

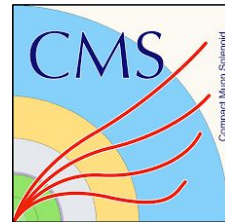
# *CP violation in SM diboson measurement*

Qiang Li (Peking University)  
2023/08/26 USTC



FIND论坛系列学术研讨会:

FIND CP violation at electroweak scale and beyond



# Seattle Snowmass Summer Meeting 2022

## Big Questions

Evolution of early Universe  
Matter Antimatter Asymmetry

Nature of Dark Matter

Origin of Neutrino Mass

Origin of EW Scale

Origin of Flavor

Exploring the Unknown

高能前沿重大问题：

早期宇宙演化、

**正反物质不对称性、**

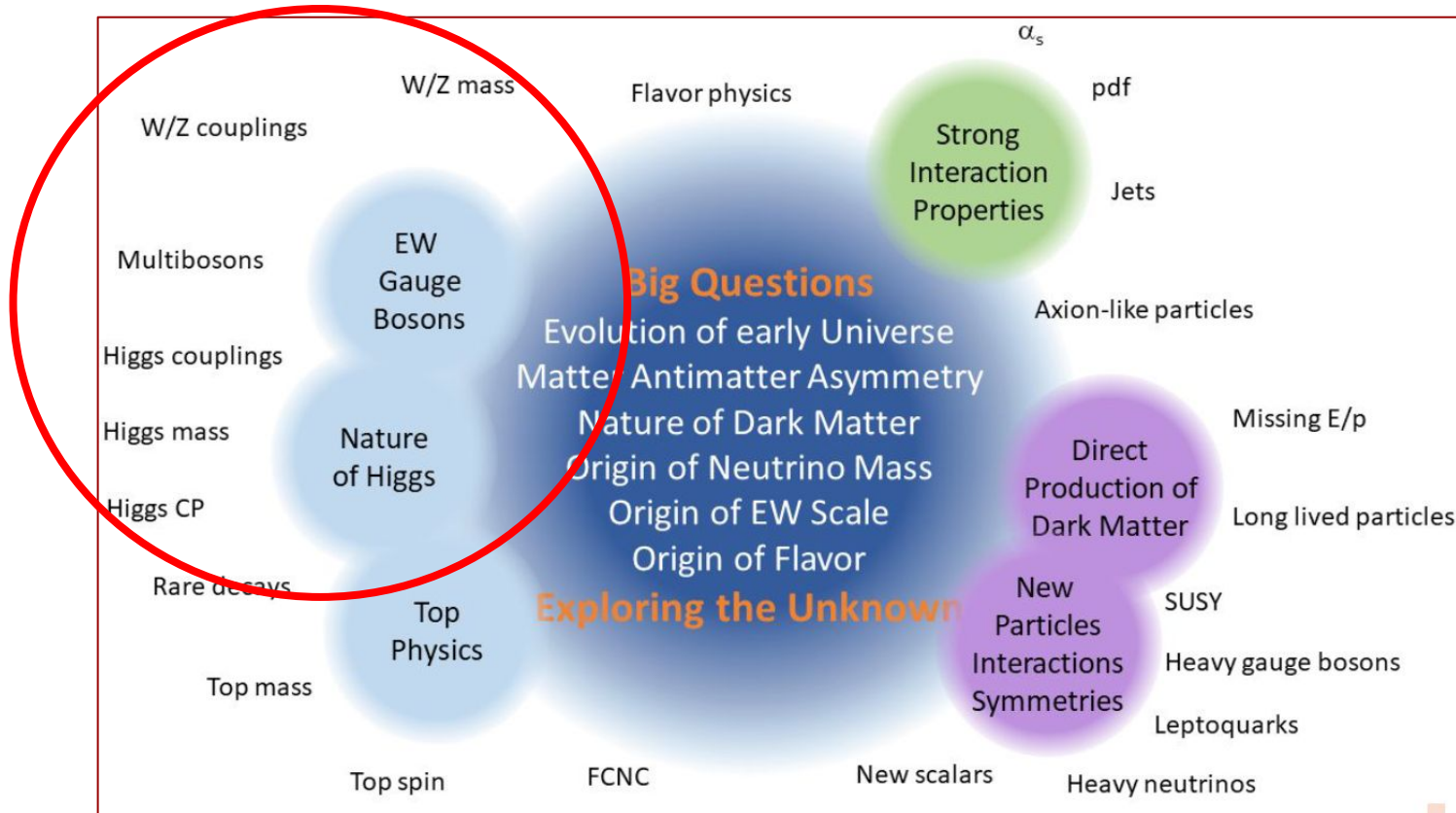
暗物质性质、

中微子质量起源、

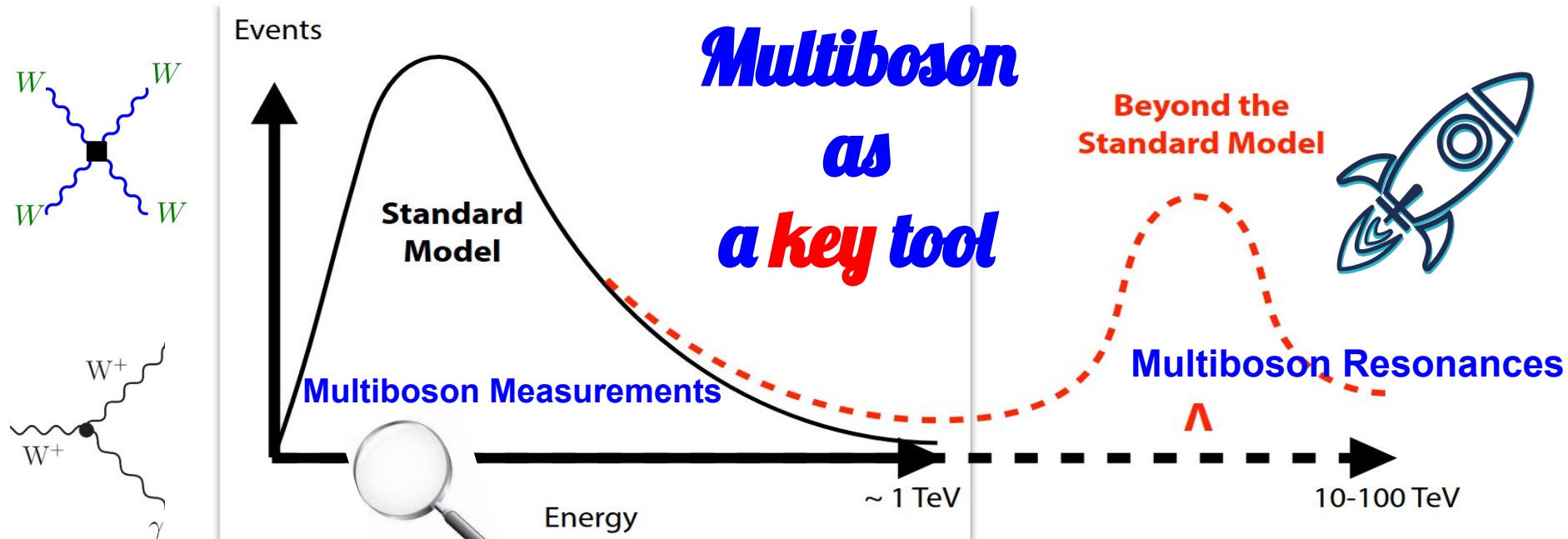
电弱标度起源、

味道起源 等

# Seattle Snowmass Summer Meeting 2022

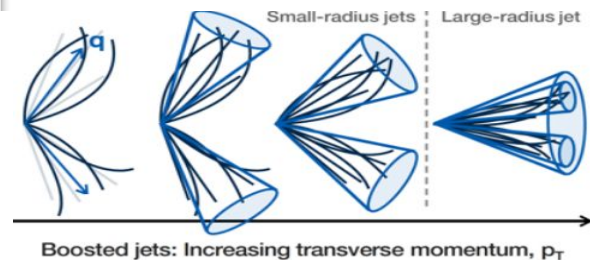


# Direct and Indirect Searches for BSM



Anomalous couplings, EFT (CP even or odd)

$$L_{\text{EFT}} = L_{\text{SM}} + \sum_i \frac{C_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{(6)} + \sum_i \frac{C_i^{(8)}}{\Lambda^4} \mathcal{O}_i^{(8)} + \dots$$



# Great Potential to explore unknown

## The large boson-boson collider

High energy.

High multiplicity.

High opportunities?

Symmetry

Brian Henning

$$|H|^2 \sim (v + h)^2 + \vec{\phi}^2$$

ops that modify HC will induce processes with longitudinal vectors

$$\text{HC: } |H|^2 \mathcal{O}_{\text{SM}} \supset v h \mathcal{O}_{\text{SM}}$$

$$\text{HwH: } |H|^2 \mathcal{O}_{\text{SM}} \supset \vec{\phi}^2 \mathcal{O}_{\text{SM}}$$

## Higgs Couplings without the Higgs

		HC	HwH	Growth
$\kappa_I$	$\mathcal{O}_{y_i}$			$\sim (E^2/\Lambda^2)$
$\kappa_\lambda$	$\mathcal{O}_6$			$\sim (vE/\Lambda^2)$
$\kappa_{Z\gamma}$ $\kappa_{\gamma\gamma}$ $\kappa_V$	$\mathcal{O}_{WW}$ $\mathcal{O}_{BB}$ $\mathcal{O}_r$			$\sim (E^2/\Lambda^2)$
$\kappa_g$	$\mathcal{O}_{gg}$			$\sim (E^2/\Lambda^2)$

