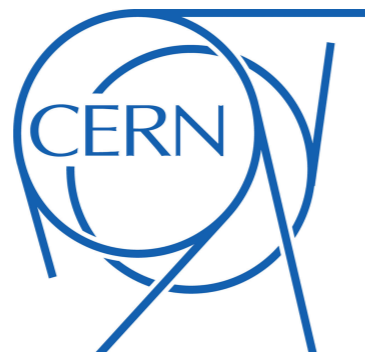


# Latest Time-dependent Measurements of $B$ decays at LHCb

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FIND论坛学术研讨会, USTC

2023-08-26



# Outline

- Time-dependent CP violation
- Flavour tagging at LHCb
- $\sin 2\beta$  measurements
- $\phi_s$  measurements
- $B_{(s)}^0 \rightarrow h^+h^-$  &  $\tau_{B_s^0}^{\text{effective}}$
- Prospects & summary

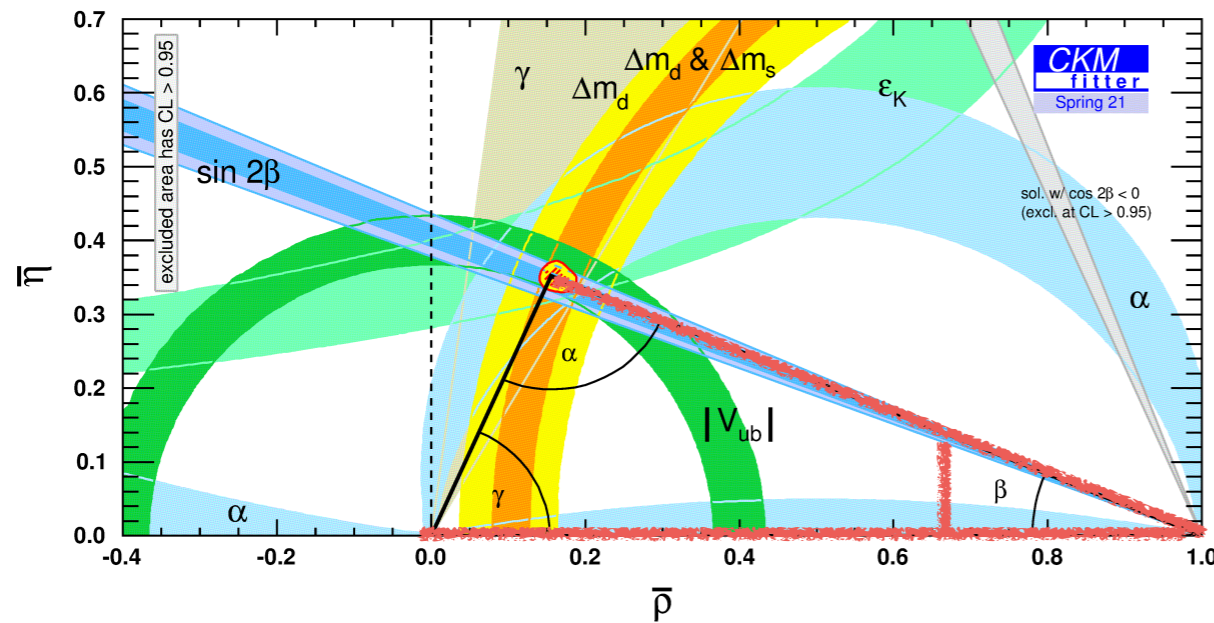


# CKM matrix

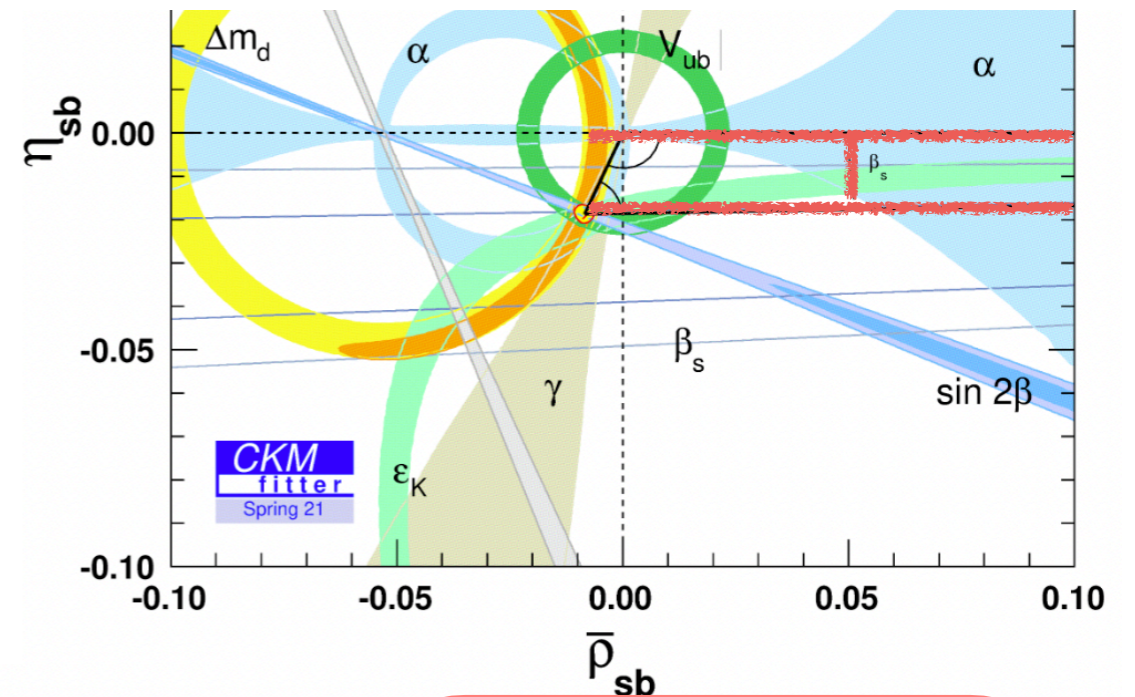
$$V_{CKM} = \begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}| e^{-i\gamma} \\ -|V_{cd}| & |V_{cs}| & |V_{cb}| \\ |V_{td}| e^{-i\beta} & -|V_{ts}| e^{i\beta_s} & |V_{tb}| \end{pmatrix} + \mathcal{O}(\lambda^5) \sim \begin{pmatrix} 1 & 0.2 & 0.004 \\ 0.2 & 1 & 0.04 \\ 0.008 & 0.04 & 1 \end{pmatrix}$$

- Key test of the SM: Verify unitarity of CKM matrix
  - Magnitudes: branching fractions or mixing frequencies
  - Phases: CP violation measurement

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$



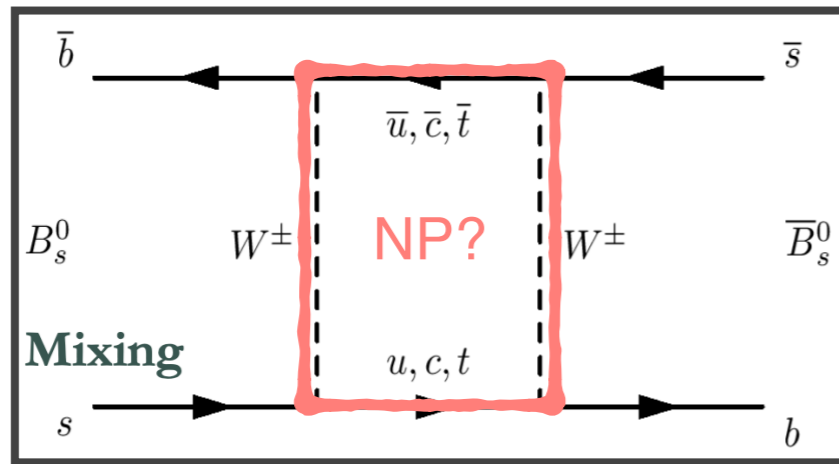
$$V_{us}V_{ub}^* + V_{cs}V_{cb}^* + V_{ts}V_{tb}^* = 0$$



$$\alpha = \arg\left(-\frac{V_{td}V_{tb}^*}{V_{ud}V_{ub}^*}\right), \beta = \arg\left(-\frac{V_{cd}V_{cb}^*}{V_{td}V_{tb}^*}\right), \gamma = \arg\left(-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}\right)$$

$$\phi_s^{SM} \approx -2\beta_s = 2\arg\left(-\frac{V_{cs}V_{cb}^*}{V_{ts}V_{tb}^*}\right)$$

# Opportunities for new physics



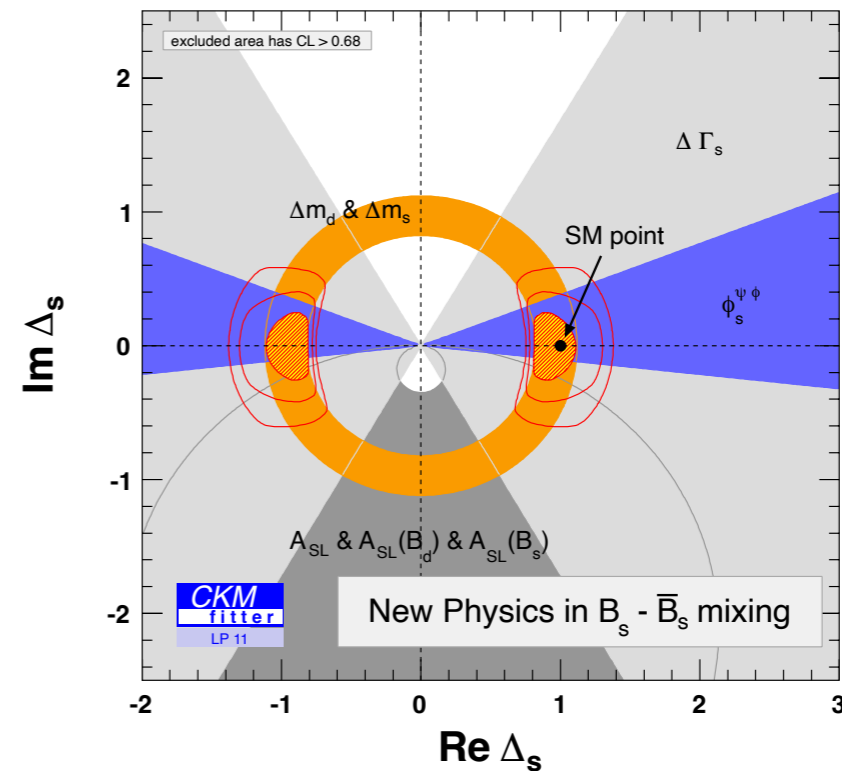
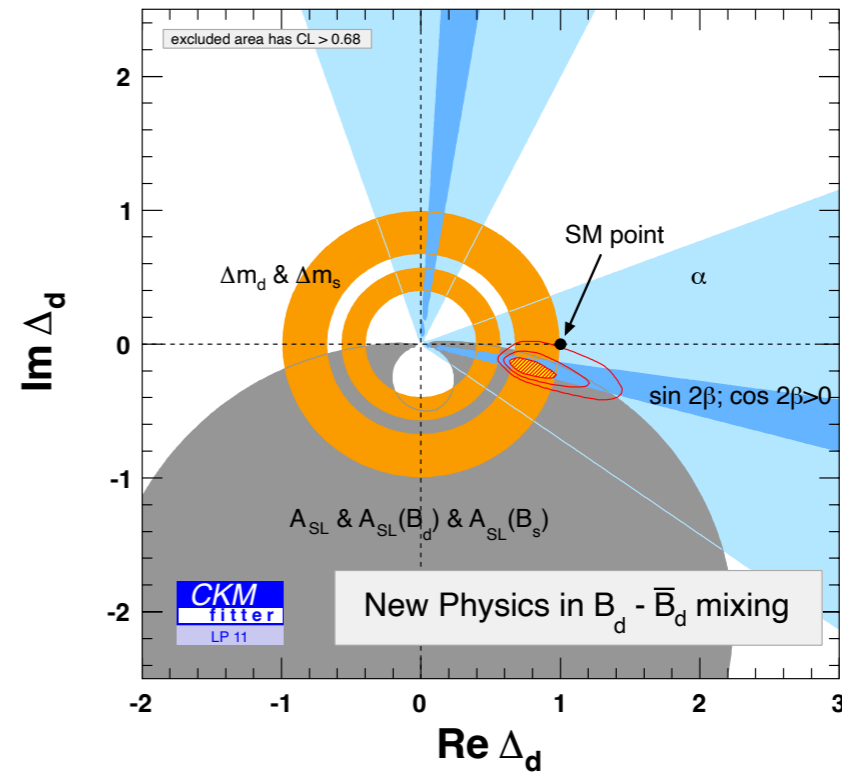
- New physics (NP) short-distance contributions can influence mixing

$$m_{12}^q = m_{12}^{SM,q} \cdot \Delta_q^{NP}$$

[PRD 86(2012)033008]

- Through B mixing, NP energy scales of up to 20 TeV for tree-level NP or 2 TeV for NP in loops can be probed

[PRD 89(2014)033016]





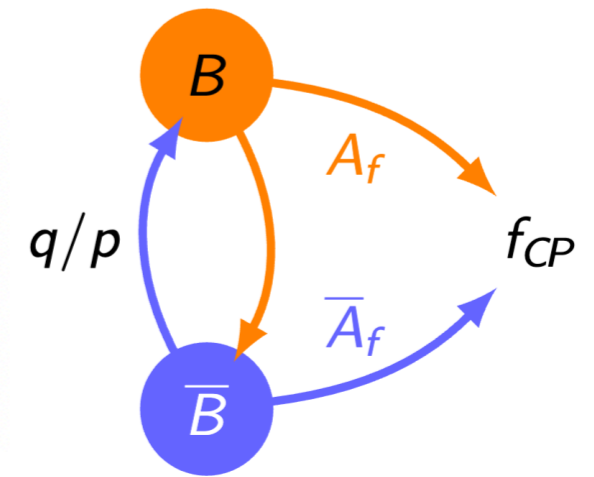
# Decay of neutral $B$ meson

- Decay rate of initial  $B$  or  $\bar{B}$

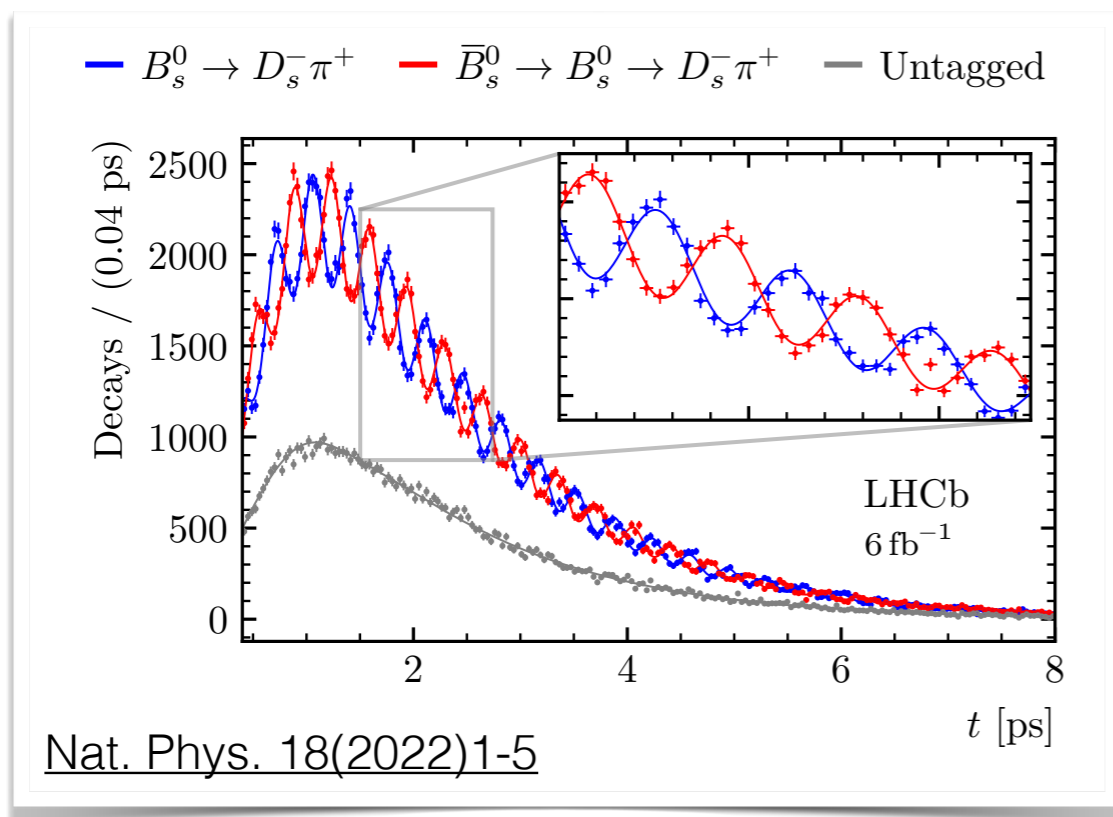
$$|\langle f | H | B \rangle|^2 = \frac{1}{2} e^{-\Gamma t} |A_f|^2 \left\{ D \cosh\left(\frac{\Delta\Gamma}{2} t\right) + A_{\Delta\Gamma} \sinh\left(\frac{\Delta\Gamma}{2} t\right) \pm C \cos(\Delta m t) \mp S \sin(\Delta m t) \right\}$$

direct  $CP$

$CP$  in interference of mixing & decay



- Mass difference  $\Delta m_{(s)} = M_H - M_L = 2 |M_{12}| \rightarrow$  oscillation frequency!
- Decay-width difference  $\Delta\Gamma_{(s)} = \Gamma_L - \Gamma_H = 2 |\Gamma_{12}| \cos\phi_{12}$



