

USTC-PNP-Nuclear Physics Mini Workshop Series

Polarization of Unstable Light (Hyper-) Nuclei in Heavy-Ion Collisions



${}^3\text{He}$

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arXiv:2405.12015 (Accepted by PRL)

Outline

1. From polarization of hadrons to polarization of loosely-bound nuclei
2. Production of light (hyper-)nuclei in heavy-ion collisions
3. (Anti-)Hypertriton polarization and its spin structure
4. Discussions: Effects of baryon spin correlations & Polarization of nucleons
5. Summary and outlook

1. Polarization of hadrons in relativistic heavy-ion collisions

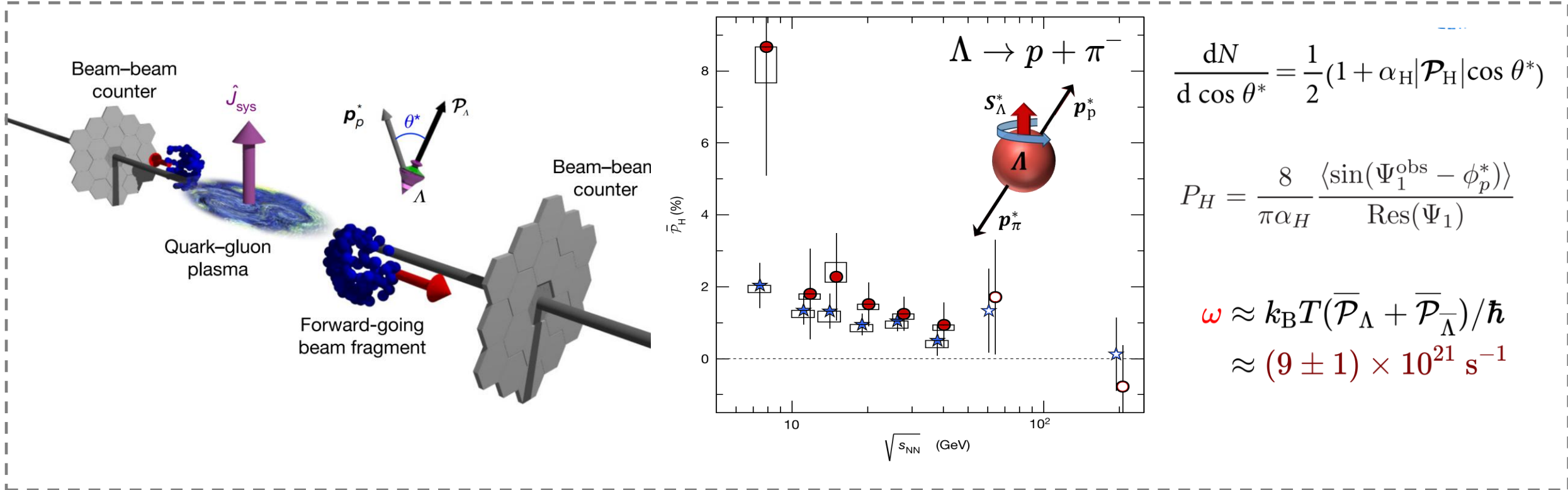
(1)

STAR, Nature 548, 62 (2017)

Z. T. Liang and X. N. Wang PRL 94, 102301 (2005)

F. Becattini, F. Piccinini, and J. Rizzo, PRC 77, 024906 (2008)

F. Becattini, M. Buzzegoli, T. Niida, S. Pu, and A. Tang, Int.J.Mod.Phys.E 33 (2024) 06, 2430006

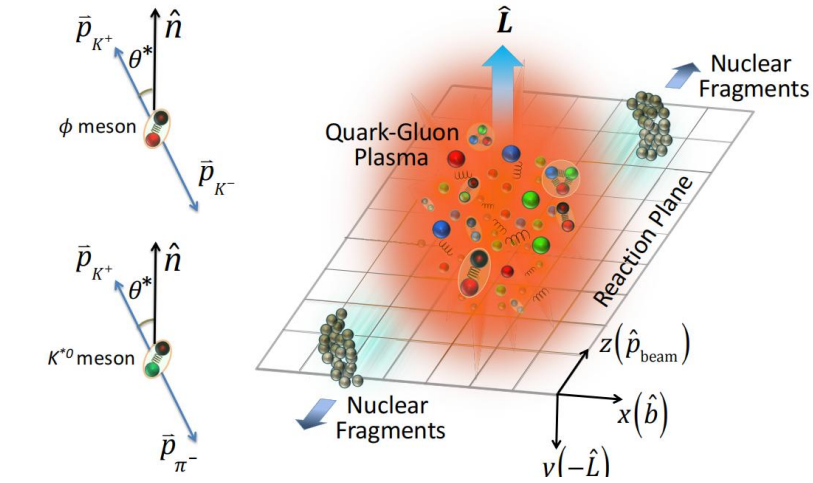


Spin polarization of Lambda hyperon \longrightarrow Vorticity of QGP

1. Polarization of hadrons in relativistic heavy-ion collisions

(2)

STAR, Nature 614, 7947 (2023)



Spin alignment of mesons

$$\frac{dN}{d(\cos\theta^*)} \propto (1 - \rho_{00}) + (3\rho_{00} - 1)\cos^2\theta^*$$



Fluctuation/correlation of strong force field

X. L. Sheng et al., PRL 131, 042304 (2023)

$$G_s^{(y)} \equiv g_\phi^2 \left[3\langle B_{\phi,y}^2 \rangle + \frac{\langle \mathbf{p}^2 \rangle_\phi}{m_s^2} \langle E_{\phi,y}^2 \rangle - \frac{3}{2} \langle B_{\phi,x}^2 + B_{\phi,z}^2 \rangle - \frac{\langle \mathbf{p}^2 \rangle_\phi}{2m_s^2} \langle E_{\phi,x}^2 + E_{\phi,z}^2 \rangle \right]$$

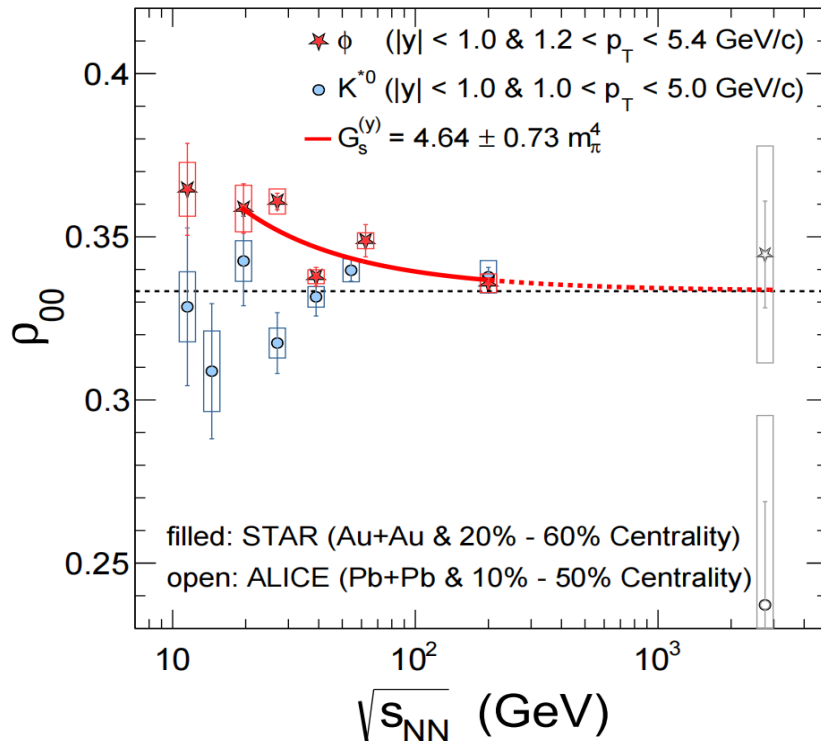
Quark-antiquark spin correlation

J. P. Lv et al., Phys.Rev.D 109 (2024) 11, 114003

Meson spectral property

F. Li and S. Liu, arXiv:2206.11890

Y. L. Yin, W. B. Dong, J. Y. Pang, S. Pu, and Q. Wang, Phys. Rev. C 110 (2024) 2, 024905



1. Polarization of light (anti-)(hyper-)nuclei

(3)

Elementary hadrons

$\Lambda(uds)$ $\Xi(uss)$ $\Omega(sss)$
 $\phi(s\bar{s})$ $K^{*0}(d\bar{s})$ $\rho^+(u\bar{d})$
 $J/\psi(c\bar{c})$...



Unstable (anti-)(hyper-)nuclei

${}^3_{\Lambda}\text{H}(np\Lambda)$ ${}^4\text{Li}(nppp)$
 ${}^3_{\Lambda}\bar{\text{H}}(\bar{n}\bar{p}\bar{\Lambda})$ ${}^4\bar{\text{Li}}(\bar{n}\bar{p}\bar{p}\bar{p})$
...

Stable (anti-)nuclei

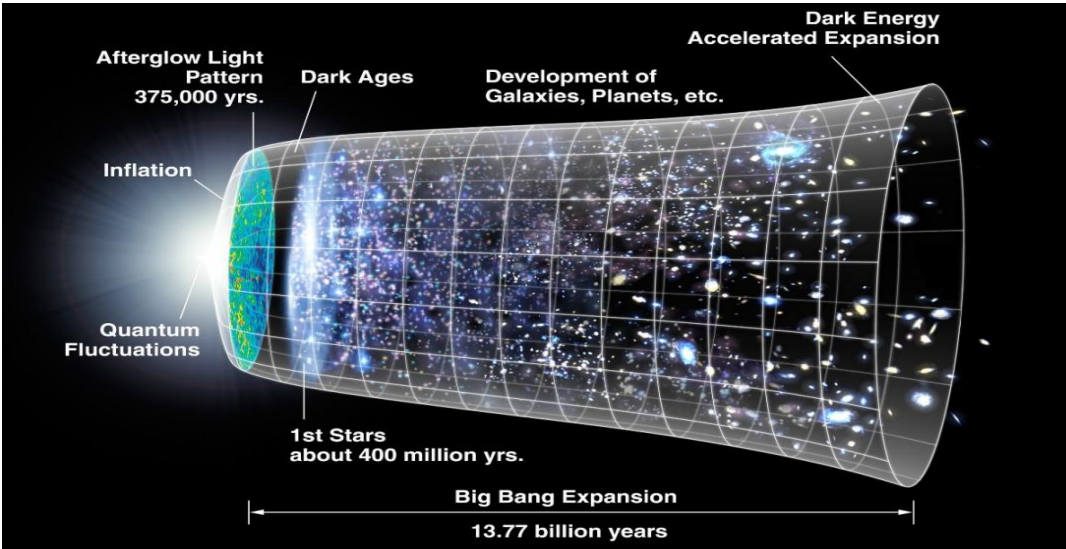
$d(np)$ ${}^3\text{He}(npp)$
 $\bar{d}(\bar{n}\bar{p})$ ${}^3\bar{\text{He}}(\bar{n}\bar{p}\bar{p})$
...

2. Little-Bang Nucleosynthesis

Big-bang nucleosynthesis is responsible for the formation of light nuclei in our Universe.

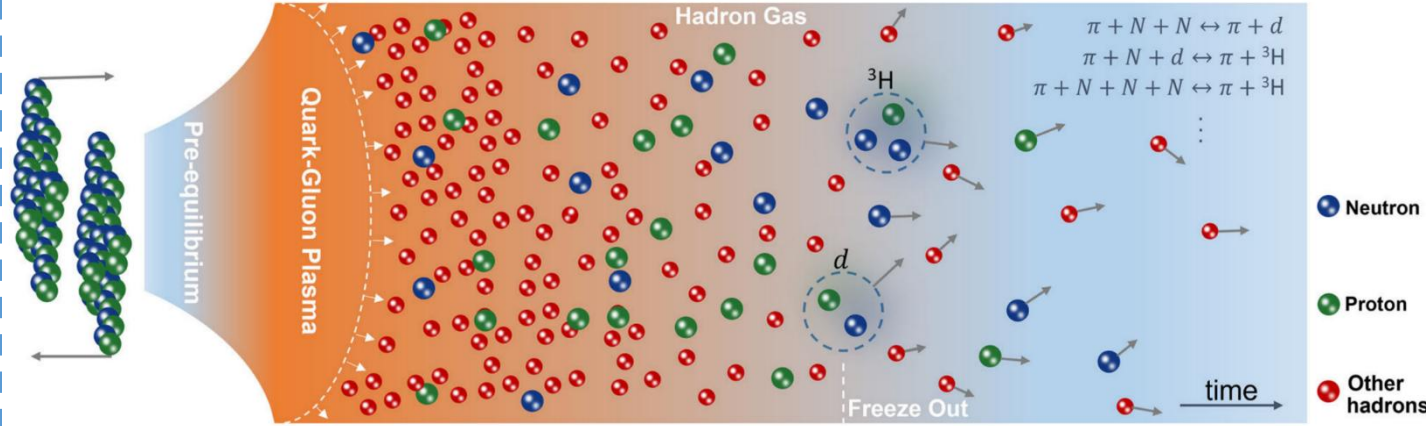
$$t \sim 100 \text{ s}, kT < 1 \text{ MeV}$$

K. A. Olive et al., Phys. Rept. 333, 389–407 (2000);
《The First Three Minutes》 S. Weinberg



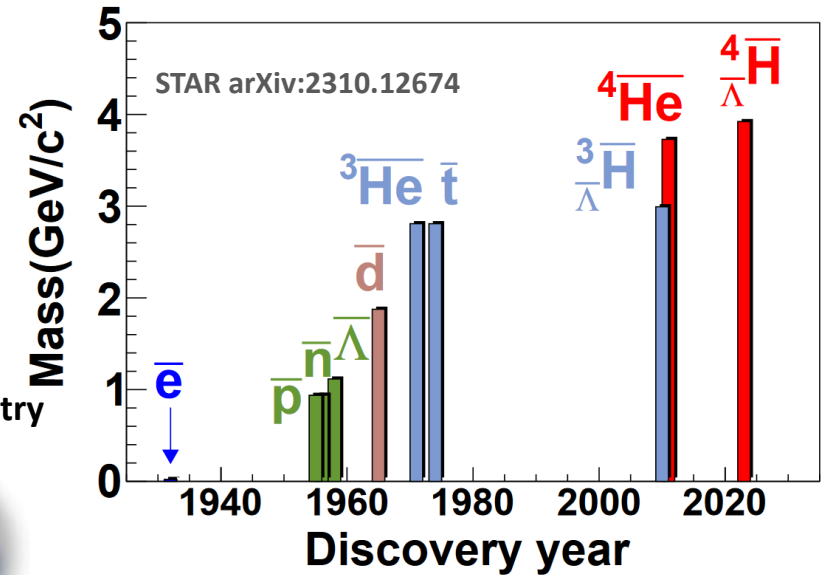
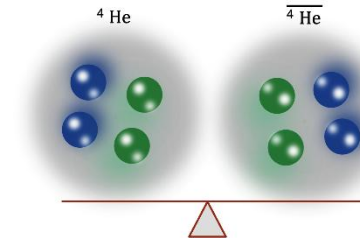
Synthesis of **antimatter** nuclei in little bangs of relativistic heavy-ion collisions $t \sim 10^{-22} \text{ s}, kT \sim 100 \text{ MeV}$