# Rich Results from Multiboson Measurements

## Stair to X

VV

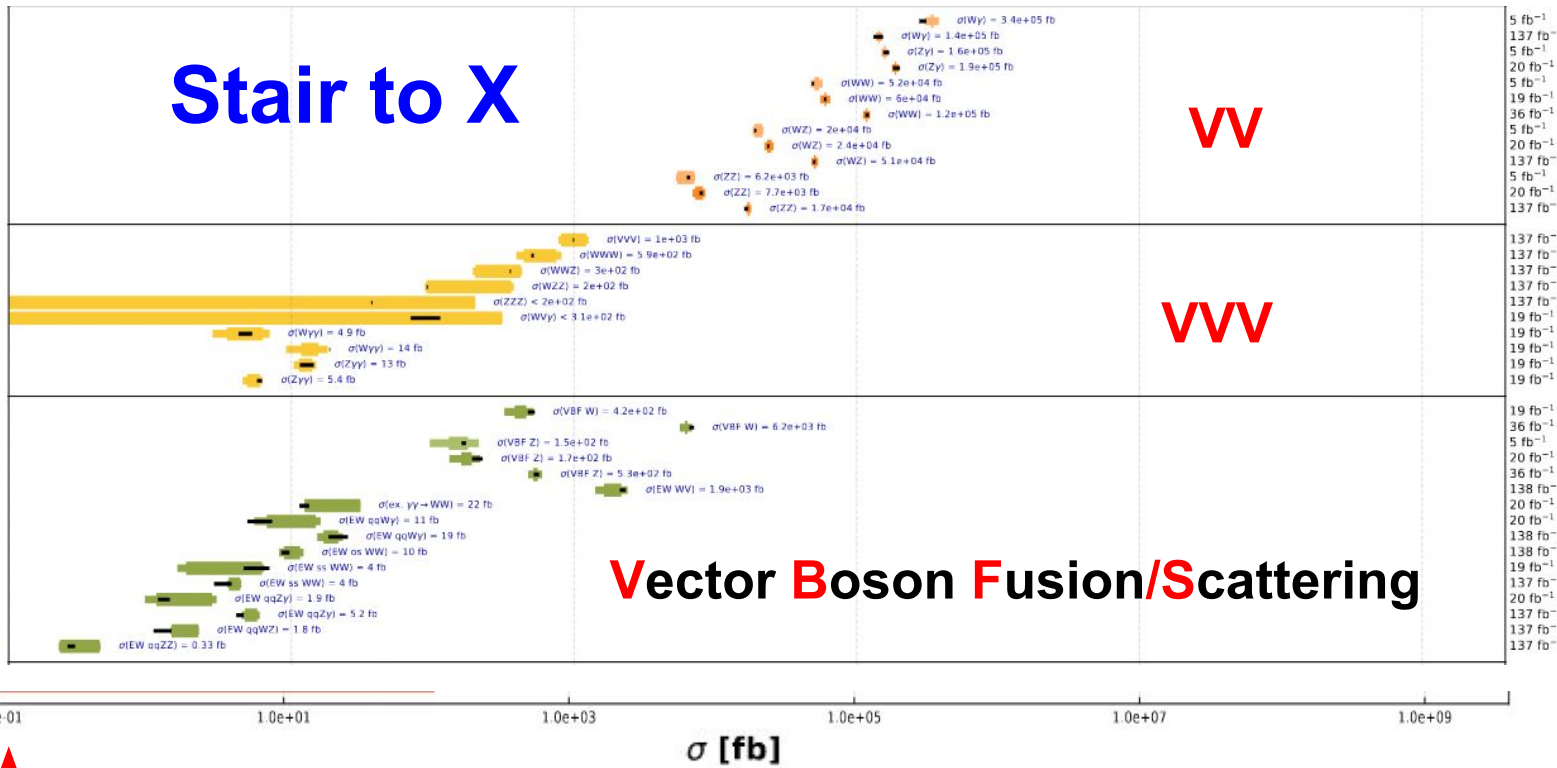
VVV

Vector Boson Fusion/Scattering

Wγ	7 TeV	PRD 89 [2014] 092005
Wγ	13 TeV	PRL 126 252002 [2021]
Zγ	7 TeV	PRD 89 [2014] 092005
Zγ	8 TeV	JHEP 04 (2015) 164
WW	7 TeV	EPJC 73 (2013) 2610
WW	8 TeV	EPJC 75 (2015) 401
WW	13 TeV	PRD 102 092001 [2020]
WZ	7 TeV	EPJC 77 (2017) 236
WZ	8 TeV	EPJC 77 (2017) 236
WZ	13 TeV	Submitted to JHEP
ZZ	7 TeV	JHEP 01 (2013) 063
ZZ	8 TeV	PLB 740 (2015) 250
ZZ	13 TeV	EPJC 81 (2021) 200