*require time-dependent measurements!*

- Benchmark for the flavor-tagged time-dependent measurement
- World-best measurement:

$$\Delta m_s = (17.7656 \pm 0.0057) \text{ ps}^{-1}$$

# Time-dependent $CP$ asymmetry

$$A_{CP}(t) = \frac{\Gamma_{\bar{B}_{(s)}^0 \rightarrow f}(t) - \Gamma_{B_{(s)}^0 \rightarrow f}(t)}{\Gamma_{\bar{B}_{(s)}^0 \rightarrow f}(t) + \Gamma_{B_{(s)}^0 \rightarrow f}(t)} = \frac{-C_f \cos(\Delta m_{d(s)} t) + S_f \sin(\Delta m_{d(s)} t)}{\cosh\left(\frac{\Delta\Gamma_{d(s)}}{2} t\right) + A_f^{\Delta\Gamma} \sinh\left(\frac{\Delta\Gamma_{d(s)}}{2} t\right)}$$

$$C_f \equiv \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2}, \quad S_f \equiv \frac{2\text{Im}\lambda_f}{1 + |\lambda_f|^2}, \quad A_f^{\Delta\Gamma} \equiv -\frac{2\text{Re}\lambda_f}{1 + |\lambda_f|^2}$$

- CPV in decay or mixing if  $|\lambda_f| \neq 1$
- For  $b \rightarrow c\bar{c}q$  transition,  $S_f \approx \sin 2\beta_{(s)}$

$$\lambda_f \equiv \frac{q}{p} \frac{\bar{A}_f}{A_f}$$

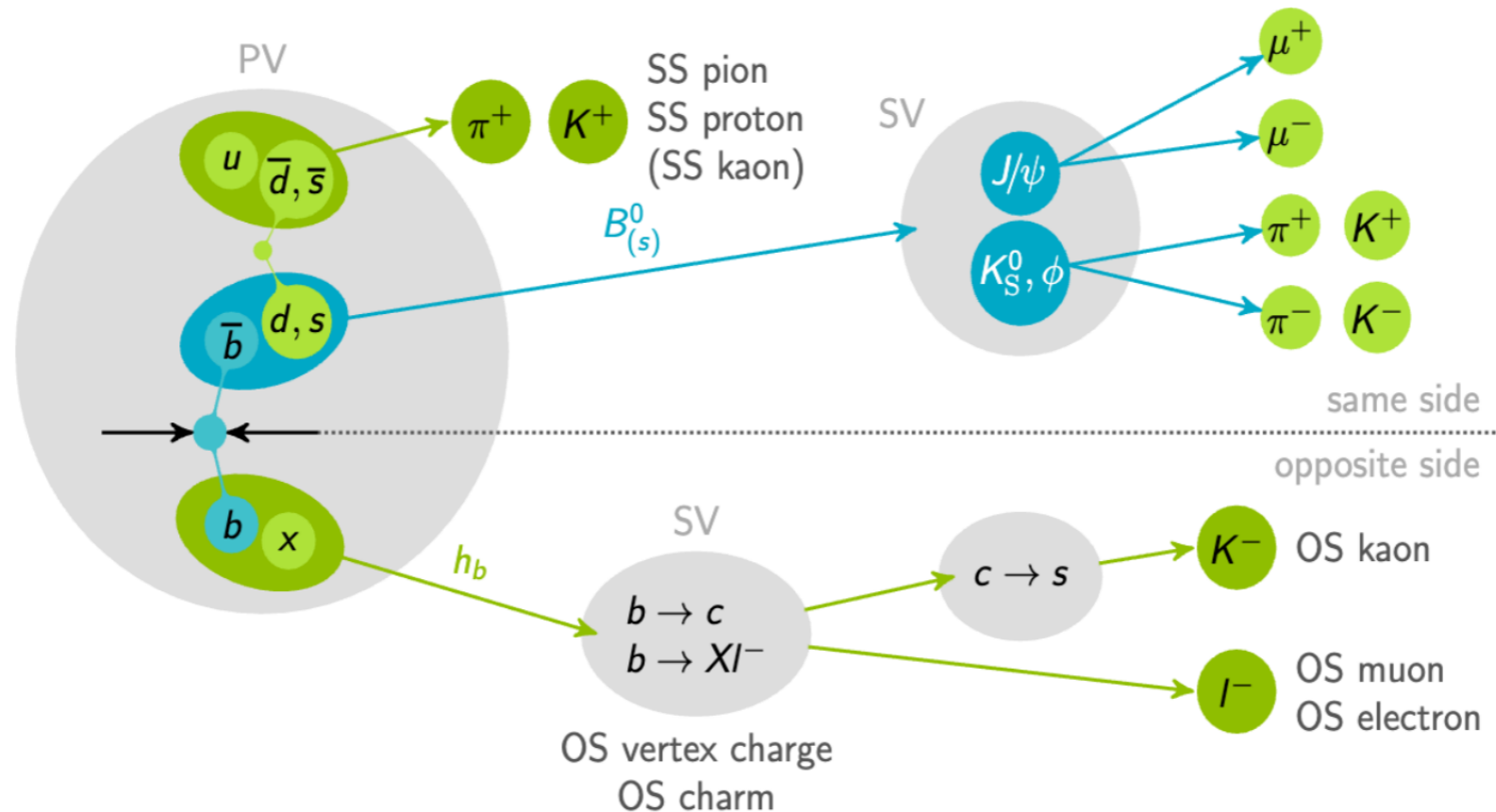
## → Experimentally

$$A_{CP}(t) \propto e^{-\frac{1}{2}\Delta m_s^2 \sigma_t^2} \cdot (1 - 2\omega) \cdot (C_f \cos(\Delta m_{(s)} t) + \eta_f S_f \sin(\Delta m_{(s)} t))$$

- Flavour tagging of  $B_{(s)}^0$  at production: probability of wrong tag  $\omega$
- Excellent decay-time resolution (vertex resolution)
- $CP$  eigenvalue of the final state  $\eta_f$

# Flavour tagging

$$\mathcal{A}^{CP} = \frac{\Gamma(\bar{B}_{(s)}^0 \rightarrow f_{CP}) - \Gamma(B_{(s)}^0 \rightarrow f_{CP})}{\Gamma(\bar{B}_{(s)}^0 \rightarrow f_{CP}) + \Gamma(B_{(s)}^0 \rightarrow f_{CP})}$$



- Same-side (SS) tagging: Use charge of  $K/\pi$  produced in the fragmentation
- Opposite-side (OS) tagging: charge of leptons or hadrons from the other  $b$  hadrons

Tagging power	$B^0 \rightarrow \psi K_S^0$	$B_s^0 \rightarrow J/\psi KK$	$B_s^0 \rightarrow \phi\phi$
$\epsilon_{\text{tag}}(1 - 2\omega)^2$	(4-6)%	4.3%	6%

\* tagging efficiency  $\epsilon_{\text{tag}}$ , mistag rate  $\omega$

# Decay-time resolution

- Decay time resolution dilutes oscillations,  $\mathcal{D} = \exp(-\frac{1}{2}\sigma_{\text{eff}}^2\Delta m_s^2)$
- Significant for  $B_s^0$  system, negligible for  $B^0$

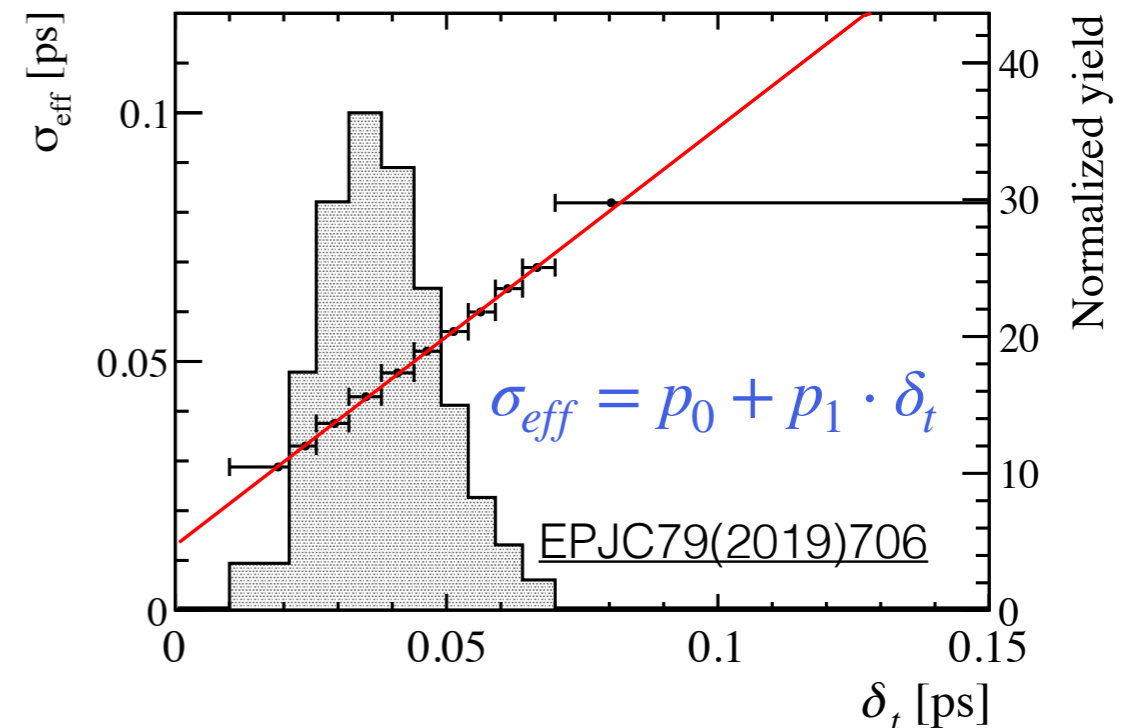
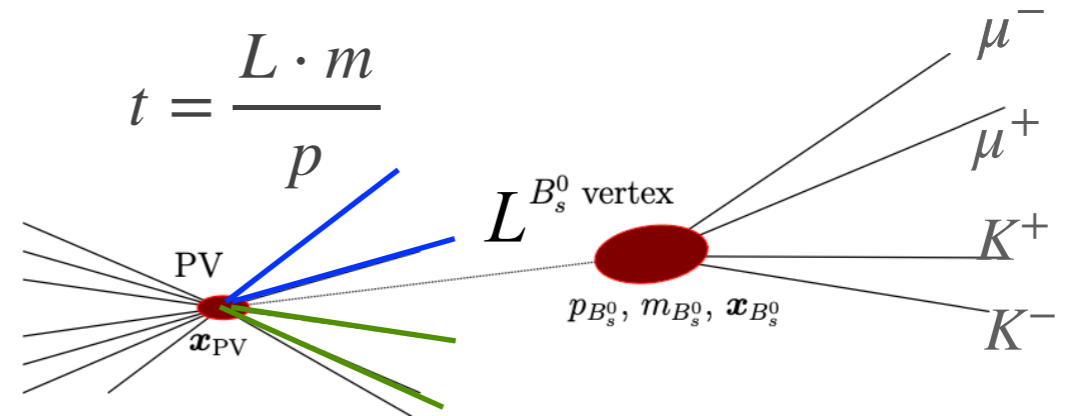
- $B^0 \rightarrow \psi K_S^0$ :  $\sigma_{MC} \sim 60$  fs
- $B_s^0 \rightarrow J/\psi KK$  &  $B_s^0 \rightarrow \phi\phi$

$$\delta_t^2 = \left(\frac{m}{p}\right)^2 \sigma_L^2 + \left(\frac{t}{p}\right)^2 \sigma_p^2$$

$\downarrow$                        $\downarrow$   
 $\sim 200 \mu\text{m}$            $\sigma_p/p \sim 0.4\%$

✓ Effective Gaussian resolution model:  
 $\sigma_{\text{eff}}$  as a function of per-event  $\delta_t$  (11 bins)

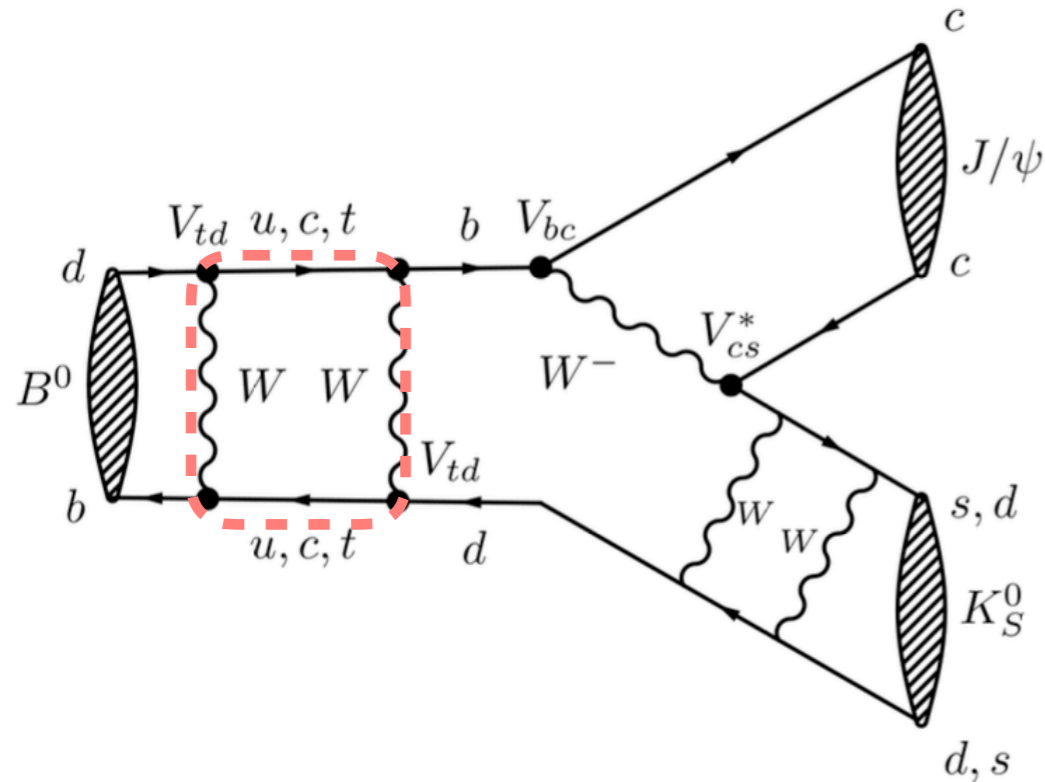
$$\sigma_{\text{eff}} \sim 42(3) \text{ fs} \rightarrow \mathcal{D} = 0.757$$





# $\sin 2\beta$ in $B^0 \rightarrow \psi K_S^0$

- Tree diagram dominated: NP in mixing
- Three decay modes in  $B^0 \rightarrow \psi K_S^0$  (*CP-odd only*)



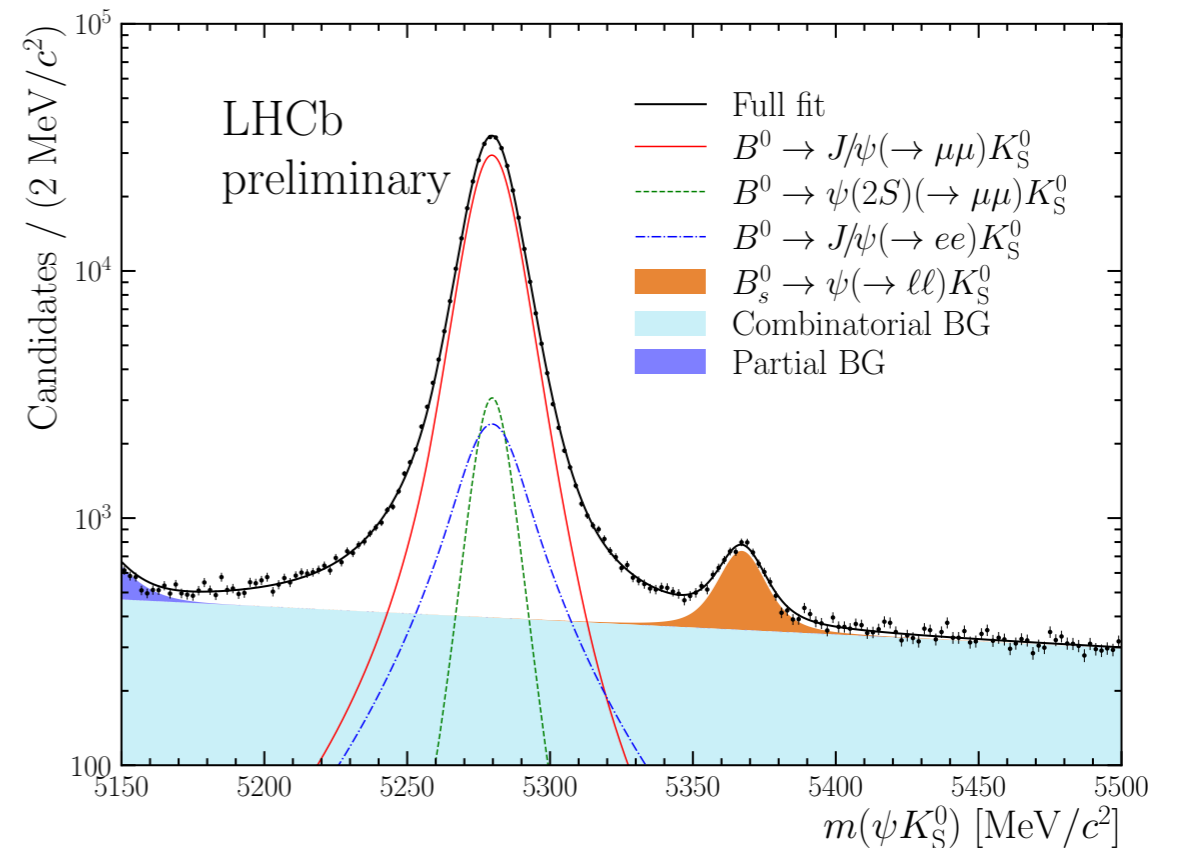
- $B^0 \rightarrow J/\psi(\mu^+\mu^-)K_S^0$  (85%)
- $B^0 \rightarrow J/\psi(e^+e^-)K_S^0$  (12%)
- $B^0 \rightarrow \psi(2S)(\mu^+\mu^-)K_S^0$  (6%)