K. J. Sun, R. Wang, C. M. Ko, Y. G. Ma, C. Shen, Nature Commun. 15, 1074 (2024)

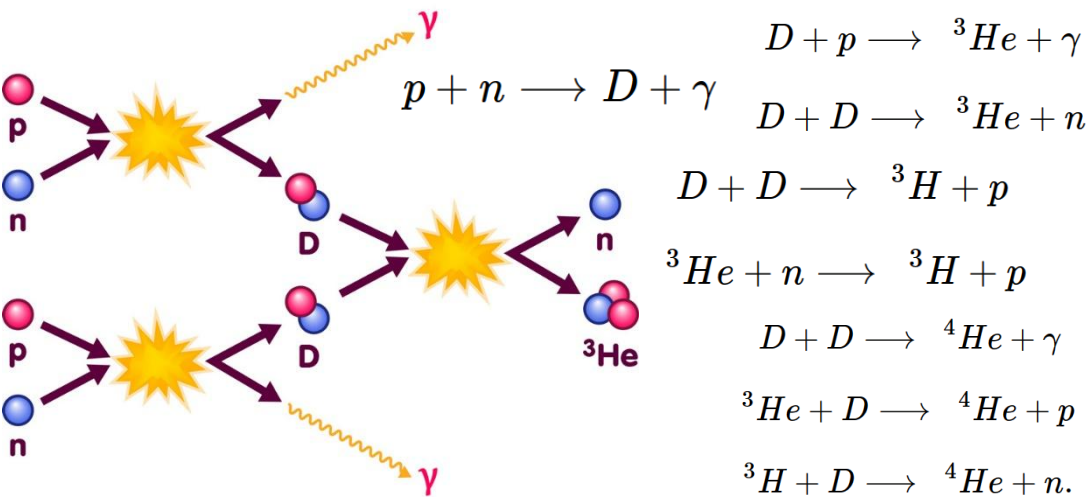


Antimatter factory

Matter-antimatter asymmetry



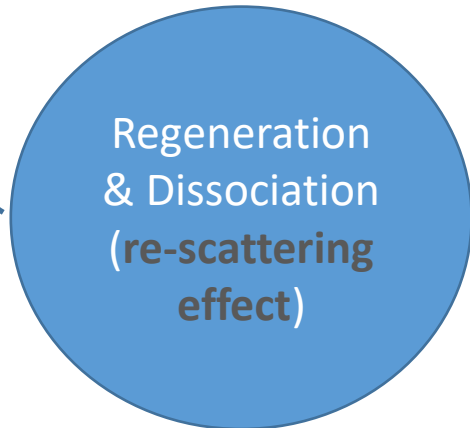
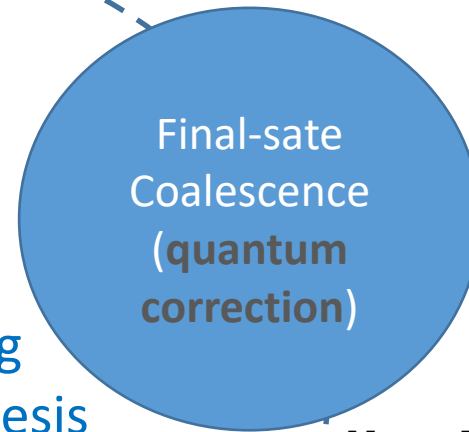
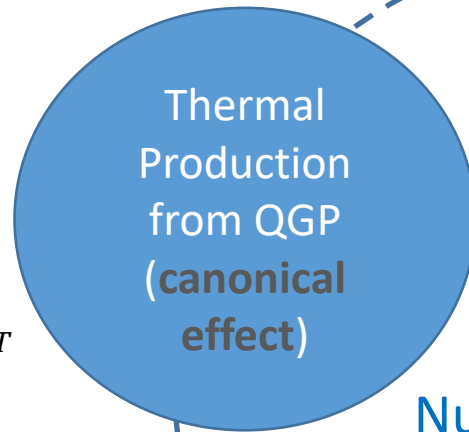
J. Chen et al., Phys. Rep. 760, 1 (2018);
P. Braun-Munzinger and B. Donigus NPA987, 144 (2019)



2. Production Mechanisms : When? Where? How?

(5)

A. Andronic, P. Braun-Munzinger, J. Stachel, H. Stöcker, PLB 697, 203 (2011)
 A. Andronic, P. Braun-Munzinger, K. Redlich, J. Stachel, Nature 561, 321 (2018)
 V. Vovchenko et al., PLB785, 171 (2018); PLB800, 135131 (2020) (Saha Eq.);
 T. Neidig et al., PLB827,136891(2022)(Rate Eq.);...



Little Bang Nucleosynthesis

$$N_A \approx g_A V (2\pi m_A T)^{3/2} e^{(A\mu_B - m_A)/T}$$

A.Z. Mekjian, PRC17,1051 (1978); P. Danielewicz, G.F. Bertsch, NPA533, 712 (1991); P. Danielewicz and P. Schuck, PLB274, 268 (1992); Y. Oh and C. M. Ko PRC76, 054910(2007); PRC80, 064902(2009); D. Oliinychenko, L. G. Pang, H. Elfner, and V. Koch, PRC99, 044907 (2019); K. J. Sun, R. Wang, C. M. Ko, Y. G. Ma, and C. Shen, 2207.12532(2022)

$$\pi NN \leftrightarrow \pi d$$

$$\pi NNN \leftrightarrow \pi t(h), \pi Nd \leftrightarrow \pi t(h)$$

J. I. Kapusta, Phys. Rev. C 21, 1301 (1980)
 H. Sato and K. Yazaki, PLB98, 153 (1981);
 E. Remler, Ann. Phys. 136, 293 (1981);
 M. Gyulassy, K. Frankel, and E. Remler, NPA402,596 (1983);
 S. Mrowczynski, J. Phys. G 13, 1089 (1987);
 S. Leupold and U. Heinz, PRC50, 1110 (1994);
 R. Scheibl and U. W. Heinz, PRC59, 1585(1999);
 K. J. Sun, C. M. Ko and B. Donigus, PLB 792, 132 (2019);
 S. Sombun et al., PRC99, 014901 (2019)
 F. Bellini et al., PRC99,054905(2019);
 PRC 103, 014907(2021);
 W. Zhao et al., PLB 820, 136571(2021);
 S. Wu et al., arXiv:2205.14302(2022);...

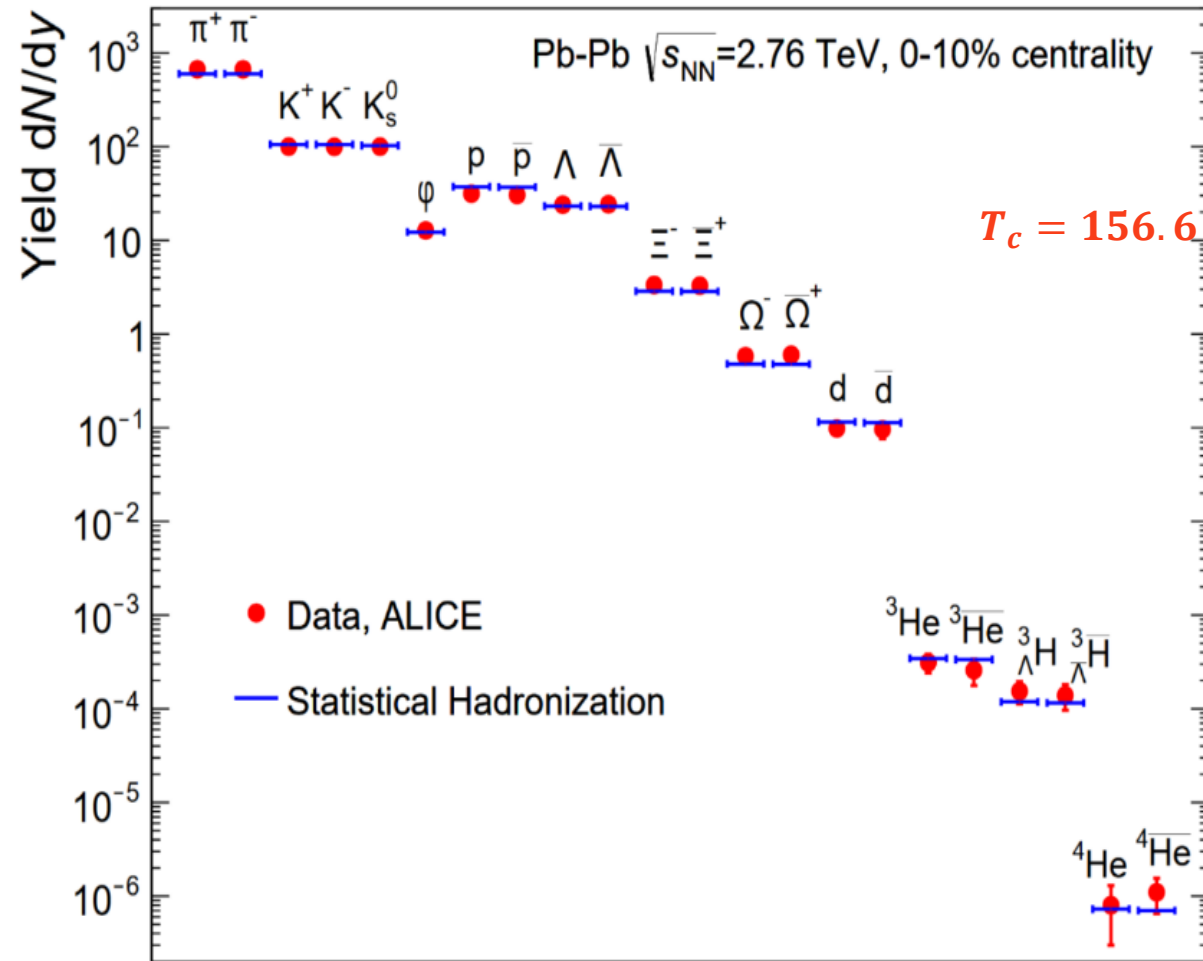
$$N_A = Tr(\hat{\rho}_s \hat{\rho}_A) = g_c \int d\Gamma \rho_s(\{x_i, p_i\}) \times W_A(\{x_i, p_i\})$$

1. Statistical hadronization or final-state coalescence?
2. Does finite nuclear size play any role?
3. Does post-hadronization dynamics have visible effects?
4. Any medium effect?

2. Statistical hadronization

(6)

Andronic, Braun-Munzinger, Redlich, Stachel, Nature 561, 321 (2018)



$$N_h \approx \frac{g_h V_C}{2\pi^2} m_h^2 T_C K_2\left(\frac{m_h}{T_C}\right)$$

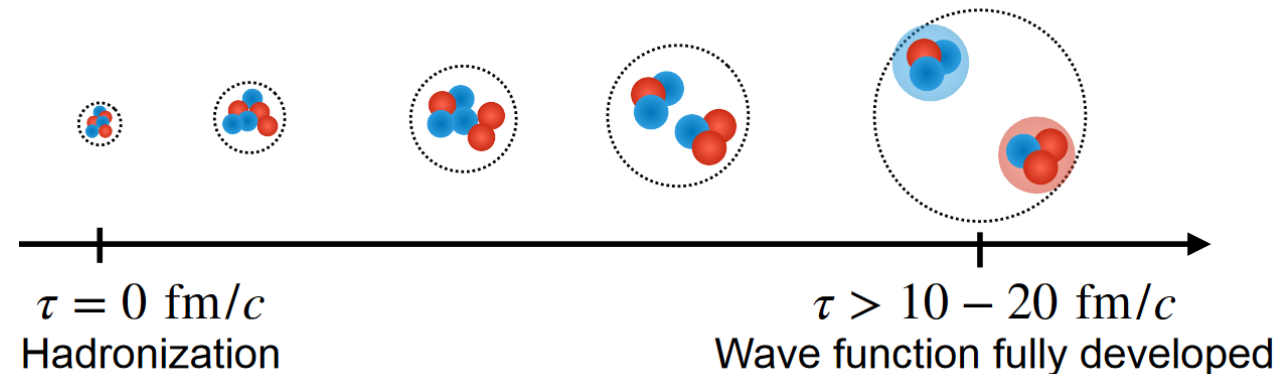
$$\approx g_h V_C \left(\frac{m_h T_C}{2\pi}\right)^{3/2} e^{-m_h/T_C}$$

T_C : Chemical freeze-out temperature, which is close to the chiral transition temperature (LQCD)

All (stable) particles including light (hyper)nuclei are produced at the QCD phase boundary and share a common chemical freeze-out

Compact multi-quark states

loosely bound states

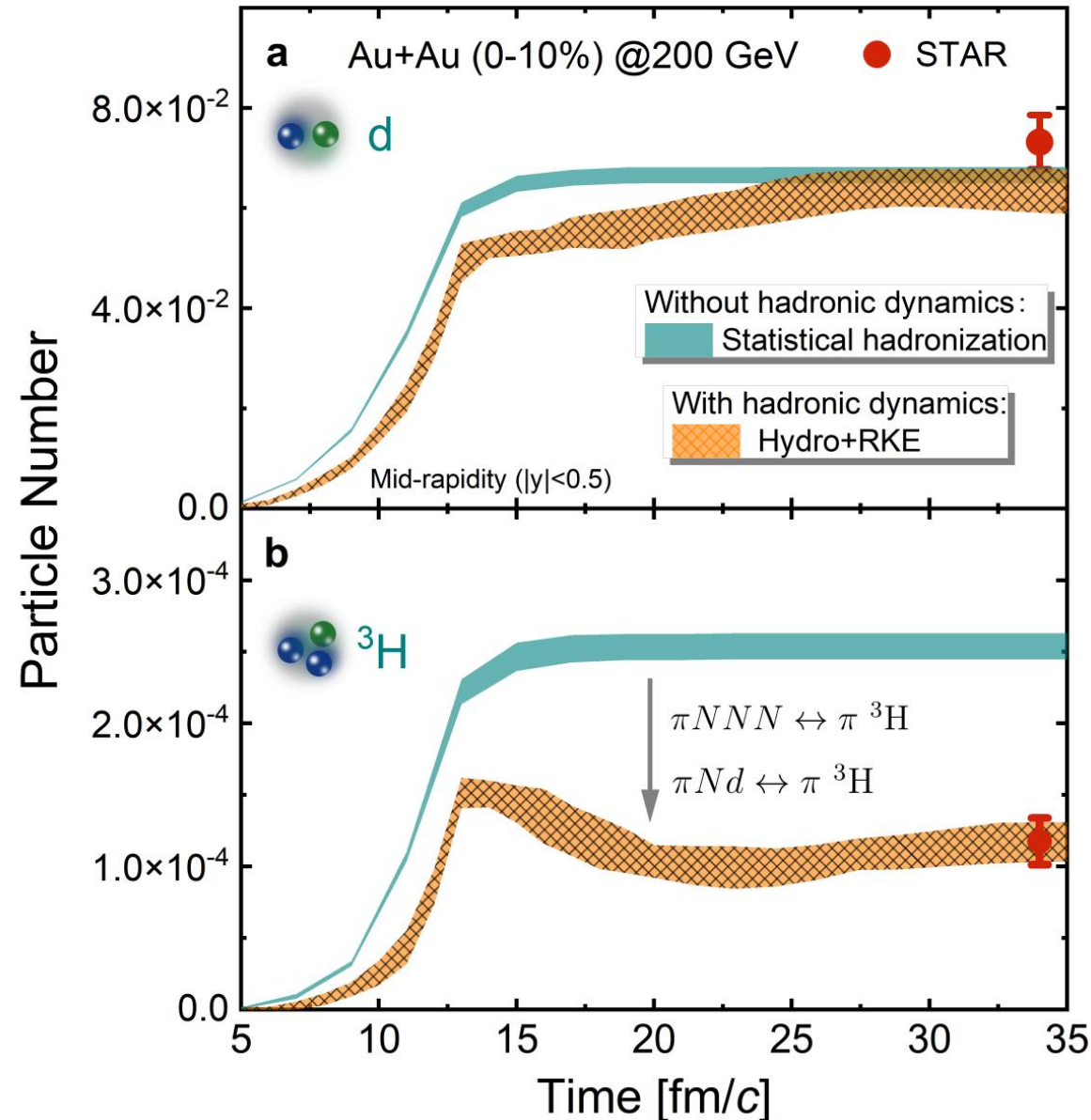


2. Hadronic Re-Scattering Effects at RHIC

(7)

K. J. Sun, R. Wang, C. M. Ko, Y. G. Ma, C. Shen, *Nat. Commun.* 15, 1074 (2024)

Data from STAR, *PRL* 130, 202301 (2023)



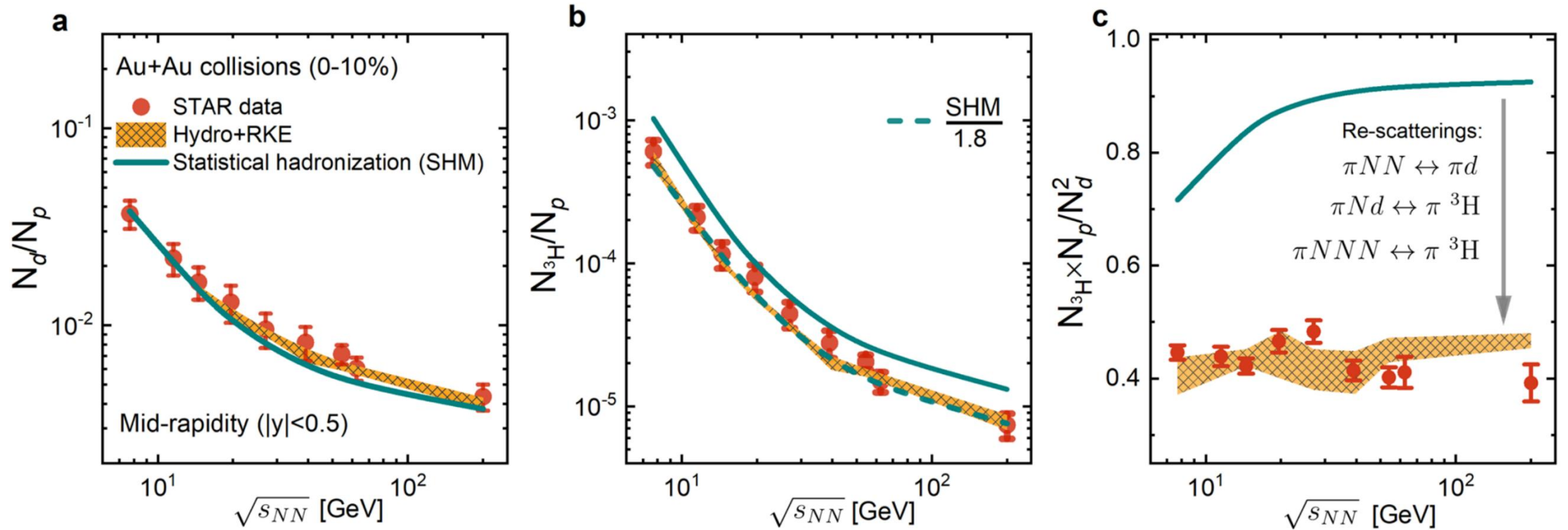
- $A = 2$ $\pi NN \leftrightarrow \pi d$, $NNN \leftrightarrow Nd$
- $A = 3$ $\pi NNN \leftrightarrow \pi t(h)$, $\pi Nd \leftrightarrow \pi t(h)$,
 $NNNN \leftrightarrow Nt(h)$, $NNd \leftrightarrow Nt(h)$, and etc.