VVV	13 TeV	PRL 125 151802 [2020]
WWW	13 TeV	PRL 125 151802 [2020]
WWZ	13 TeV	PRL 125 151802 [2020]
WZZ	13 TeV	PRL 125 151802 [2020]
ZZZ	13 TeV	PRL 125 151802 [2020]
WVγ	8 TeV	PRD 90 032008 [2014]
Wγγ	8 TeV	JHEP 10 (2017) 072
Wγγ	13 TeV	JHEP 10 (2021) 174
Zγγ	8 TeV	JHEP 10 (2017) 072
Zγγ	13 TeV	JHEP 10 (2021) 174

VBF W	8 TeV	JHEP 11 (2016) 147
VBF W	13 TeV	EPJC 80 (2020) 43
VBF Z	7 TeV	JHEP 10 (2013) 101
VBF Z	8 TeV	EPJC 75 (2015) 56
VBF Z	13 TeV	EPJC 78 (2018) 589
EW WW	13 TeV	Submitted to PLB
ex γγ → WW	8 TeV	JHEP 08 (2016) 119
EW qqWγ	8 TeV	JHEP 06 (2017) 106
EW qqWγ	13 TeV	SMP 21-011
EW ss WW	13 TeV	Submitted to PLB
EW ss WW	8 TeV	PRL 114 051801 [2015]
EW ss WW	13 TeV	PRL 120 081801 [2018]
EW qqZγ	8 TeV	PLB 770 (2017) 380
EW qqZγ	13 TeV	PRD 104 072001 [2021]
EW qqWZ	13 TeV	PLB 809 (2020) 135/10
EW qqZZ	13 TeV	PLB 812 (2020) 135992



↑  
0.1 fb

[CMS](#) SM Summary Plot 2022/9

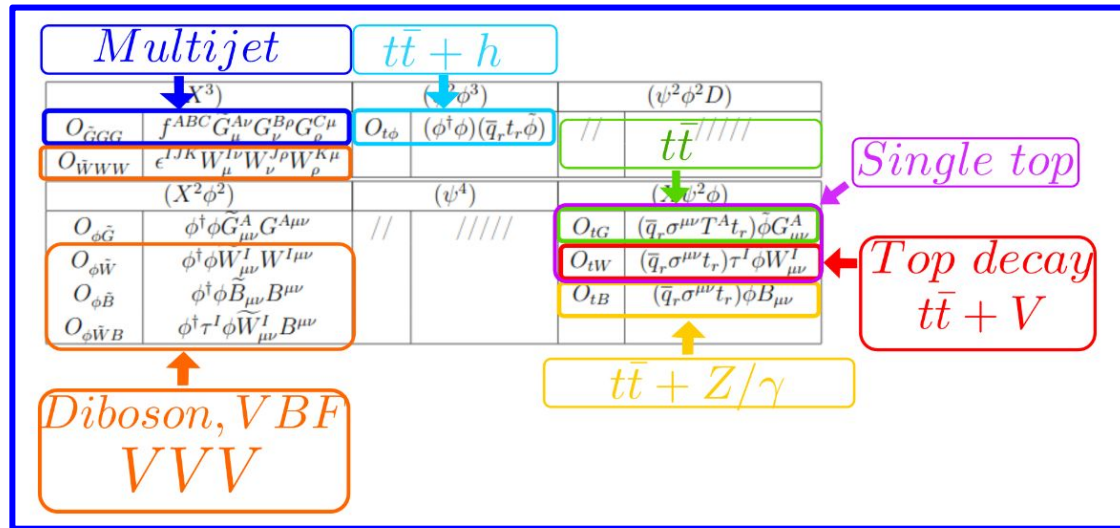
(see also [ATLAS](#) )

# CP Violation in di-boson...

**SMEFT** (e.g.: [Celine Degrande](#), [Julien Toucheque](#)): 10 CP-odd operators integrated in a FeynRules model with massless fermions and UFO package ready to use in MC event generators.