sWeight from Mass fit to subtract background

$$N_{J/\psi(\rightarrow\mu\mu)K_S^0} = 306\,322 \pm 619$$

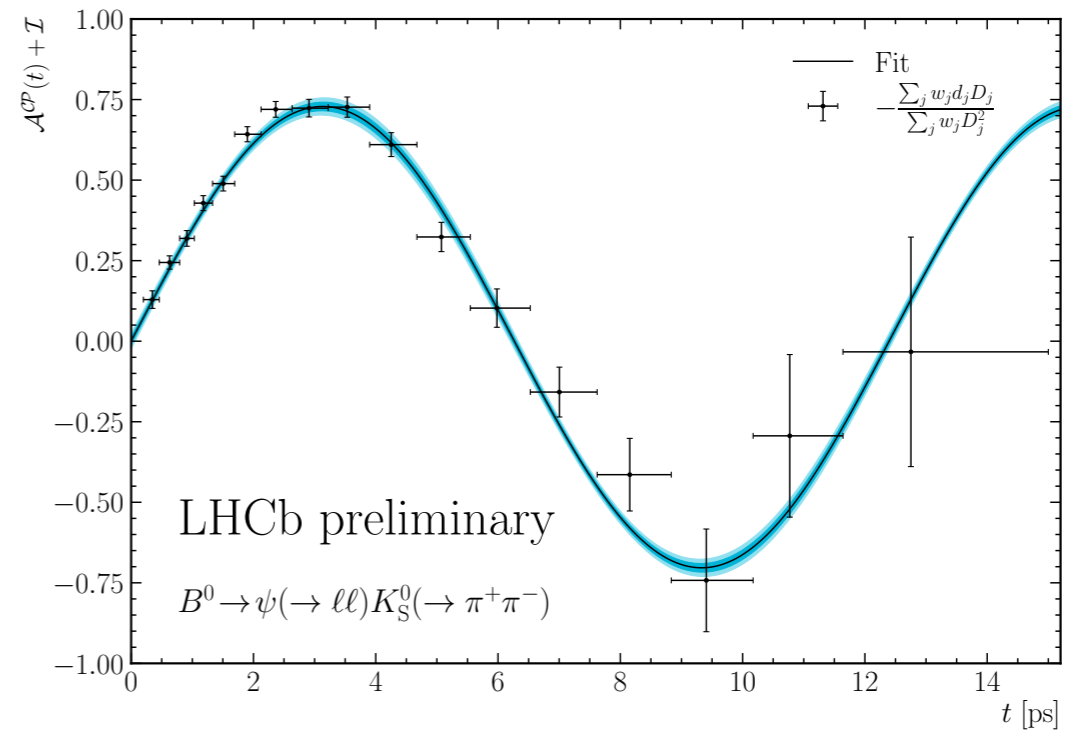
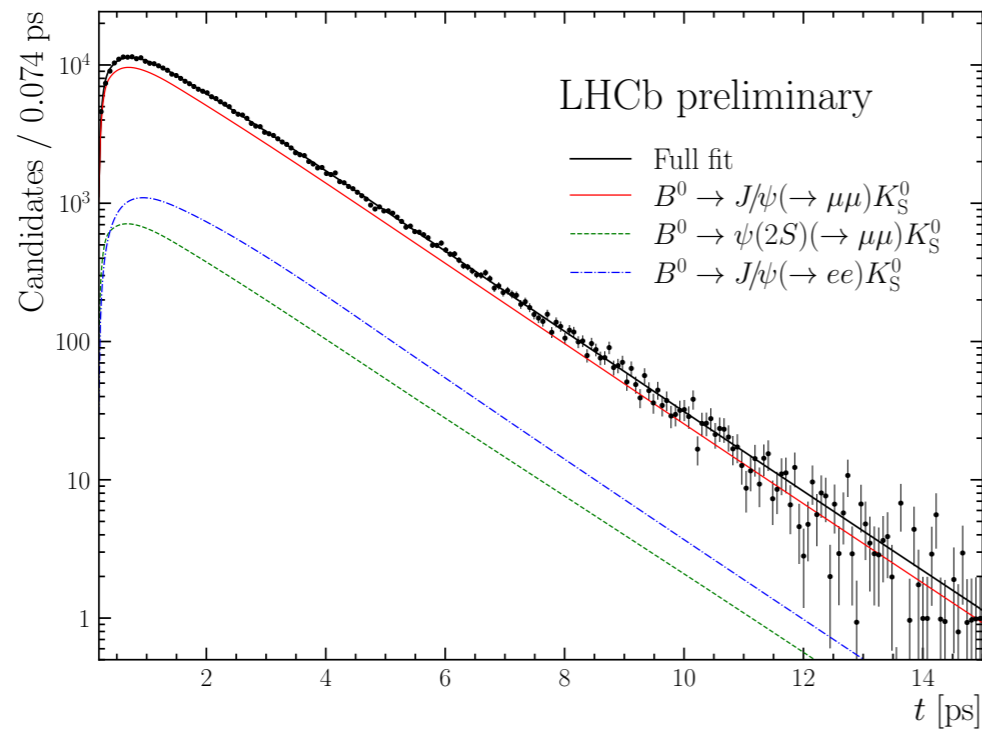
$$N_{J/\psi(\rightarrow ee)K_S^0} = 42\,870 \pm 269$$

$$N_{\psi(2S)(\rightarrow\mu\mu)K_S^0} = 23\,570 \pm 164$$



# $\sin 2\beta$ in $B^0 \rightarrow \psi K_S^0$

- Simultaneous fits to the decay time of  $B^0$

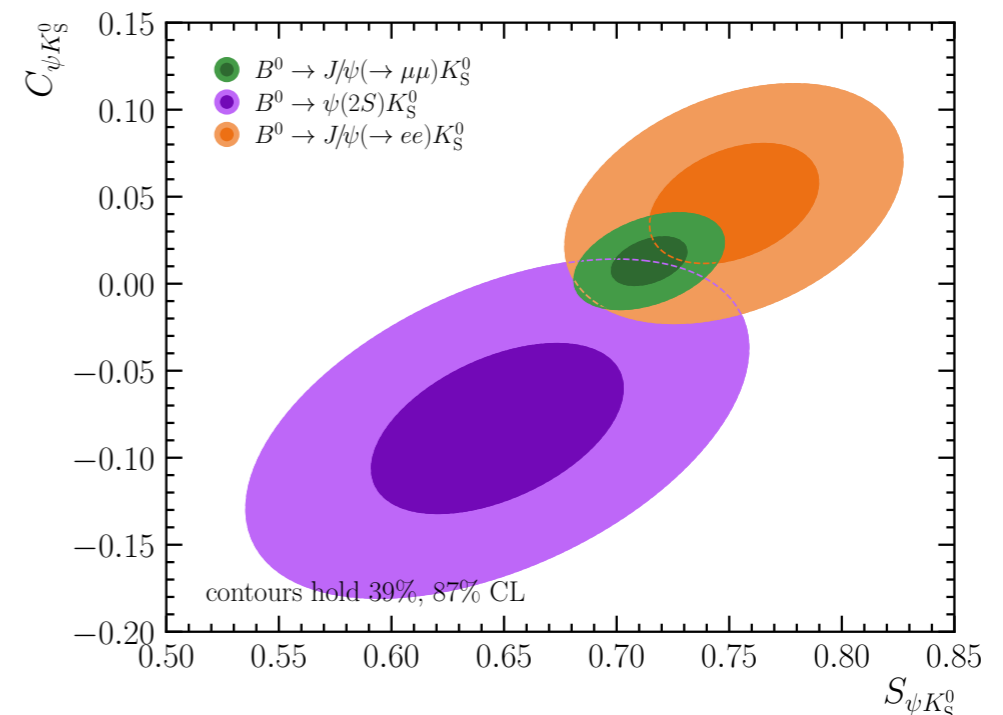


## Combined fit result

$$S_{\psi K_S^0}^{\text{Run 2}} = 0.716 \pm 0.013 (\text{stat}) \pm 0.008 (\text{syst})$$

$$C_{\psi K_S^0}^{\text{Run 2}} = 0.012 \pm 0.012 (\text{stat}) \pm 0.003 (\text{syst})$$

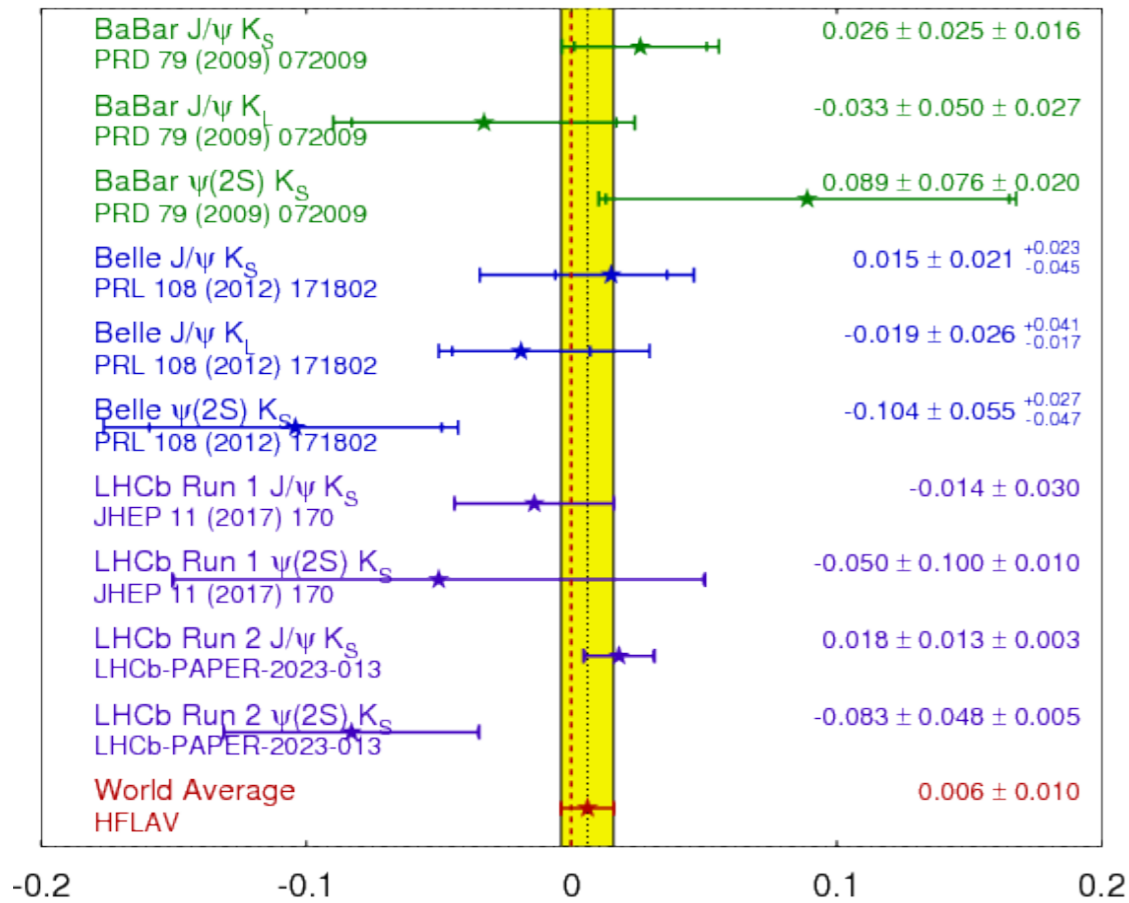
- The **most precise measurement** in single measurement to date



# $\sin 2\beta$ combinations

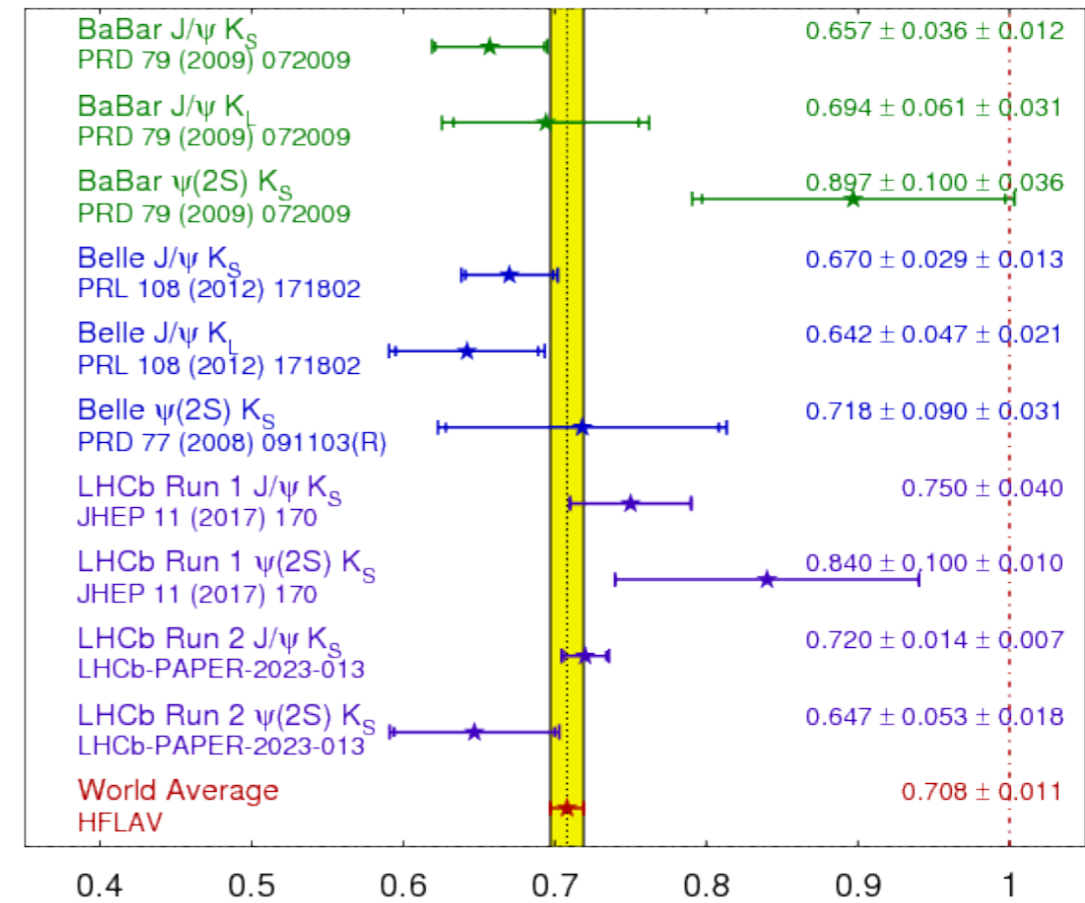
$b \rightarrow ccs$   $C_{CP}$

**HFLAV**  
Summer 2023  
PRELIMINARY



$\sin(2\beta) \equiv \sin(2\phi_1)$

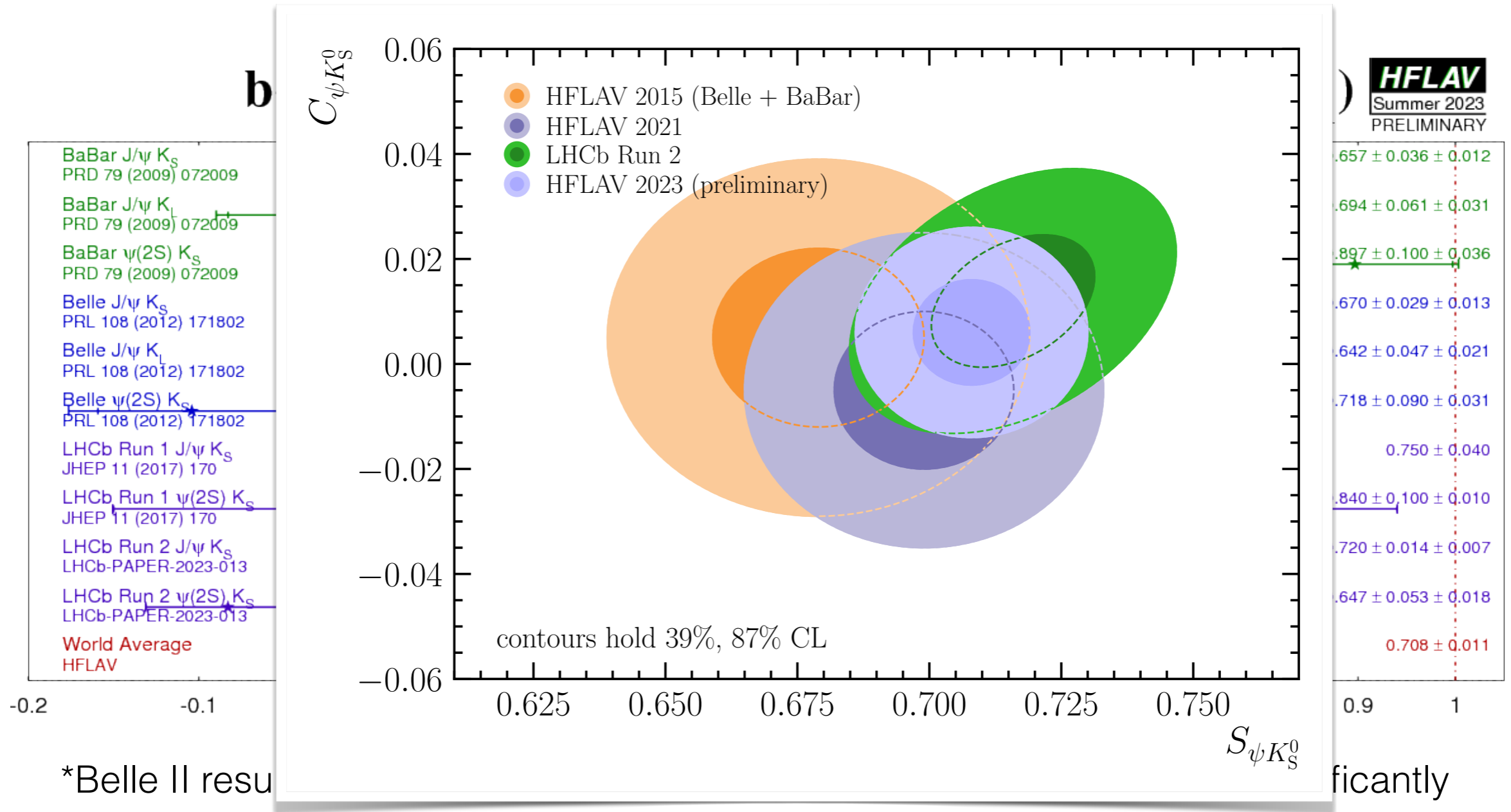
**HFLAV**  
Summer 2023  
PRELIMINARY



\*Belle II results is not included, which should not affect the current WA significantly