2. Hadronic Re-Scattering Effects at RHIC

(8)

K. J. Sun, R. Wang, C. M. Ko, Y. G. Ma, C. Shen, *Nat. Commun.* 15, 1074 (2024)

Data from STAR, *PRL* 130, 202301 (2023)



Hadronic re-scatterings have small effects on the final deuteron yields (see also D. Oliinychenko et al. *PRC* 99, 044907 (2019)), but they reduce the triton yields by about a factor of 1.8.

2. Final-state coalescence

(9)

Density Matrix Formulation (sudden approximation)

$$N_A = \text{Tr}(\hat{\rho}_S \hat{\rho}_A) = g_c \int d\Gamma \rho_s(\{x_i, p_i\}) \times W_A(\{x_i, p_i\})$$

“Quantum mechanical correction”

Two-body coalescence $a + b \rightarrow c$:

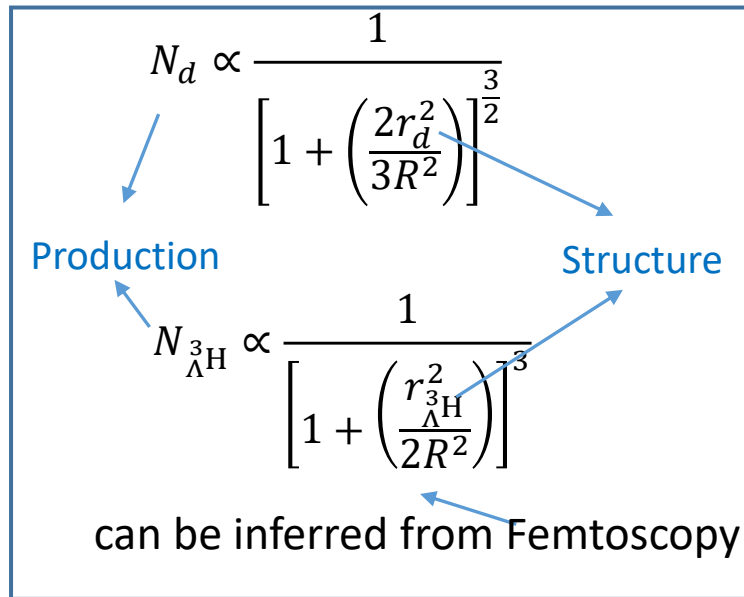
$$N_c = \frac{2J_c + 1}{(2J_a + 1)(2J_b + 1)} \int \frac{dx_a dk_a}{(2\pi)^3} \frac{dx_b dk_b}{(2\pi)^3} f_a(x_a, k_a) f_b(x_b, k_b) W_c(x, k)$$

$$\approx \frac{2J_c + 1}{(2J_a + 1)(2J_b + 1)} \frac{N_a N_b}{\left(\frac{m_a m_b T}{m_a + m_b} (R_a^2 + R_b^2)\right)^{3/2}} \times \frac{1}{\left(1 + \frac{\sigma^2}{R_a^2 + R_b^2}\right)^{3/2}}$$

$$f_a = \frac{N_a}{(m_a T R_a^2)^{3/2}} e^{-\frac{k_a^2}{2m_a T} - \frac{x_a^2}{2R_a^2}}$$

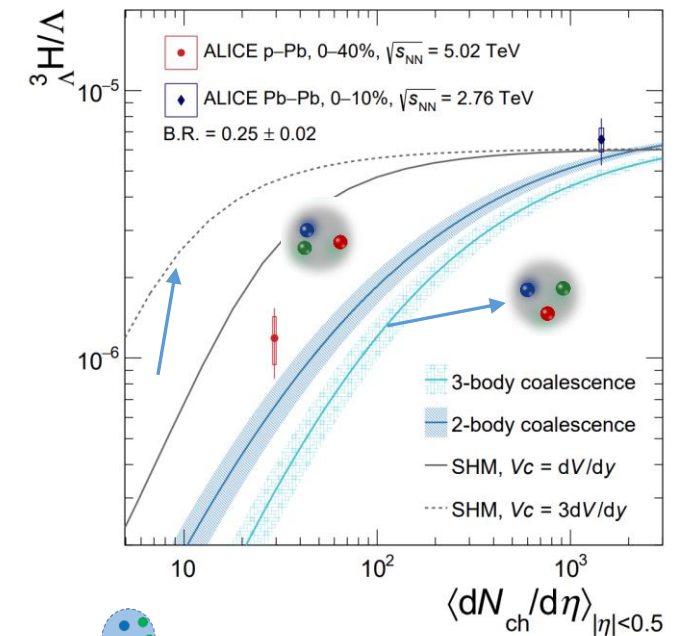
$$W_c = 8e^{-x^2/\sigma^2 - \sigma^2 k^2}$$

$$N_a = \int \frac{dx_a dk_a}{(2\pi)^3} f_a(x_a, k_a) \quad 1 = \int \frac{dx dk}{(2\pi)^3} W_c(x, k)$$



ALICE Results (${}^3_{\Lambda}\text{H}$)

Phys. Rev. Lett. 128, 055203(2022)

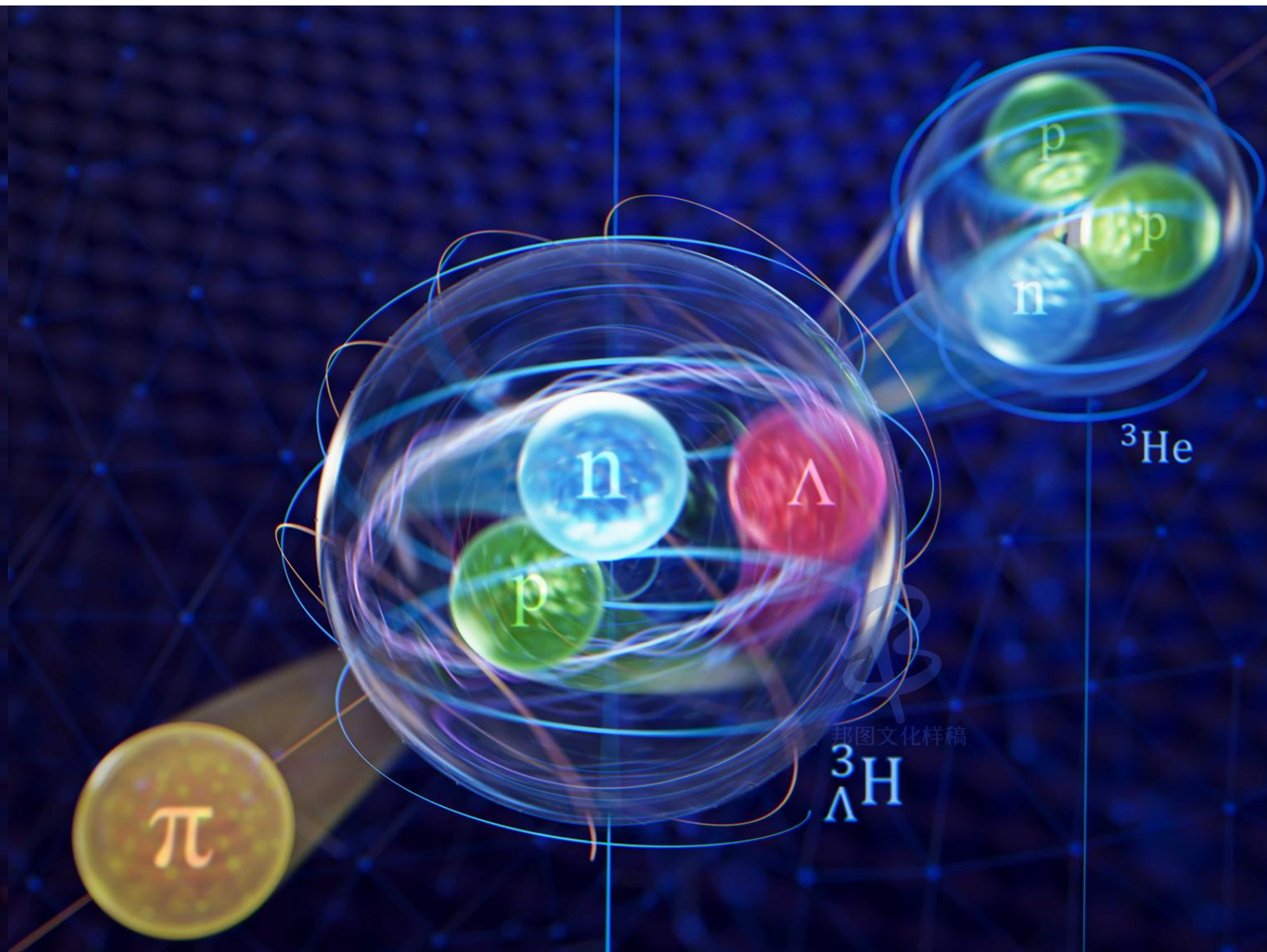


R. Scheibl and U. W. Heinz, PRC59, 1585(1999);

F. Bellini et al., PRC99,054905(2019);

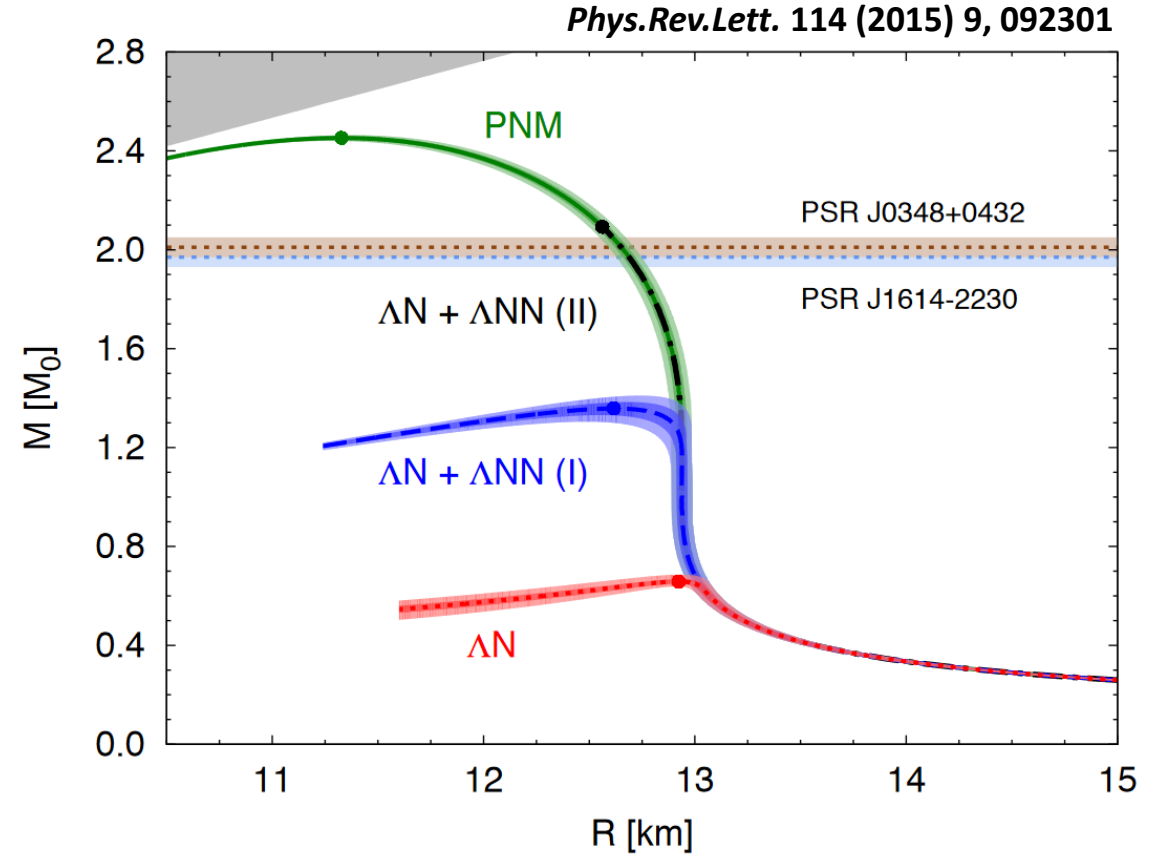
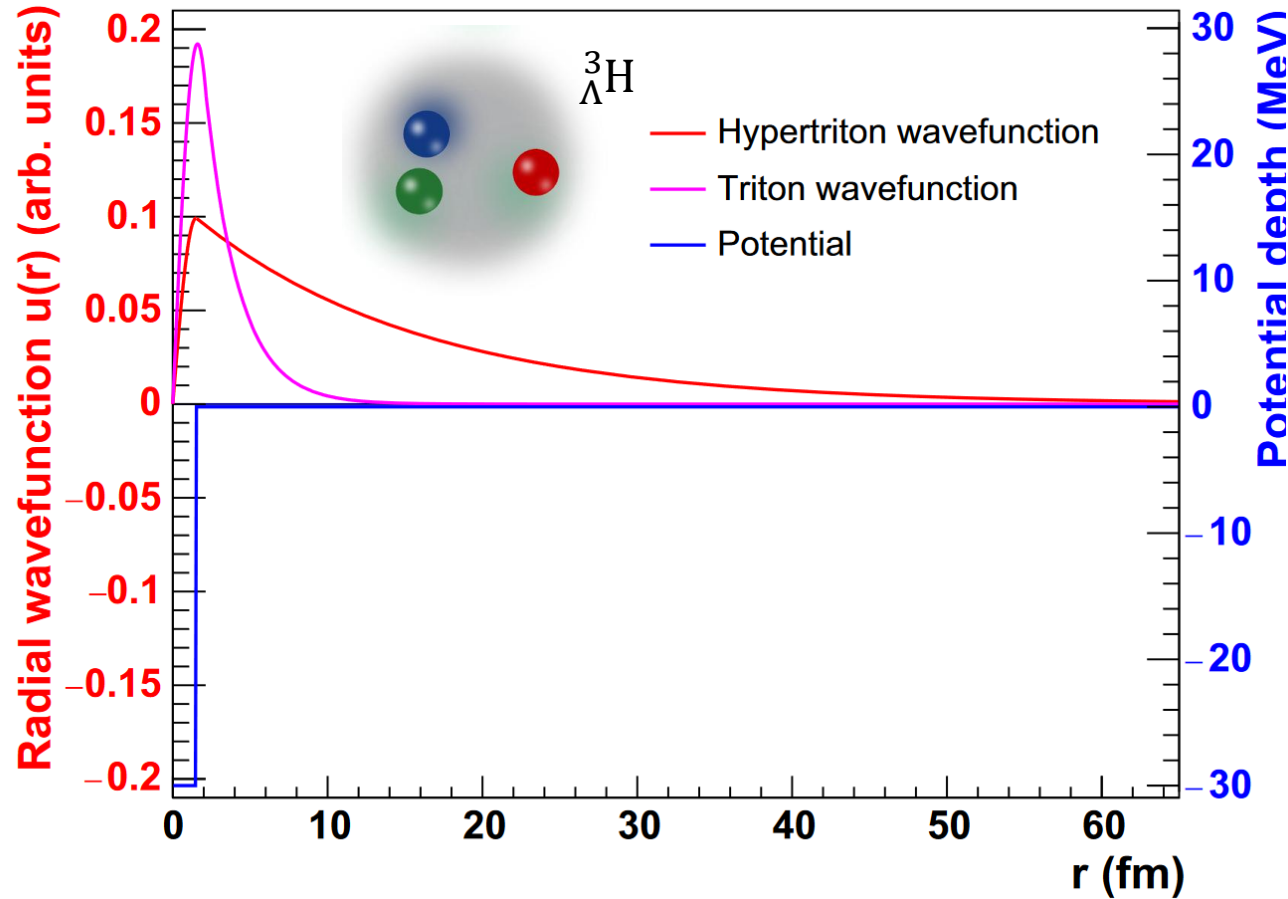
K. J. Sun, C. M. Ko and B. Dönig, PLB 792, 132 (2019);

