$

选择电子:

- $0.8 \leq \frac{E_e}{p_e} \leq 1.2, |p_e| \geq 0.9\text{GeV}$

重建 π^0 :

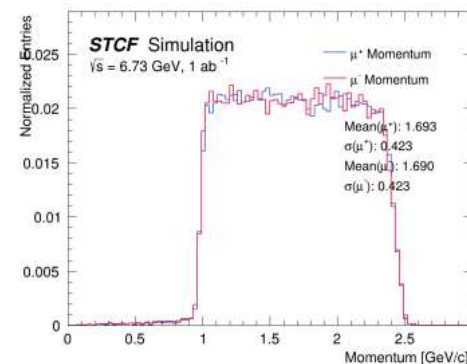
- $0.12\text{GeV} \leq M_{\gamma\gamma} \leq 0.15\text{GeV}$
- $1C$ 运动学拟合 $\chi^2 \leq 60$

重建 η_c :

- $2.78\text{GeV} \leq M_{K+K-\pi^0} \leq 3.08\text{GeV}$

重建 J/ψ :

- 顶点拟合 $\chi^2 \leq 60$
- $3.05\text{GeV} \leq M_{\mu^+\mu^-} \leq 3.15\text{GeV}$
- $3.05\text{GeV} \leq M_{e^+e^-} \leq 3.15\text{GeV}$

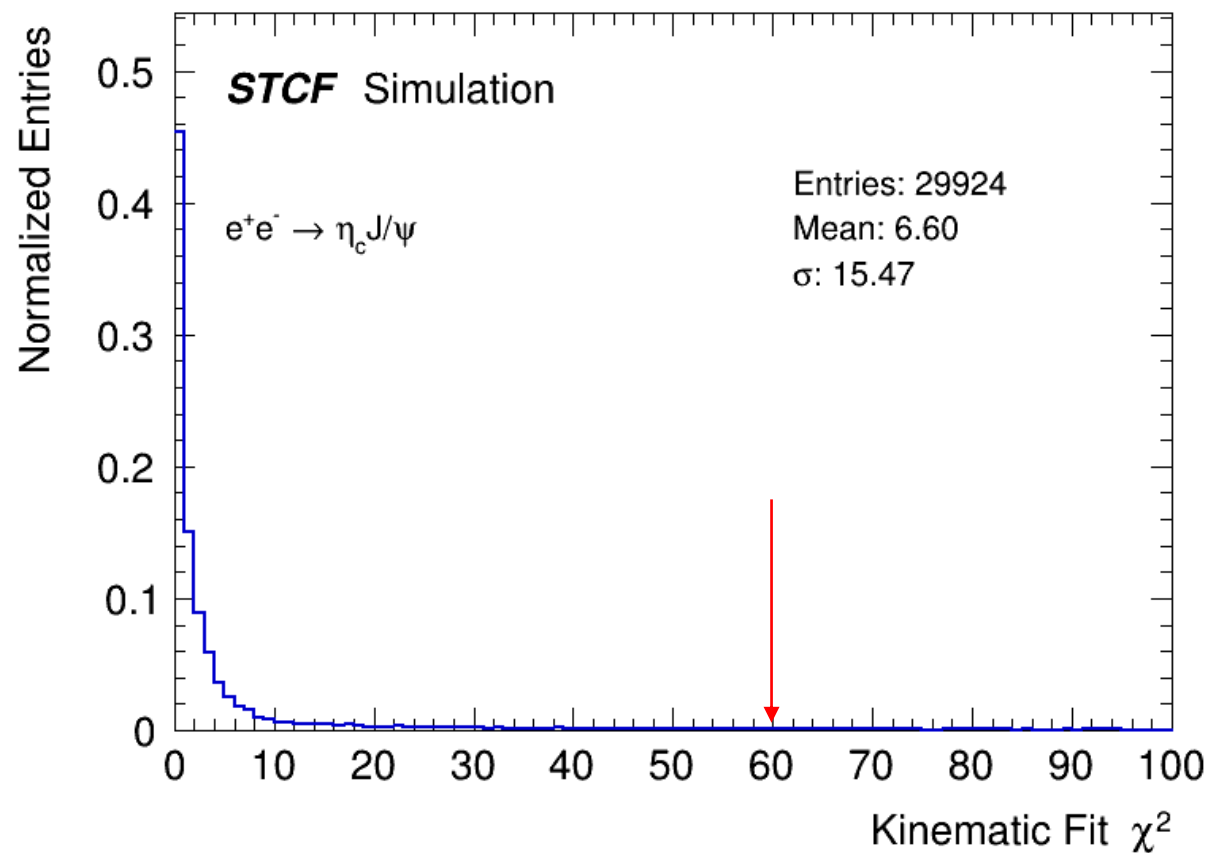
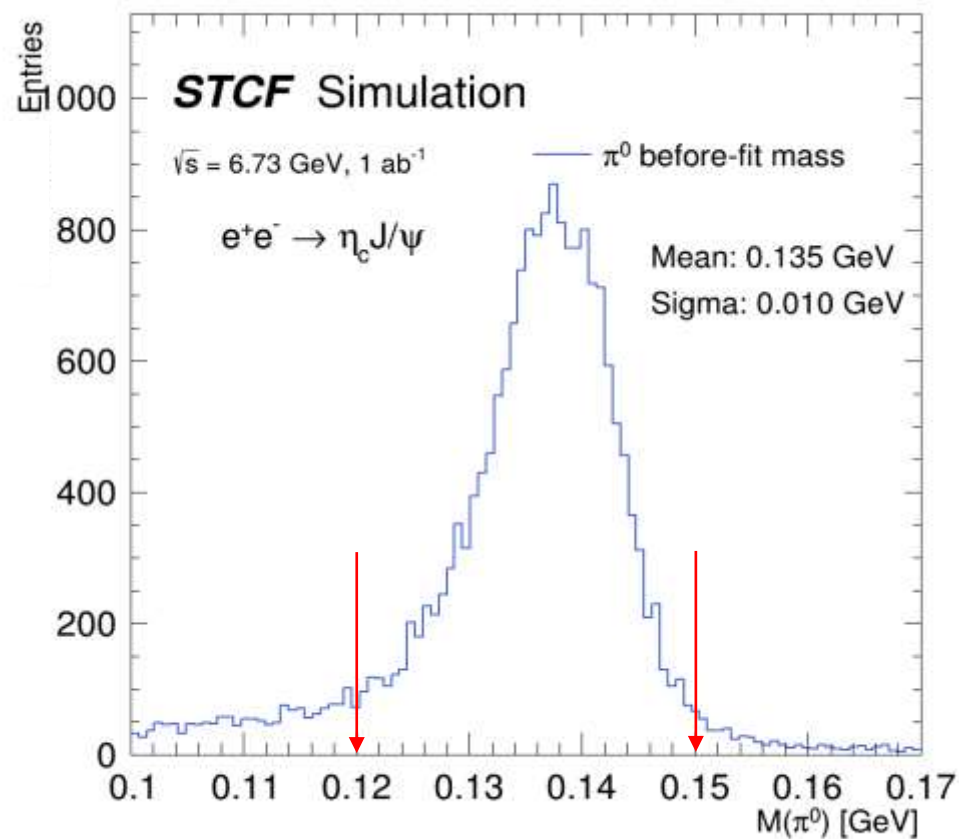


➤ $0.12\text{GeV} \leq M_{\gamma\gamma} \leq 0.15\text{GeV}$

➤ 1C运动学拟合 $\chi^2 \leq 60$

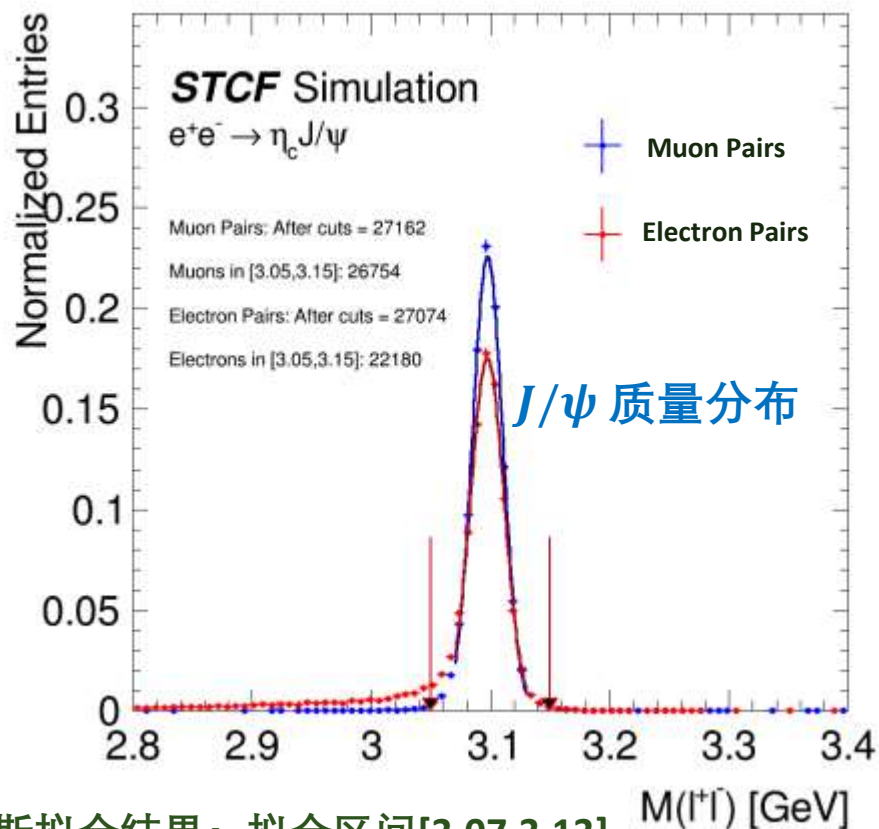
$\sqrt{s} = 6.73\text{ GeV}$

找质量最接近pi0 mass的光子组合



➤ $J/\psi \rightarrow \mu^+ \mu^-$ 和 $J/\psi \rightarrow e^+ e^-$ 的质量分布对比

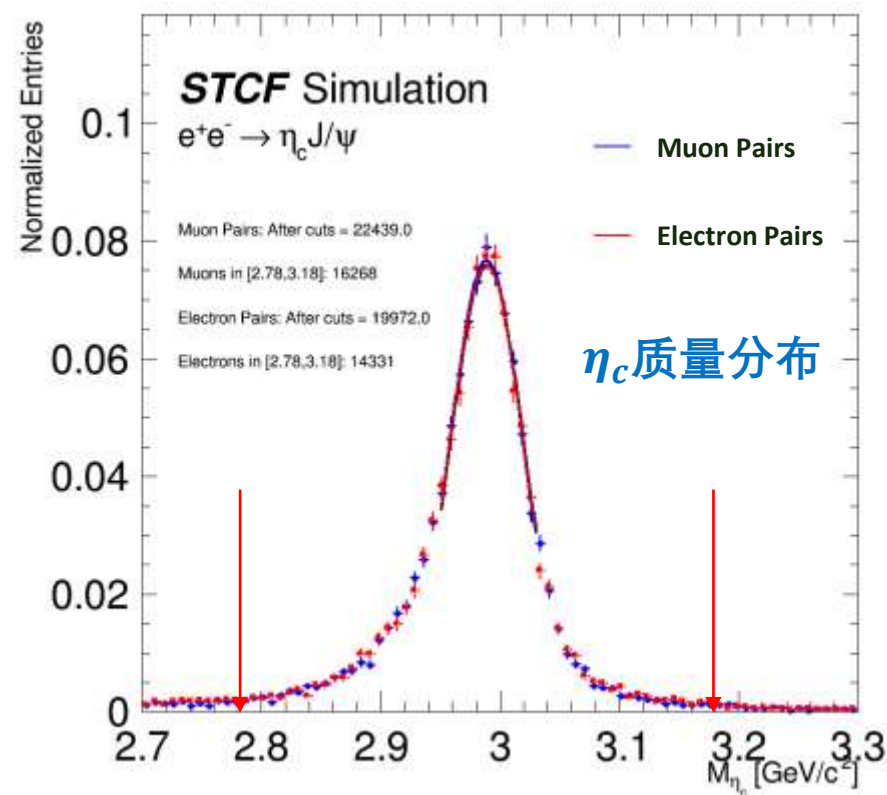
J/ψ Mass cut: $3.05 \text{ GeV} < M_{Le^+Le^-} < 3.15 \text{ GeV}$



单高斯拟合结果：拟合区间[3.07,3.13]

- $\mu: \sigma = 12.79 \pm 0.07 \text{ MeV}$, 峰值 = 3.097 ± 0.001
- $e: \sigma = 14.05 \pm 0.10 \text{ MeV}$, 峰值 = 3.096 ± 0.001

η_c Mass cut: $2.78 \text{ GeV} < M_{K^+K^-\pi^0} < 3.18 \text{ GeV}$



单高斯拟合结果：拟合区间[2.95,3.03]

- $\mu: \sigma = 30.31 \pm 0.6 \text{ MeV}$, 峰值 = 2.988 ± 0.001
- $e: \sigma = 30.67 \pm 0.7 \text{ MeV}$, 峰值 = 2.989 ± 0.001