- Consistent with other measurements, still statistical uncertainty limited
- **LHCb results dominate the latest World Average**

# sin 2β combinations



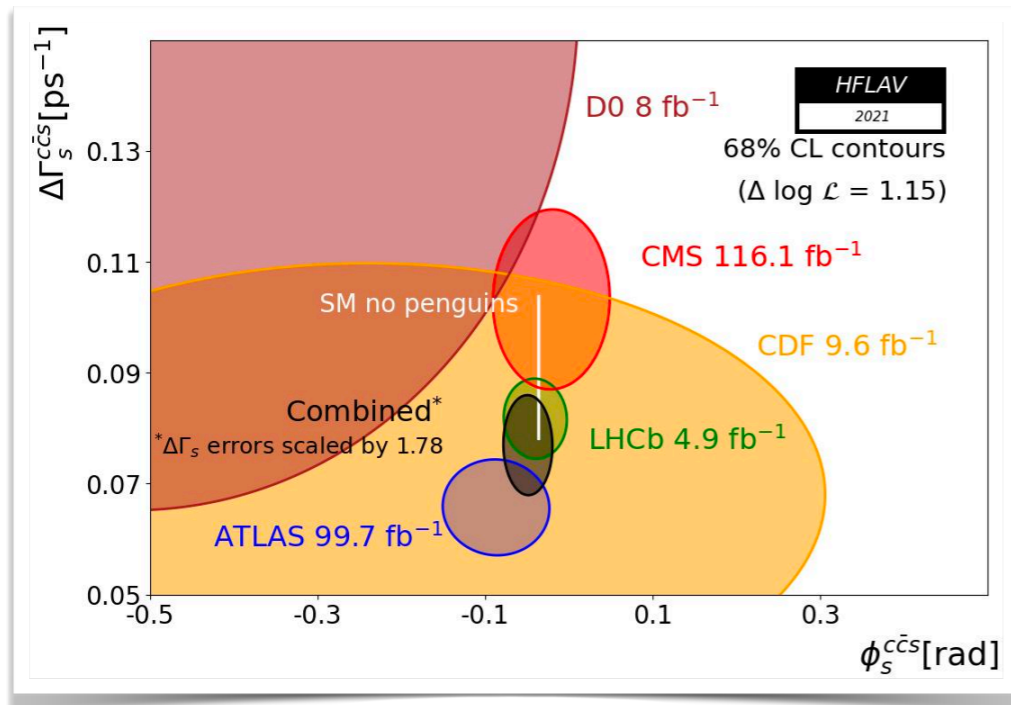
- Consistent with other measurements, still statistical uncertainty limited
- **LHCb results dominate the latest World Average**



# $\phi_s$ in $B_s^0 \rightarrow J/\psi\phi(KK)$

arXiv: 2308.01468  
submitted to PRL

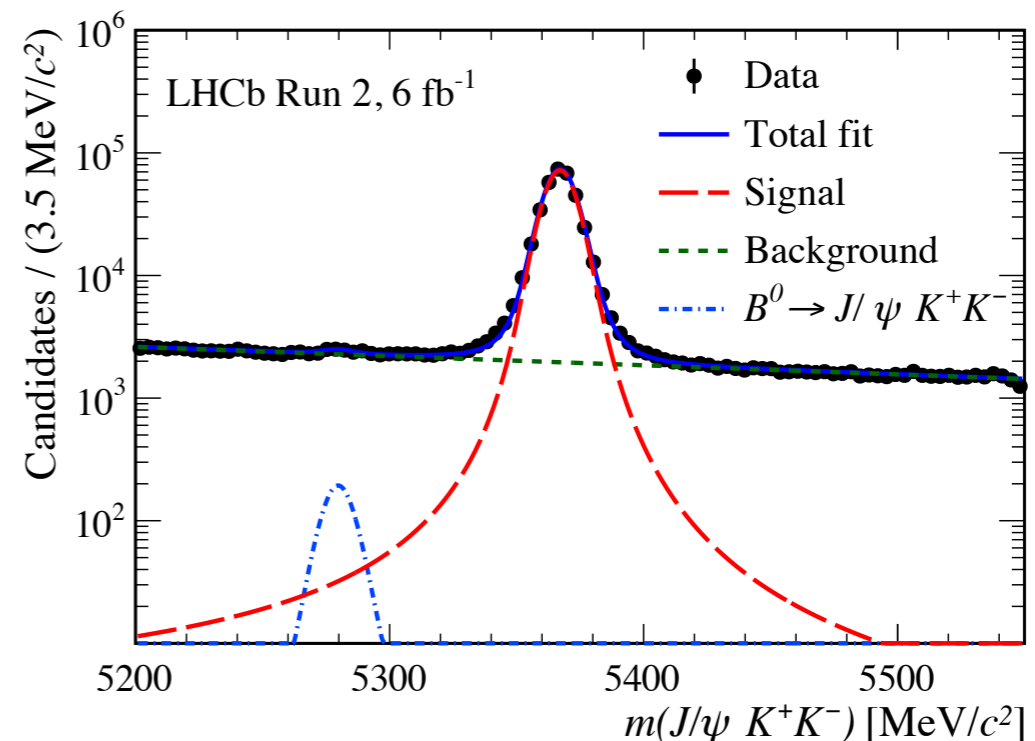
- Golden model to measure  $\phi_s : b \rightarrow c\bar{c}s$  transition process  $B_s^0 \rightarrow J/\psi\phi(KK)$
- Sensitive to New Physics, small contribution could be clearly visible



- $-\beta_s^{\text{SM}} = -0.0368^{+0.0009}_{-0.0006}$  rad
- 2022 world average:  
 $\phi_s^{c\bar{c}s, \text{WA}} = (-0.049 \pm 0.019)$  rad
- Tension between  $\Delta\Gamma_s$  measurements from different experiments

sWeight from Mass fit to subtract background

Total signal candidates  $\sim 349000$

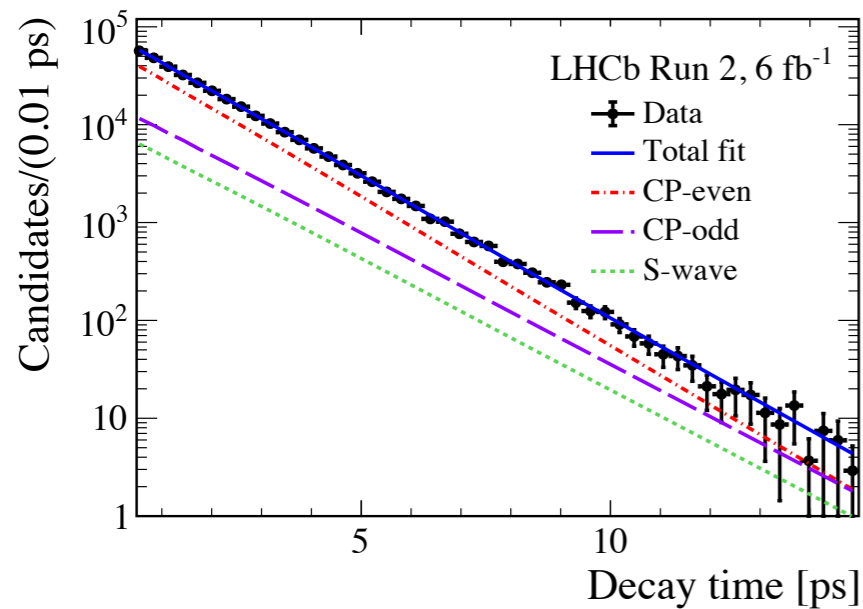


# $\phi_s$ in $B_s^0 \rightarrow J/\psi\phi(KK)$

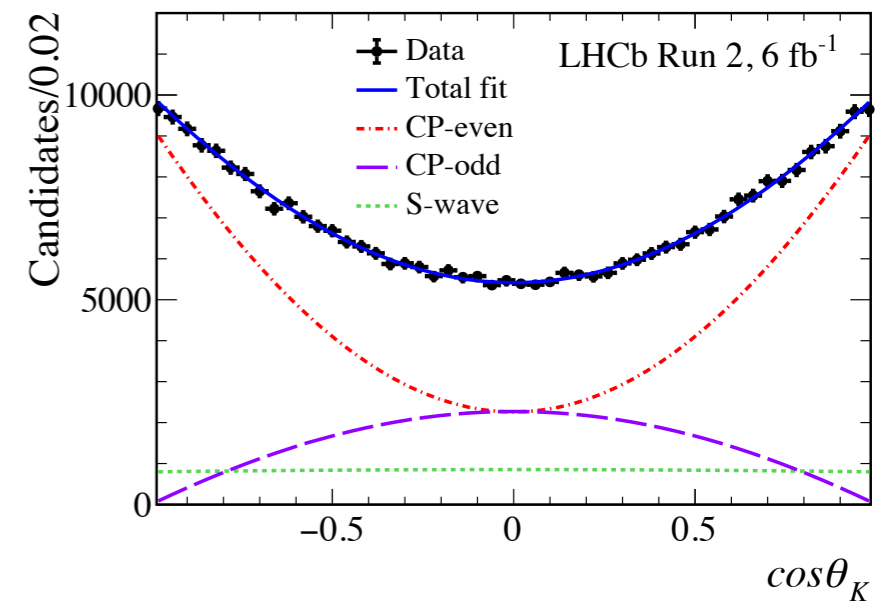
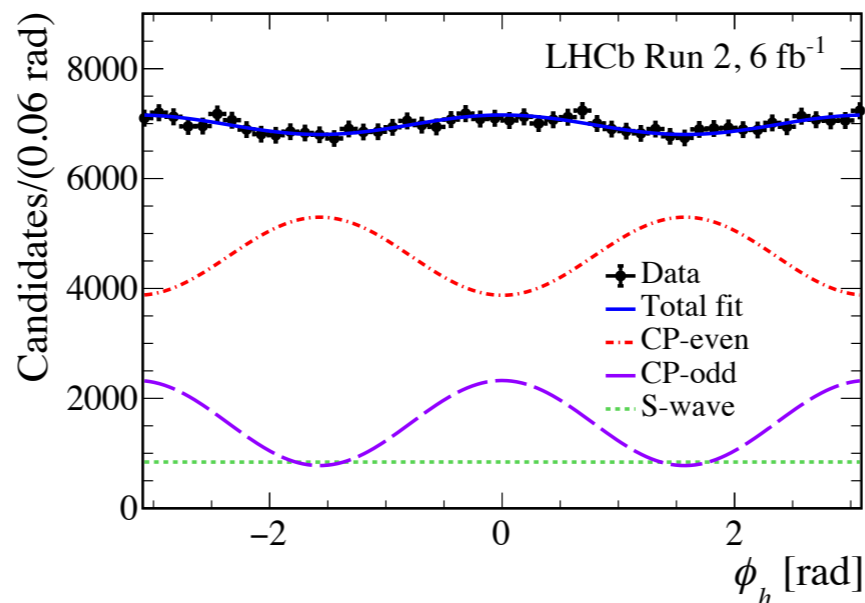
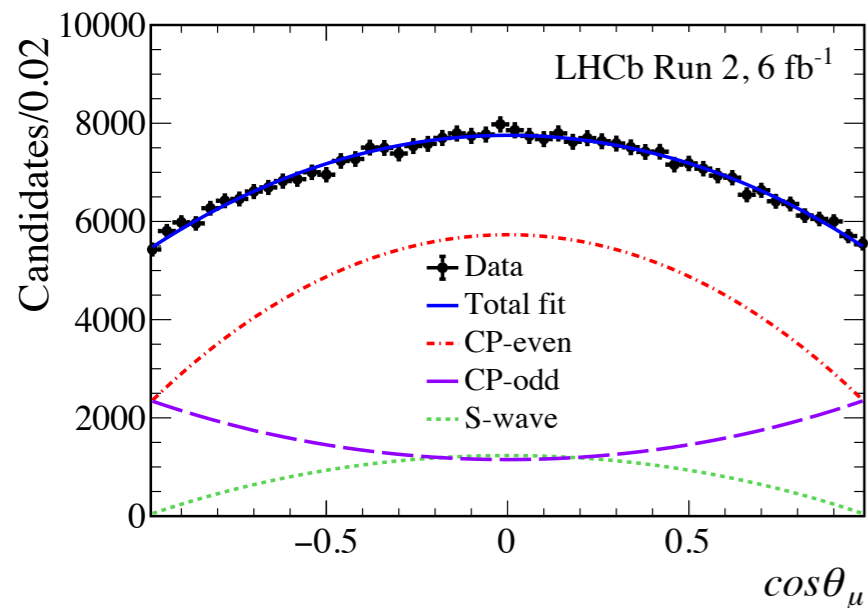
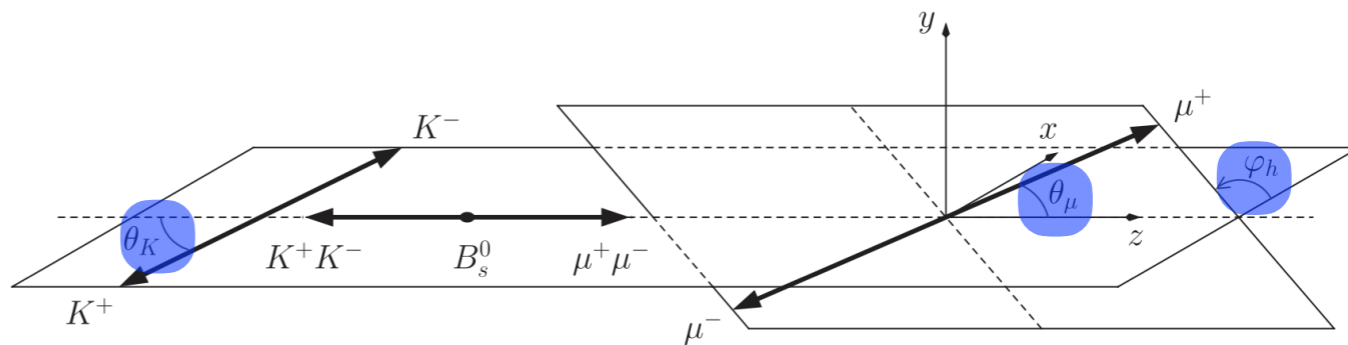
arXiv: 2308.01468  
submitted to PRL

- Time-dependent flavour-tagged angular analysis for  $B_s^0 \rightarrow VV$

$$\mathcal{P}(t, \theta_K, \theta_\mu, \phi_h | \delta_t) \propto \sum_{k=1}^{10} N_k h_k(t) f_k(\theta_K, \theta_\mu, \phi_h) \rightarrow \phi_s, \Delta m_s, \Delta \Gamma_s, \Gamma_s - \Gamma_d$$



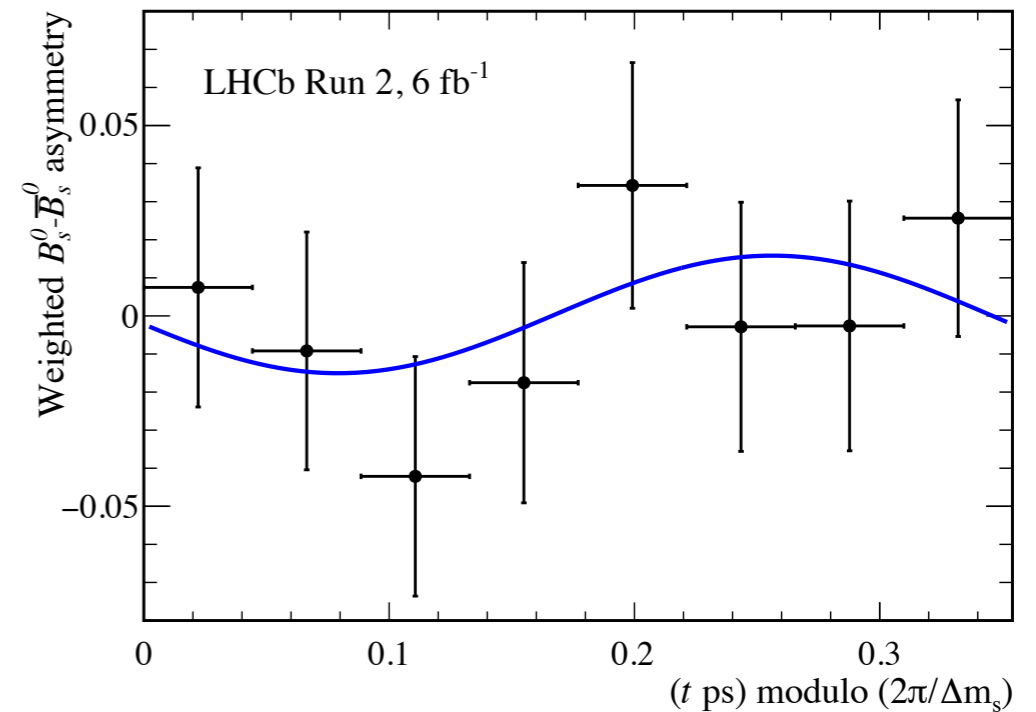
\* Amplitudes  $f_k$  based on helicity frame to disentangle CP-odd and CP-even components



# $\phi_s$ in $B_s^0 \rightarrow J/\psi KK$

arXiv: 2308.01468  
submitted to PRL

Parameters	Values <sup>1</sup>
$\phi_s$ [rad]	$-0.039 \pm 0.022 \pm 0.006$
$ \lambda $	$1.001 \pm 0.011 \pm 0.005$
$\Gamma_s - \Gamma_d$ [ $\text{ps}^{-1}$ ]	$-0.0057^{+0.0013}_{-0.0015} \pm 0.0014$
$\Delta\Gamma_s$ [ $\text{ps}^{-1}$ ]	$0.0846 \pm 0.0044 \pm 0.0024$
$\Delta m_s$ [ $\text{ps}^{-1}$ ]	$17.743 \pm 0.033 \pm 0.009$
$ A_{\perp} ^2$	$0.2463 \pm 0.0023 \pm 0.0024$
$ A_0 ^2$	$0.5179 \pm 0.0017 \pm 0.0032$
$\delta_{\perp} - \delta_0$ [rad]	$2.903^{+0.075}_{-0.074} \pm 0.048$
$\delta_{\parallel} - \delta_0$ [rad]	$3.146 \pm 0.060 \pm 0.052$