(Anti-)Hypertriton Polarization



3. The halo-like nucleus: (anti-)hypertriton

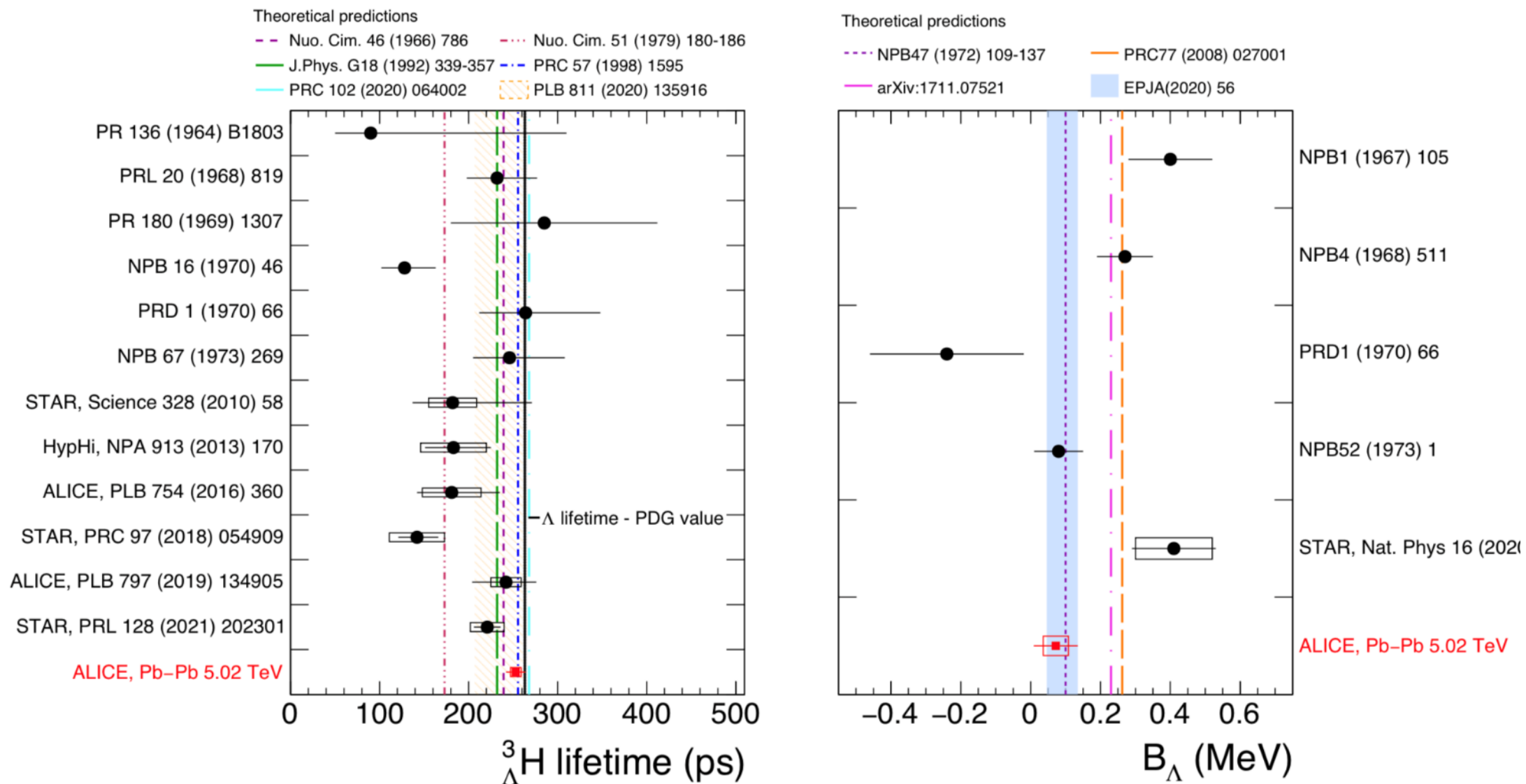
(10)



3. Binding energy and lifetime

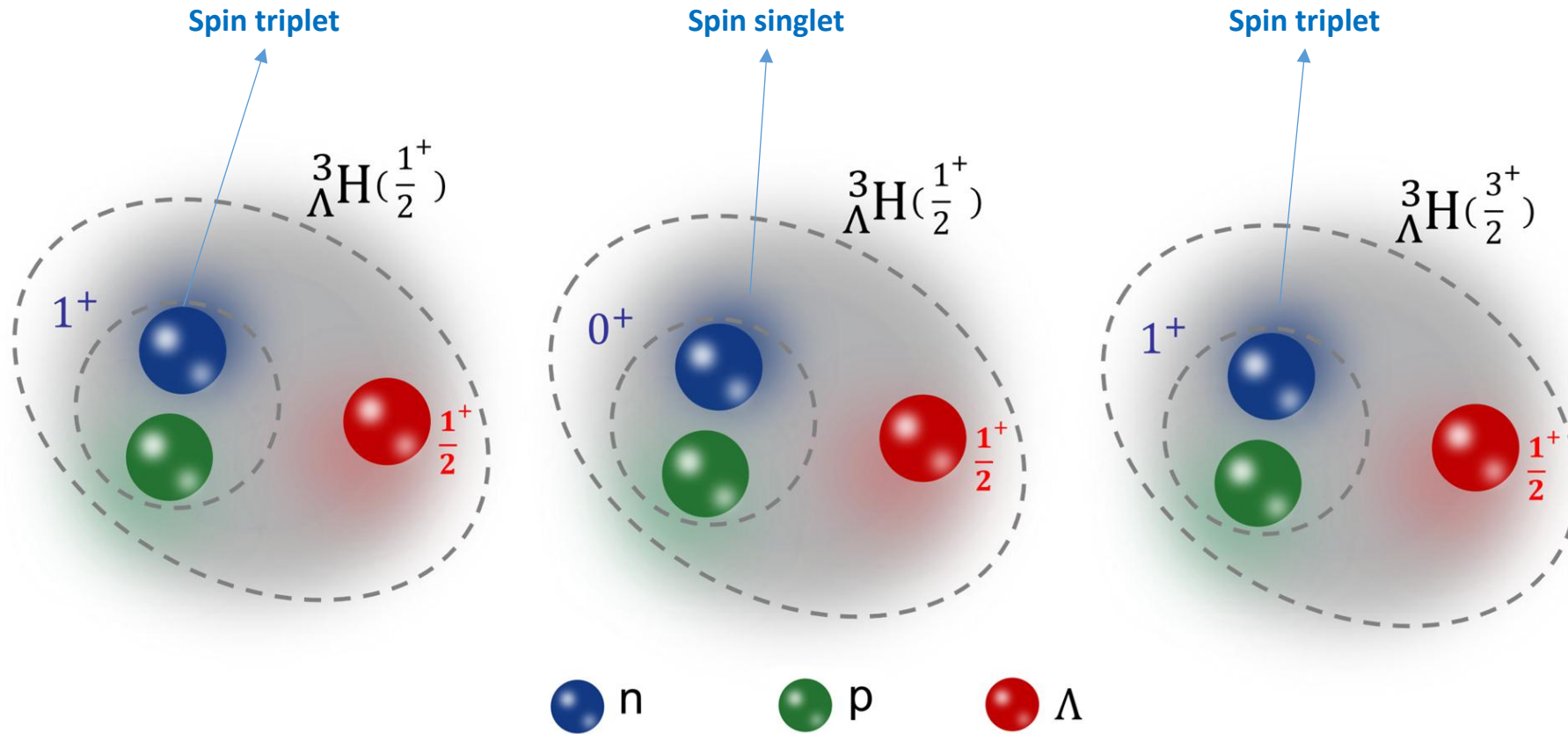
ALICE, PRL 131, 102302 (2023)

Y. G. Ma, Nucl. Sci. Tech. 3497 (2023)

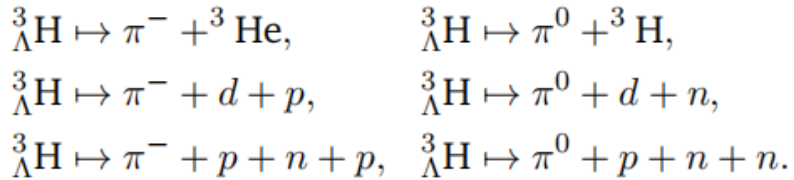


3. Spin of (anti-)hypertriton ?

(12)

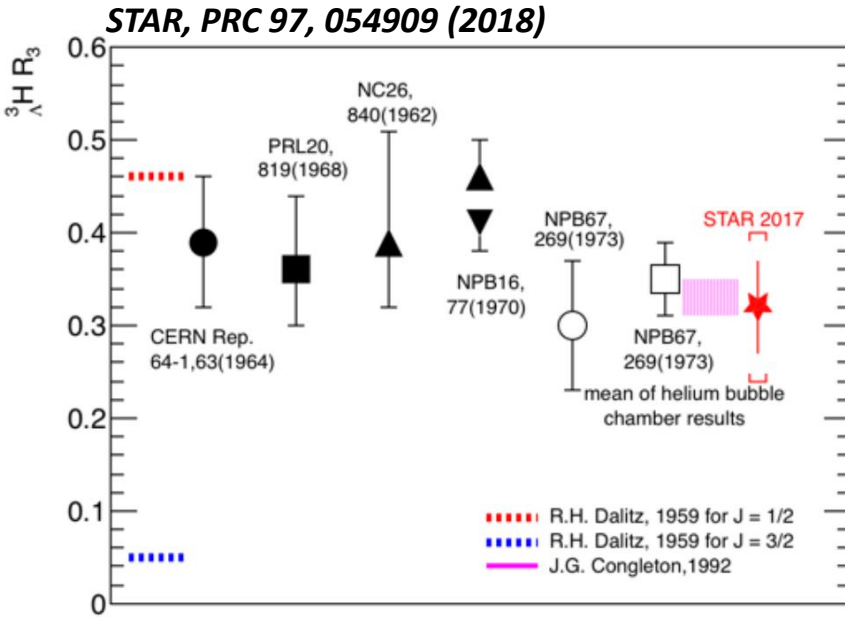
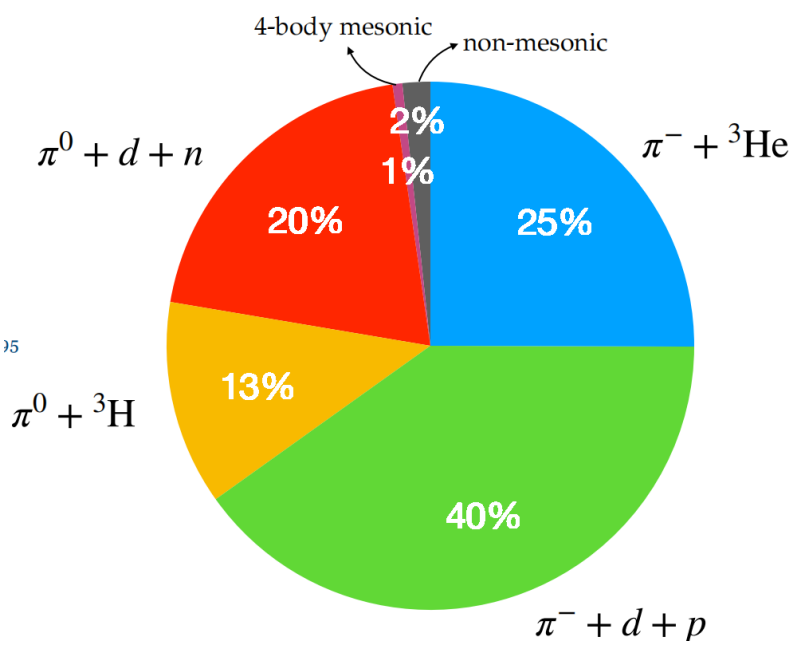


3. Spin of (anti-)hypertriton ?



Relative branching ratio:

$$R_3 = \frac{\text{B.R.}({}^3_{\Lambda}H \rightarrow {}^3\text{He}\pi^-)}{\text{B.R.}({}^3_{\Lambda}H \rightarrow {}^3\text{He}\pi^-) + \text{B.R.}({}^3_{\Lambda}H \rightarrow dp\pi^-)}$$



Favors spin 1/2

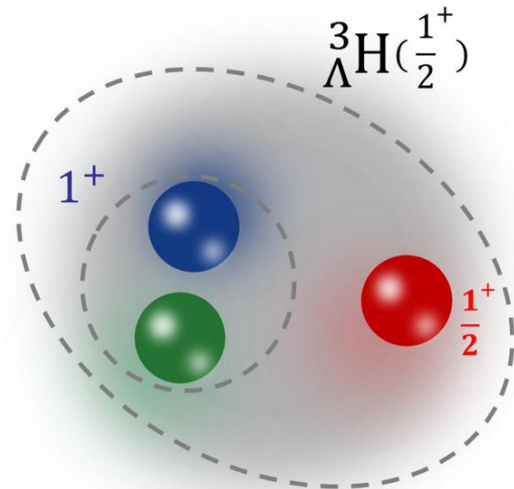
PHYSICAL REVIEW D **87**, 034506 (2013)
Light nuclei and hypernuclei from quantum chromodynamics in the limit of SU(3) flavor symmetry
 S. R. Beane,¹ E. Chang,² S. D. Cohen,³ W. Detmold,^{4,5} H. W. Lin,³ T. C. Luu,⁶ K. Orginos,^{4,5} A. Parreño,² M. J. Savage,³ and A. Walker-Loud^{7,8}

Label	A	s	I	J^π	Local SU(3) irreps	This work
N	1	0	1/2	1/2 ⁺	8	8
Λ	1	-1	0	1/2 ⁺	8	8
Σ	1	-1	1	1/2 ⁺	8	8
Ξ	1	-2	1/2	1/2 ⁺	8	8
d	2	0	0	1 ⁺	$\overline{10}$	$\overline{10}$
nn	2	0	1	0 ⁺	27	27
$n\Lambda$	2	-1	1/2	0 ⁺	27	27
$n\Lambda$	2	-1	1/2	1 ⁺	$8_A, \overline{10}$	-
$n\Sigma$	2	-1	3/2	0 ⁺	27	27
$n\Sigma$	2	-1	3/2	1 ⁺	10	10
$n\Xi$	2	-2	0	1 ⁺	8_A	8_A
$n\Xi$	2	-2	1	1 ⁺	$8_A, \overline{10}, \overline{10}$	-
H	2	-2	0	0 ⁺	1, 27	1, 27
${}^3\text{H}, {}^3\text{H}$	3	0	1/2	1/2 ⁺	$\overline{35}$	$\overline{35}$
${}^3\text{H}(1/2^+)$	3	-1	0	1/2 ⁺	$\overline{35}$	-
${}^3_{\Lambda}H(3/2^+)$	3	-1	0	3/2 ⁺	$\overline{10}$	$\overline{10}$
${}^3_{\Lambda}\text{He}, {}^3_{\Lambda}\text{H}, nn\Lambda$	3	-1	1	1/2 ⁺	27, 35	27, 35
${}^3_{\Sigma}\text{He}$	3	-1	1	3/2 ⁺	27	27
${}^4\text{He}$	4	0	0	0 ⁺	$\overline{28}$	$\overline{28}$
${}^4_{\Lambda}\text{He}, {}^4_{\Lambda}\text{H}$	4	-1	1/2	0 ⁺	$\overline{28}$	-
${}^4_{\Lambda\Lambda}\text{He}$	4	-2	1	0 ⁺	27, 28	27, 28
$\Lambda\Xi^0 pnn$	5	-3	0	3/2 ⁺	$\overline{10} + \dots$	$\overline{10}$