• Cut Flow 对比

$\sqrt{s} = 6.73 \text{ GeV}$

Cut Flow($J/\psi \rightarrow \mu\mu$)	N_{obs}	相对效率	Cut Flow($J/\psi \rightarrow ee$)	N_{obs}	相对效率
<i>total number:</i>	50000	100.00%	<i>total number:</i>	50000	100.00%
$nGoodm \geq 2 \& nGoodp \geq 2:$	34432	68.86%	$nGoodm \geq 2 \& nGoodp \geq 2:$	33918	67.84%
$nGoody \geq 2:$	29762	86.44%	$nGoody \geq 2:$	29832	87.95%
$n\mu_p \geq 1 \text{ and } n\mu_m \geq 1:$	26712	89.75%	$ne_p \geq 1 \text{ and } ne_m \geq 1:$	26677	89.42%
$J/\psi \text{ mass cut \& } vtx_ \chi^2 \leq 60:$	26321	98.54%	$J/\psi \text{ mass cut \& } vtx_ \chi^2 \leq 60:$	21956	82.30%
$nK_m \geq 1 \text{ and } nK_p \geq 1:$	23150	87.95%	$nK_m \geq 1 \text{ and } nK_p \geq 1:$	19503	88.83%
$\pi^0 \text{ mass cut \& } km_ \chi^2 < 60:$	20436	88.28%	$\pi^0 \text{ mass cut \& } km_ \chi^2 < 60:$	17061	87.48%
$\eta_c \text{ mass cut}$	17363	84.96%	$\eta_c \text{ mass cut}$	14378	84.27%
<i>total cut:</i>	32.48%		<i>total cut:</i>	28.76%	



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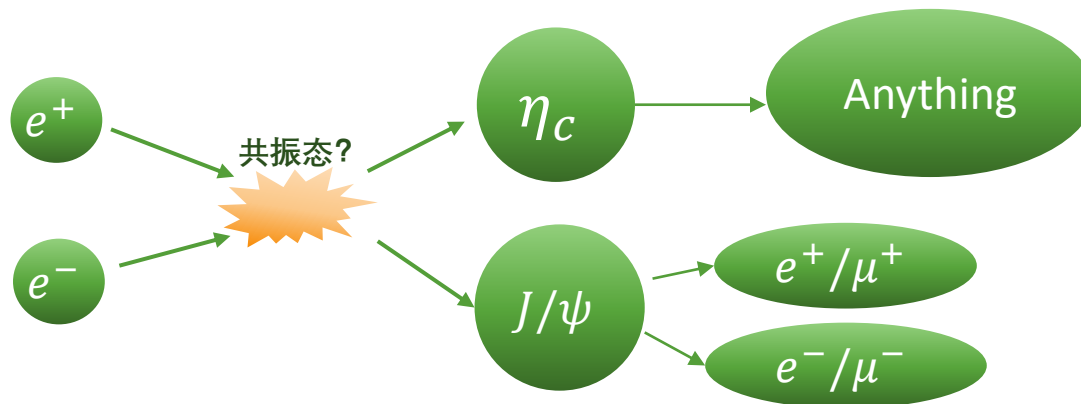
产生子: ConExc

$\sqrt{s}$: 6.73GeV

事例数: 100000

信号道: $e^+e^- \rightarrow T_{4c} \rightarrow \eta_c J/\psi$,

- $\eta_c \rightarrow anything$
- $J/\psi \rightarrow \mu^+\mu^- \text{ and } e^+e^-$



衰变卡

```

oPhotos
Particle vpho 6.7300 0.0
Decay vpho
1.0000 gamma gamma* ConExc -2 443 441;
Enddecay
#
Decay gamma*
1.0000 eta_c J/psi PHSP;
Enddecay
#
Decay J/psi
0.0594 e+ e- PHOTOS VLL;
Enddecay
#
Decay eta_c
0.027 eta' pi+ pi- PHSP;
0.014 eta' pi0 pi0 PHSP;
0.006 rho0 rho0 HELAMP 1.0 0.0 0.0 0.0 -1.0 0.0;
0.012 rho+ rho- HELAMP 1.0 0.0 0.0 0.0 -1.0 0.0;
0.0100 K*0 K- pi+ PHSP;
0.0100 anti-K*0 K+ pi- PHSP;
0.0034 K*+ K*- HELAMP 1.0 0.0 0.0 0.0 -1.0 0.0;
0.0034 K*0 anti-K*0 HELAMP 1.0 0.0 0.0 0.0 -1.0 0.0;
0.011 K*0 anti-K*0 pi+ pi- PHSP;
0.0029 phi K+ K- PHSP;
0.00194 phi phi HELAMP 1.0 0.0 0.0 0.0 -1.0 0.0;
0.0288 K+ anti-K0 pi- PHSP;
0.0288 K- K0 pi+ PHSP;
0.0144 K0 anti-K0 pi0 PHSP;
0.0117 pi0 K+ K- PHSP;
0.0326 eta pi+ pi- PHSP;
0.0163 eta pi0 pi0 PHSP;
    
```

- 利用Breit-Wigner公式获得输入截面分布模拟共振态

- 公式: $\sigma(e^+e^- \rightarrow T_{4c}) = \mathcal{B}_{T_{4c} \rightarrow e^+e^-} \mathcal{B}_{T_{4c} \rightarrow \eta_c J/\psi} \frac{12\pi\Gamma_0^2}{(s-m_{T_{4c}}^2)^2 + m_{T_{4c}}^2\Gamma_0^2}$

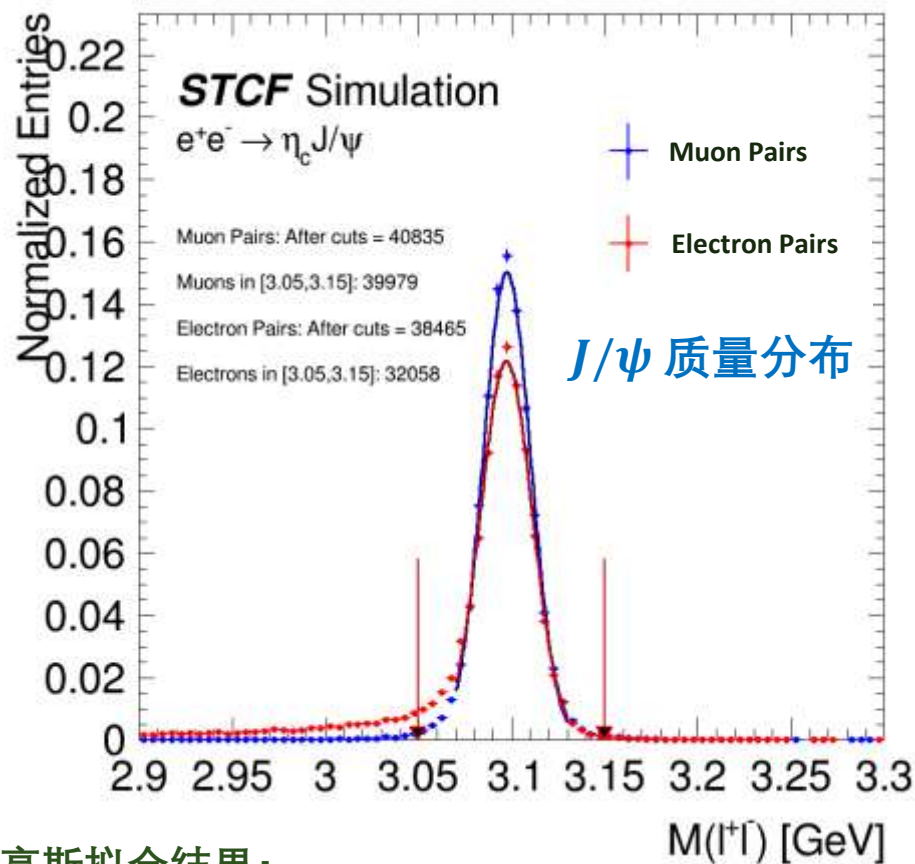
6.72000	1.74915	0.0
6.72500	2.48728	0.0
6.73000	3.80113	0.0
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6.74000	12.90311	0.0
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6.75500	32.20762	0.0
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6.76500	6.43104	0.0
6.77000	3.77999	0.0
6.77500	2.46962	0.0
6.78000	1.73409	0.0
6.78500	1.28226	0.0
6.79000	0.98561	0.0

➤ $J/\psi \rightarrow \mu^+ \mu^-$ 和 $J/\psi \rightarrow e^+ e^-$ 的质量分布对比

$$M_{\text{recoil}}(J/\psi) \equiv \sqrt{|p_{e^+e^-} - p_{J/\psi}|^2/c^2}$$

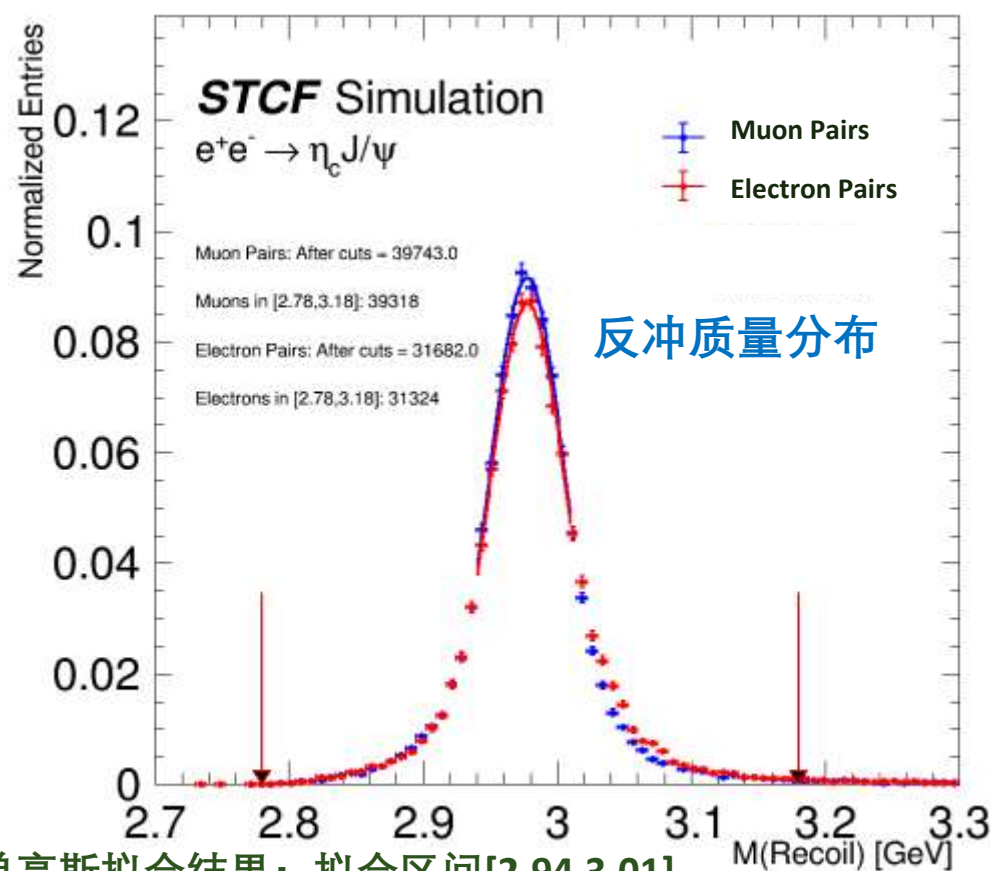
J/ψ Mass cut: $3.05 \text{ GeV} < M_{l^+l^-} < 3.15 \text{ GeV}$

Recoil Mass cut: $2.78 \text{ GeV} < M_{\text{recoil}} < 3.18 \text{ GeV}$



单高斯拟合结果:

- $\mu: \sigma = 13.40 \pm 0.06 \text{ MeV}$, 峰值 = 3.097 ± 0.007
- $e: \sigma = 15.05 \pm 0.08 \text{ MeV}$, 峰值 = 3.096 ± 0.009



单高斯拟合结果: 拟合区间[2.94, 3.01]