- The **most precise measurement** in single channel to date
- Compatible with prediction assuming the SM  $-\beta_s^{\text{SM}} = -0.0368^{+0.0009}_{-0.0006}$  rad
- No evidence of CP violation
- Consistent and combined with all LHCb measurements

$$(B_s^0 \rightarrow J/\psi hh, D_s^+ D_s^-, \psi(2S)KK) \quad \phi_s = -0.031 \pm 0.018 \text{ rad}$$

# $\phi_s$ polarisation dependent fit

arXiv: 2308.01468  
submitted to PRL

- New physics effects can vary in different polarisation states
  - Allow  $|\lambda|$  and  $\phi_s$  to differ in polarisation states
  - Shows no evidence for any polarisation dependence

Parameters	Values (stat. unc. only)
$\phi_s^0$ [rad]	$-0.034 \pm 0.023$
$\phi_s^{\parallel} - \phi_s^0$ [rad]	$-0.002 \pm 0.021$
$\phi_s^{\perp} - \phi_s^0$ [rad]	$-0.001 \begin{matrix} + 0.020 \\ - 0.021 \end{matrix}$
$\phi_s^S - \phi_s^0$ [rad]	$0.022 \begin{matrix} + 0.027 \\ - 0.026 \end{matrix}$
$ \lambda^0 $	$0.969 \begin{matrix} + 0.025 \\ - 0.024 \end{matrix}$
$ \lambda^{\parallel}/\lambda^0 $	$0.982 \begin{matrix} + 0.055 \\ - 0.052 \end{matrix}$
$ \lambda^{\perp}/\lambda^0 $	$1.107 \begin{matrix} + 0.081 \\ - 0.075 \end{matrix}$
$ \lambda^S/\lambda^0 $	$1.121 \begin{matrix} + 0.085 \\ - 0.078 \end{matrix}$

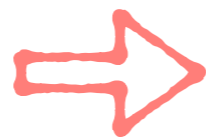


# $\phi_s$ combinations in $b \rightarrow c\bar{c}s$ transition

Previous World Average:

$$\phi_s^{c\bar{c}s} = -0.049 \pm 0.019 \text{ rad}$$

$$\phi_s^{J/\psi KK} = -0.070 \pm 0.022 \text{ rad}$$



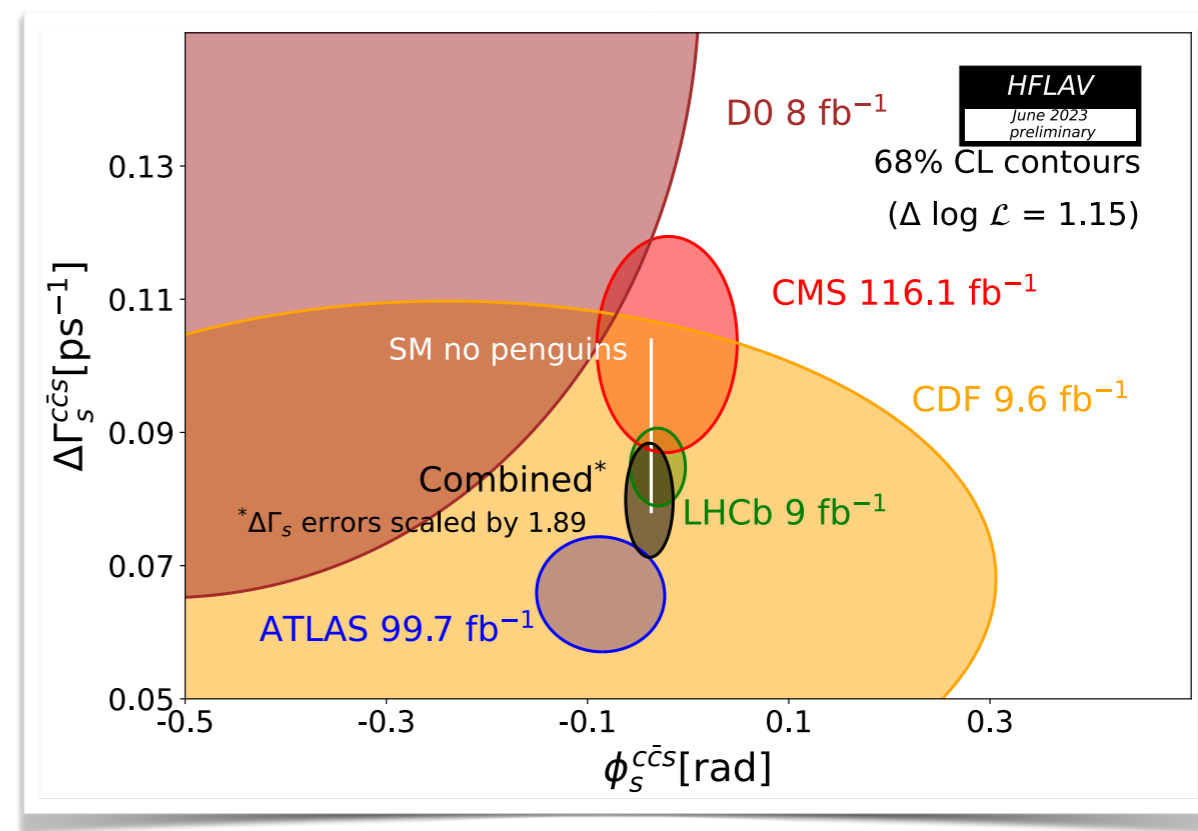
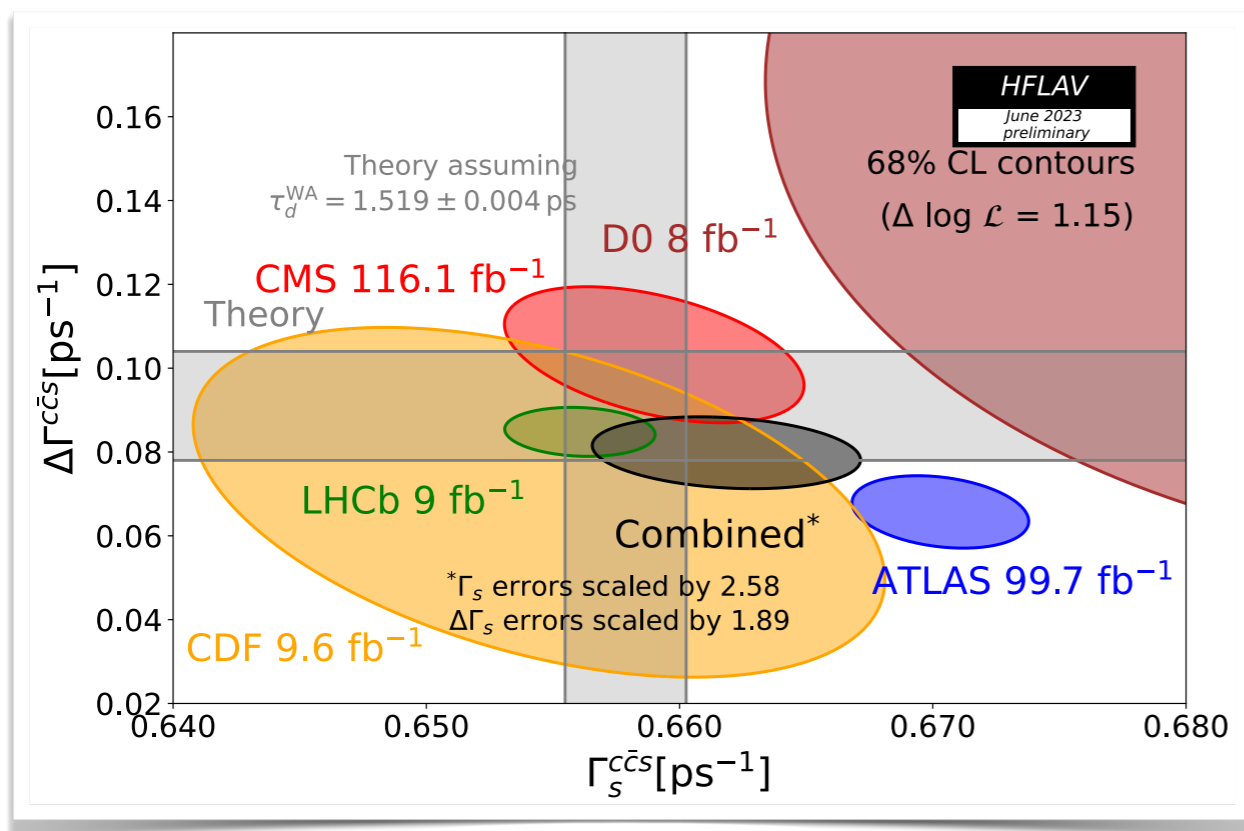
**New World Average:** (preliminary)

$$\phi_s^{c\bar{c}s} = -0.050 \pm 0.016 \text{ rad (16\%)}$$

$$\phi_s^{J/\psi KK} = -0.039 \pm 0.017 \text{ rad (23\%)}$$

- Consistent with the Global fits with SM assumption

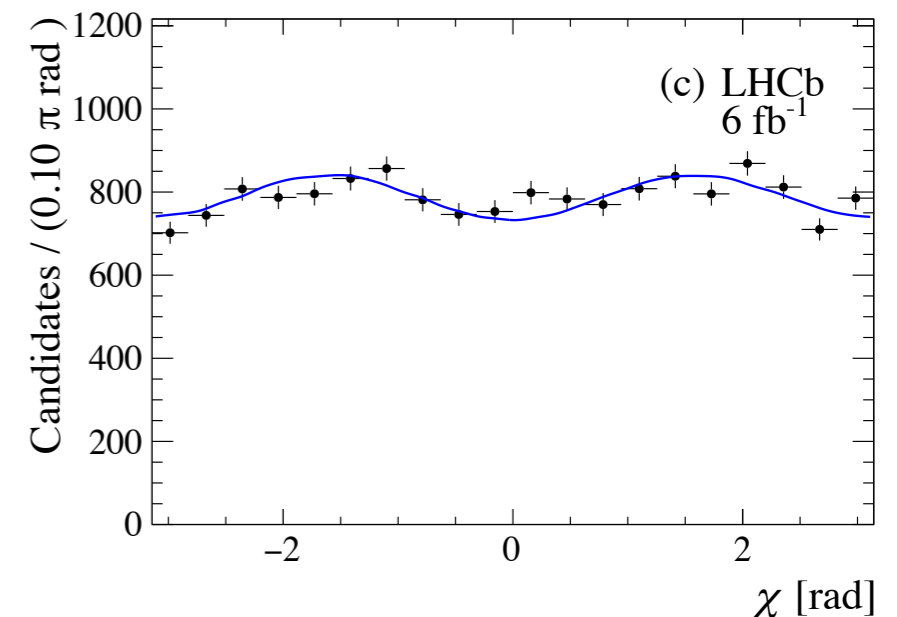
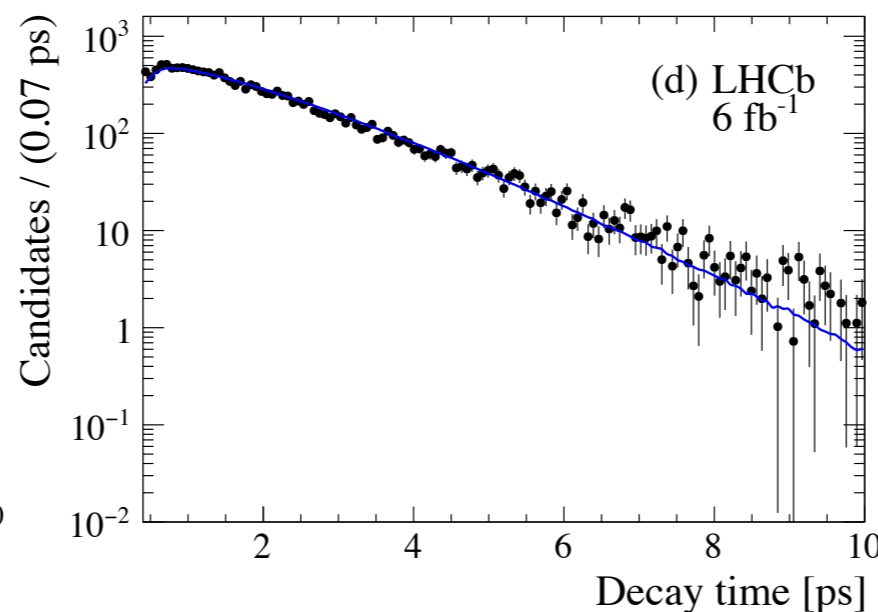
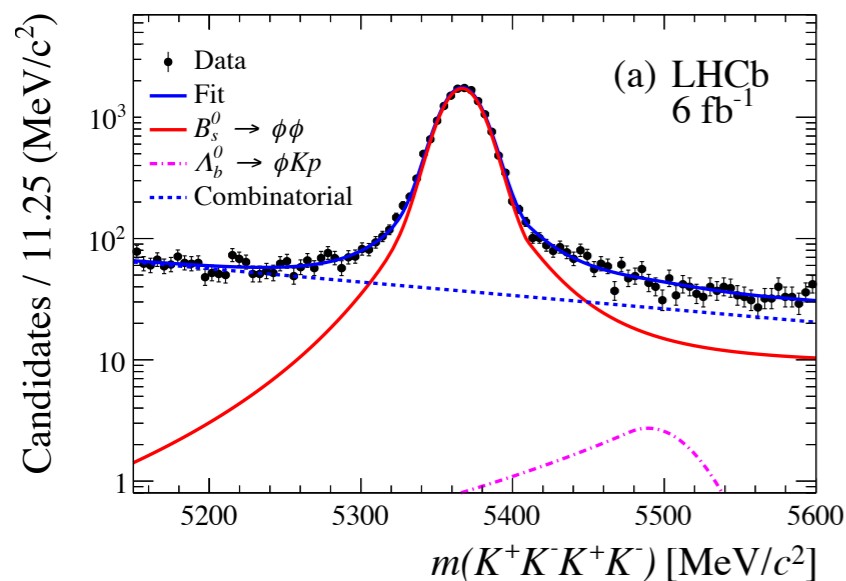
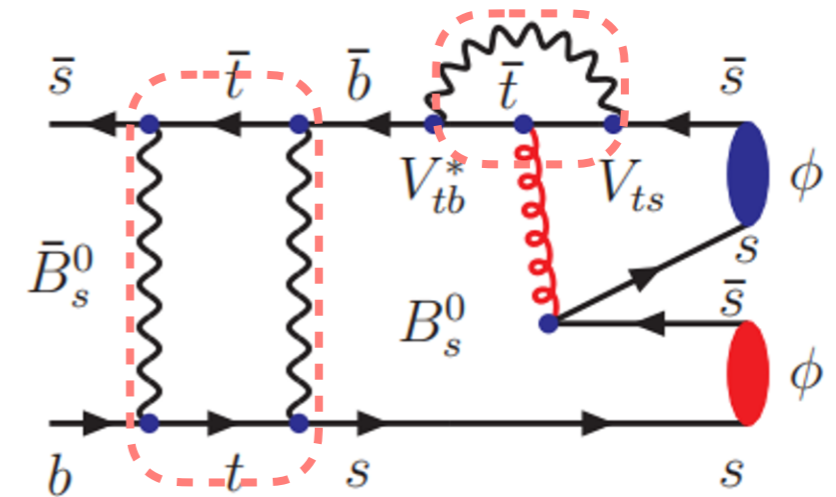
$$\phi_s^{\text{CKMFitter}} \approx -2\beta_s = (-0.0368^{+0.0006}_{-0.0009}) \text{ rad} \quad \phi_s^{\text{UTFitter}} = (-0.0370 \pm 0.0010) \text{ rad}$$



# $\phi_s$ in $b \rightarrow s\bar{s}s$ transition

LHCb-PAPER-2023-001

- Benchmark channel  $B_s^0 \rightarrow \phi(KK)\phi(KK)$  proceeds via  $b \rightarrow s\bar{s}s$  transition
  - Penguin dominated decay
  - NP contributes in penguin or mixing process
- Similar analysis strategy as  $B_s^0 \rightarrow J/\psi\phi(KK)$ 
  - flavour-tagged time-dependent angular analysis