Favors spin 3/2

3. (Anti-)hypertriton polarization and its spin structure

(14)



$$\begin{aligned} |\frac{1}{2}, \uparrow\rangle_{\Lambda\text{H}} &= \frac{\sqrt{6}}{3} |\frac{1}{2}, \frac{1}{2}\rangle_n |\frac{1}{2}, \frac{1}{2}\rangle_p |\frac{1}{2}, -\frac{1}{2}\rangle_{\Lambda} \\ &- \frac{\sqrt{6}}{6} (|\frac{1}{2}, \frac{1}{2}\rangle_n |\frac{1}{2}, -\frac{1}{2}\rangle_p |\frac{1}{2}, \frac{1}{2}\rangle_{\Lambda} \\ &+ |\frac{1}{2}, -\frac{1}{2}\rangle_n |\frac{1}{2}, \frac{1}{2}\rangle_p |\frac{1}{2}, \frac{1}{2}\rangle_{\Lambda}), \end{aligned}$$

$$\begin{aligned} |\frac{1}{2}, \downarrow\rangle_{\Lambda\text{H}} &= -\frac{\sqrt{6}}{3} |\frac{1}{2}, -\frac{1}{2}\rangle_n |\frac{1}{2}, -\frac{1}{2}\rangle_p |\frac{1}{2}, \frac{1}{2}\rangle_{\Lambda} \\ &+ \frac{\sqrt{6}}{6} (|\frac{1}{2}, \frac{1}{2}\rangle_n |\frac{1}{2}, -\frac{1}{2}\rangle_p |\frac{1}{2}, -\frac{1}{2}\rangle_{\Lambda} \\ &+ |\frac{1}{2}, -\frac{1}{2}\rangle_n |\frac{1}{2}, \frac{1}{2}\rangle_p |\frac{1}{2}, -\frac{1}{2}\rangle_{\Lambda}). \end{aligned}$$

Coalescence model for hypertriton production (without baryon spin correlation)

$$E_i \frac{d^3 N_{i, \pm \frac{1}{2}}}{d\mathbf{p}_i^3} = \int_{\Sigma^\mu} d^3 \sigma_\mu p_i^\mu w_{i, \pm \frac{1}{2}}(\mathbf{x}_i, \mathbf{p}_i) \bar{f}_i(\mathbf{x}_i, \mathbf{p}_i)$$

$$w_{i, \pm \frac{1}{2}} = \frac{1}{2} [1 \pm \mathcal{P}_i(\mathbf{x}_i, \mathbf{p}_i)]$$

$$\hat{\rho}_i = \text{diag} \left(\frac{1 + \mathcal{P}_i}{2}, \frac{1 - \mathcal{P}_i}{2} \right)$$

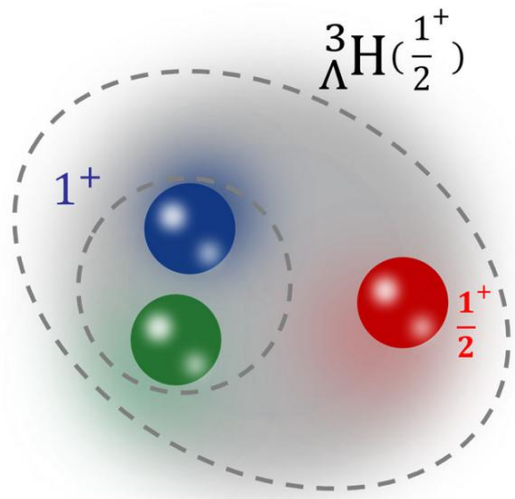
$$\bar{f}_i = \frac{g_i}{(2\pi)^3} [\exp(p_i^\mu u_\mu / T) / \xi_i + 1]^{-1}$$

$$\hat{\rho}_{np\Lambda} = \hat{\rho}_n \otimes \hat{\rho}_p \otimes \hat{\rho}_\Lambda$$

$$\begin{aligned} E \frac{d^3 N_{\Lambda\text{H}, \pm \frac{1}{2}}}{d\mathbf{P}^3} &= E \int \prod_{i=n,p,\Lambda} p_i^\mu d^3 \sigma_\mu \frac{d^3 p_i}{E_i} \bar{f}_i(\mathbf{x}_i, \mathbf{p}_i) \\ &\times \left(\frac{2}{3} w_{n, \pm \frac{1}{2}} w_{p, \pm \frac{1}{2}} w_{\Lambda, \mp \frac{1}{2}} + \frac{1}{6} w_{n, \pm \frac{1}{2}} w_{p, \mp \frac{1}{2}} w_{\Lambda, \pm \frac{1}{2}} \right. \\ &\left. + \frac{1}{6} w_{n, \mp \frac{1}{2}} w_{p, \pm \frac{1}{2}} w_{\Lambda, \pm \frac{1}{2}} \right) \\ &\times W_{\Lambda\text{H}}(\mathbf{x}_n, \mathbf{x}_p, \mathbf{x}_\Lambda; \mathbf{p}_n, \mathbf{p}_p, \mathbf{p}_\Lambda) \delta(\mathbf{P} - \sum_i \mathbf{p}_i) \end{aligned}$$

3. (Anti-)hypertriton polarization and its spin structure

(15)



$$\begin{aligned}\mathcal{P}_{\Lambda\text{H}} &\approx \frac{\frac{2}{3}\mathcal{P}_n + \frac{2}{3}\mathcal{P}_p - \frac{1}{3}\mathcal{P}_{\Lambda} - \mathcal{P}_n\mathcal{P}_p\mathcal{P}_{\Lambda}}{1 - \frac{2}{3}(\mathcal{P}_n + \mathcal{P}_p)\mathcal{P}_{\Lambda} + \frac{1}{3}\mathcal{P}_n\mathcal{P}_p} \\ &\approx \frac{2}{3}\mathcal{P}_n + \frac{2}{3}\mathcal{P}_p - \frac{1}{3}\mathcal{P}_{\Lambda} \\ &\approx \mathcal{P}_{\Lambda}\end{aligned}$$

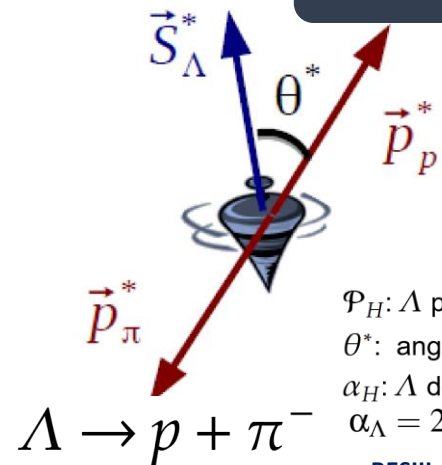
3. (Anti-)hypertriton polarization and its spin structure

(16)

K. J. Sun et al., arXiv:2405.12015(2024)

Parity-violating weak decay

Λ hyperons



$$\frac{dN}{d \cos \theta^*} = \text{Tr}[T^+ \hat{\rho} T]$$

$$\rho_\Lambda = \begin{pmatrix} \frac{1 + \mathcal{P}_\Lambda}{2} & \\ & \frac{1 - \mathcal{P}_\Lambda}{2} \end{pmatrix}$$

\mathcal{P}_H : Λ polarization
 θ^* : angle between proton momentum and Λ rest frame
 α_H : Λ decay parameter
 $\alpha_\Lambda = 2\text{Re}(T_s^* T_p) = 0.732 \pm 0.014$

BESIII, Phys. Rev. Lett. 129, 131801 (2022).

The transition matrix

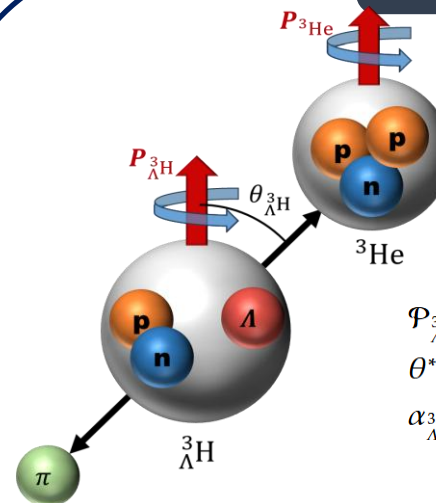
$$T(\Lambda \rightarrow \pi^- + p) = \frac{1}{\sqrt{4\pi}} \begin{pmatrix} T_s + T_p \cos \theta_p^* & T_p \sin \theta_p^* e^{i\phi_p^*} \\ T_p \sin \theta_p^* e^{-i\phi_p^*} & T_s - T_p \cos \theta_p^* \end{pmatrix}$$

The angular distribution

$$\frac{dN}{d \cos \theta^*} = \frac{1}{2} (1 + \alpha_H |\mathcal{P}_H| \cos \theta^*)$$

H denotes Λ and $\bar{\Lambda}$

Hypertriton



$$\rho_{\Lambda^3\text{H}} = \begin{pmatrix} \frac{1 + \mathcal{P}_{\Lambda^3\text{H}}}{2} & \\ & \frac{1 - \mathcal{P}_{\Lambda^3\text{H}}}{2} \end{pmatrix}$$

$\mathcal{P}_{\Lambda^3\text{H}}$: $\Lambda^3\text{H}$ polarization
 θ^* : Angle between ${}^3\text{He}$ momentum and $\Lambda^3\text{H}$ rest frame
 $\alpha_{\Lambda^3\text{H}}$: $\Lambda^3\text{H}$ decay parameter

$$T({}^3\Lambda\text{H} \rightarrow \pi^- + {}^3\text{He})$$

$$= \frac{F}{6\sqrt{\pi}} \begin{pmatrix} 3T_s - T_p \cos \theta^* & -T_p \sin \theta^* e^{i\phi^*} \\ -T_p \sin \theta^* e^{-i\phi^*} & 3T_s + T_p \cos \theta^* \end{pmatrix}$$

$$\frac{dN}{d \cos \theta^*} = \frac{1}{2} \left(1 + \alpha_{\Lambda^3\text{H}} \mathcal{P}_{\Lambda^3\text{H}} \cos \theta^* \right)$$

3. (Anti-)hypertriton polarization and its spin structure

(16)

K. J. Sun et al., arXiv:2405.12015(2024)

Parity-violating weak decay

Λ hyperons

Hypertriton

\vec{S}_Λ^*
 \vec{p}_p^*
 \vec{p}_π^*
 θ^*

\mathcal{P}_H : Λ polarization
 θ^* : angle between proton momentum and Λ spin
 α_H : Λ decay parameter
 $\alpha_\Lambda = 2\text{Re}(T_s^* T_p) = 0.732 \pm 0.01$
 BESIII, Phys. Rev. Lett. 129, 131801 (2022)

$\Lambda \rightarrow p + \pi^-$

$$\frac{dN}{d \cos \theta^*} = \text{Tr}[T^+ \hat{\rho} T]$$

$$\rho_\Lambda = \begin{pmatrix} \frac{1 + \mathcal{P}_\Lambda}{2} & \\ & \frac{1 - \mathcal{P}_\Lambda}{2} \end{pmatrix}$$

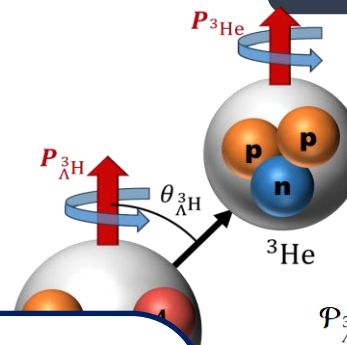
The transition matrix

$$T(\Lambda \rightarrow \pi^- + p) = \frac{1}{\sqrt{4\pi}} \begin{pmatrix} T_s + T_p \cos \theta_p^* & T_p \sin \theta_p^* e^{-i\phi_p^*} \\ T_p \sin \theta_p^* e^{-i\phi_p^*} & T_s - T_p \cos \theta_p^* \end{pmatrix}$$

The angular distribution

$$\frac{dN}{d \cos \theta^*} = \frac{1}{2} (1 + \alpha_H |\mathcal{P}_H| \cos \theta^*)$$

H denotes Λ and $\bar{\Lambda}$



$$\rho_{\Lambda^3\text{H}} = \begin{pmatrix} \frac{1 + \mathcal{P}_{\Lambda^3\text{H}}}{2} & \\ & \frac{1 - \mathcal{P}_{\Lambda^3\text{H}}}{2} \end{pmatrix}$$

$\mathcal{P}_{\Lambda^3\text{H}}$: ^3H polarization
 θ^* : Angle between ^3He momentum and ^3H rest frame
 $\alpha_{\Lambda^3\text{H}}$: ^3H decay parameter

$$\alpha_{\Lambda^3\text{H}} \approx -\frac{1}{3T_s^2 + \frac{1}{3}T_p^2} \alpha_\Lambda$$

$$\approx -\frac{1}{2.58} \alpha_\Lambda$$

Sign flip !

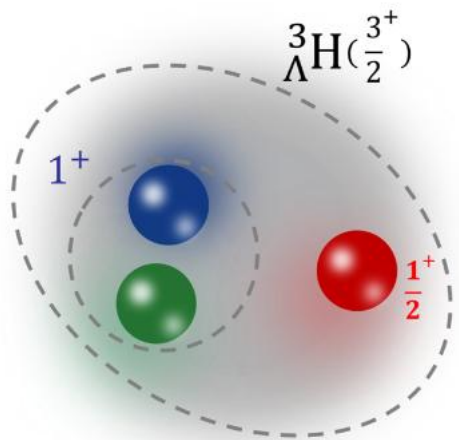
$\pi^- + ^3\text{He}$

$$\begin{pmatrix} 3T_s - T_p \cos \theta^* & -T_p \sin \theta^* e^{i\phi^*} \\ -T_p \sin \theta^* e^{-i\phi^*} & 3T_s + T_p \cos \theta^* \end{pmatrix}$$

$$\frac{dN}{d \cos \theta^*} = \frac{1}{2} (1 + \alpha_{\Lambda^3\text{H}} \mathcal{P}_{\Lambda^3\text{H}} \cos \theta^*)$$

3. (Anti-)hypertriton polarization and its spin structure

(17)