Impose  $U(1)^{14}$  symmetry

Hermitian and non-Hermitian operators



## EWDim6/HISZ

$$\delta\mathcal{L}_{AC} = \frac{c_{www} \text{Tr}[W_{\mu\nu} W^{\nu\rho} W_{\rho}^{\mu}] + c_w (D_{\mu}\Phi)^{\dagger} W^{\mu\nu} (D_{\nu}\Phi) + c_b (D_{\mu}\Phi)^{\dagger} B^{\mu\nu} (D_{\nu}\Phi)}{\Lambda^2} + \frac{\tilde{c}_{www} \text{Tr}[\tilde{W}_{\mu\nu} W^{\nu\rho} W_{\rho}^{\mu}] + \tilde{c}_w (D_{\mu}\Phi)^{\dagger} \tilde{W}^{\mu\nu} (D_{\nu}\Phi)}{\Lambda^2}$$

# Different conventions...

## SMEFT

## EWDim6/HISZ

Wilson Coefficient	Operator
$C_W$ ( $C_{WWW}$ )	$\epsilon^{abc} W_\mu^{a\nu} W_\nu^{b\rho} W_\rho^{c\mu}$
$C_{HD}$	$ H^\dagger(D_\mu\Phi) ^2$
$C_{HWB}$	$H^\dagger\sigma^a\Phi W_{\mu\nu}^a B^{\mu\nu}$
$C_{Hl}^{(1)}$	$(H^\dagger i\overleftrightarrow{D}_\mu H)(\bar{l}_p\gamma^\mu l_r)$
$C_{Hl}^{(3)}$	$(H^\dagger i\overleftrightarrow{D}_\mu H)(\bar{l}_p\tau^I\gamma^\mu l_r)$
$C_{Hq}^{(1)}$	$(H^\dagger i\overleftrightarrow{D}_\mu H)(\bar{q}_p\gamma^\mu q_r)$
$C_{Hq}^{(3)}$	$(H^\dagger i\overleftrightarrow{D}_\mu H)(\bar{q}_p\tau^I\gamma^\mu q_r)$
$C_{Hud}$	$i\left(\tilde{H}^\dagger D_\mu H\right)\bar{u}_R\gamma^\mu d_R$
$C_{ll}$	$(\bar{l}_p\gamma_\mu l_r)(\bar{l}_s\gamma^\mu l_t)$
$C_{Hd}$	$(H^\dagger i\overleftrightarrow{D}_\mu H)(\bar{d}_p\gamma^\mu d_r)$

Table 1: The various other dim-6 EFT operators.

The minimal set of dimension-6 operators explored in CMS in  $WW$  and  $WZ$  final states are the following:

$$\mathcal{O}_{WWW} = \text{Tr} [W_{\mu\nu}W^{\nu\rho}W_\rho^\mu] \quad (1.1)$$

$$\mathcal{O}_W = (D_\mu\Phi)^\dagger\overleftrightarrow{W}^{\mu\nu}(D_\nu\Phi) \quad (1.2)$$

$$\mathcal{O}_B = (D_\mu\Phi)^\dagger\overleftrightarrow{B}^{\mu\nu}(D_\nu\Phi) \quad (1.3)$$

which are the three C and P conserving operators. In addition, there are two additional C and P violating operators are:

$$\mathcal{O}_{\tilde{W}WW} = \text{Tr} [\tilde{W}_{\mu\nu}W^{\nu\rho}W_\rho^\mu] \quad (1.4)$$

$$\mathcal{O}_{\tilde{W}} = (D_\mu\Phi)^\dagger\tilde{W}^{\mu\nu}(D_\nu\Phi) \quad (1.5)$$

These operators seem to be defined in an *ad-hoc* basis first making their appearance in Ref. [1] and subsequently in Ref. [2].

[1] K. Hagiwara et al. “Low energy effects of new interactions in the electroweak boson sector” [Phy. Rev. D Vol 48 No. 5](#)

[2] C. Degrande et al. “Effective Field Theory: A Modern Approach to Anomalous Couplings” [arXiv:1205.4231](#)

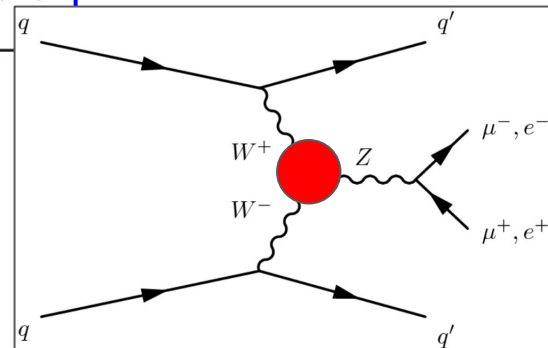
[Ref](#)

$$\mathcal{O}_{WWW} = \frac{g^3}{4}Q_W,$$



# ATLAS VBF Z

Wilson coefficient	Includes $ \mathcal{M}_{d6} ^2$	95% confidence interval [ $\text{TeV}^{-2}$ ]		p-value (SM)
		Expected	Observed	
$c_W/\Lambda^2$	No	[-0.30, 0.30]	[-0.19, 0.41]	45.9%
	Yes	[-0.31, 0.29]	[-0.19, 0.41]	43.2%
$\tilde{c}_W/\Lambda^2$	No	[-0.12, 0.12]	[-0.11, 0.14]	82.0%
	Yes	[-0.12, 0.12]	[-0.11, 0.14]	81.8%
$c_{HWB}/\Lambda^2$	No	[-2.45, 2.45]	[-3.78, 1.13]	29.0%
	Yes	[-3.11, 2.10]	[-6.31, 1.01]	25.0%
$\tilde{c}_{HWB}/\Lambda^2$	No	[-1.06, 1.06]	[0.23, 2.34]	1.7%
	Yes	[-1.06, 1.06]	[0.23, 2.35]	1.6%