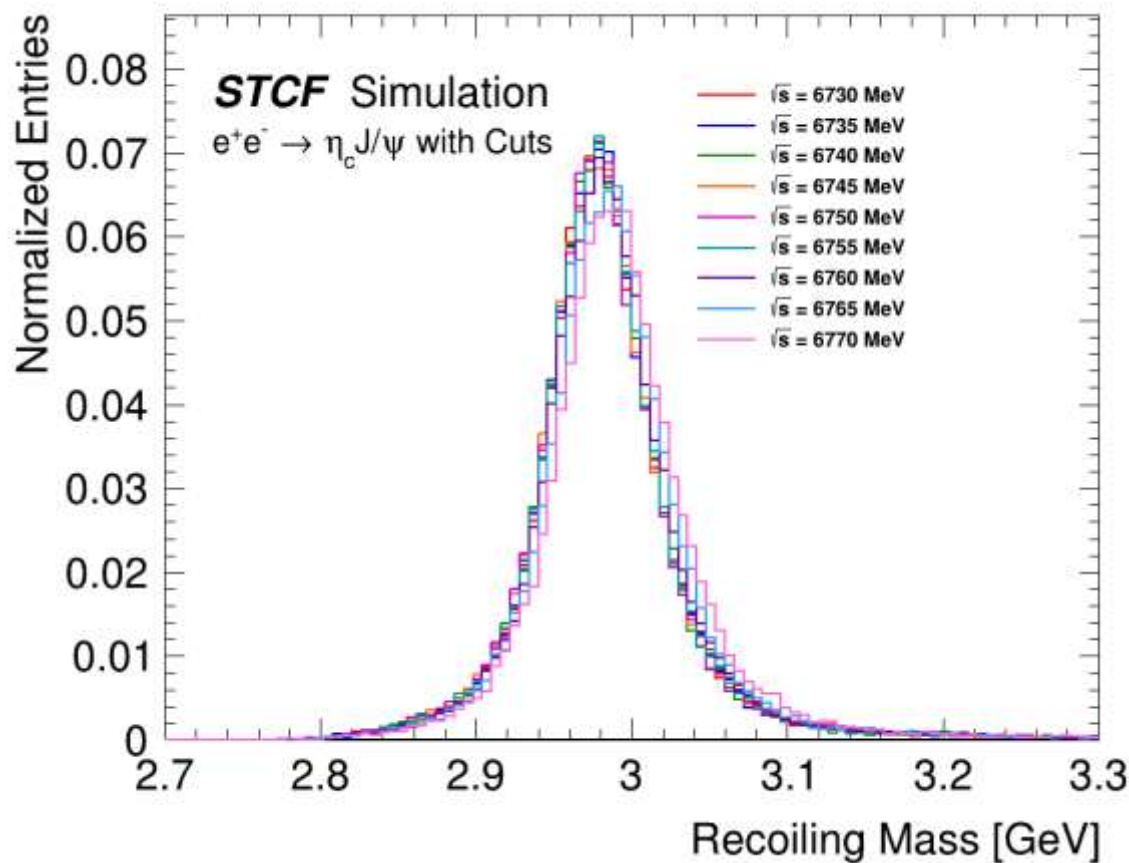
- $\mu: \sigma = 28.38 \pm 0.46 \text{ MeV}$, 峰值 = 2.977 ± 0.001
- $e: \sigma = 28.93 \pm 0.56 \text{ MeV}$, 峰值 = 2.978 ± 0.001

➤ Cut Flow 对比

Cut Flow($J/\psi \rightarrow \mu\mu$)	N_{obs}	相对效率	Cut Flow($J/\psi \rightarrow ee$)	N_{obs}	相对效率
<i>total number:</i>	50000	100.00%	<i>total number:</i>	50000	100.00%
$n_{Goodm} \geq 1 \& n_{Goodp} \geq 1:$	49582	99.16%	$n_{Goodm} \geq 1 \& n_{Goodp} \geq 1:$	49522	99.04%
$n_{\mu_p} \geq 1 \text{ and } n_{\mu_m} \geq 1:$	40436	81.55%	$n_{e_p} \geq 1 \text{ and } n_{e_m} \geq 1:$	39242	79.24%
$J/\psi \text{ vtxfit}_{\chi^2} \leq 60:$	40404	99.99%	$J/\psi \text{ vtxfit}_{\chi^2} \leq 60:$	39225	99.96%
<i>$J/\psi \text{ mass cut} \& \text{ vtx}_{\chi^2} \leq 60:$</i>	<i>39743</i>	<i>98.36%</i>	<i>$J/\psi \text{ mass cut} \& \text{ vtx}_{\chi^2} \leq 60:$</i>	<i>32452</i>	<i>82.73%</i>
Recoil mass cut:	39099	98.38%	Recoil mass cut:	31886	98.26%
<i>total cut:</i>	<i>78.20%</i>		<i>total cut:</i>	<i>63.77%</i>	

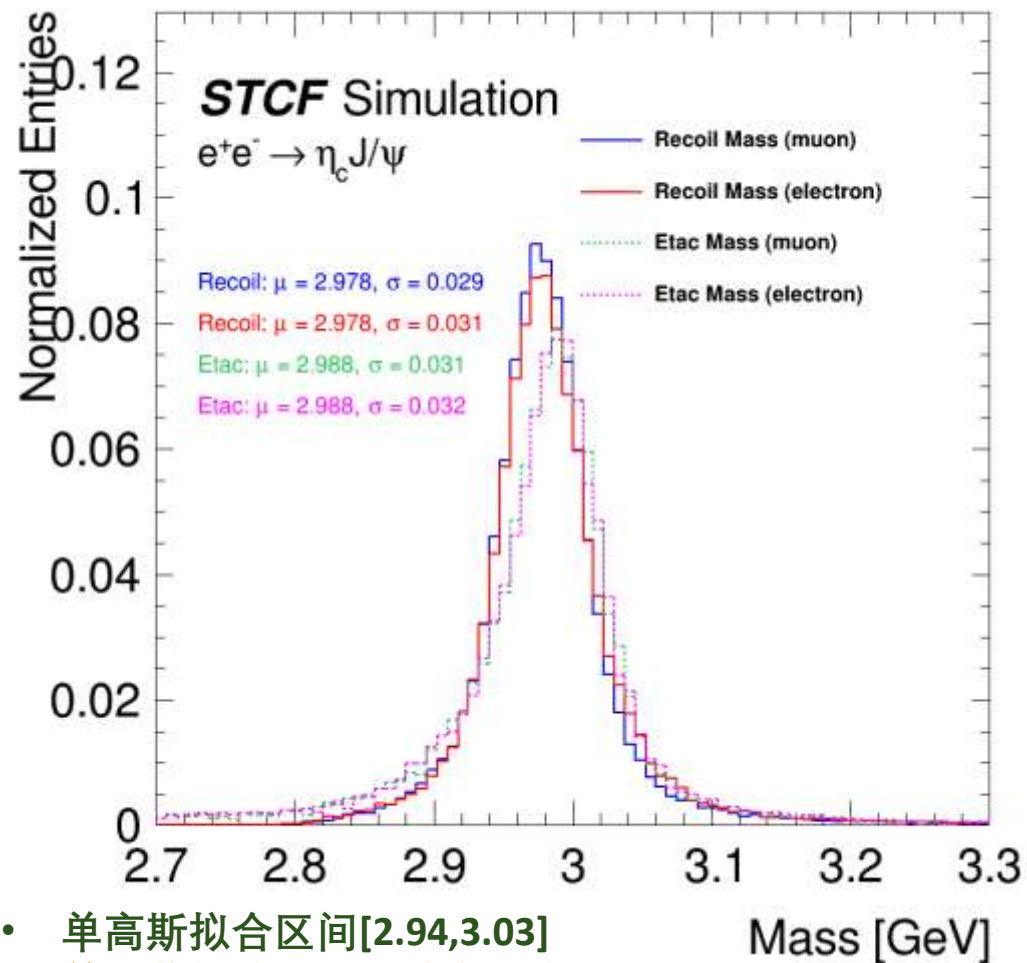


$\sqrt{s}$: 6.73 GeV ~ 6.77 GeV Step size: 5 MeV 9个能量点
不同能量点下的反冲质量分布



- 随着能量点的变化, 反冲质量的峰值只有很微小的偏移

单标获得的反冲质量分布 VS 双标获得的 η_c 质量分布



- 单高斯拟合区间[2.94, 3.03]
- 单标获得的 η_c 质量分布更窄
- 双标获得的 η_c 质量更接近PDG上的值

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- Continuum本底截面:

Belle拟合截面函 $\sigma = A \frac{\sqrt{2\mu\Delta M}}{\left(\frac{s}{s_0}\right)^n}$

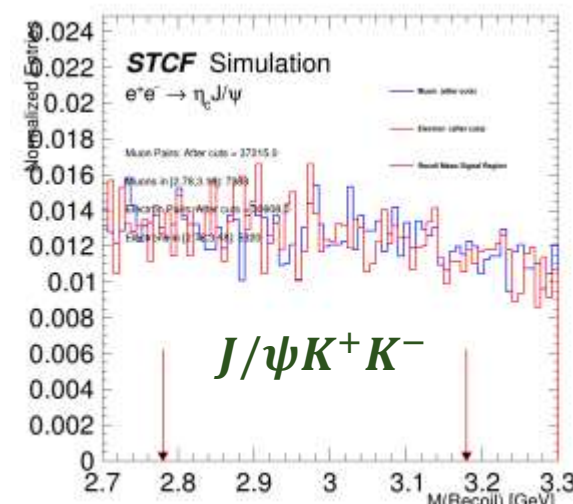
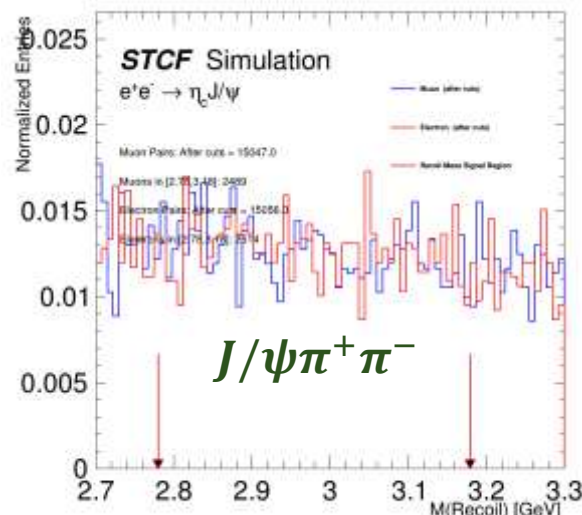
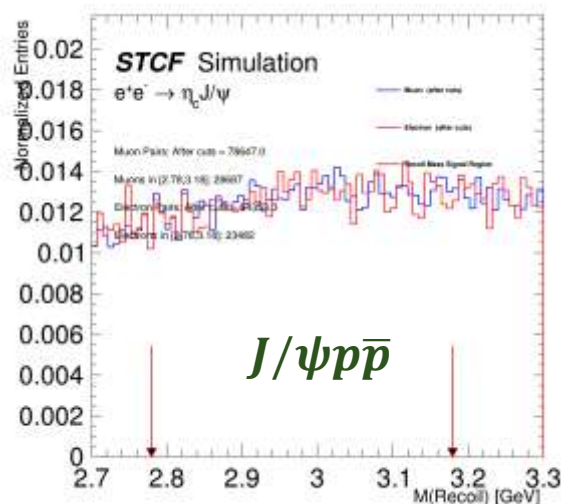
- $J/\psi p\bar{p}$ 本底、 $J/\psi\pi^+\pi^-$ 本底和 $J/\psi K^+K^-$ 本底的截面都是根据目前在5GeV以下的结果，按照1/100预估质心能量在6.75GeV下对应的截面。

$$N_{obs} = \sigma \epsilon L \mathcal{B}$$

$\sqrt{s}=6.75\text{GeV}$	双标 J/ψ 和 η_c			单标 J/ψ		
	选择效率	预估截面(fb)	事例数	选择效率	预估截面(fb)	事例数
信号						
Continuum本底	31.00%	64.43	3	70.50%	64.43	548
$J/\psi p\bar{p}$ 本底	31.00%	819.26	35	70.50%	819.26	6886
$J/\psi\pi^+\pi^-$ 本底	1.38%	20	3	11.40%	20	27
$J/\psi K^+K^-$ 本底	0.42%	30	2	4.88%	30	18
强子本底	1.41%	30	5	14.23%	30	51
	0.00%		0	0.00%		0

分别用 5×10^5 不同的本底样本进行本底分析获得的Recoil Mass分布

平本底



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$$\Gamma_{T_{4c}}^{ee} = 20\text{eV},$$

$$\Gamma_{T_{4c}} = 10\text{MeV}$$

$$\Gamma_{\eta_c J/\psi} = 1\text{MeV}$$

$$\mathcal{B}_{T_{4c} \rightarrow e^+ e^-} \approx 2 * 10^{-6}, \mathcal{B}_{T_{4c} \rightarrow \eta_c J/\psi} = \frac{1}{10} \approx 0.1$$

$$\sigma(e^+ e^- \rightarrow T_{4c} \rightarrow \eta_c J/\psi) = \mathcal{B}_{T_{4c} \rightarrow e^+ e^-} \mathcal{B}_{T_{4c} \rightarrow \eta_c J/\psi} \frac{12\pi \Gamma_{T_{4c}}^2}{(s - m_{T_{4c}}^2)^2 + m_{T_{4c}}^2 \Gamma_{T_{4c}}^2}$$