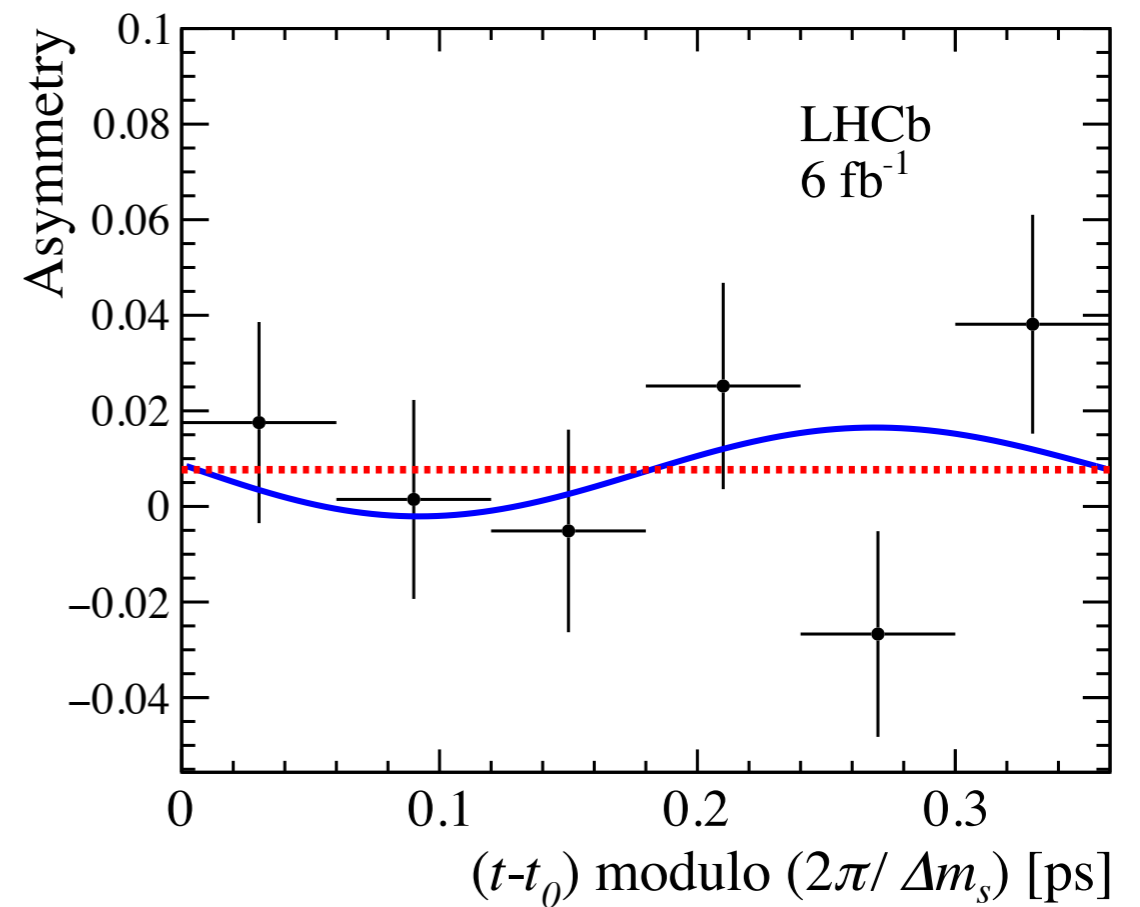
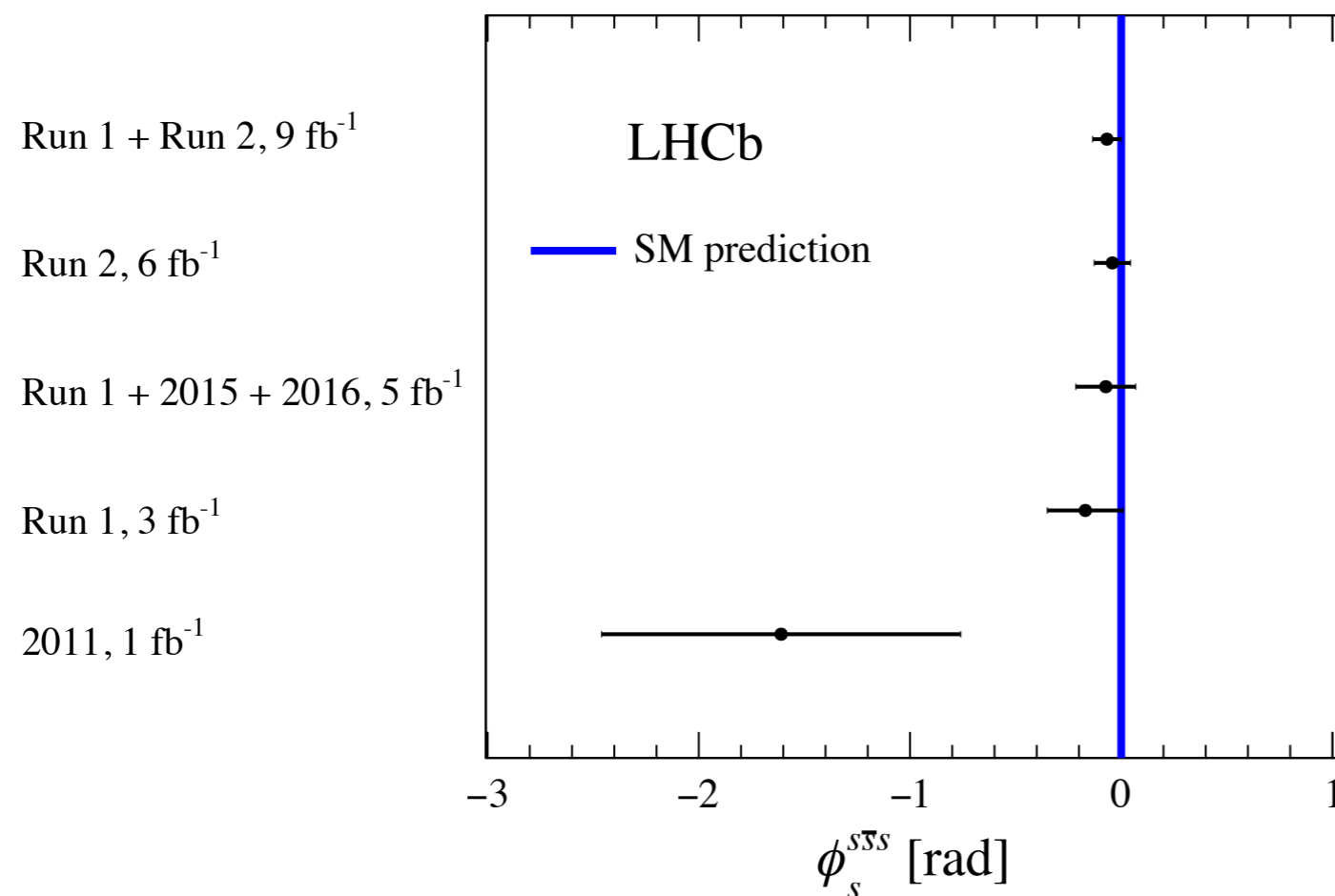


# $\phi_s$ in $b \rightarrow s\bar{s}s$ transition

LHCb-PAPER-2023-001  
accepted by PRL

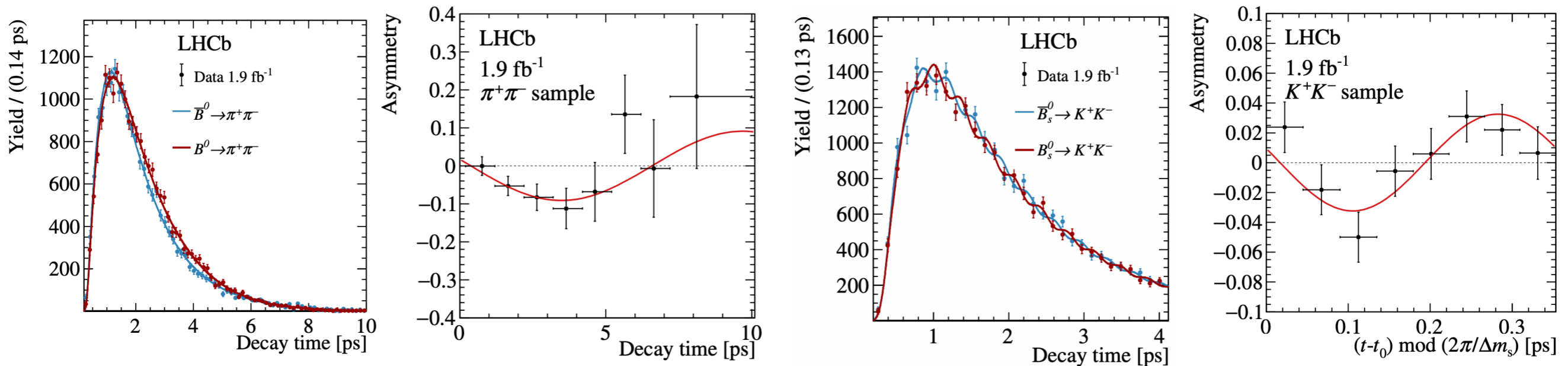
$$\phi_s^{s\bar{s}s} = -0.042 \pm 0.075 \pm 0.009 \text{ rad}, |\lambda| = 1.004 \pm 0.030 \pm 0.009$$

- The most precise measurement in any penguin dominated  $B$  decays
- No polarisation dependence is observed

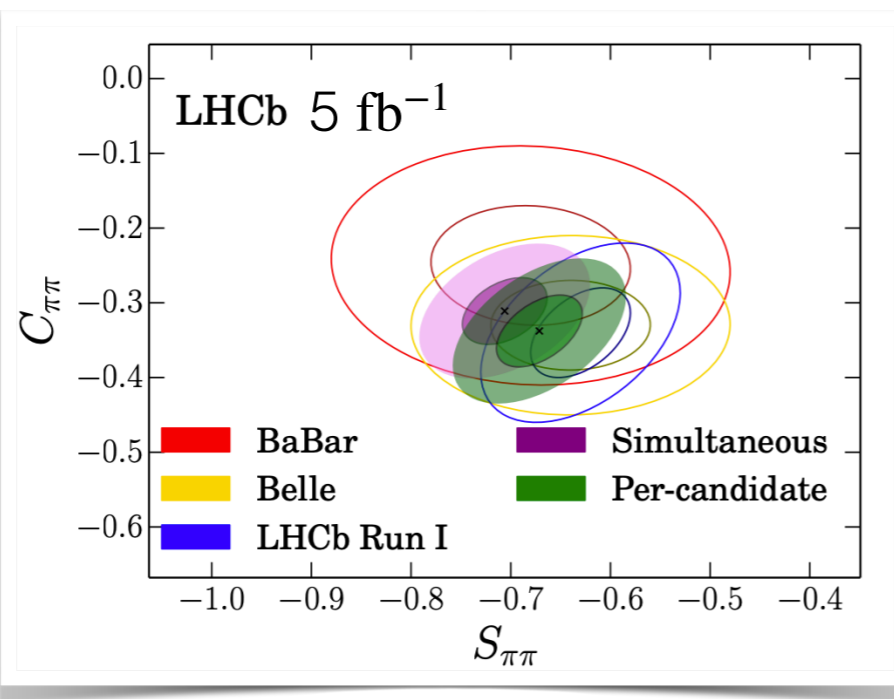


# CP asymmetry in $B_{(s)}^0 \rightarrow h^+h^-$

- Simultaneous fit to the invariant mass,  $B_{(s)}^0$  decay time and tagging decision for  $B^0 \rightarrow \pi^+\pi^-$ ,  $B_s^0 \rightarrow K^+K^-$ ,  $B_{(s)}^0 \rightarrow K\pi$ , providing constraints to  $\alpha$ ,  $\gamma$ ,  $\sin 2\beta_s$
- The first observation of time-dependent CP violation in  $B_s^0$  decay



Analysis of full Run 2 data in progress



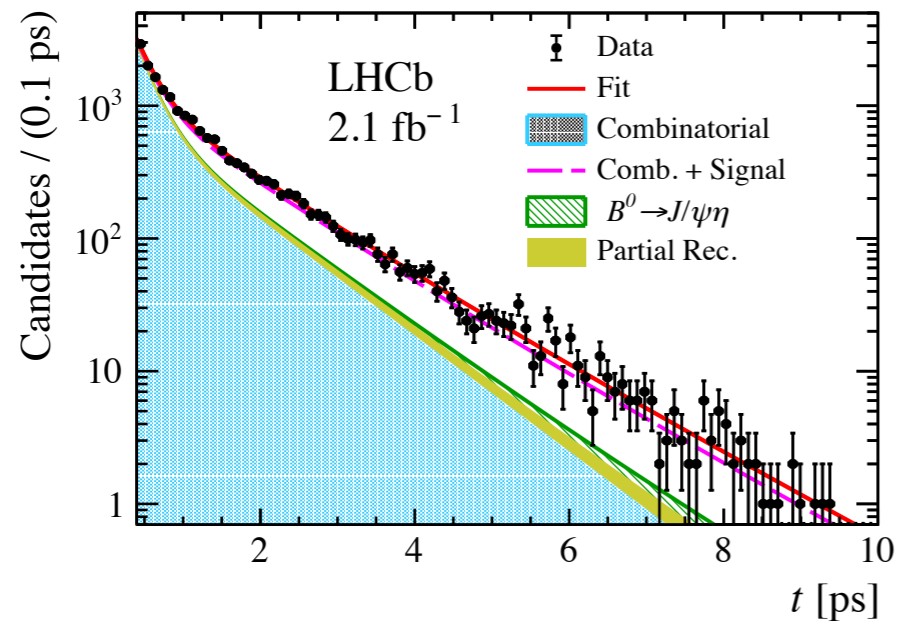
$$\begin{aligned}
 C_{\pi\pi} &= -0.311 \pm 0.045 \pm 0.015, \\
 S_{\pi\pi} &= -0.706 \pm 0.042 \pm 0.013, \\
 A_{CP}^{B^0} &= -0.0824 \pm 0.0033 \pm 0.0033, \\
 A_{CP}^{B_s^0} &= 0.236 \pm 0.013 \pm 0.011, \\
 C_{KK} &= 0.164 \pm 0.034 \pm 0.014, \\
 S_{KK} &= 0.123 \pm 0.034 \pm 0.015, \\
 A_{KK}^{\Delta\Gamma} &= -0.83 \pm 0.05 \pm 0.09,
 \end{aligned}$$



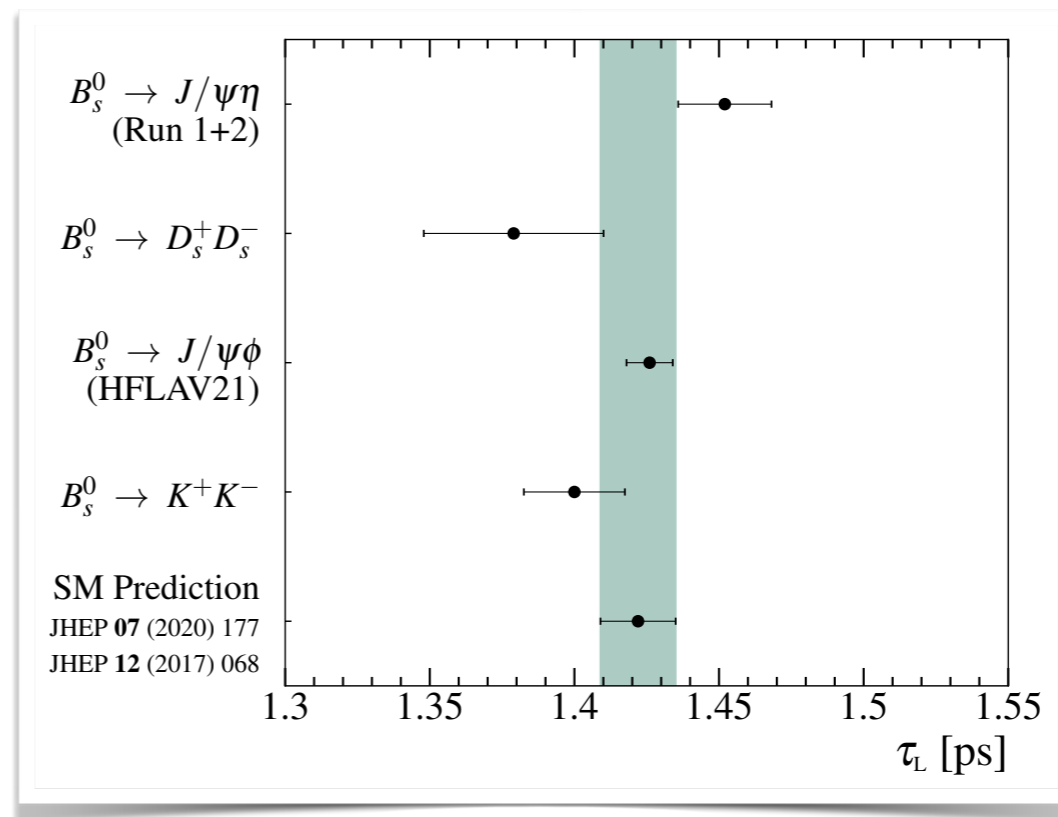
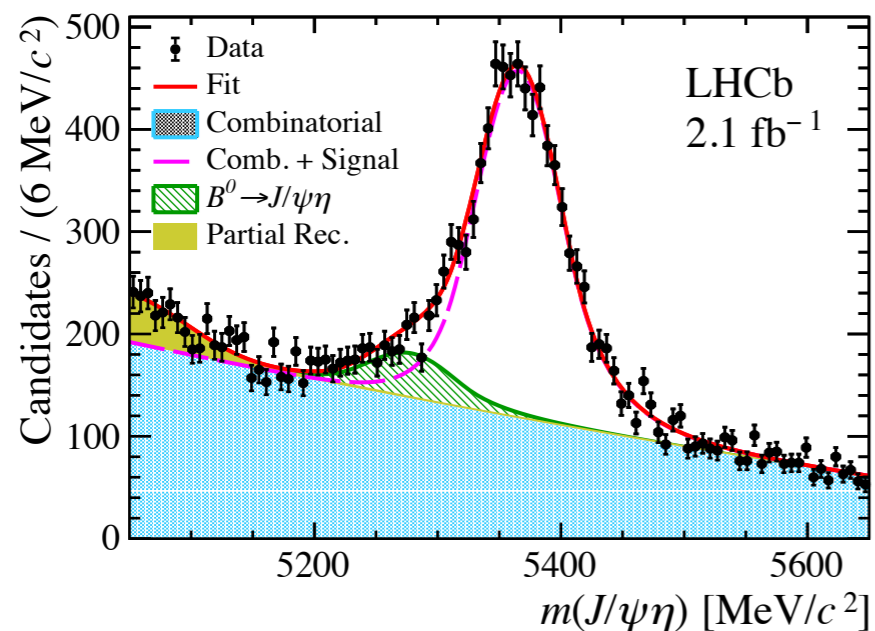
# Effective lifetime measurements in $B_s^0 \rightarrow J/\psi\eta$