The 95% confidence intervals for the CP-even and CP-odd operators can be translated into the HISZ basis [83–85] and be compared with previous ATLAS and CMS results. The observed and expected 95% confidence intervals for the  $c_{WWW}/\Lambda^2$  Wilson coefficient are  $[-2.7, 5.8] \text{ TeV}^{-2}$  and  $[-4.4, 4.1] \text{ TeV}^{-2}$ , respectively. The observed and expected 95% confidence intervals for the  $\tilde{c}_{WWW}/\Lambda^2$  Wilson coefficient are  $[-1.6, 2.0] \text{ TeV}^{-2}$  and  $[-1.7, 1.7] \text{ TeV}^{-2}$  respec-

$$\mathcal{O}_{WWW} = \frac{g^3}{4} Q_W,$$

**CWWW:**

**EWDim6/SMEFT~14.2**

# Current LHC related limits

- 1 ATLAS VBF W
- 2 ATLAS VBF Z

Operators	$\sigma(pp \rightarrow Wjj)^1$	$\Delta\phi_{jj}(pp \rightarrow Zjj)^2$	EDMs <sup>3</sup>
$\mathcal{O}_{\widetilde{WWW}}$	[-14, 14] (expected)	[-0.12, 0.12] (expected)	$\leq 1.74 \cdot 10^{-4}$
	[-11, 11] (measured)	[-0.11, 0.14] (measured)	
$\mathcal{O}_{\phi\widetilde{WB}}$	//	[-1.06, 1.06] (expected)	$\leq 5.57 \cdot 10^{-6}$
	//	[-0.23, 2.34] (measured)	

Table: Collection of the constraints on the two dimension-six operators with  $\Lambda = 1\text{TeV}$  at 95% CL.

- 3: CMS WZ

Parameter	95% CI, exp. ( $\text{TeV}^{-2}$ )	95% CI, obs. ( $\text{TeV}^{-2}$ )	Best fit, obs. ( $\text{TeV}^{-2}$ )
$c_w/\Lambda^2$	[-2.0, 1.3]	[-2.5, 0.3]	-1.3
$c_{www}/\Lambda^2$	[-1.3, 1.3]	[-1.0, 1.2]	0.1
$c_b/\Lambda^2$	[-86, 125]	[-43, 113]	44
$\tilde{c}_{www}/\Lambda^2$	[-0.76, 0.65]	[-0.62, 0.53]	-0.03
$\tilde{c}_w/\Lambda^2$	[-46, 46]	[-32, 32]	0

# Current SM related limits

## 4 ATLAS WW (2016)

**Table 6** The expected and observed 95% CL intervals for the anomalous coupling parameters of the EFT model [109]. There is a change in convention relative to Ref. [6] that changes the sign on some of these parameters

Parameter	Observed 95% CL [TeV <sup>-2</sup> ]	Expected 95% CL [TeV <sup>-2</sup> ]
$c_{WWW}/\Lambda^2$	[-3.4, 3.3]	[-3.0, 3.0]
$c_W/\Lambda^2$	[-7.4, 4.1]	[-6.4, 5.1]
$c_B/\Lambda^2$	[-21, 18]	[-18, 17]
$c_{\tilde{W}WW}/\Lambda^2$	[-1.6, 1.6]	[-1.5, 1.5]
$c_{\tilde{W}}/\Lambda^2$	[-76, 76]	[-91, 91]

shell Z bosons. These are described by two CP-violating ( $f_4^V$ ) and two CP-conserving ( $f_5^V$ ) parameters, where V = Z or  $\gamma$ .

$$\begin{aligned}
 -0.0012 < f_4^Z < 0.0010, & \quad -0.0010 < f_5^Z < 0.0013, \\
 -0.0012 < f_4^\gamma < 0.0013, & \quad -0.0012 < f_5^\gamma < 0.0013.
 \end{aligned}$$

## 5 CMS W $\gamma$ (2016)

Another one with full Run2 but only CP-even

Coefficient	Exp. lower	Exp. upper	Obs. lower	Obs. upper
$c_{WWW}/\Lambda^2$	-0.85	0.87	-0.90	0.91
$c_B/\Lambda^2$	-46	45	-40	41
$c_{\tilde{W}WW}/\Lambda^2$	-0.43	0.43	-0.45	0.45
$c_{\tilde{W}}/\Lambda^2$	-23	22	-20	20