$$\cong 64.43\text{fb}(\text{峰值})$$

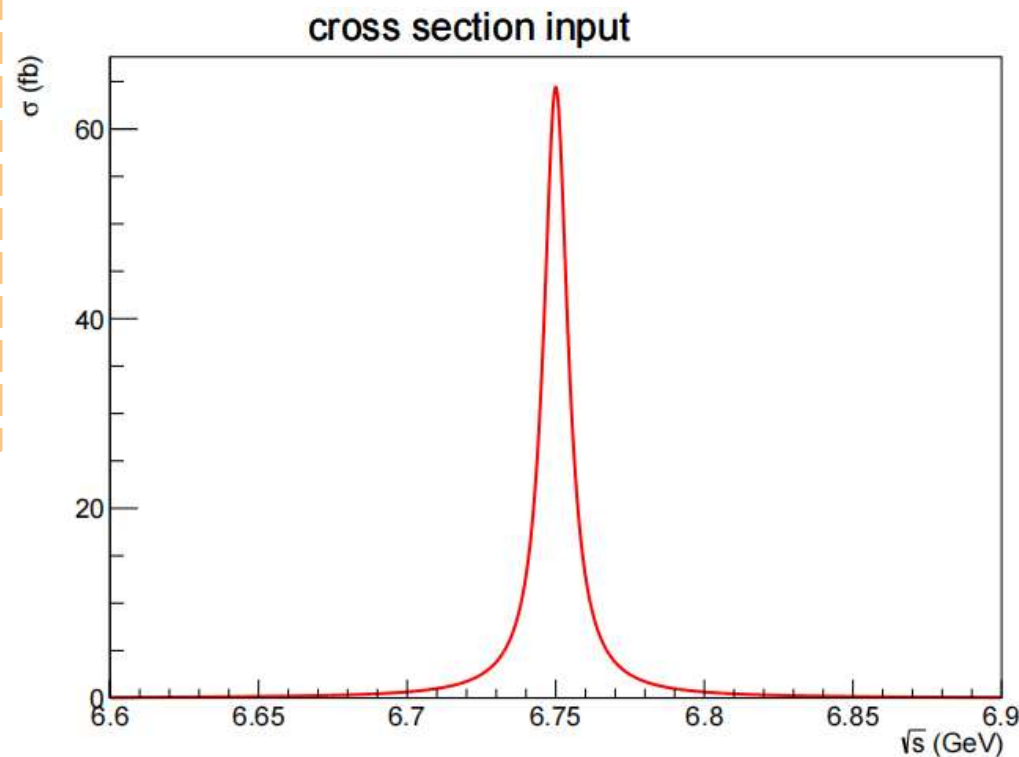
$$L = 100\text{fb}^{-1}$$

$$\mathcal{B}(J/\psi \rightarrow e^+ e^-, \mu^+ \mu^-) = 0.11932 = 11.932\%$$

$$\mathcal{B}(\eta_c \rightarrow K^+ K^- \pi^0) = 0.0115 = 1.15\%$$

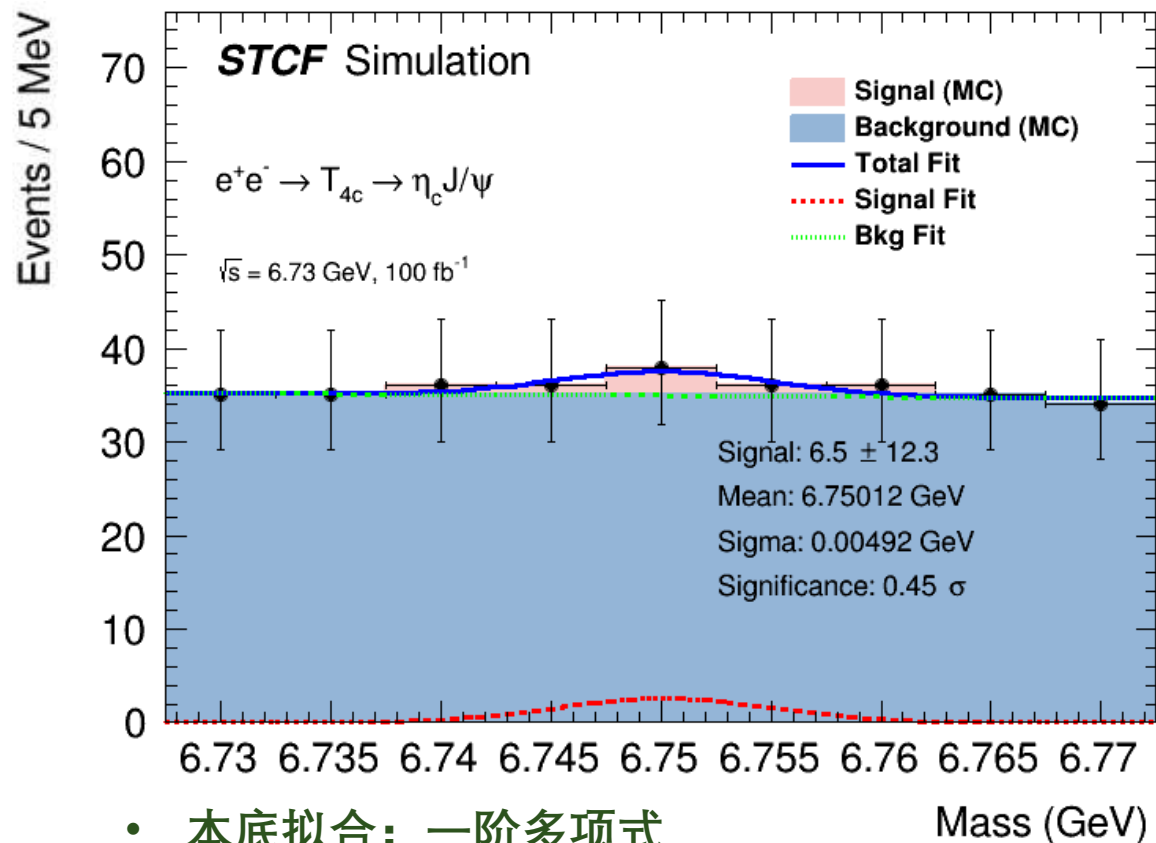
$$N_{obs} = \sigma \epsilon L \mathcal{B}(J/\psi \rightarrow e^+ e^-, \mu^+ \mu^-) \mathcal{B}(\eta_c \rightarrow K^+ K^- \pi^0) \cong 3(\text{peak})$$

- 以 100fb^{-1} 积分亮度预估STCF每年可产生约 $1 * 10^5$ 个 T_{4c} ($N_{obs} = \sigma L$)



双标

$\sqrt{s}$: 6.73GeV~6.77GeV Step size:5MeV 8 steps



- 本底拟合：一阶多项式
- 信号拟合：高斯

- *significance* 计算公式：

$$S = [2(\ln L_m(s+b) - \ln L_m(b))]^{1/2}$$

log likelihood value from the fit w/o signal

log likelihood value from the fit

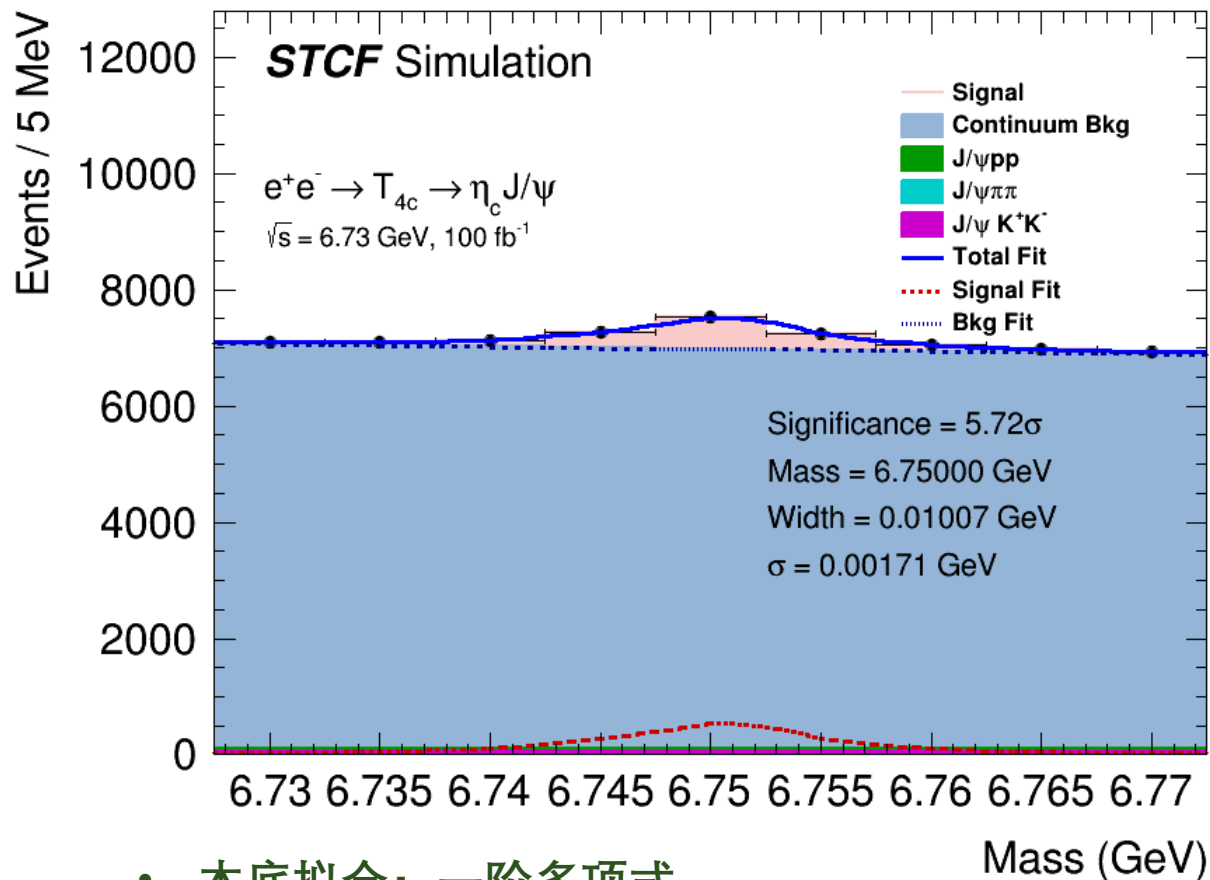
- $L = 100 \text{ fb}^{-1}$
- *significance* = 0.45σ

- 拟合结果：
- $N_{sig} = 6.5 \pm 12.3$
 - $N_{back} = 314.4 \pm 24.6$
 - $Mean = 6.75 \pm 0.01 \text{ GeV}$
 - $\sigma = 4.92 \pm 1.82 \text{ MeV}$

- 统计结果：
- $N_{sig} = 8$
 - $N_{back} = 313$



单标 J/ψ $\sqrt{s}$: 6.73 GeV~6.77 GeV Step size: 5 MeV 8 steps



- 本底拟合：一阶多项式
- 信号拟合：高斯卷积BW函数

- *significance* 计算公式：

$$S = [2(\ln L_m(s+b) - \ln L_m(b))]^{1/2}$$

log likelihood value from the fit w/o signal
 log likelihood value from the fit

- $L = 100 \text{ fb}^{-1}$
- *significance* = 5.72σ

- 拟合结果：
- $N_{sig} = 1530.3 \pm 473.4$
 - $N_{back} = 62791.7 \pm 299.6$
 - $Mean = 6.75 \pm 0.001 \text{ GeV}$
 - $\sigma = 1.7 \pm 2.0 \text{ MeV}$

- 统计结果：
- $N_{sig} = 1487$
 - $N_{back} = 62377$

不同截面预估下的结果

➤ 双标	能量点/GeV	6.73	6.735	6.74	6.745	6.75	6.755	6.76	6.765	6.77	significance
	input截面(fb)	3.8	6.5	12.9	32.2	64.4	32.2	12.9	6.4	3.8	0.45 σ
	N_{obs} (信号)	0	0	1	1	3	1	1	0	0	
	5倍 input截面(fb)	19.0	32.3	64.5	161.2	322.2	161.0	64.4	32.2	18.9	1.97 σ
	5倍 N_{obs} (信号)	1	1	3	7	14	7	3	1	1	
	10倍 input截面(fb)	38.0	64.6	129.0	322.3	644.4	322.1	128.7	64.3	37.8	3.58 σ
	10倍 N_{obs} (信号)	2	3	6	14	28	14	6	3	2	
➤ 单标	能量点/GeV	6.73	6.735	6.74	6.745	6.75	6.755	6.76	6.765	6.77	significance
	input截面(fb)	3.8	6.5	12.9	32.2	64.4	32.2	12.9	6.4	3.8	5.72 σ
	N_{obs} (信号)	32	55	109	274	548	273	109	55	32	
	5倍 input截面(fb)	19.0	32.3	64.5	161.2	322.2	161.0	64.4	32.2	18.9	26.76 σ
	5倍 N_{obs} (信号)	161	274	547	1370	2738	1366	547	273	160	
	10倍 input截面(fb)	38.0	64.6	129.0	322.3	644.4	322.1	128.7	64.3	37.8	57.66 σ
	10倍 N_{obs} (信号)	323	548	1094	2740	5476	2732	1094	546	320	

感谢各位的聆听!