EPJC83 (2023) 629

- $CP$ -even decay  $B_s^0 \rightarrow J/\psi(\mu^+\mu^-)\eta(\gamma\gamma)$  allows to determine  $\tau_L = 1/\Gamma_L$
- Simultaneous fit to invariant mass and decay time



$$\tau_L = 1.452 \pm 0.014 \pm 0.007 \pm 0.002 \text{ ps}$$



Agree with the SM prediction and other measurements

# Effective lifetime measurements in $B_s^0 \rightarrow J/\psi\eta'$

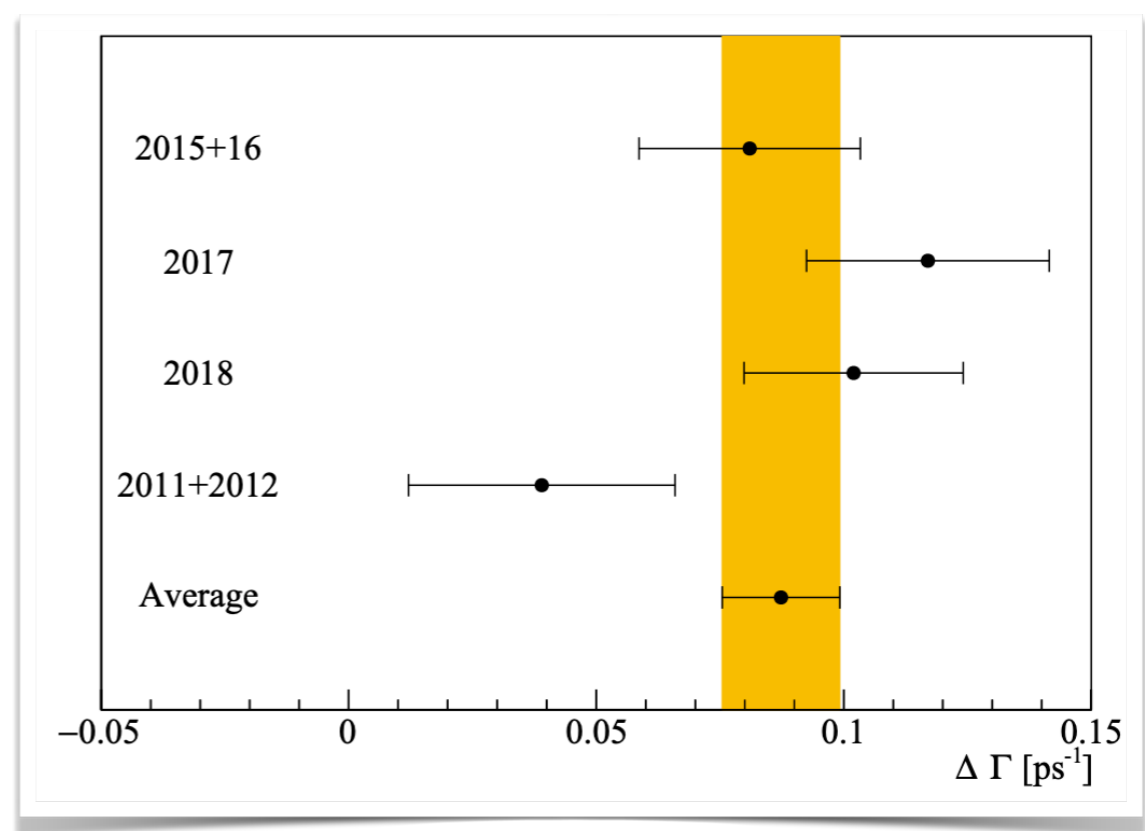
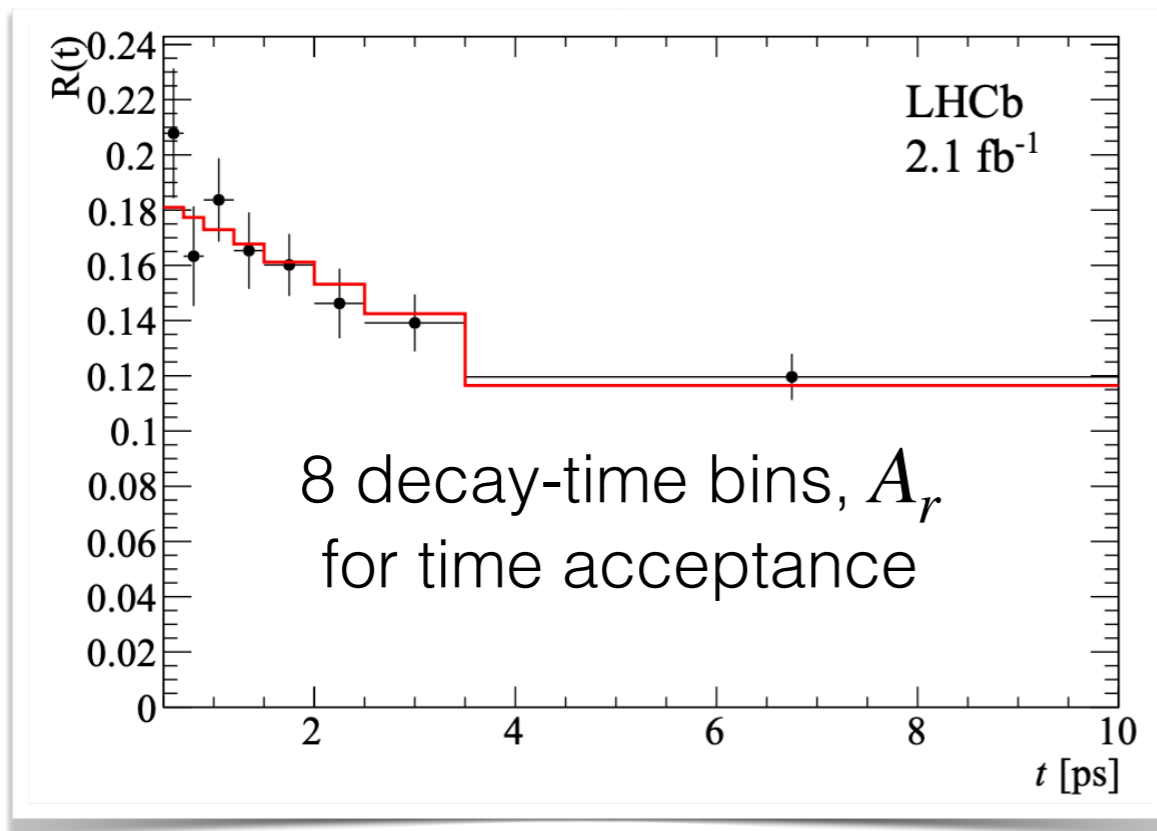
- Simultaneous analysis of  $CP$ -even decay  $B_s^0 \rightarrow J/\psi(\mu^+\mu^-)\eta'(\pi^+\pi^-\gamma)$  and  $CP$ -odd decay  $B_s^0 \rightarrow J/\psi\rho^0$  to determine  $\Delta\Gamma_s$
- Fit to the ratio of decay time  $R(t)$  in 8 bins

LHCb-PAPER-2023-025

in preparation

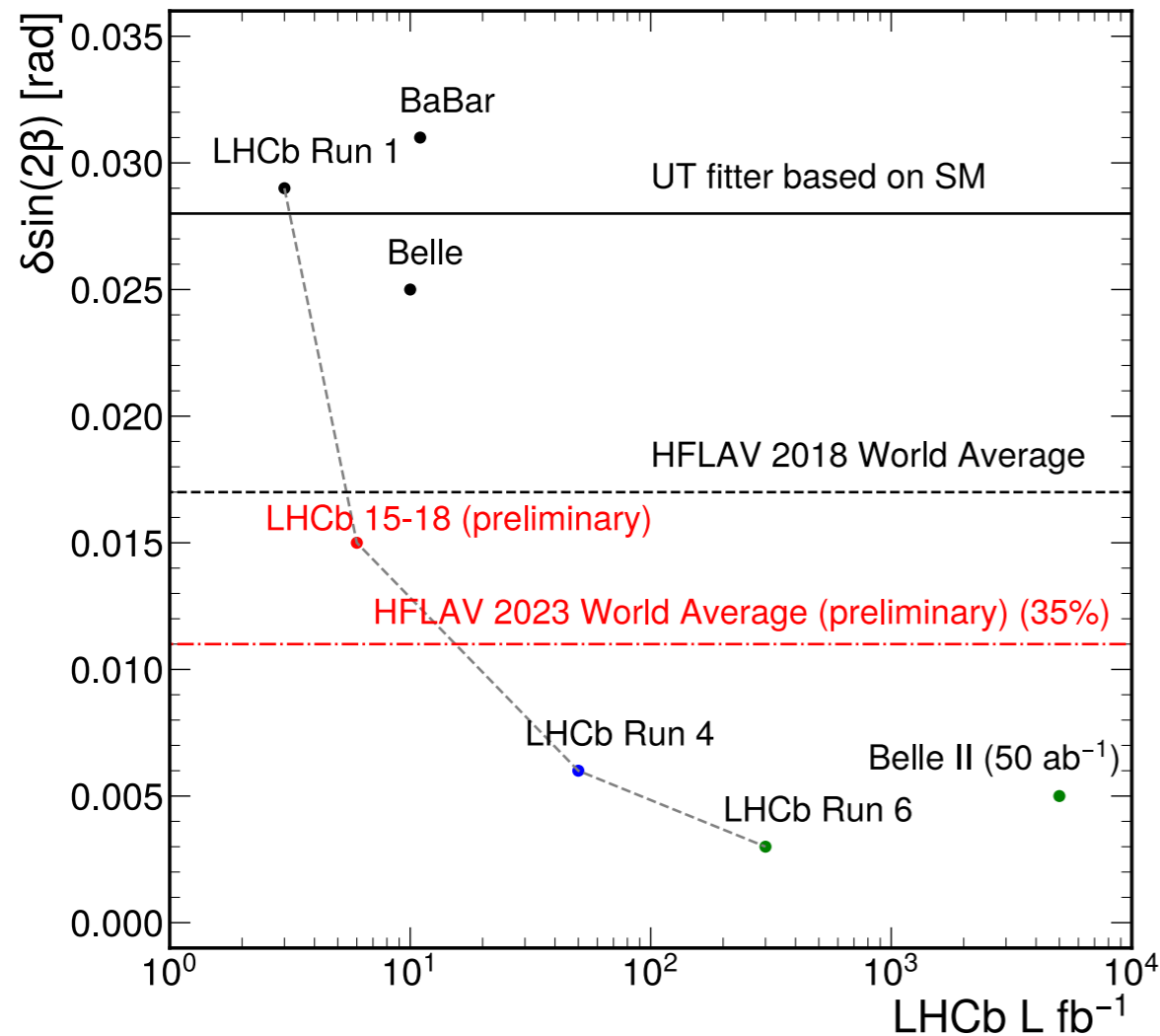
$$R(t) = A_r(t) \cdot \frac{N_L}{N_H}$$

$$\Delta\Gamma_s = 0.087 \pm 0.012 \pm 0.009 \text{ ps}^{-1}$$

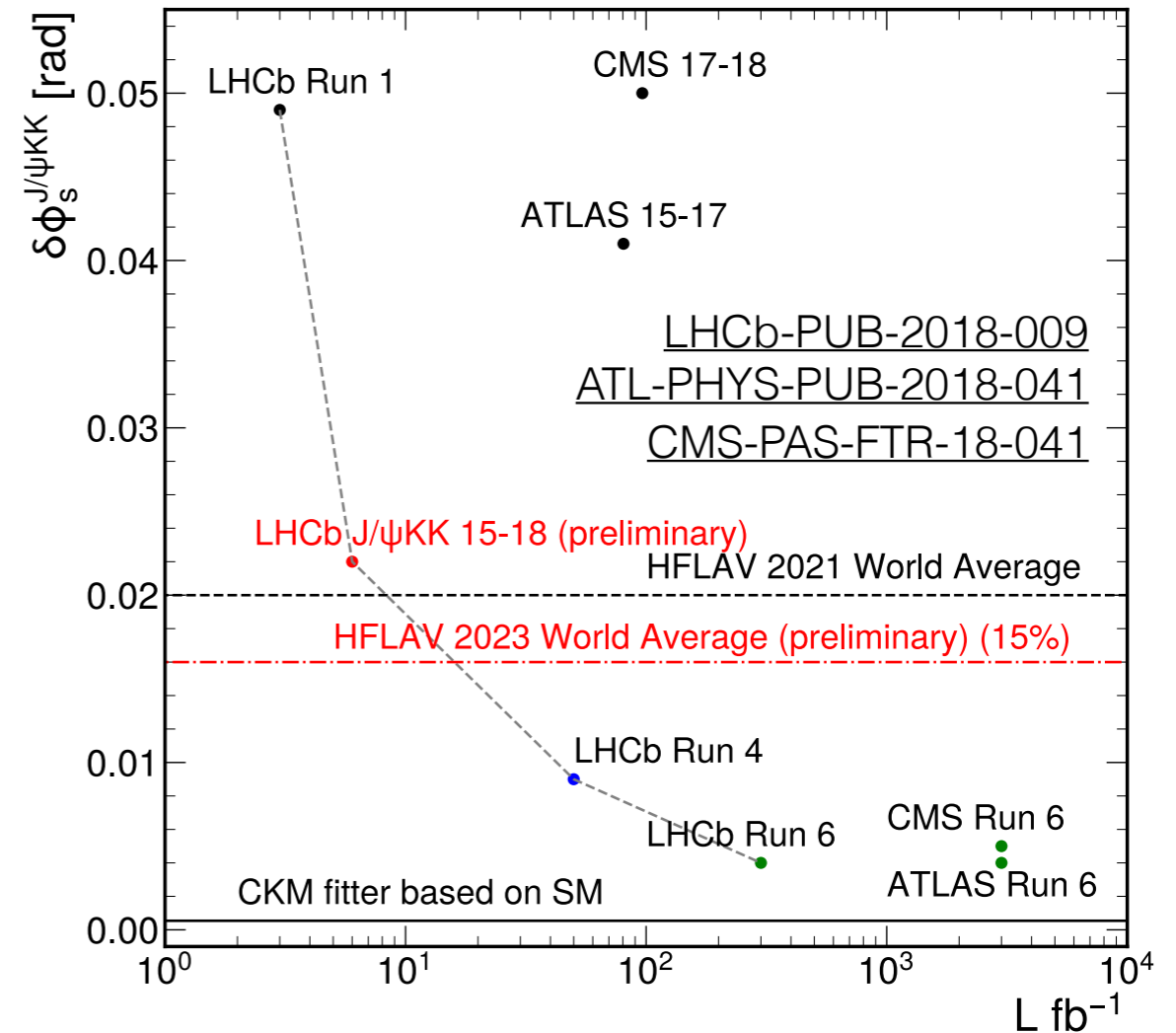


Agree with the World Average:  $0.074 \pm 0.006 \text{ ps}^{-1}$

# Looking at future



[LHCb-PUB-2018-009](#)  
[BelleII physics book](#)



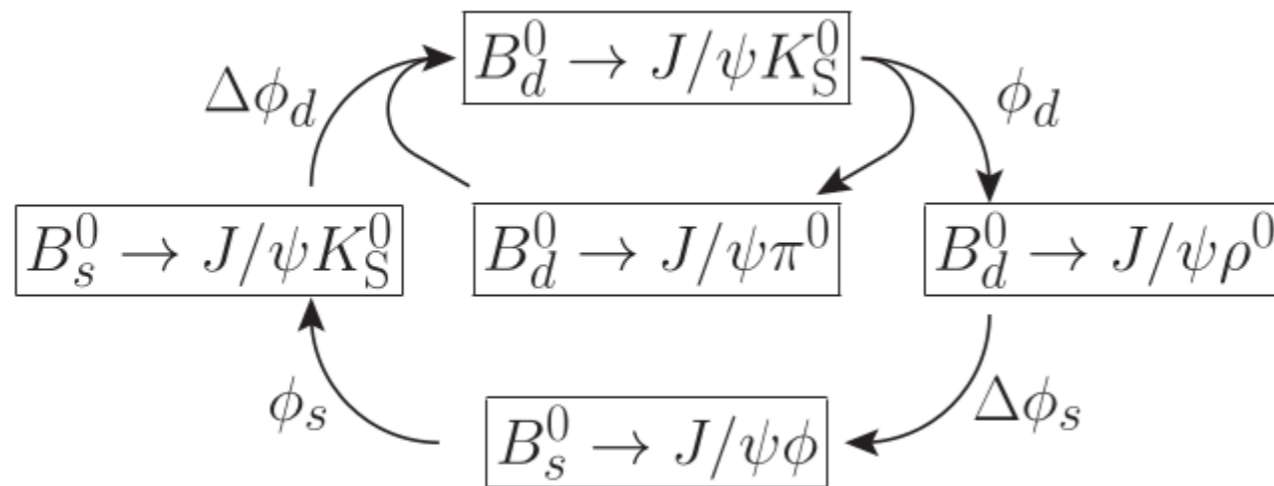
- Further precision improvement with more data and more decay modes
- Great opportunities to search for NP indirectly, up to  $> \text{TeV}$  scale

# Control of penguin contribution

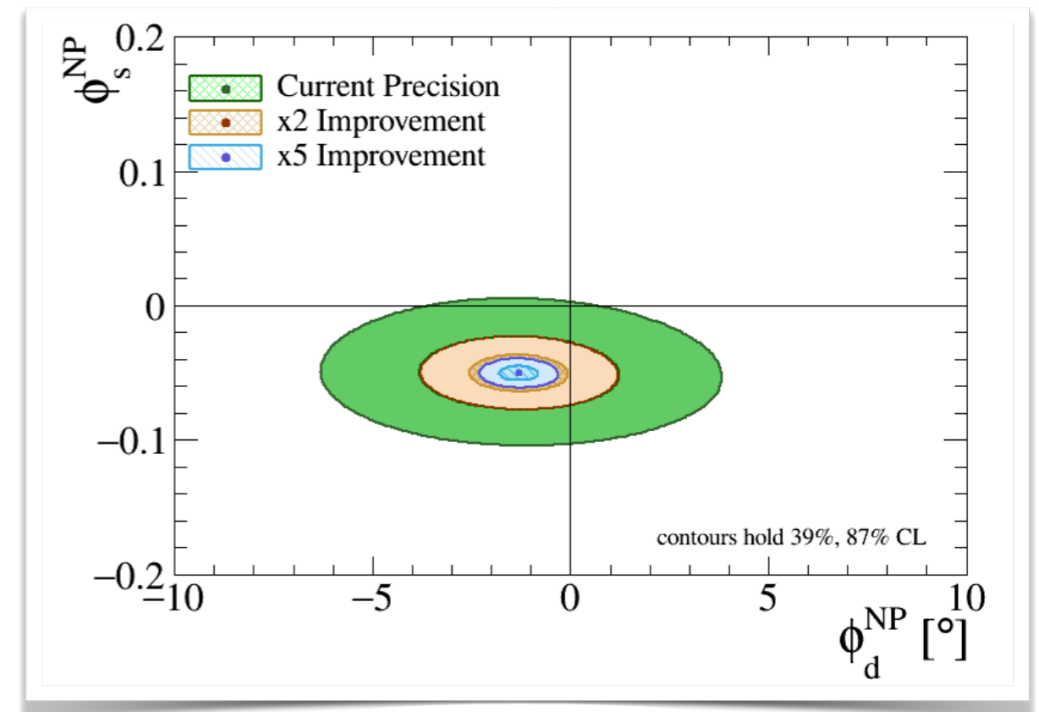
- $\sigma(\phi_s) \sim 0.016$  comparable with the theoretical estimation of  $\Delta\phi_s^{\text{penguin}} \sim 1^\circ \approx 0.017$ , better control of penguin effect necessary
- Combined analysis of penguin contributions in  $\phi_s$  and  $\phi_d$  ( $\sin 2\beta$ ), using SU(3) flavor symmetry

$$\phi_d = \sin(2\beta^{\text{tree}}) + \Delta\phi_d^{\text{penguin}} + \phi_d^{\text{NP}}$$

$$\phi_s = \phi_s^{\text{tree}} + \Delta\phi_s^{\text{penguin}} + \phi_s^{\text{NP}}$$