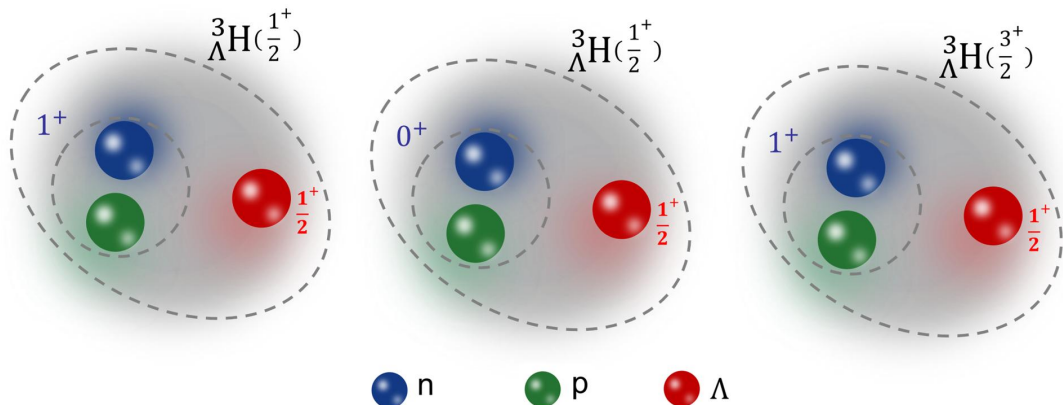


$$\hat{\rho}_{\Lambda}^{{}^3\text{H}} \approx \text{diag} \left[\frac{(1 + \mathcal{P}_{\Lambda})^3}{4(1 + \mathcal{P}_{\Lambda}^2)}, \frac{(1 - \mathcal{P}_{\Lambda})(1 + \mathcal{P}_{\Lambda})^2}{4(1 + \mathcal{P}_{\Lambda}^2)}, \frac{(1 - \mathcal{P}_{\Lambda})^2(1 + \mathcal{P}_{\Lambda})}{4(1 + \mathcal{P}_{\Lambda}^2)}, \frac{(1 - \mathcal{P}_{\Lambda})^3}{4(1 + \mathcal{P}_{\Lambda}^2)} \right]$$

$$T({}^3_{\Lambda}\text{H} \rightarrow \pi^- + {}^3\text{He}) = \frac{FT_p}{\sqrt{6\pi}} \begin{pmatrix} e^{i\phi^*} \sin\theta^* & 0 \\ -\frac{2}{\sqrt{3}} \cos\theta^* & \frac{e^{i\phi^*} \sin\theta^*}{\sqrt{3}} \\ -\frac{e^{-i\phi^*} \sin\theta^*}{\sqrt{3}} & -\frac{2}{\sqrt{3}} \cos\theta^* \\ 0 & -e^{-i\phi^*} \sin\theta^* \end{pmatrix}$$

$$\frac{dN}{d\cos\theta^*} = \frac{1}{2} \left[1 + \left(\hat{\rho}_{\frac{1}{2}, \frac{1}{2}} + \hat{\rho}_{-\frac{1}{2}, -\frac{1}{2}} - \frac{1}{2} \right) (3\cos^2\theta^* - 1) \right]$$

$$\hat{\rho}_{\frac{1}{2}, \frac{1}{2}} + \hat{\rho}_{-\frac{1}{2}, -\frac{1}{2}} - \frac{1}{2} \approx -\frac{\mathcal{P}_{\Lambda}^2}{1 + \mathcal{P}_{\Lambda}^2} \approx -\mathcal{P}_{\Lambda}^2$$



J^P	structure	decay mode	$\frac{dN}{d\cos\theta^*}$
$\frac{1}{2}^+$	$\Lambda(\frac{1}{2}^+) - np(1^+)$	${}^3_{\Lambda}\text{H} \rightarrow \pi^- + {}^3\text{He}$	$\frac{1}{2} (1 - \frac{1}{2.58} \alpha_{\Lambda} \mathcal{P}_{\Lambda} \cos\theta^*)$
$\frac{1}{2}^+$	$\Lambda(\frac{1}{2}^+) - np(0^+)$	${}^3_{\Lambda}\text{H} \rightarrow \pi^- + {}^3\text{He}$	$\frac{1}{2} (1 + \alpha_{\Lambda} \mathcal{P}_{\Lambda} \cos\theta^*)$
$\frac{3}{2}^+$	$\Lambda(\frac{1}{2}^+) - np(1^+)$	${}^3_{\Lambda}\text{H} \rightarrow \pi^- + {}^3\text{He}$	$\frac{1}{2} (1 - \mathcal{P}_{\Lambda}^2 (3\cos^2\theta^* - 1))$
$\frac{1}{2}^-$	$\bar{\Lambda}(\frac{1}{2}^-) - \bar{n}\bar{p}(1^-)$	${}^3_{\Lambda}\bar{\text{H}} \rightarrow \pi^+ + {}^3\bar{\text{He}}$	$\frac{1}{2} (1 - \frac{1}{2.58} \alpha_{\bar{\Lambda}} \mathcal{P}_{\bar{\Lambda}} \cos\theta^*)$
$\frac{1}{2}^-$	$\bar{\Lambda}(\frac{1}{2}^-) - \bar{n}\bar{p}(0^-)$	${}^3_{\Lambda}\bar{\text{H}} \rightarrow \pi^+ + {}^3\bar{\text{He}}$	$\frac{1}{2} (1 + \alpha_{\bar{\Lambda}} \mathcal{P}_{\bar{\Lambda}} \cos\theta^*)$
$\frac{3}{2}^-$	$\bar{\Lambda}(\frac{1}{2}^-) - \bar{n}\bar{p}(1^-)$	${}^3_{\Lambda}\bar{\text{H}} \rightarrow \pi^+ + {}^3\bar{\text{He}}$	$\frac{1}{2} (1 - \mathcal{P}_{\bar{\Lambda}}^2 (3\cos^2\theta^* - 1))$

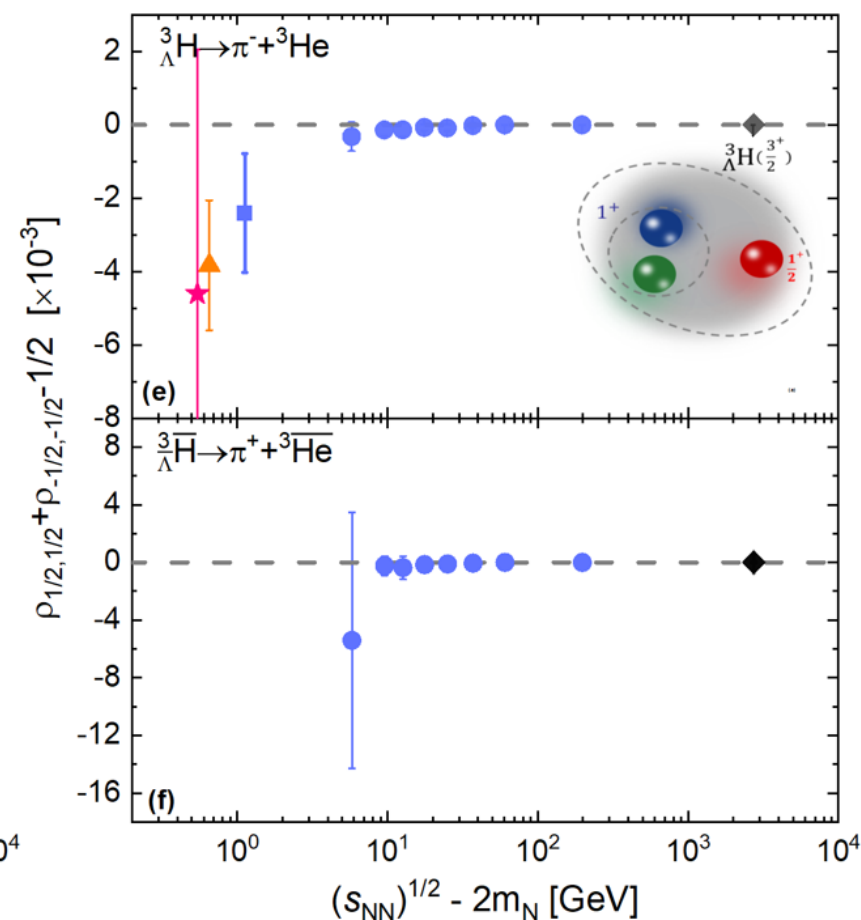
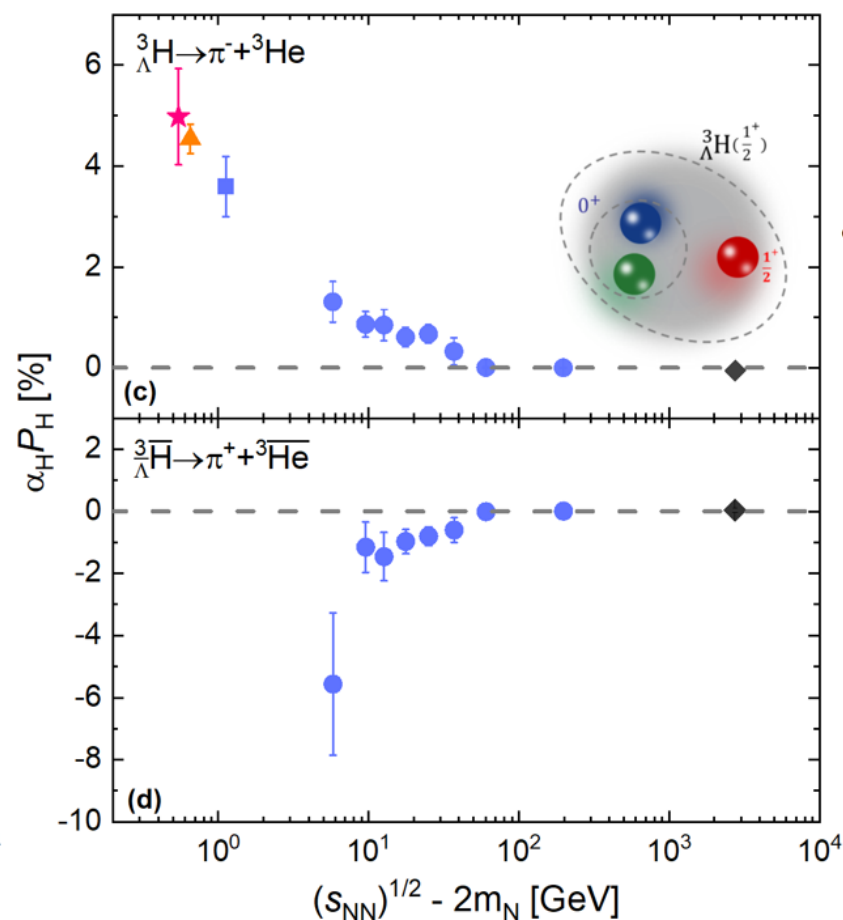
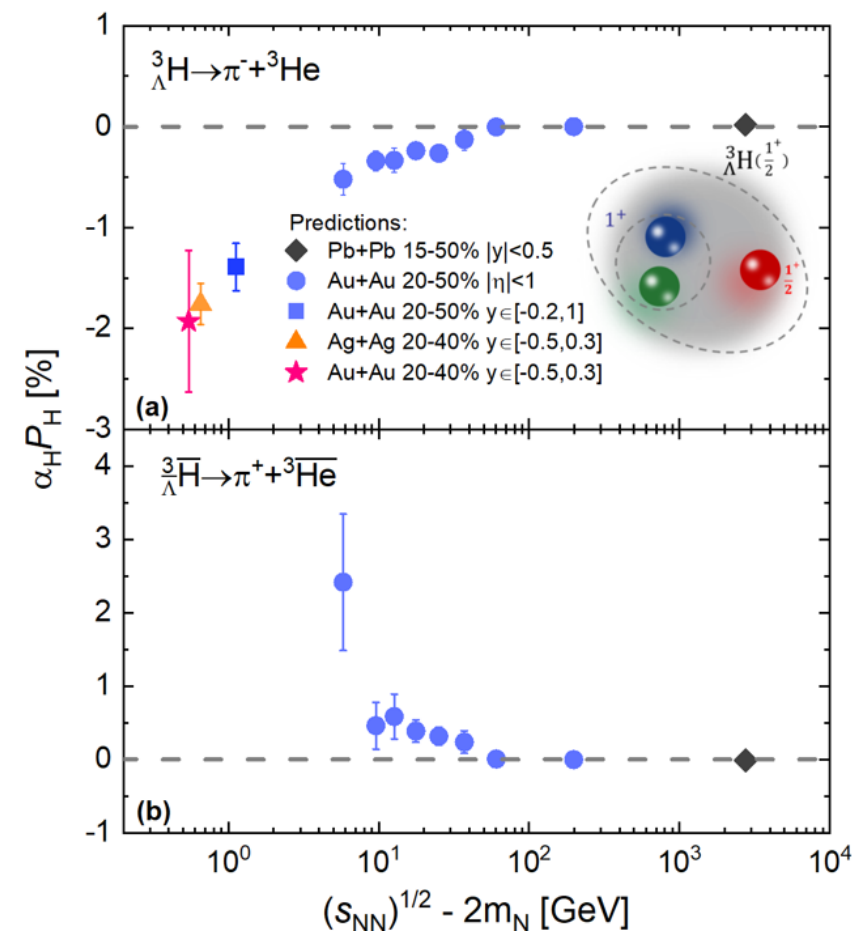
3. (Anti-)hypertriton polarization and its spin structure

(18)

The measurement of hypertriton polarization provides a novel method to uniquely determine its internal spin structure

$$\alpha_{\Lambda}^{3\text{H}} \approx -\frac{1}{2.58} \alpha_{\Lambda}$$

$$\alpha_{\Lambda}^{3\text{H}} \approx \alpha_{\Lambda}$$



4. Effects of baryon spin correlation

(19)

$$\begin{aligned}\hat{\rho}_{np\Lambda} &= \hat{\rho}_n \otimes \hat{\rho}_p \otimes \hat{\rho}_\Lambda + \frac{1}{2^2} (c_{np}^{\alpha\beta} \hat{\sigma}_{n,\alpha} \otimes \hat{\sigma}_{p,\beta} \otimes \hat{\rho}_\Lambda \\ &\quad + c_{p\Lambda}^{\alpha\beta} \hat{\sigma}_{p,\alpha} \otimes \hat{\sigma}_{\Lambda,\beta} \otimes \hat{\rho}_n + c_{n\Lambda}^{\alpha\beta} \hat{\sigma}_{n,\alpha} \otimes \hat{\sigma}_{\Lambda,\beta} \otimes \hat{\rho}_p) \\ &\quad + \frac{1}{2^3} c_{np\Lambda}^{\alpha\beta\gamma} \hat{\sigma}_{n,\alpha} \otimes \hat{\sigma}_{p,\beta} \otimes \hat{\sigma}_{\Lambda,\gamma},\end{aligned}$$

$$\mathcal{P}_{\Lambda H}^3 \approx \frac{\frac{2}{3}\langle\mathcal{P}_n\rangle + \frac{2}{3}\langle\mathcal{P}_p\rangle - \frac{1}{3}\langle\mathcal{P}_\Lambda\rangle - \langle\mathcal{P}_n\mathcal{P}_p\mathcal{P}_\Lambda\rangle + C_-}{1 - \frac{2}{3}(\langle(\mathcal{P}_n + \mathcal{P}_p)\mathcal{P}_\Lambda\rangle) + \frac{1}{3}\langle\mathcal{P}_n\mathcal{P}_p\rangle + C_+}$$

$$C_- = -\frac{1}{4}(\langle c_{np}^{zz}\mathcal{P}_\Lambda\rangle + \langle c_{p\Lambda}^{zz}\mathcal{P}_n\rangle + \langle c_{n\Lambda}^{zz}\mathcal{P}_p\rangle) - \frac{1}{4}\langle c_{np\Lambda}^{zzz}\rangle,$$

$$C_+ = \frac{1}{12}(\langle c_{np}^{zz}\rangle - 2\langle c_{p\Lambda}^{zz}\rangle - 2\langle c_{n\Lambda}^{zz}\rangle).$$