汇报人：董焯娟



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SUN YAT-SEN UNIVERSITY

Backup



中山大學
SUN YAT-SEN UNIVERSITY

- Yin J H, Li Y B, Won E, et al. Search for the double-charmonium state with $\eta c J/\psi$ at Belle[J]. Journal of High Energy Physics, 2023, 2023(8): 1-21.
- 1. Chen Z Z, Chen X L, Yang P F, et al. P-wave fully charm and fully bottom tetraquark states[J]. Physical Review D, 2024, 109(9): 094011.
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- 3. Dong W C, Wang Z G. Going in quest of potential tetraquark interpretations for the newly observed $T \psi$ ψ states in light of the diquark-antidiquark scenarios[J]. Physical Review D, 2023, 107(7): 074010.
- 4. Debastiani V R, Navarra F S. A non-relativistic model for the tetraquark[J]. Chinese Physics C, 2019, 43(1): 013105.
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Exclusive MC production under OSCAR

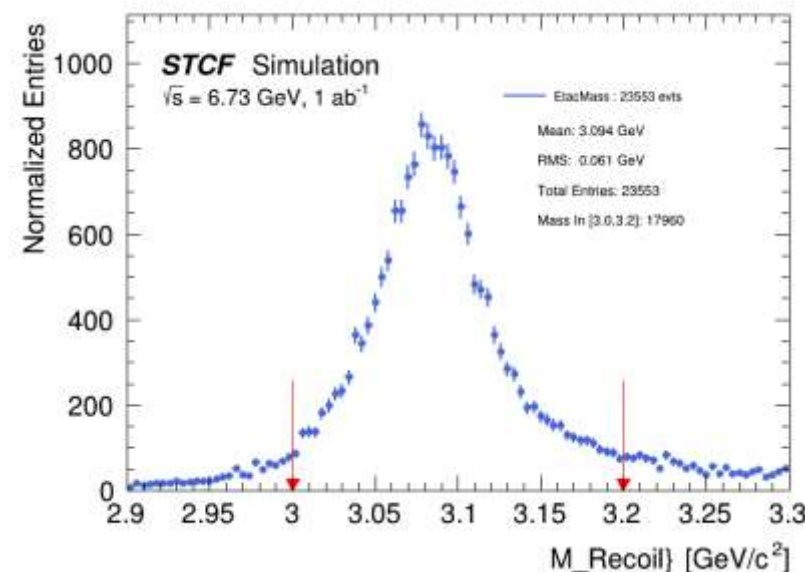
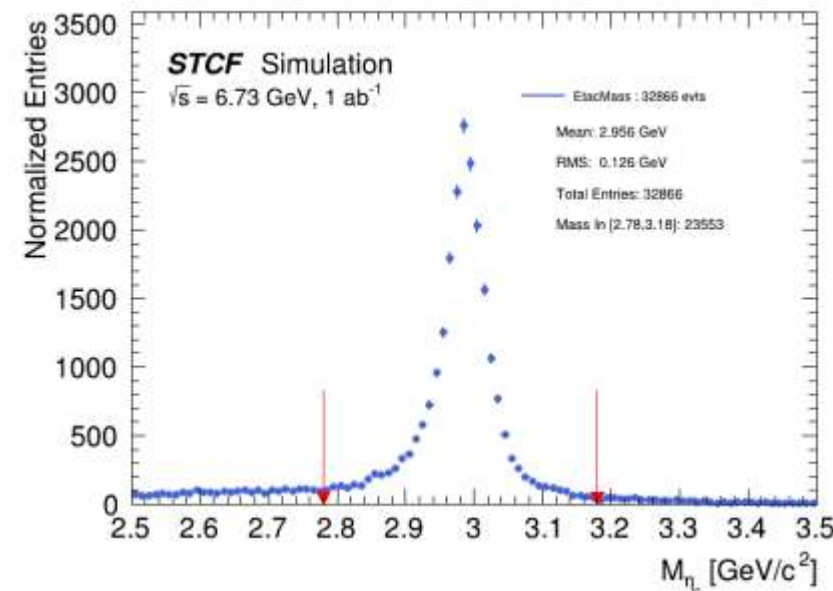
Generator: ConExc

$\sqrt{s}$: 6.73GeV Number of event: 100000

Signal Channel: $e^+e^- \rightarrow T_{4c} \rightarrow \eta_c J/\psi$,

- $\eta_c \rightarrow K^+ K^- \pi^0, J/\psi \rightarrow anything$

Cut Flow	N_{obs}	Relative Efficiency
total number:	50000	100.00%
$n_{Good} \geq 2$:	49015	98.05%
$n_{Good\gamma} \geq 2$:	48676	99.30%
$n_{K_p} \geq 1$:	40225	82.64%
$n_{K_m} \geq 1$:	32866	81.71%
$n_{\pi^0} \geq 1$:	31284	95.13%
η_c mass cut:	23553	75.29%
Recoil mass cut:	17960	76.25%
total cut:	35.92%	



缪子

能量点/GeV	6.73	6.735	6.74	6.745	6.75	6.755	6.76	6.765	6.77
N_{obs} (MC)	17363	17500	17367	17521	16870	17557	17421	17311	17005
亮度 (fb^{-1})	100	100	100	100	100	100	100	100	100
选择效率	34.73%	35.00%	34.73%	35.04%	34.43%	35.11%	34.84%	34.62%	34.70%
input截面(fb)	3.8011	6.4568	12.9031	32.2315	64.4391	32.2076	12.8726	6.431	3.78
N_{obs} (函数)	0.1	0.2	0.3	0.8	1.5	0.8	0.3	0.2	0.1

电子

能量点/GeV	6.73	6.735	6.74	6.745	6.75	6.755	6.76	6.765	6.77
N_{obs} (MC)	14378	14282	14129	14416	14001	14026	14418	14315	14275
亮度 (fb^{-1})	100	100	100	100	100	100	100	100	100
选择效率	28.76%	28.56%	28.83%	28.83%	28.57%	28.62%	28.84%	28.63%	28.55%
input截面(fb)	3.8011	6.4568	12.9031	32.2315	64.4391	32.2076	12.8726	6.431	3.78
N_{obs} (函数)	0.1	0.1	0.3	0.6	1.3	0.6	0.3	0.1	0.1

缪子

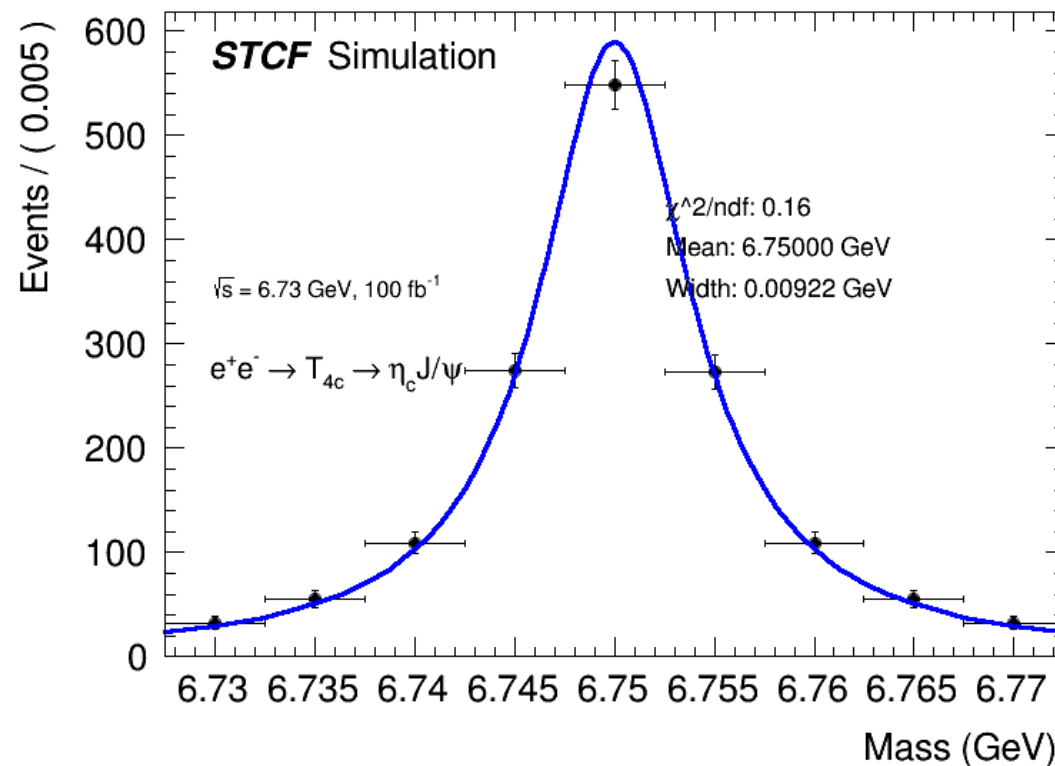
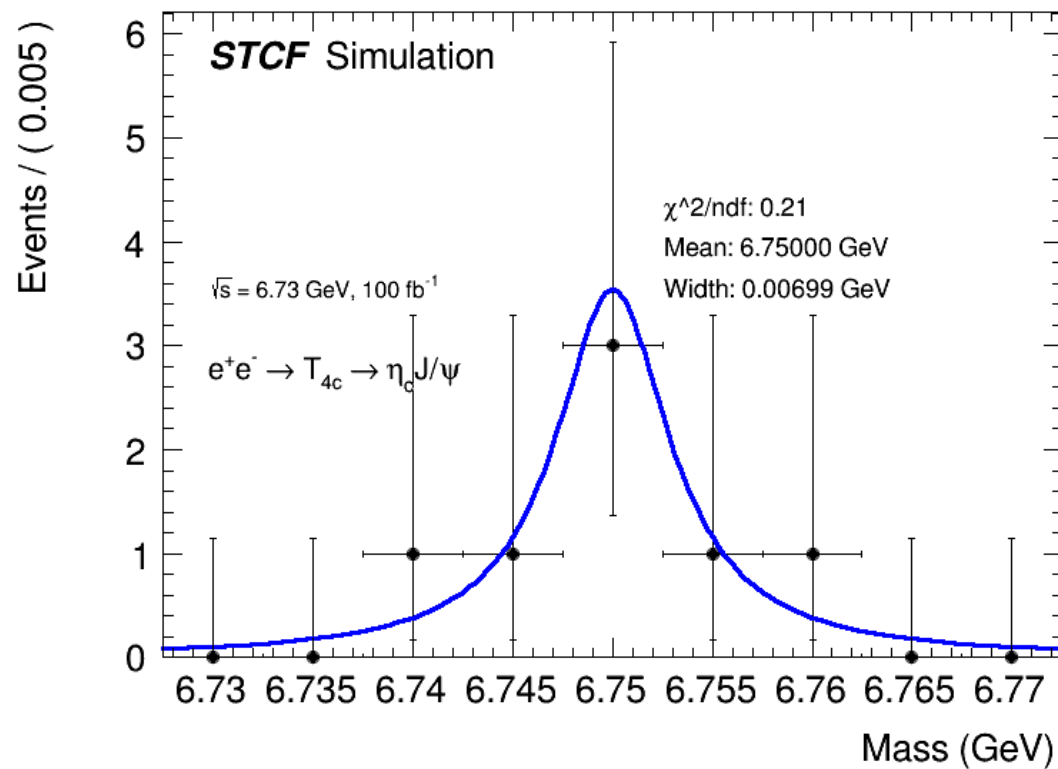
能量点/GeV	6.73	6.735	6.74	6.745	6.75	6.755	6.76	6.765	6.77
N_{obs} (MC)	39290	39121	39152	39252	39296	39230	39410	39242	39240
亮度 (fb^{-1})	100	100	100	100	100	100	100	100	100
选择效率	78.58%	78.24%	78.30%	78.50%	78.59%	78.46%	78.82%	78.48%	78.48%
input截面(fb)	3.8011	6.4568	12.9031	32.2315	64.4391	32.2076	12.8726	6.431	3.78
N_{obs} (函数)	17.8	30.1	60.2	150.8	301.9	150.6	60.5	30.1	17.7

电子

能量点/GeV	6.73	6.735	6.74	6.745	6.75	6.755	6.76	6.765	6.77
N_{obs} (MC)	31287	29457	31308	31411	30698	30652	31886	30745	31238
亮度 (fb^{-1})	100	100	100	100	100	100	100	100	100
选择效率	63.85%	64.04%	63.89%	64.10%	63.95%	63.86%	63.77%	64.05%	63.75%
input截面(fb)	3.8011	6.4568	12.9031	32.2315	64.4391	32.2076	12.8726	6.431	3.78
N_{obs} (函数)	14.5	24.6	49.1	123.2	245.7	122.6	48.9	24.6	14.4