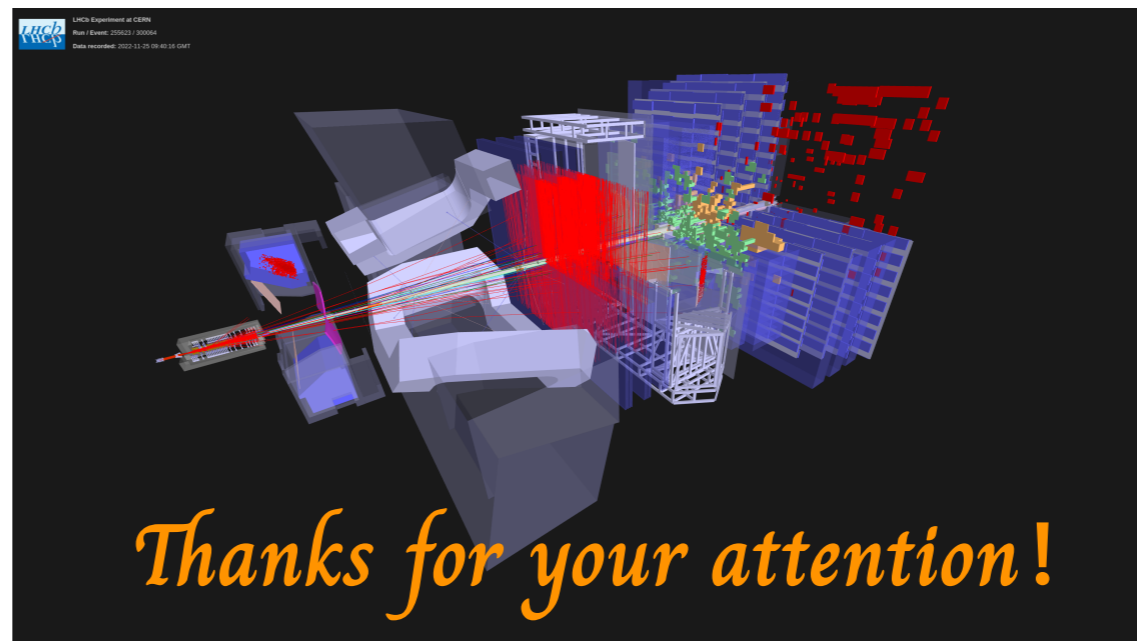


J.Phys.G 48 (2021) 6, 065002



# Summary

- ✓ LHCb dominates the world average of many CPV measurements
- ✓ Flag-ship time-dependent measurements of CP violation in  $B$ -meson decays with full LHCb data sample, providing **the most precise results** for
  - ✓  $\phi_s$  in  $b \rightarrow c\bar{c}s$  transition,  $\sigma(\phi_s) \sim 20$  mrad
  - ✓  $\phi_s^{s\bar{s}s}$  in penguin dominant  $B$  decays
  - ✓  $\sin 2\beta = 0.716 \pm 0.013(\text{stat.}) \pm 0.008(\text{syst.})$
- ✓ New results for  $\Delta\Gamma_s$  and  $\Gamma_L$
- ✓ Looking forward to further test of the SM and search for new physics with more data from Upgrade I & II





*Back up slides*

# Systematics for $\sin 2\beta$

LHCb-PAPER-2023-013  
in preparation

Source	$\sigma(S)$	$\sigma(C)$
Fitter validation	0.0004	0.0006
$\Delta\Gamma_d$ uncertainty	0.0055	0.0017
FT calibration portability	0.0053	0.0001
FT $\Delta\epsilon_{\text{tag}}$ portability	0.0014	0.0017
Decay-time bias model	0.0007	0.0013

$$S_{J/\psi(\rightarrow\mu^+\mu^-)K_S^0}^{\text{Run 2}} = 0.714 \pm 0.015 \text{ (stat)} \pm 0.0074 \text{ (syst)}$$

$$C_{J/\psi(\rightarrow\mu^+\mu^-)K_S^0}^{\text{Run 2}} = 0.013 \pm 0.014 \text{ (stat)} \pm 0.0025 \text{ (syst)}$$

$$S_{\psi(2S)K_S^0}^{\text{Run 2}} = 0.647 \pm 0.053 \text{ (stat)} \pm 0.018 \text{ (syst)}$$

$$C_{\psi(2S)K_S^0}^{\text{Run 2}} = -0.083 \pm 0.048 \text{ (stat)} \pm 0.0053 \text{ (syst)}$$

$$S_{J/\psi(\rightarrow e^+e^-)K_S^0}^{\text{Run 2}} = 0.752 \pm 0.037 \text{ (stat)} \pm 0.084 \text{ (syst)}$$

$$C_{J/\psi(\rightarrow e^+e^-)K_S^0}^{\text{Run 2}} = 0.046 \pm 0.034 \text{ (stat)} \pm 0.0077 \text{ (syst)}$$

# Time-dependent angular fit

EPJC79(2019)706

$$\mathcal{P}(t, \theta_K, \theta_\mu, \phi_h | \delta_t) \propto \sum_{k=1}^{10} N_k h_k(t) f_k(\theta_K, \theta_\mu, \phi_h) \rightarrow \phi_s, \Delta m_s, \Delta \Gamma_s, \Gamma_s - \Gamma_d$$

$$\begin{aligned} & \mathcal{P}(t, \Omega | q^{\text{OS}}, q^{\text{SSK}}, \eta^{\text{OS}}, \eta^{\text{SSK}}, \delta_t) \\ & \propto \sum_{k=1}^{10} C_{\text{SP}}^k N_k f_k(\Omega) \varepsilon_{\text{data}}^{B_s^0}(t) \\ & \cdot \left\{ \left[ \mathcal{Q}(q^{\text{OS}}, q^{\text{SSK}}, \eta^{\text{OS}}, \eta^{\text{SSK}}) h_k(t | B_s^0) \right. \right. \\ & \left. \left. + \bar{\mathcal{Q}}(q^{\text{OS}}, q^{\text{SSK}}, \eta^{\text{OS}}, \eta^{\text{SSK}}) h_k(t | \bar{B}_s^0) \right] \otimes \mathcal{R}(t - t' | \delta_t) \right\} \end{aligned}$$

## Angular amplitudes

$C_{\text{SP}}^k$  account for the interference between P- and S- wave

flavor tagging

time-dependent oscillation

decay-time efficiency

decay-time resolution

$$h_k(t | B_s^0) = \frac{3}{4\pi} e^{-\Gamma t} \left( a_k \cosh \frac{\Delta \Gamma t}{2} + b_k \sinh \frac{\Delta \Gamma t}{2} + c_k \cos(\Delta m t) + d_k \sin(\Delta m t) \right),$$

$$h_k(t | \bar{B}_s^0) = \frac{3}{4\pi} e^{-\Gamma t} \left( a_k \cosh \frac{\Delta \Gamma t}{2} + b_k \sinh \frac{\Delta \Gamma t}{2} - c_k \cos(\Delta m t) - d_k \sin(\Delta m t) \right),$$

$a_k, b_k, c_k, d_k$  involve strong and weak phases ( $\delta, \phi_s$ ) of each component

$k$	$A_k$	$f_k(\theta_\mu, \theta_K, \varphi_h)$
1	$ A_0 ^2$	$2 \cos^2 \theta_K \sin^2 \theta_\mu$
2	$ A_{\parallel} ^2$	$\sin^2 \theta_k (1 - \sin^2 \theta_\mu \cos^2 \varphi_h)$
3	$ A_{\perp} ^2$	$\sin^2 \theta_k (1 - \sin^2 \theta_\mu \sin^2 \varphi_h)$
4	$ A_{\parallel} A_{\perp} $	$\sin^2 \theta_k \sin^2 \theta_\mu \sin 2\varphi_h$
5	$ A_0 A_{\parallel} $	$\frac{1}{2} \sqrt{2} \sin 2\theta_k \sin 2\theta_\mu \cos \varphi_h$
6	$ A_0 A_{\perp} $	$-\frac{1}{2} \sqrt{2} \sin 2\theta_k \sin 2\theta_\mu \sin \varphi_h$
7	$ A_S ^2$	$\frac{2}{3} \sin^2 \theta_\mu$
8	$ A_S A_{\parallel} $	$\frac{1}{3} \sqrt{6} \sin \theta_k \sin 2\theta_\mu \cos \varphi_h$
9	$ A_S A_{\perp} $	$-\frac{1}{3} \sqrt{6} \sin \theta_k \sin 2\theta_\mu \sin \varphi_h$
10	$ A_S A_0 $	$\frac{4}{3} \sqrt{3} \cos \theta_K \sin^2 \theta_\mu$

# Systematics for $\phi_s$

arXiv: 2308.01468

submitted to PRL

\* Uncertainties ( $\times 0.01$ )    **Dominated sys.**    **Sub-dominated sys.**    **Stat. limited**

Source	$ A_0 ^2$	$ A_\perp ^2$	$\phi_s$ [rad]	$ \lambda $	$\delta_\perp - \delta_0$ [rad]	$\delta_\parallel - \delta_0$ [rad]	$\Gamma_s - \Gamma_d$ [ps $^{-1}$ ]	$\Delta\Gamma_s$ [ps $^{-1}$ ]	$\Delta m_s$ [ps $^{-1}$ ]
Mass parametrization	0.04	0.03	0.03	0.02	0.15	0.12	0.02	0.04	0.03
Mass: shape statistical	0.04	0.04	0.05	0.09	0.62	0.33	0.02	0.01	0.11
Mass factorization	<b>0.11</b>	<b>0.10</b>	<b>0.42</b>	0.19	0.54	0.60	<b>0.12</b>	<b>0.16</b>	0.18
$B_c^+$ contamination	0.04	0.05	—	0.02	—	0.17	(0.07)	(0.03)	—
D-wave component	0.04	0.04	0.02	—	0.07	0.13	0.01	0.03	0.02
Bkgcat 60	0.07	0.04	0.02	0.10	0.18	0.18	0.02	—	0.01
Multiple candidates	0.01	—	<b>0.27</b>	<b>0.22</b>	0.90	0.41	0.01	0.01	0.24
Particle identification	0.06	0.09	<b>0.27</b>	<b>0.27</b>	1.31	0.51	0.05	<b>0.15</b>	<b>0.46</b>
$C_{SP}$ factors	—	0.01	0.01	0.03	0.73	0.41	—	0.01	0.04
DTR model portability	—	—	0.08	0.03	0.26	0.09	—	—	0.09
DTR calibration	—	—	0.03	0.02	0.11	0.07	—	—	0.05
Time bias correction	0.04	0.05	0.06	0.05	0.77	0.11	0.03	0.05	<b>0.44</b>
Angular efficiency	0.05	<b>0.14</b>	<b>0.25</b>	<b>0.32</b>	0.42	0.44	0.01	0.02	0.13
Angular resolution	0.01	0.01	0.02	0.01	0.02	0.08	—	0.01	0.02
Kinematic weighting	<b>0.24</b>	0.09	0.01	0.01	0.98	0.86	0.02	0.03	<b>0.31</b>
Momentum uncertainty	0.08	0.04	0.04	—	0.07	0.11	0.01	—	0.13
Longitudinal scale	0.07	0.04	0.04	—	0.10	0.09	0.02	—	<b>0.31</b>
Neglected correlations	—	—	—	—	<b>4.20</b>	<b>4.96</b>	—	—	—
Total sys. unc.	0.32	0.24	<b>0.6</b>	<b>0.5</b>	<b>4.8</b>	5.2	0.14	<b>0.24</b>	<b>0.9</b>
Stat. unc.	0.17	0.23	2.2	1.1	7.5	6.0	0.14	0.44	3.3

- $\phi_s$ ,  $|\lambda|$ ,  $\Delta\Gamma_s$ ,  $\Delta m_s$  are statistically limited

# Systematics for $\phi_s^{s\bar{s}s}$

LHCb-PAPER-2023-001  
accepted by PRL

Source	$\phi_s^{s\bar{s}s}$	$ \lambda $	$ A_0 ^2$	$ A_\perp ^2$	$\delta_{\parallel} - \delta_0$	$\delta_\perp - \delta_0$
Time resolution	4.9	2.6	0.8	0.8	0.1	3.4
Flavor tagging	4.8	4.7	0.9	1.3	1.2	9.7
Angular acceptance	3.9	4.9	1.4	1.7	4.7	1.2
Time acceptance	2.3	1.7	0.1	0.1	5.6	0.7
Mass fit & factorization	2.2	4.4	1.9	2.3	2.3	2.5
MC truth match	1.1	0.2	0.1	0.1	0.2	0.3
Fit bias	0.8	0.7	0.9	0.3	3.6	0.7
Candidate multiplicity	0.3	0.2	0.1	0.8	0.2	0.1
Total	8.8	8.6	2.7	3.3	8.5	10.7

Parameter	Result
$\phi_s^{s\bar{s}s}$ [rad]	$-0.042 \pm 0.075 \pm 0.009$
$ \lambda $	$1.004 \pm 0.030 \pm 0.009$
$ A_0 ^2$	$0.384 \pm 0.007 \pm 0.003$
$ A_\perp ^2$	$0.310 \pm 0.006 \pm 0.003$
$\delta_{\parallel} - \delta_0$ [rad]	$2.463 \pm 0.029 \pm 0.009$
$\delta_\perp - \delta_0$ [rad]	$2.769 \pm 0.105 \pm 0.011$



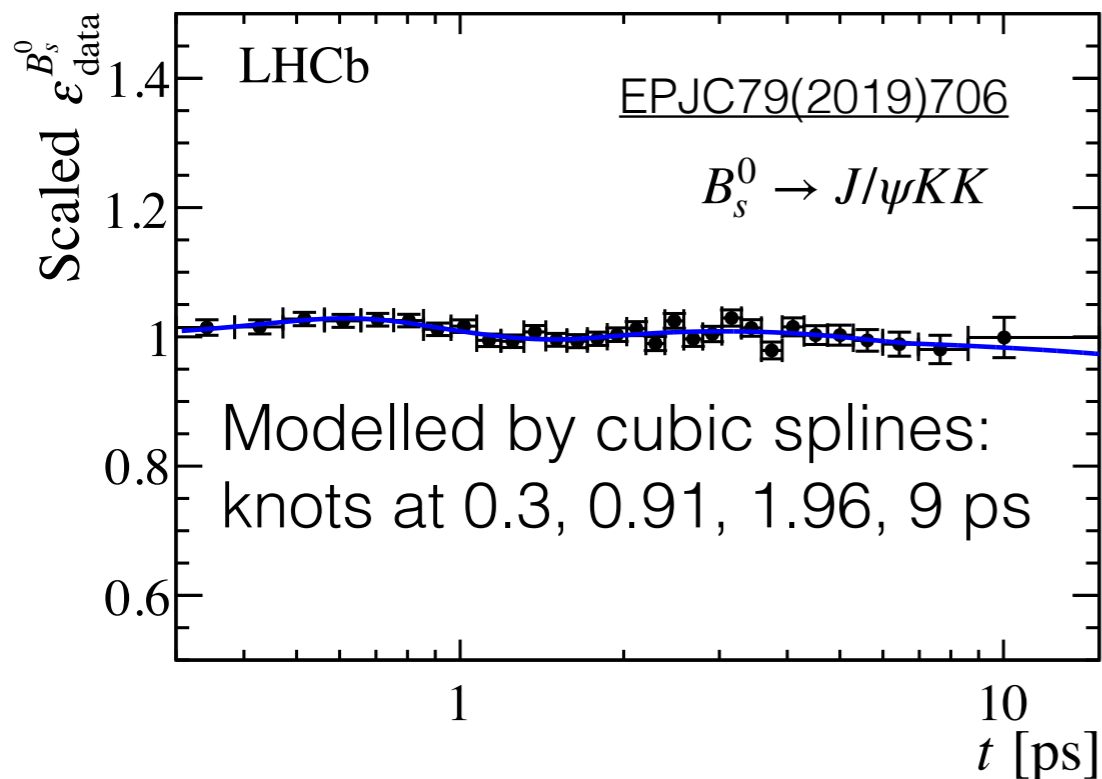
# Decay time & angular efficiencies

- Reconstruction and selection criteria introduce non-uniform efficiency

- Decay-time efficiencies:

Data driven method

$$\varepsilon_{\text{data}}^{B_s^0}(t) = \varepsilon_{\text{data}}^{B^0}(t) \times \frac{\varepsilon_{\text{sim}}^{B_s^0}(t)}{\varepsilon_{\text{sim}}^{B^0}(t)}$$



$$f(t) \propto \varepsilon(t) \cdot e^{-t/\tau} \otimes G(0, \sigma_t)$$

- Angular efficiencies for  $B_s^0$  decays estimated with simulation