## 6 CMS ZZ (2016)

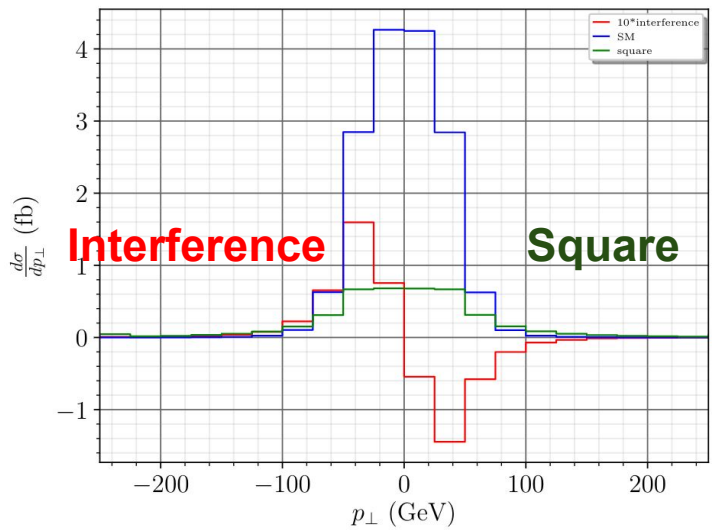
## 7 ATLAS ZZ (Full Run2)

[aNTGC](#)

aNTGC parameter	Interference only		Full	
	Expected	Observed	Expected	Observed
$f_2^Z$	[-0.16, 0.16]	[-0.12, 0.20]	[-0.013, 0.012]	[-0.012, 0.012]
$f_\gamma^4$	[-0.30, 0.30]	[-0.34, 0.28]	[-0.015, 0.015]	[-0.015, 0.015]

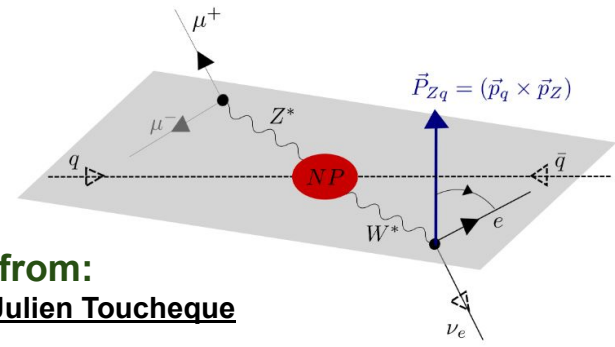
# interference, BSM, asymmetry, polarization, Optimized observables...

$p p \rightarrow \mu^- \mu^+ e^+ \nu_e$  for  $C_{WW\widetilde{W}} = 1$  and  $\Lambda = 1\text{TEV}$  at 13 TEV



Those squared amplitudes are CP-even and do contribute to CP-even observables but are more suppressed in  $1/\Lambda$ . Therefore, analyzing CP-odd operators with the total cross-section is expected to lead to less stringent constraints on their Wilson coefficients but the main drawback is that they do not test whether CP is actually broken. In general, conventional CP-even observables are not suited to efficiently probe CP violating effects since they present no or small variations from expected SM simulations by relying on  $\Lambda^{-4}$ -suppressed effects [33-35].

## Triple product



Pheno studies from:  
Celine Degrande, Julien Toucheque

- Definition :

$$p_{\perp}(p_e, p_q) = \vec{p}_e \cdot (\vec{p}_Z \times \vec{p}_q)$$

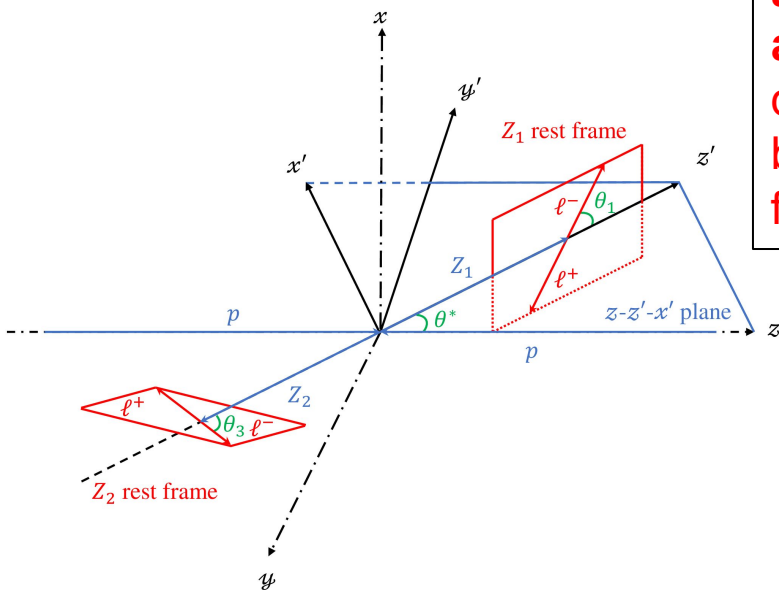
**However,  
 we are not  
 always  
 sensitive to  
 interference  
 yet!**

In current LHC di-boson analyses, CP-odd either ignored, or treated same as CP-even



Many talks from this workshop!