➤ 只拟合信号



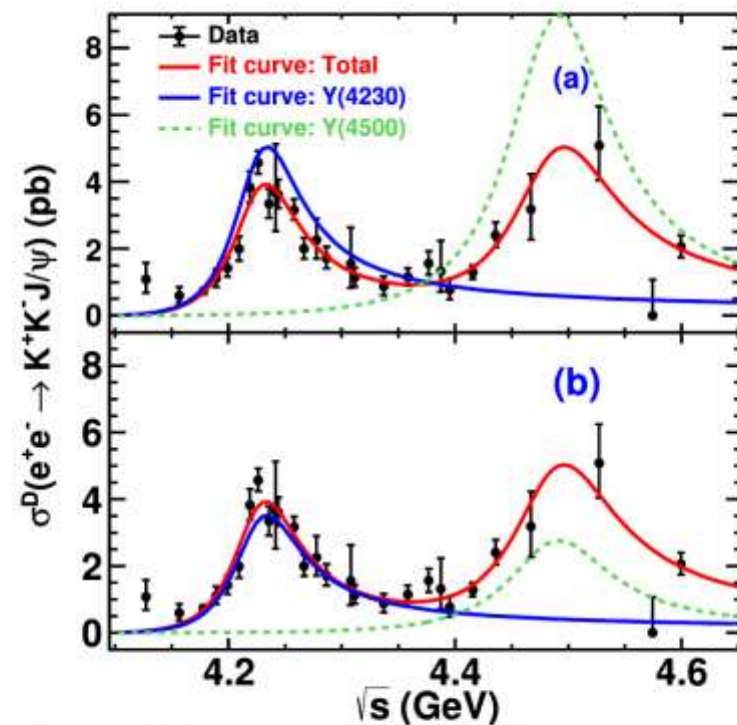
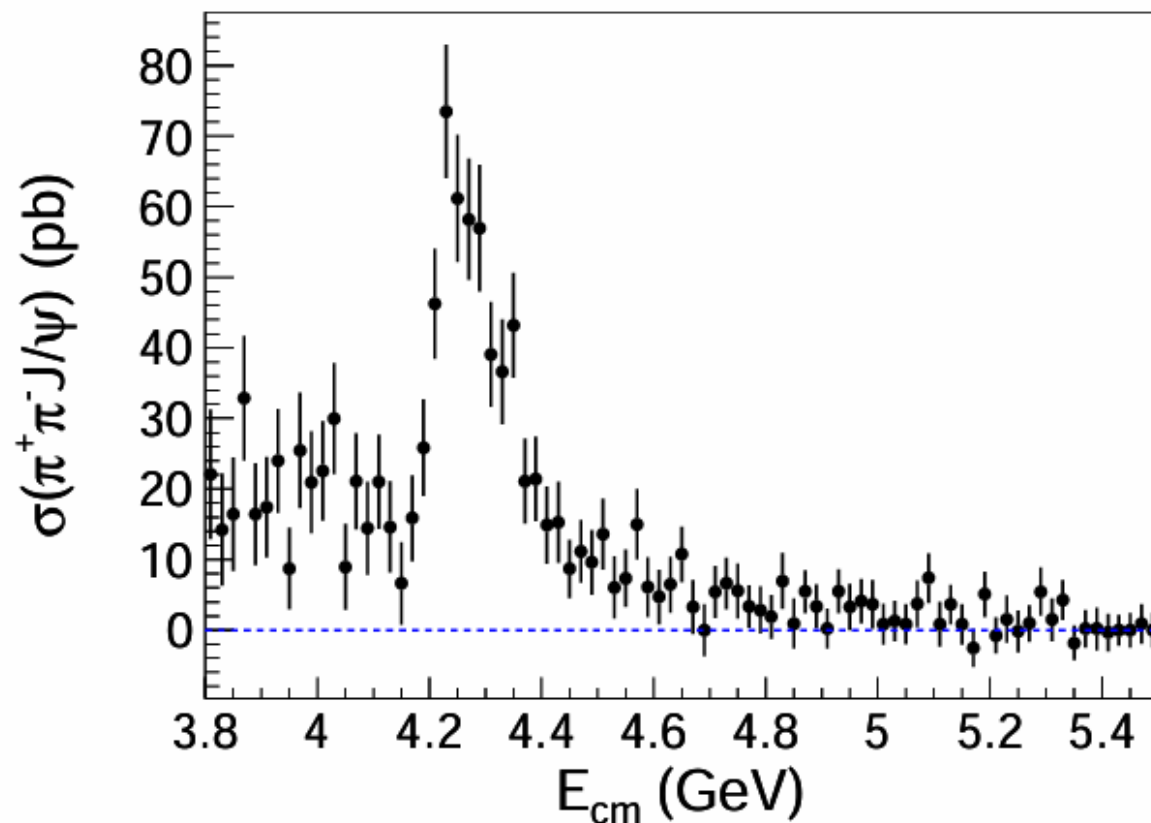


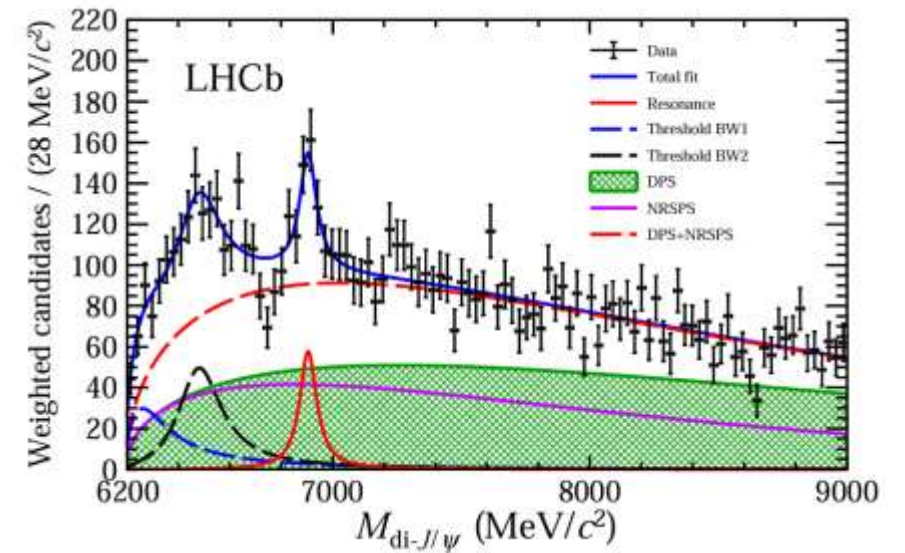
Figure 6: Cross sections of $e^+ e^- \rightarrow K^+ K^- J/\psi$, indicated by error bars with only statistical uncertainties. They are fitted by a coherent sum of two Breit-Wigner functions indicated by red solid curves. The Blue and green dashed curves are the amplitudes describing the resonances $Y(4230)$ and $Y(4500)$, respectively. (a) corresponds to solution I, (b) corresponds to solution II [23].



➤ Observation of structure in the J/ψ -pair mass spectrum

- **States:** $T_{c\bar{c}c\bar{c}}(6550)^0$, $T_{c\bar{c}c\bar{c}}(6900)^0$, $T_{c\bar{c}c\bar{c}}(7290)^0$
- **Quantum numbers:** $I^G(J^{PC}) = 0^+(?^{?+})$
- **Minimal quark content:** $c\bar{c}c\bar{c}$
- **Experiments:** LHCb(first observed), ATLAS, CMS
- **Production:** prompt pp collisions
- **Decay modes:** $J/\psi J/\psi$
- **Nearby thresholds:** $J/\psi\psi(2S)$, $\chi_{c0}\chi_{c0}$, ...
- **Characteristic widths:** 80 – 191 MeV

- LHCb Collaboration. Observation of structure in the J/ψ -pair mass spectrum[J]. Science bulletin, 2020, 65(23): 1983-1993.

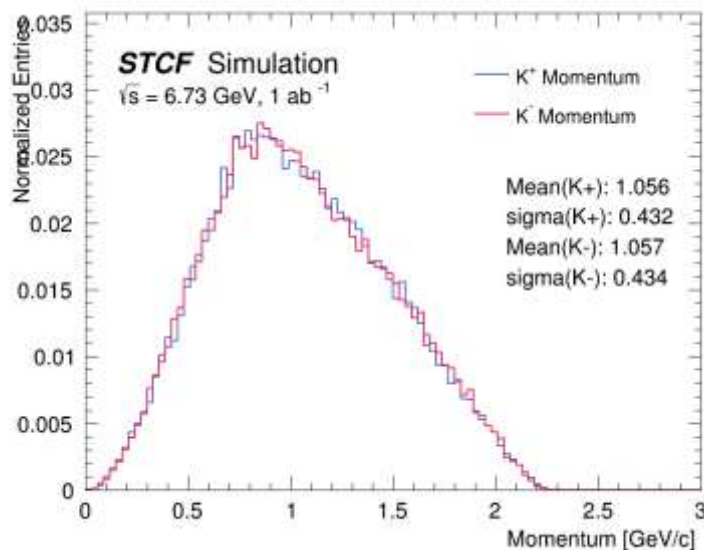


LHCb results:

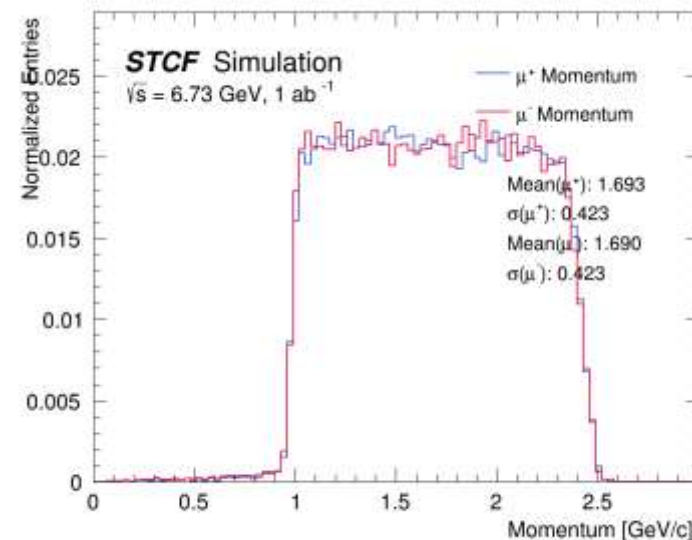
Structure	Significance	
	$p_T^{\text{di-}J/\psi}$ -threshold	$p_T^{\text{di-}J/\psi}$ -binned
Any structure beyond NRSPS plus DPS	3.4σ	6.0σ
Threshold enhancement plus $X(6900)$	6.4σ	6.9σ
Threshold enhancement	6.0σ	6.5σ
$X(6900)$	5.1σ	5.4σ