'genuine' correlation terms

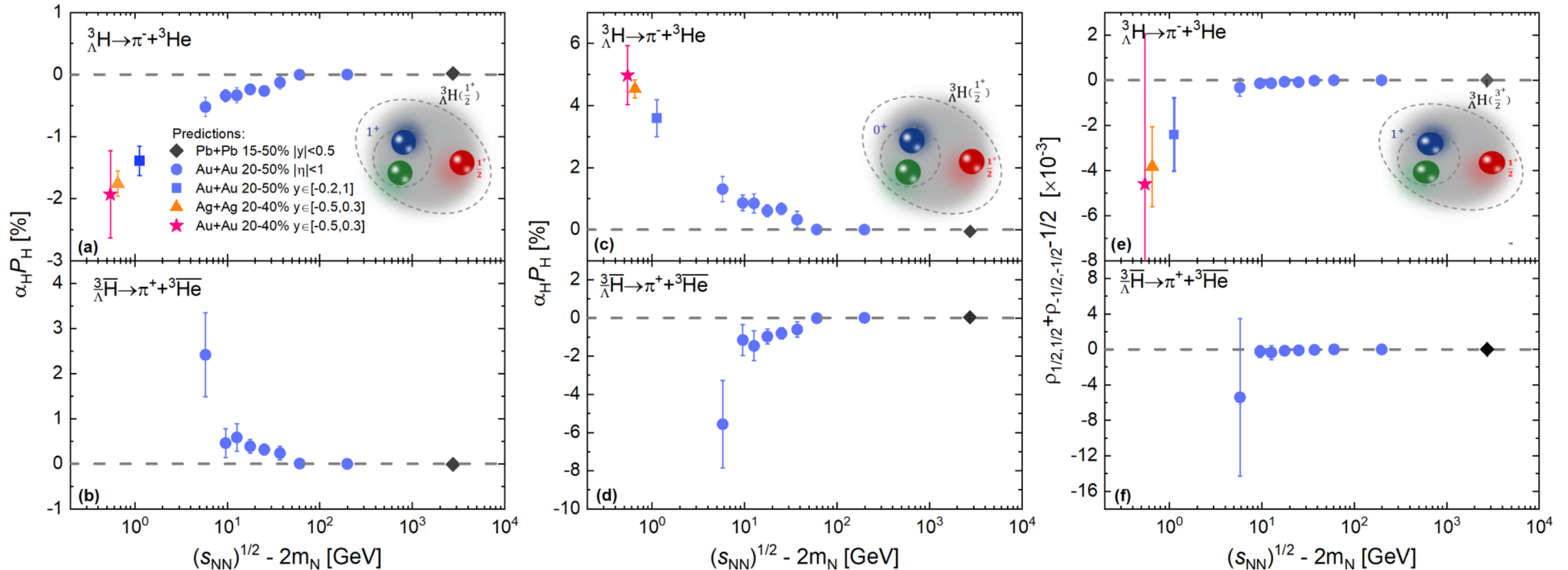
Induced correlations

We can express the polarization of a particle as $\mathcal{P} = \langle\mathcal{P}\rangle + \delta\mathcal{P}$ with $\delta\mathcal{P}$ denoting its space and momentum dependent fluctuations, which leads to the relations $\langle\mathcal{P}_n\mathcal{P}_p\rangle = \langle\mathcal{P}_n\rangle\langle\mathcal{P}_p\rangle + \langle\delta\mathcal{P}_n\delta\mathcal{P}_p\rangle$ and $\langle\mathcal{P}_n\mathcal{P}_p\mathcal{P}_\Lambda\rangle = \langle\mathcal{P}_n\rangle\langle\mathcal{P}_p\rangle\langle\mathcal{P}_\Lambda\rangle + \langle\delta\mathcal{P}_n\delta\mathcal{P}_p\rangle\langle\mathcal{P}_\Lambda\rangle + \langle\delta\mathcal{P}_n\delta\mathcal{P}_\Lambda\rangle\langle\mathcal{P}_p\rangle + \langle\delta\mathcal{P}_p\delta\mathcal{P}_\Lambda\rangle\langle\mathcal{P}_n\rangle + \langle\delta\mathcal{P}_n\delta\mathcal{P}_p\delta\mathcal{P}_\Lambda\rangle$. Assuming again $\langle\mathcal{P}_n\rangle \approx \langle\mathcal{P}_p\rangle \approx \langle\mathcal{P}_\Lambda\rangle$ and neglecting the three-body correlation, we then have

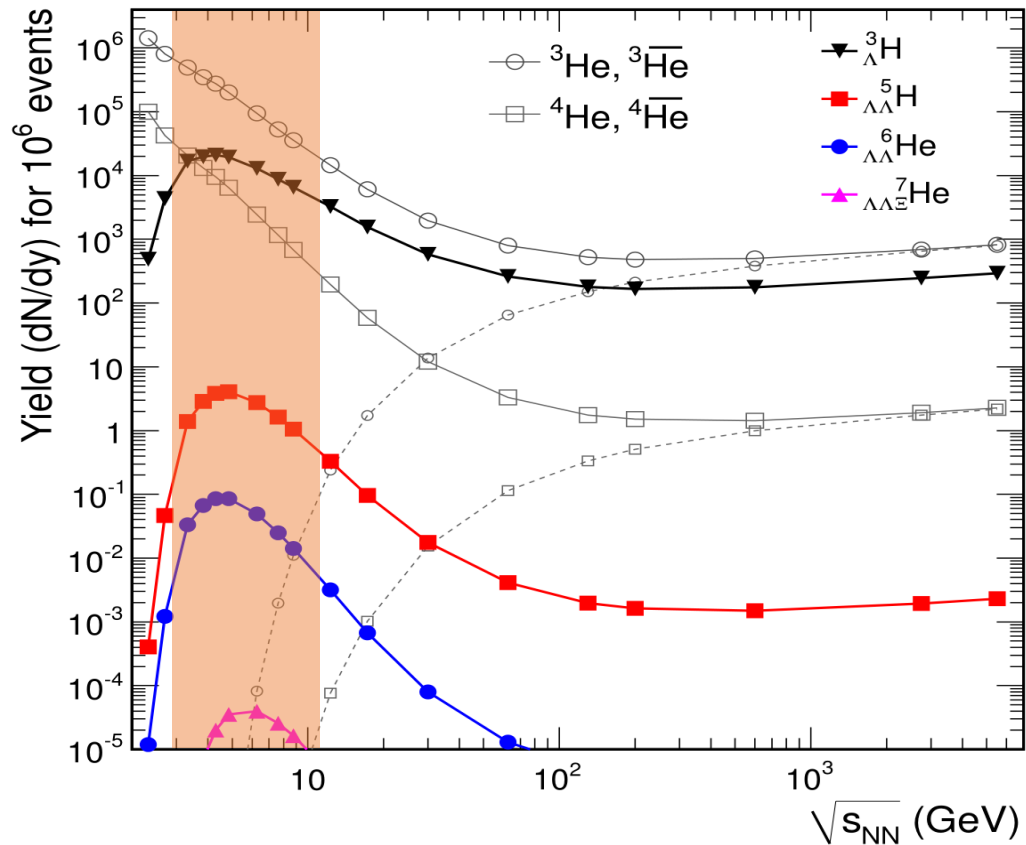
$$\mathcal{P}_{\Lambda H}^3 \approx (1 - \langle\delta\mathcal{P}_n\delta\mathcal{P}_p\rangle - \langle\delta\mathcal{P}_p\delta\mathcal{P}_\Lambda\rangle - \langle\delta\mathcal{P}_n\delta\mathcal{P}_\Lambda\rangle)\langle\mathcal{P}_\Lambda\rangle.$$

This result suggests that it is possible to extract the information on the spin-spin correlations among nucleons and Λ hyperons from the measurement of hypertriton polarization in heavy-ion collisions, although it is non-trivial in practice.

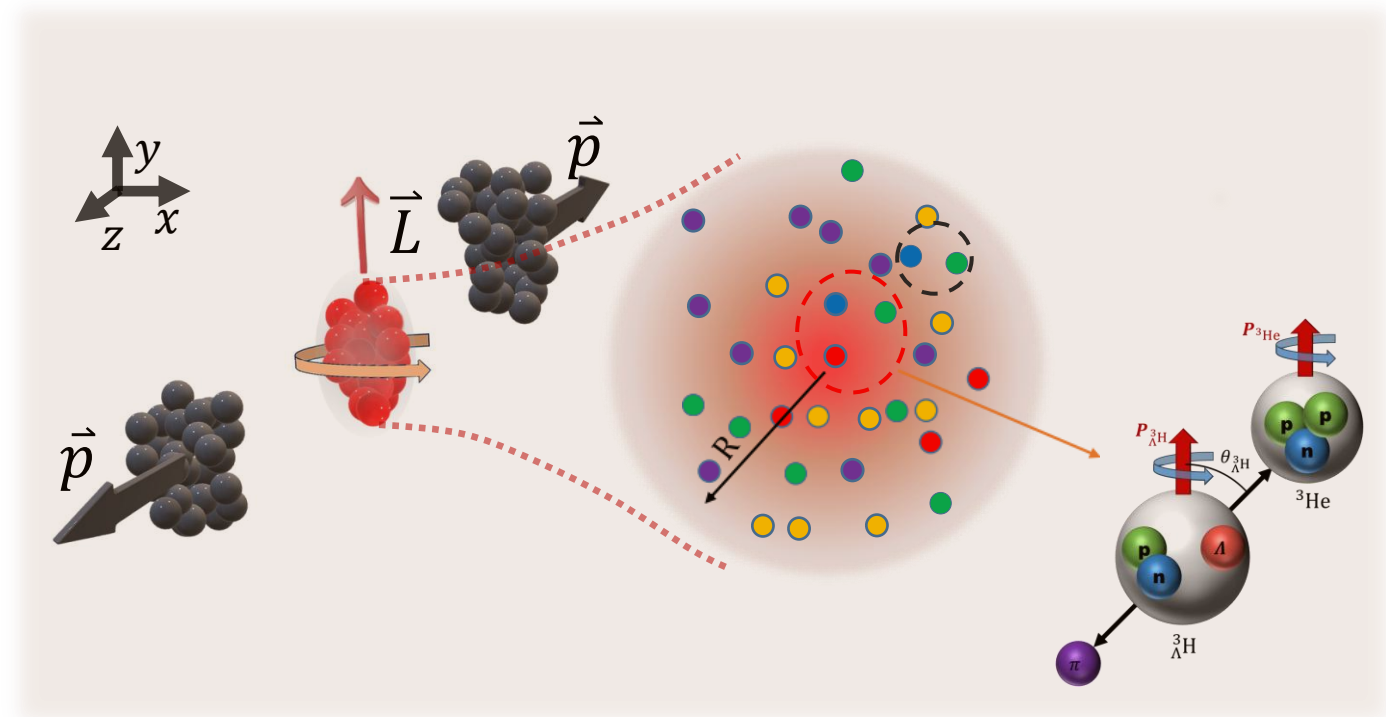
1. (Anti-)hypertriton is globally polarized in non-central heavy-ion collisions.
2. (Anti-)hypertriton polarization and its decay pattern provide a novel method to uniquely determine the spin structure of its wavefunction.



A. Andronic et al., Phys. Lett. B 697, 203-207 (2011)



- FAIR/CBM (2.4-4.9 GeV)
- HIAF/CEE (2.1-4.5 GeV)
- NICA/MPD (4-11 GeV)



A novel tool to study the evolution of strongly-interacting matter at high-baryon density region

Backup

3. (Anti-)hypertriton polarization and its spin structure

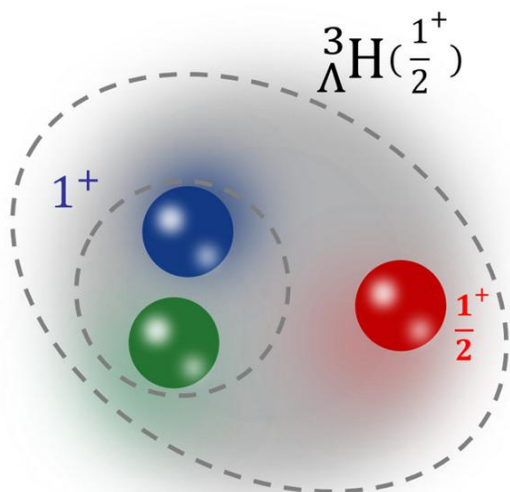
(8)

Parity-violating weak decay:

$$T(\Lambda \rightarrow \pi^- + p) = \frac{1}{\sqrt{4\pi}} \begin{pmatrix} T_s + T_p \cos \theta_p^* & T_p \sin \theta_p^* e^{i\phi_p^*} \\ T_p \sin \theta_p^* e^{-i\phi_p^*} & T_s - T_p \cos \theta_p^* \end{pmatrix}$$

$$T({}^3_\Lambda\text{H} \rightarrow \pi^- + {}^3\text{He})$$

$$= \frac{F}{6\sqrt{\pi}} \begin{pmatrix} 3T_s - T_p \cos \theta^* & -T_p \sin \theta^* e^{i\phi^*} \\ -T_p \sin \theta^* e^{-i\phi^*} & 3T_s + T_p \cos \theta^* \end{pmatrix}$$



The normalized angular distribution of the ${}^3\text{He}$ in the decay ${}^3_\Lambda\text{H} \rightarrow \pi^- + {}^3\text{He}$ is given by

$$\frac{dN}{d \cos \theta^*} = \text{Tr}[T^+ \hat{\rho} T] = \frac{1}{2} (1 + \alpha_{{}^3_\Lambda\text{H}} \mathcal{P}_{{}^3_\Lambda\text{H}} \cos \theta^*), \quad (7)$$

in terms of the hypertriton decay parameter $\alpha_{{}^3_\Lambda\text{H}} \approx -\frac{1}{3T_s^2 + \frac{1}{3}T_p^2} \alpha_\Lambda \approx -\frac{1}{2.58} \alpha_\Lambda$. The angular distribution of ${}^3\text{He}$ in the decay ${}^3_\Lambda\text{H} \rightarrow \pi^- + {}^3\text{He}$ can thus be further expressed as

$$\frac{dN}{d \cos \theta^*} \approx \frac{1}{2} \left(1 - \frac{1}{2.58} \alpha_\Lambda \mathcal{P}_\Lambda \cos \theta^* \right). \quad (8)$$

Compared to the angular distribution of the proton in the Λ decay, which has the form

Sign flip !

$$\frac{dN}{d \cos \theta_p^*} = \frac{1}{2} (1 + \alpha_\Lambda \mathcal{P}_\Lambda \cos \theta_p^*), \quad (9)$$

the ${}^3\text{He}$ in ${}^3_\Lambda\text{H}$ decay has an opposite sign in its angular dependence.

4. Effects of baryon spin correlation

(17)

Z. T. Liang, Chirality 2023

$$\left. \begin{aligned} \left| \rho_{00}^V - \frac{1}{3} \right| \gg P_\Lambda^2 \sim P_q^2 \\ \rho_{00}^V - \frac{1}{3} \sim \langle P_q P_{\bar{q}} \rangle \end{aligned} \right\} \text{The STAR data show that: } \langle P_q P_{\bar{q}} \rangle \neq \langle P_q \rangle \langle P_{\bar{q}} \rangle \quad \langle P_q P_{\bar{q}} \rangle \gg \langle P_q \rangle \langle P_{\bar{q}} \rangle$$

By studying P_H , we study the **average** of quark polarization P_q ;
by studying ρ_{00}^V , we study the **correlation** between P_q and $P_{\bar{q}}$.

How to separate long range or local correlations

$$C_{NN}^{H_i \bar{H}_j} \equiv \frac{N_{H_i \bar{H}_j}^{\uparrow\uparrow} + N_{H_i \bar{H}_j}^{\downarrow\downarrow} - N_{H_i \bar{H}_j}^{\uparrow\downarrow} - N_{H_i \bar{H}_j}^{\downarrow\uparrow}}{N_{H_i \bar{H}_j}^{\uparrow\uparrow} + N_{H_i \bar{H}_j}^{\downarrow\downarrow} + N_{H_i \bar{H}_j}^{\uparrow\downarrow} + N_{H_i \bar{H}_j}^{\downarrow\uparrow}}$$

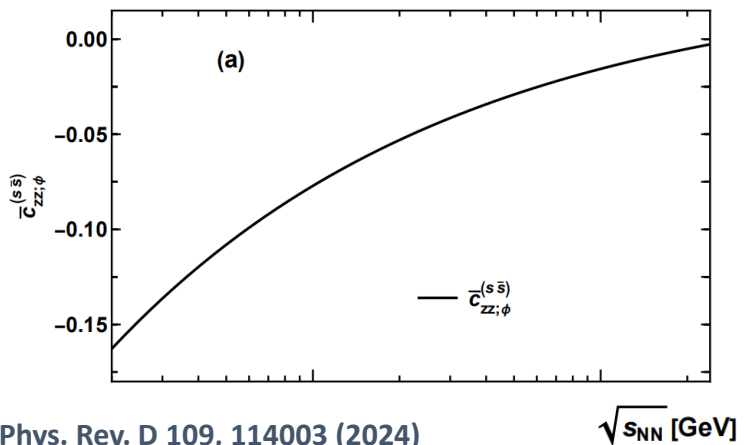
$$\begin{aligned} \rho_{10}^V &= \frac{P_{qz}(1+P_{\bar{q}y}) + (1+P_{qy})P_{\bar{q}z} - iP_{qx}(1+P_{\bar{q}y}) - i(1+P_{qy})P_{\bar{q}x}}{\sqrt{2}(3+\vec{P}_q \cdot \vec{P}_{\bar{q}})} \\ \rho_{0-1}^V &= \frac{P_{qz}(1-P_{\bar{q}y}) + (1-P_{qy})P_{\bar{q}z} - iP_{qx}(1-P_{\bar{q}y}) - i(1-P_{qy})P_{\bar{q}x}}{\sqrt{2}(3+\vec{P}_q \cdot \vec{P}_{\bar{q}})} \\ \rho_{1-1}^V &= \frac{P_{qz}P_{\bar{q}z} - P_{qx}P_{\bar{q}x} + i(P_{qx}P_{\bar{q}y} + P_{qy}P_{\bar{q}x})}{3+\vec{P}_q \cdot \vec{P}_{\bar{q}}} \end{aligned}$$

sensitive to the long range correlation

They should be sensitive to the local correlations.