Kaon 动量分布--truth

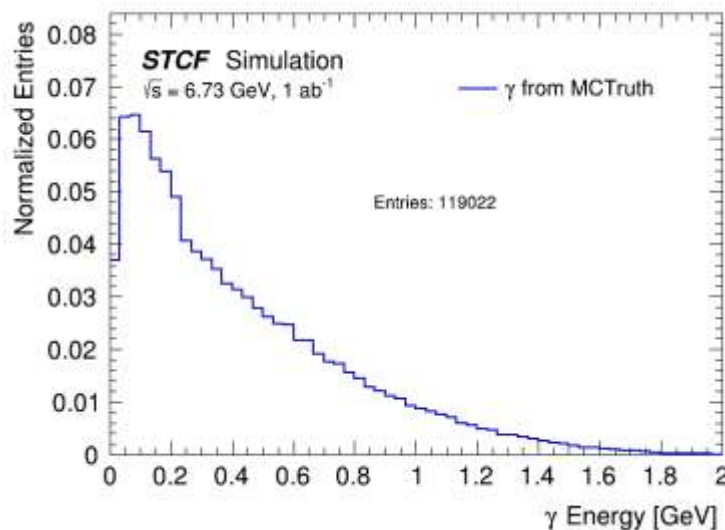


muon 动量分布--truth

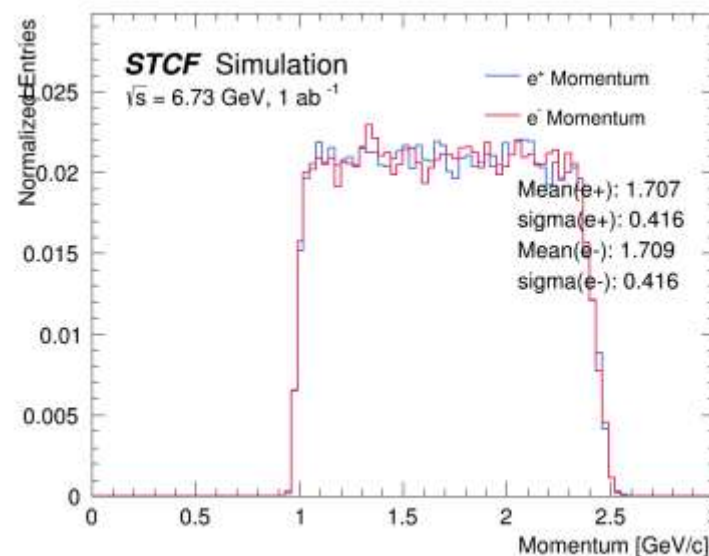


动量大部分大于0.9GeV/c

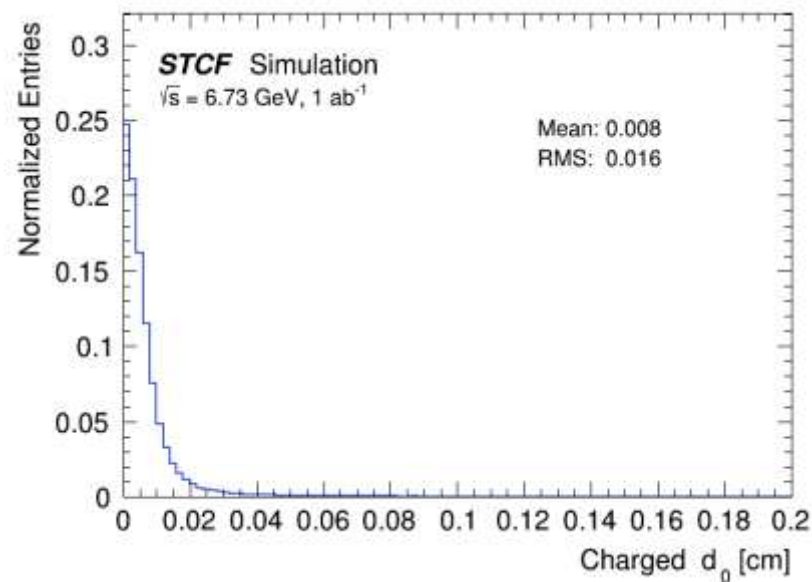
光子能量分布--truth



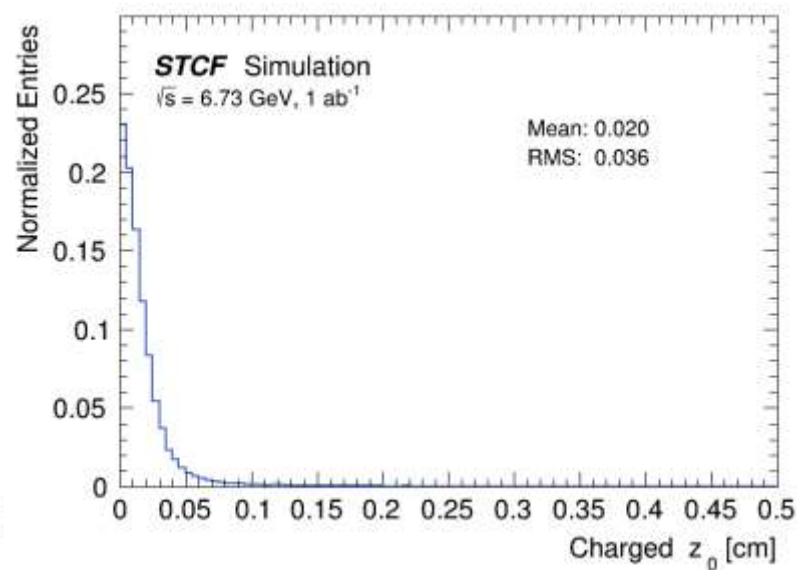
电子动量分布--truth



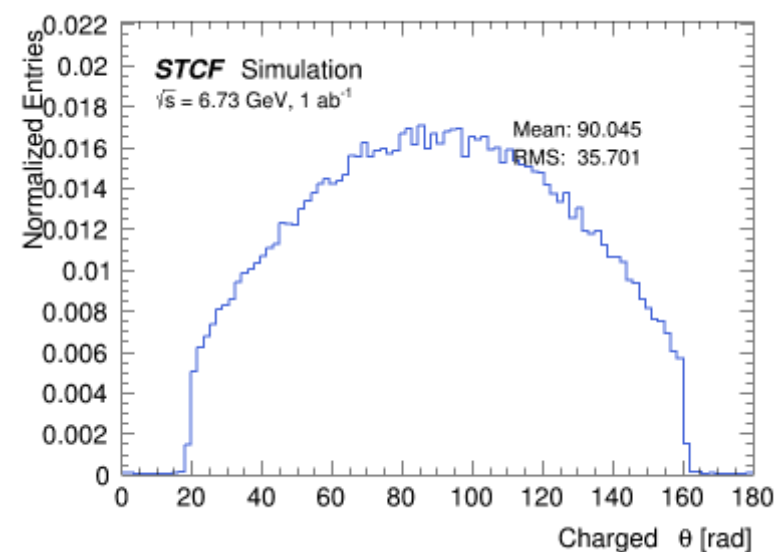
➤ 径迹参数从POCA点得到



d_0 分布



z_0 分布



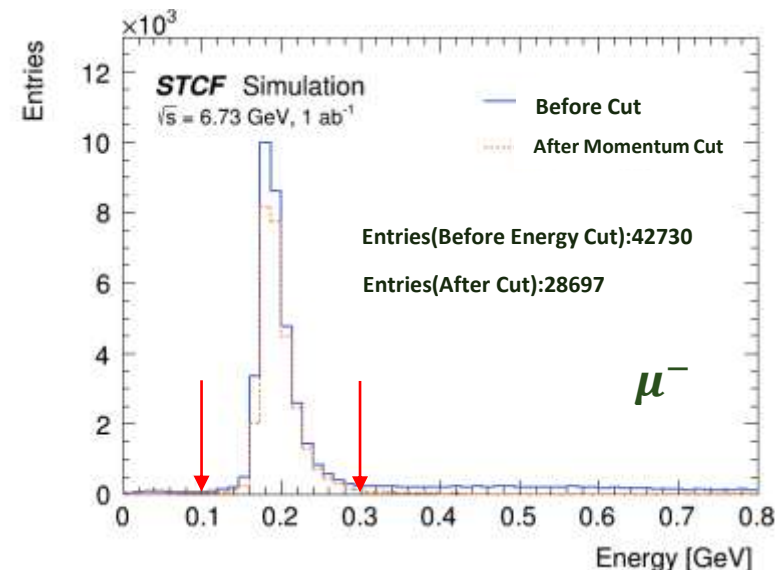
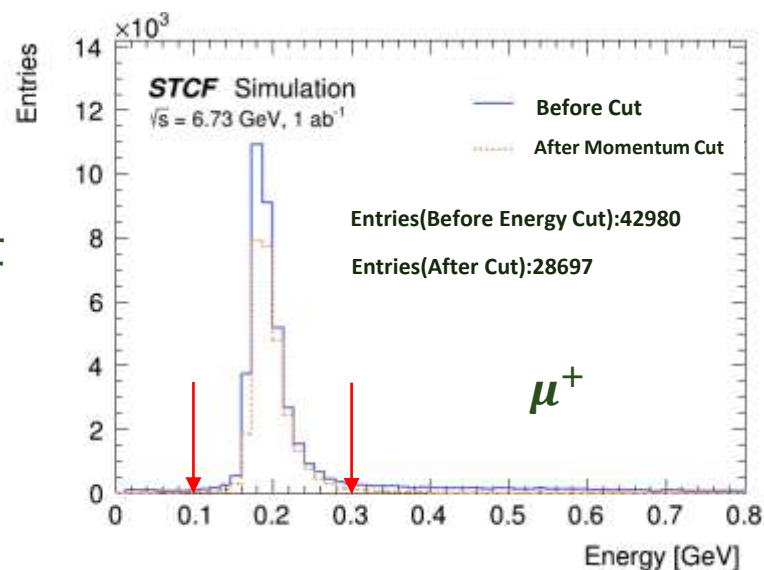
θ 分布



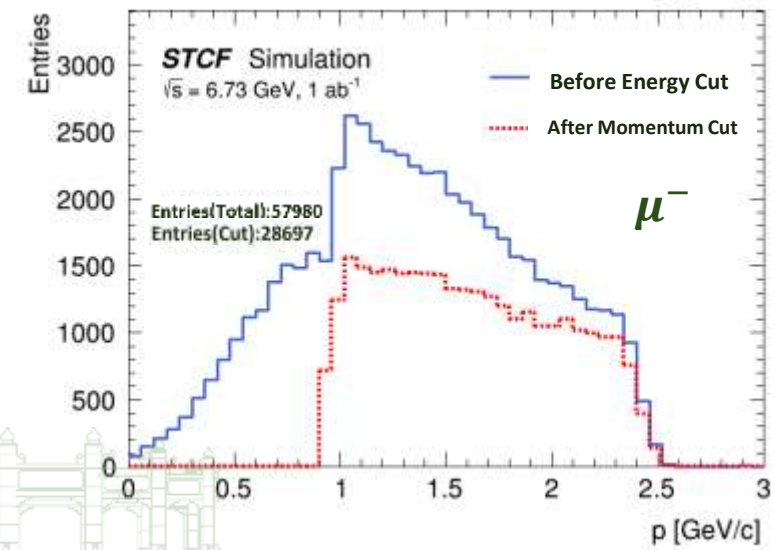
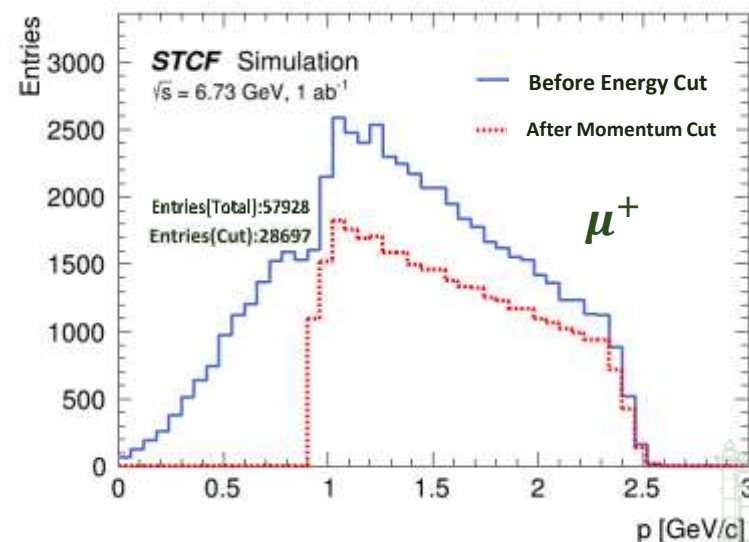
- 筛选条件: $0.1 \leq E_{emc} \leq 0.3$, $|p_{\mu}| \geq 0.9 \text{ GeV}$

$\sqrt{s} = 6.73 \text{ GeV}$

Emc里的能量
沉积分布:



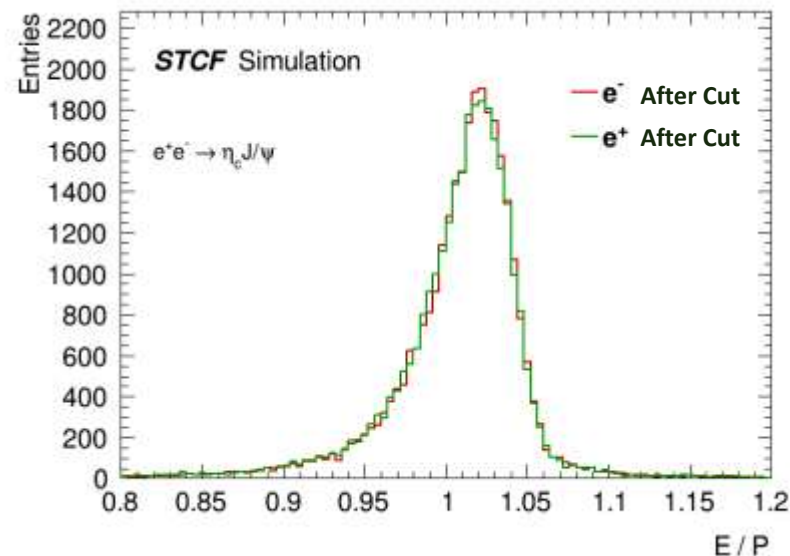
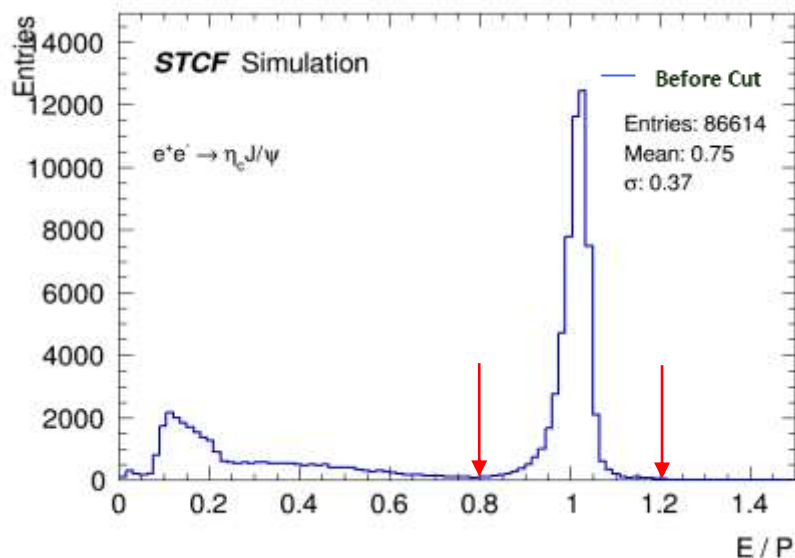
动量分布:



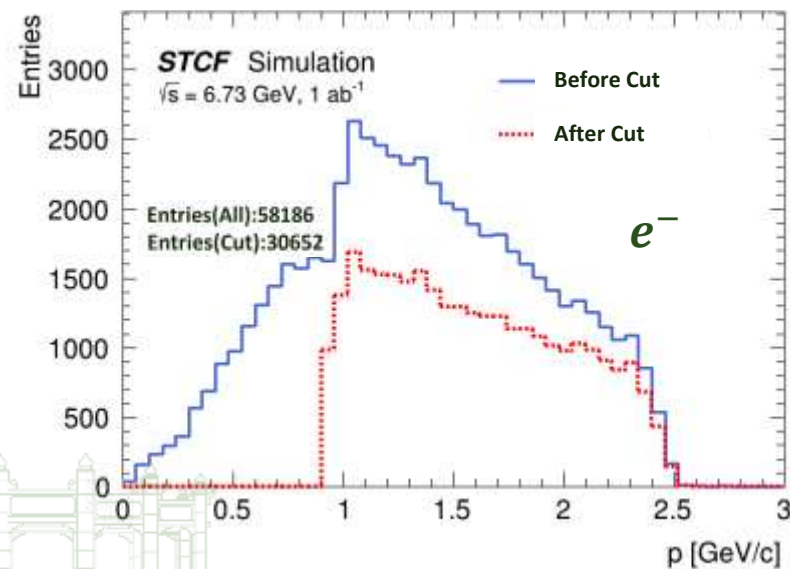
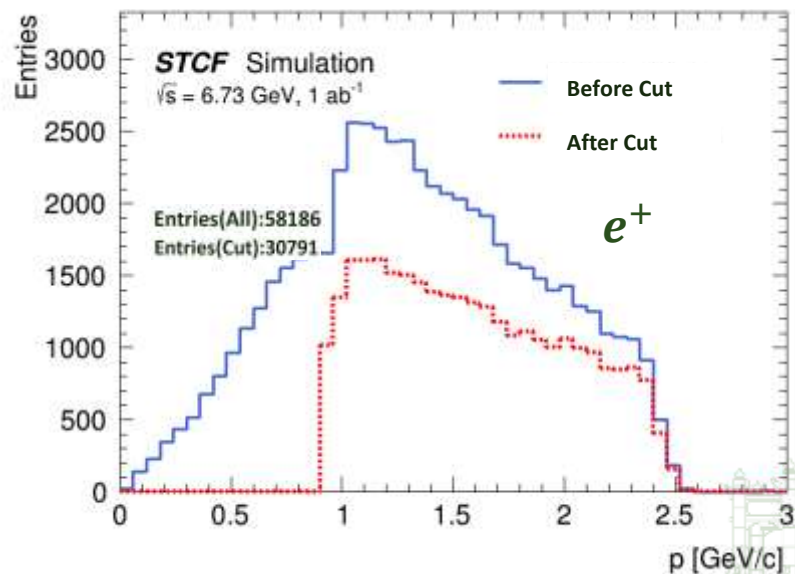
- 筛选条件 $0.8 \leq \frac{E_e}{p_e} \leq 1.2$, $|p_e| \geq 0.9 \text{ GeV}$

$\sqrt{s} = 6.73 \text{ GeV}$

E/P分布:

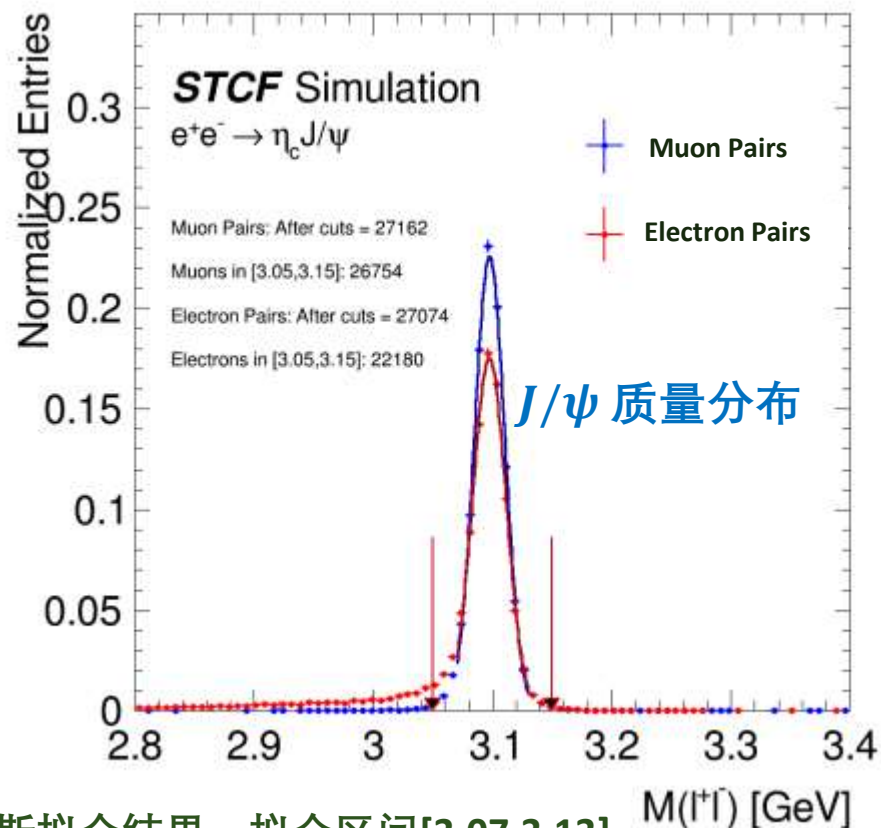


动量分布:



➤ $J/\psi \rightarrow \mu^+ \mu^-$ 和 $J/\psi \rightarrow e^+ e^-$ 的质量分布对比

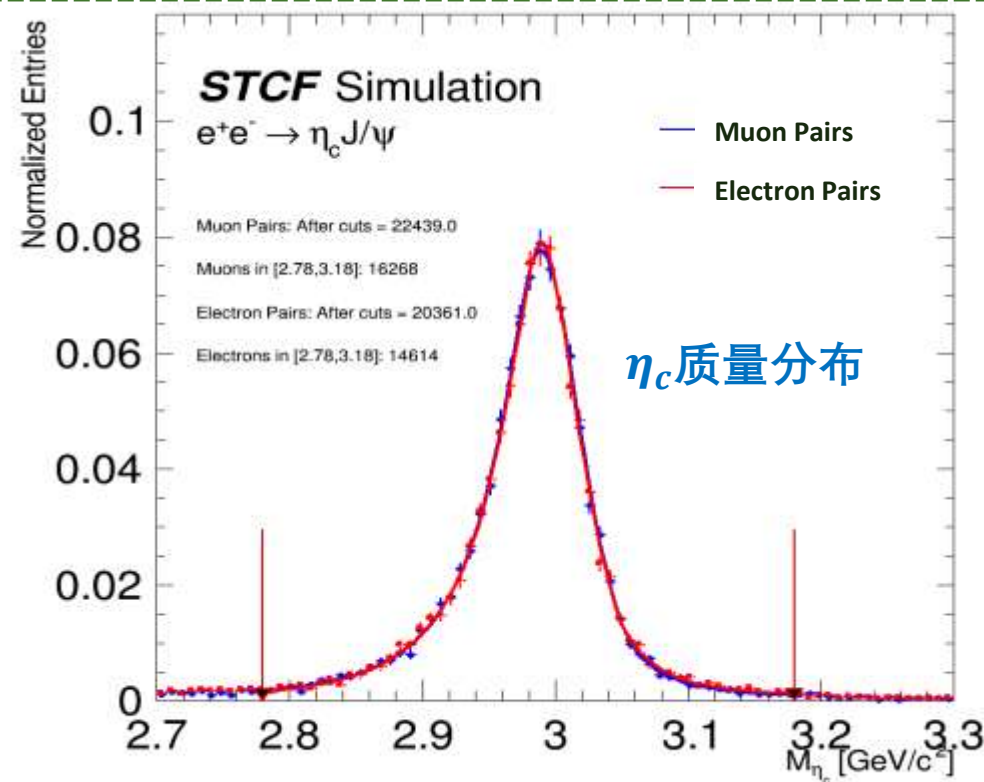
J/ψ Mass cut: $3.05 \text{ GeV} < M_{Le^+Le^-} < 3.15 \text{ GeV}$



单高斯拟合结果: 拟合区间[3.07, 3.13]

- $\mu: \sigma = 12.79 \pm 0.07 \text{ MeV}, \text{mean} = 3.097 \pm 0.001$
- $e: \sigma = 14.05 \pm 0.10 \text{ MeV}, \text{mean} = 3.096 \pm 0.001$

η_c Mass cut: $2.78 \text{ GeV} < M_{K^+K^-\pi^0} < 3.18 \text{ GeV}$

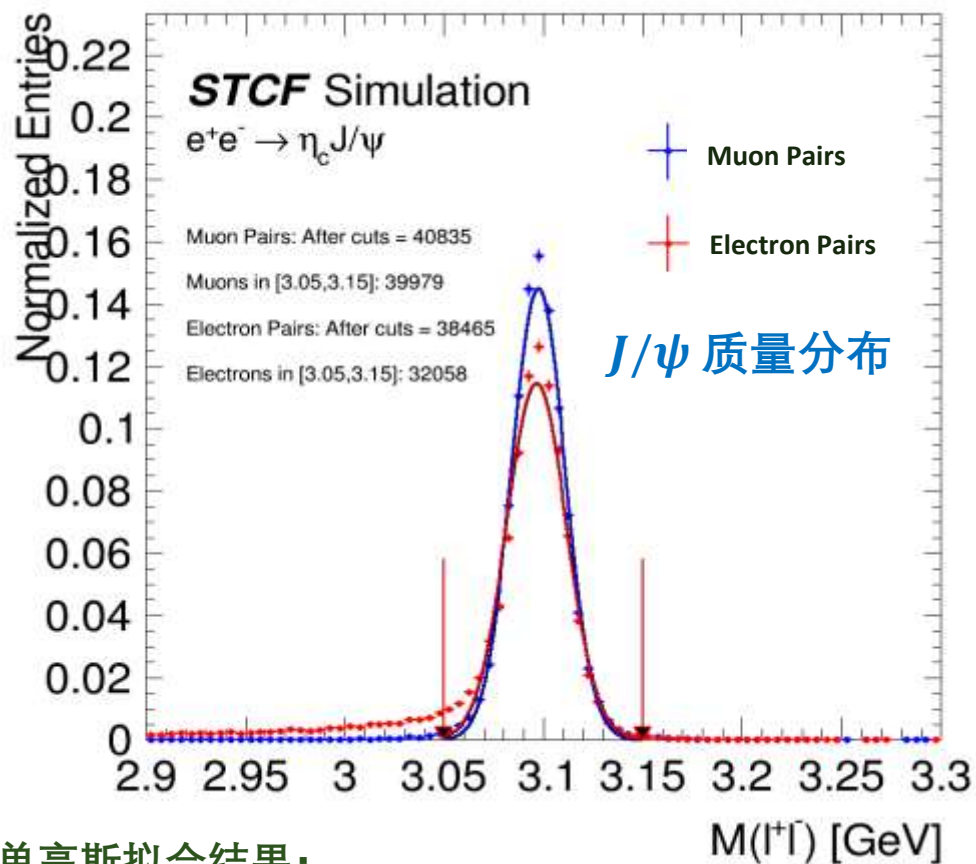


单高斯+双左右两个 Crystal Ball 拟合结果:

- $\mu: \sigma = 49.99 \pm 5.02 \text{ MeV}, \text{mean} = 2.989 \pm 0.023$
- $e: \sigma = 49.99 \pm 5.21 \text{ MeV}, \text{mean} = 2.979 \pm 0.006$

➤ $J/\psi \rightarrow \mu^+ \mu^-$ 和 $J/\psi \rightarrow e^+ e^-$ 的质量分布对比

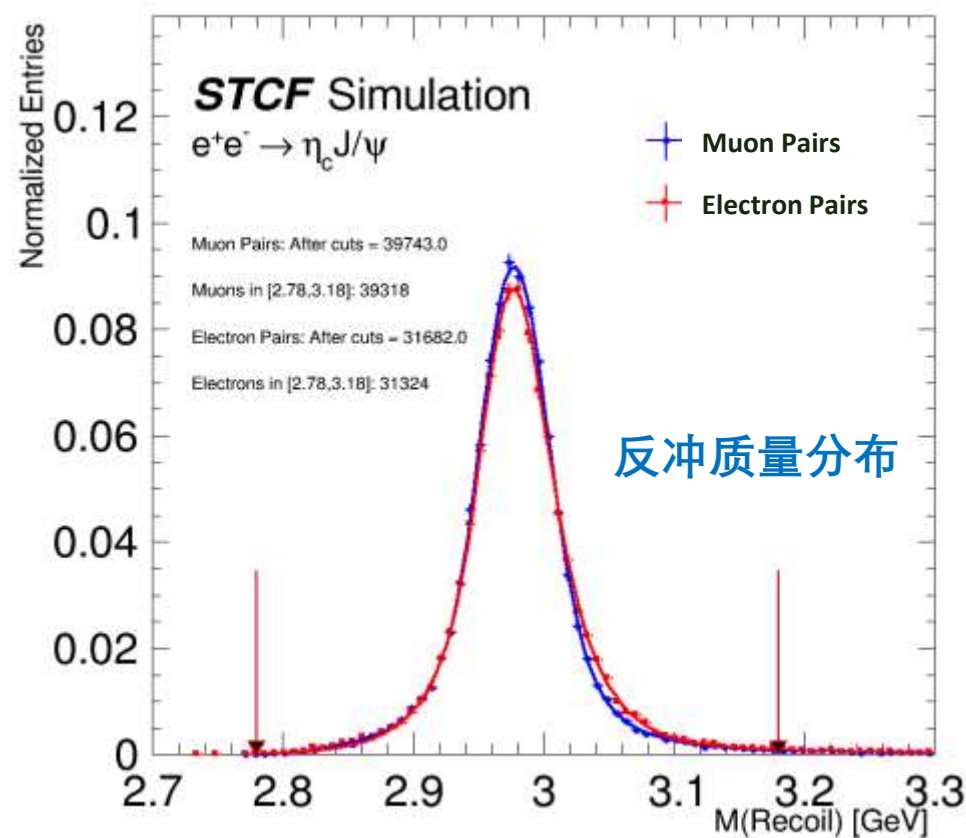
J/ψ Mass cut: $3.05 \text{ GeV} < M_{l^+ l^-} < 3.15 \text{ GeV}$



单高斯拟合结果:

- $\mu: \sigma = 13.40 \pm 0.06 \text{ MeV}, \text{mean} = 3.097 \pm 0.007$
- $e: \sigma = 15.05 \pm 0.08 \text{ MeV}, \text{mean} = 3.096 \pm 0.009$

Recoil Mass cut: $2.78 \text{ GeV} < M_{\text{recoil}} < 3.18 \text{ GeV}$



单高斯+双左右两个 Crystal Ball拟合结果:

- $\mu: \sigma = 37.13 \pm 1.89 \text{ MeV}, \text{mean} = 2.881 \pm 0.003$
- $e: \sigma = 34.63 \pm 2.50 \text{ MeV}, \text{mean} = 3.019 \pm 0.003$