Global quark spin correlations in relativistic heavy ion collisions

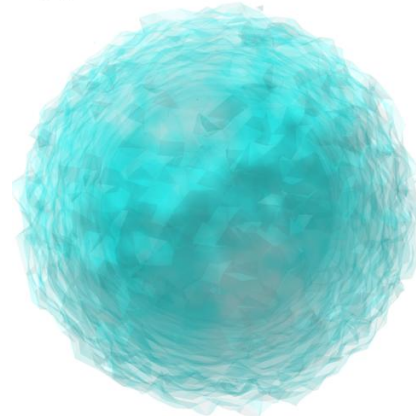
Ji-peng Lv,^{1,*} Zi-han Yu,^{1,†} Zuo-tang Liang,^{1,‡} Qun Wang,^{2,3,§} and Xin-Nian Wang^{4,¶}



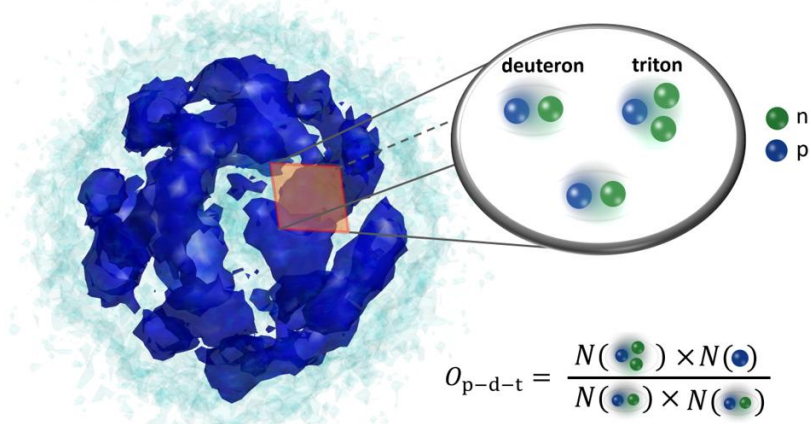
J. P. Lv et al., Phys. Rev. D 109, 114003 (2024)

C. M. Ko, NST 34, 80 (2023).

(a) Crossover



(b) First-order



$$O_{p-d-t} = \frac{N(\text{deuteron}) \times N(\text{triton})}{N(\text{neutron}) \times N(\text{proton})}$$

$$\begin{aligned} N_d &\approx N_d^{(0)}(1 + C_{np}) + \frac{3}{2^{1/2}} \left(\frac{2\pi}{mT} \right)^{3/2} \\ &\times \int d^3\mathbf{x}_1 d^3\mathbf{x}_2 C_2(\mathbf{x}_1, \mathbf{x}_2) \frac{e^{-\frac{(\mathbf{x}_1 - \mathbf{x}_2)^2}{2\sigma_d^2}}}{(2\pi\sigma_d^2)^{3/2}} \\ N_t &\approx \frac{3^{3/2}}{4} \left(\frac{2\pi}{mT} \right)^3 \int d^3\mathbf{x}_1 d^3\mathbf{x}_2 d^3\mathbf{x}_3 \rho_{nnp}(\mathbf{x}_1, \mathbf{x}_2, \mathbf{x}_3) \\ &\times \frac{1}{3^{3/2}(\pi\sigma_t^2)^3} e^{-\frac{(\mathbf{x}_1 - \mathbf{x}_2)^2}{2\sigma_t^2} - \frac{(\mathbf{x}_1 + \mathbf{x}_2 - 2\mathbf{x}_3)^2}{6\sigma_t^2}}, \end{aligned}$$

$$\begin{aligned} \rho_{nnp}(\mathbf{x}_1, \mathbf{x}_2, \mathbf{x}_3) &\approx \rho_n(\mathbf{x}_1)\rho_n(\mathbf{x}_2)\rho_p(\mathbf{x}_3) \\ &+ C_2(\mathbf{x}_1, \mathbf{x}_2)\rho_p(\mathbf{x}_3) + C_2(\mathbf{x}_2, \mathbf{x}_3)\rho_n(\mathbf{x}_1) \\ &+ C_2(\mathbf{x}_3, \mathbf{x}_1)\rho_n(\mathbf{x}_2) + C_3(\mathbf{x}_1, \mathbf{x}_2, \mathbf{x}_3) \end{aligned}$$

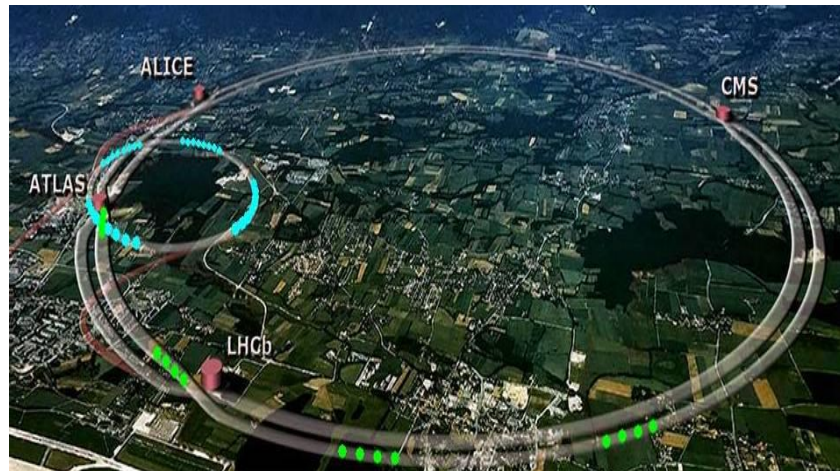
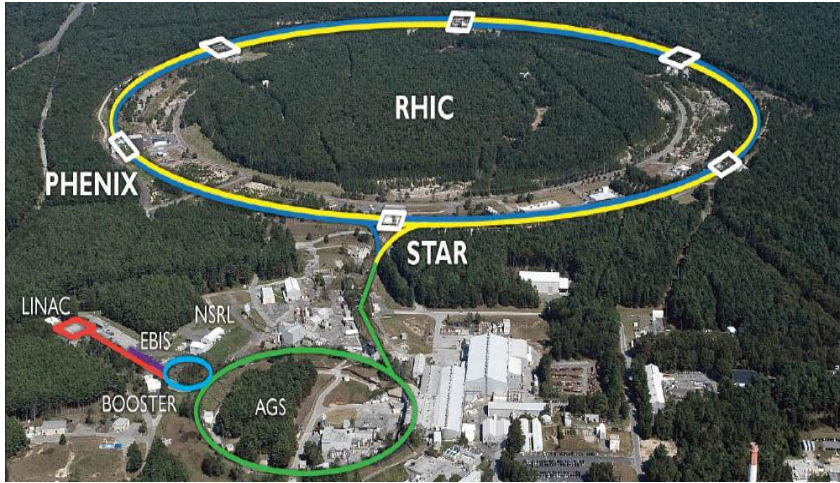
$$\rho_{np}(\mathbf{x}_1, \mathbf{x}_2) = \rho_n(\mathbf{x}_1)\rho_p(\mathbf{x}_2) + C_2(\mathbf{x}_1, \mathbf{x}_2)$$

$$\frac{N_t N_p}{N_d^2} \approx \frac{1}{2\sqrt{3}} \left[1 + \Delta\rho_n + \frac{\lambda}{\sigma} G\left(\frac{\xi}{\sigma}\right) \right]$$

K. J. Sun, L. W. Chen, C. M. Ko, and Z. Xu, Phys. Lett. B 774, 103 (2017);

K. J. Sun, C. M. Ko, and F. Li, PLB 816, 136258 (2021);

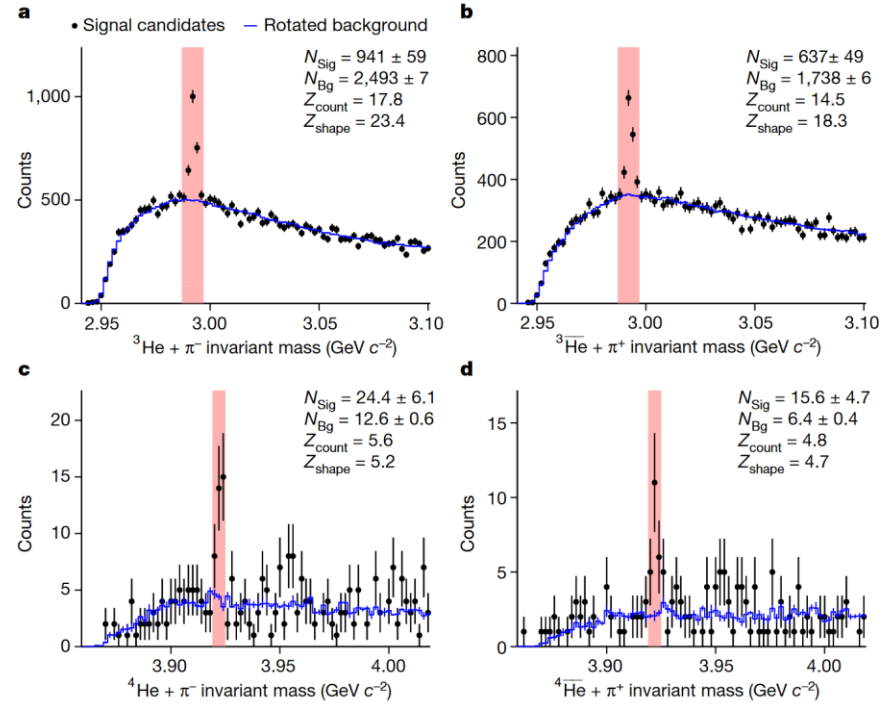
Antimatter factory



Observation of the antimatter hypernucleus $\bar{\Lambda}^4\bar{H}$

STAR Collaboration

Nature (2024) | [Cite this ar](#)



PHYSICAL REVIEW C **93**, 064909 (2016)

Antimatter $\bar{\Lambda}^4\bar{H}$ hypernucleus production and the $\bar{\Lambda}^3\bar{H}/\bar{\Lambda}^3\bar{He}$ puzzle in relativistic heavy-ion collisions

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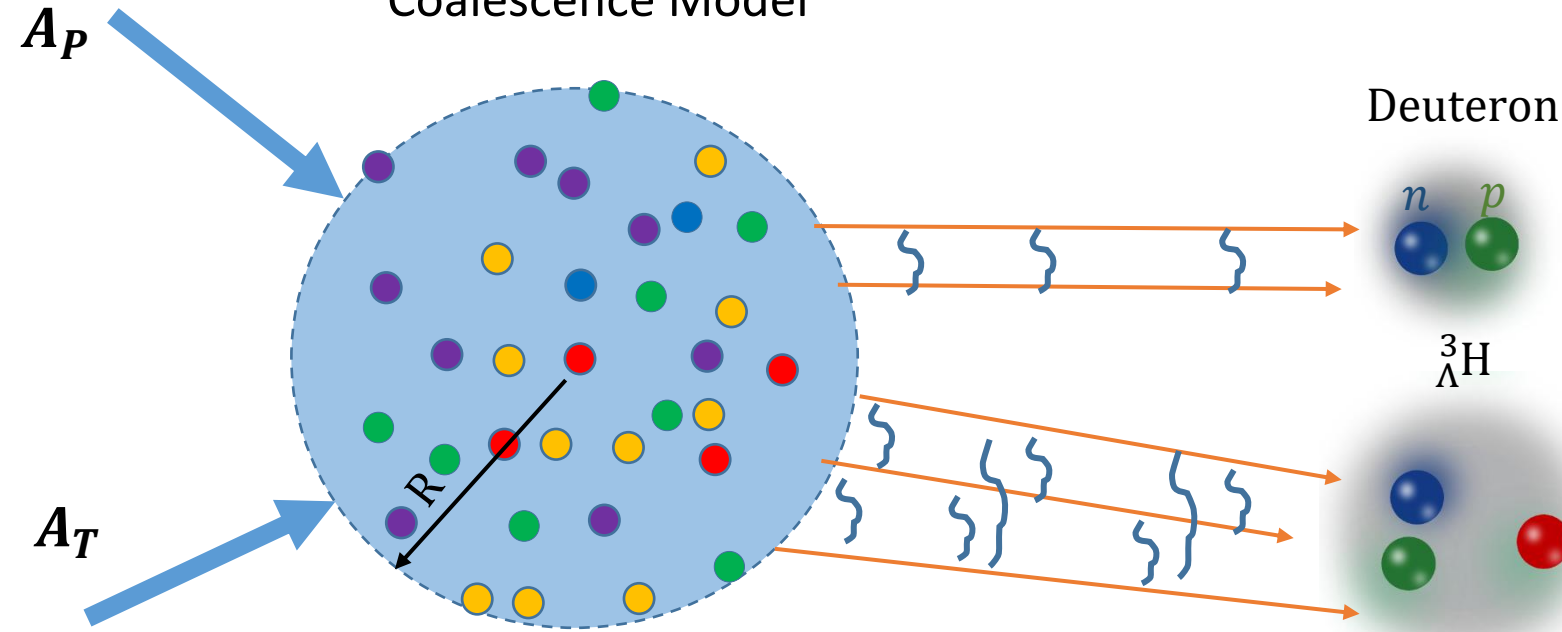
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(Received 26 April 2016; published 29 June 2016)

We show that the measured yield ratio $\bar{\Lambda}^3\bar{H}/\bar{\Lambda}^3\bar{He}$ ($\bar{\Lambda}^3\bar{H}/\bar{\Lambda}^3\bar{He}$) in Au + Au collisions at $\sqrt{s_{NN}} = 200$ GeV and in Pb + Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV can be understood within a covariant coalescence model if (anti-) Λ particles freeze out earlier than (anti-)nucleons but their relative freeze-out time is closer at $\sqrt{s_{NN}} = 2.76$ TeV than at $\sqrt{s_{NN}} = 200$ GeV. The earlier (anti-) Λ freeze-out can significantly enhance the yield of (anti)hypernucleus $\bar{\Lambda}^4\bar{H}$ ($\bar{\Lambda}^4\bar{H}$), leading to that $\bar{\Lambda}^4\bar{H}$ has a comparable abundance with $\bar{\Lambda}^4\bar{He}$ and thus provides an easily measured antimatter candidate heavier than $\bar{\Lambda}^4\bar{He}$. The future measurement on $\bar{\Lambda}^4\bar{H}$ ($\bar{\Lambda}^4\bar{H}$) would be very useful to understand the (anti-) Λ freeze-out dynamics and the production mechanism of (anti)hypernuclei in relativistic heavy-ion collisions.

Final-state coalescence

Coalescence Model



Density Matrix Formulation (sudden approximation)

$$N_A = \text{Tr}(\hat{\rho}_s \hat{\rho}_A)$$

$$= g_c \int d\Gamma \rho_s(\{x_i, p_i\}) \times W_A(\{x_i, p_i\})$$

Wigner function of light cluster

Overlap between source distribution function and Wigner function of light nuclei

Two-body coalescence $a + b \rightarrow c$:

$$N_c = \frac{2J_c + 1}{(2J_a + 1)(2J_b + 1)} \int \frac{dx_a dk_a}{(2\pi)^3} \frac{dx_b dk_b}{(2\pi)^3} f_a(x_a, k_a) f_b(x_b, k_b) W_c(x, k)$$

$$\approx \frac{2J_c + 1}{(2J_a + 1)(2J_b + 1)} \frac{N_a N_b}{\left(\frac{m_a m_b T}{m_a + m_b} (R_a^2 + R_b^2)\right)^{3/2}} \times \frac{1}{\left(1 + \frac{\sigma^2}{R_a^2 + R_b^2}\right)^{3/2}}$$

$$f_a = \frac{N_a}{(m_a T R_a^2)^{3/2}} e^{-\frac{k_a^2}{2m_a T} - \frac{x_a^2}{2R_a^2}}$$

$$W_c = 8e^{-x^2/\sigma^2 - \sigma^2 k^2}$$

$$N_a = \int \frac{dx_a dk_a}{(2\pi)^3} f_a(x_a, k_a) \quad 1 = \int \frac{dx dk}{(2\pi)^3} W_c(x, k)$$

“Quantum mechanical correction”

$$N_d \propto \frac{1}{\left[1 + \left(\frac{2r_d^2}{3R^2}\right)\right]^{3/2}}$$

Production Structure

$$N_{\Lambda^3\text{H}} \propto \frac{1}{\left[1 + \left(\frac{r_{\Lambda^3\text{H}}^2}{2R^2}\right)\right]^3}$$

can be inferred from Femtoscopy