## 7 ATLAS ZZ (Full Run2)



**Polar &/or azimuthal angles from the diboson rest and boson decay frames**

CMS WG (Full Run2)  
only for CP-even operator though

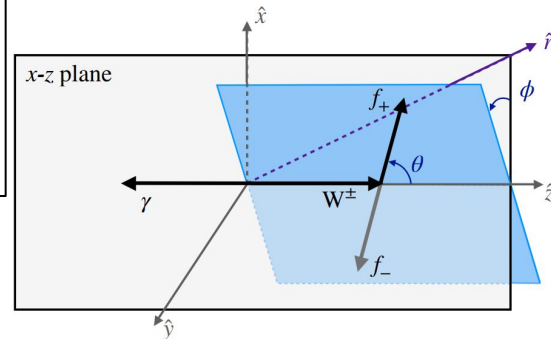


Figure 2: Scheme of the special coordinate system for  $W^\pm\gamma$  production, defined by a Lorentz boost to the center-of-mass frame along the direction  $\hat{r}$ . The  $z$  axis is chosen as the  $W^\pm$  boson direction in this frame, and  $y$  is given by  $\hat{z} \times \hat{r}$ . The  $W^\pm$  boson decay plane is indicated in blue, where the labels  $f_+$  and  $f_-$  refer to positive and negative helicity final-state fermions. The angles  $\phi$  and  $\theta$  are the azimuthal and polar angles of  $f_+$ .

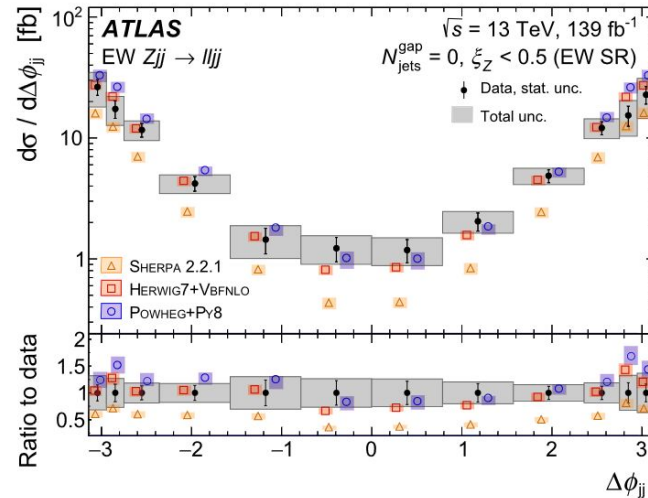
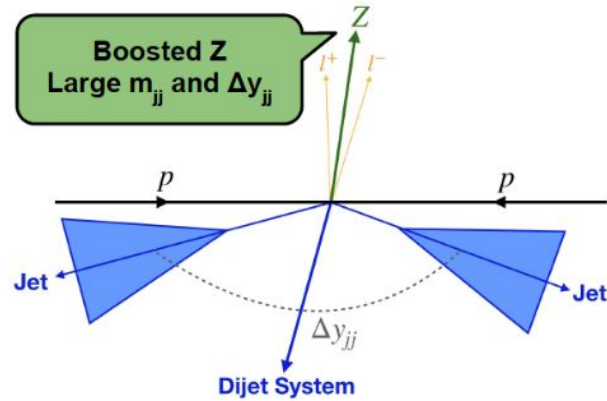
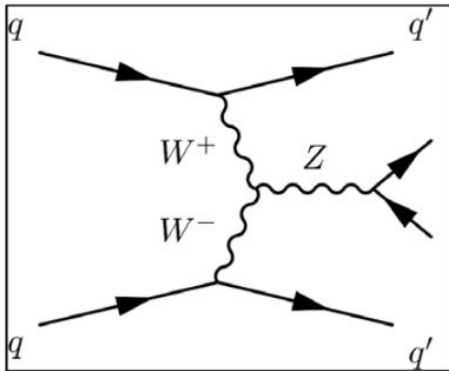
To improve the sensitivity, the two CP-sensitive angles  $\theta_1(\theta_3)$  and  $\phi_1(\phi_3)$  are combined to form an angular observable  $T_{yz,1(3)} = \sin \phi_{1(3)} \times \cos \theta_{1(3)}$  which maximises the asymmetry for each  $Z$  boson system.

The OO defined for the CP study combines the CP-sensitive polar and azimuthal angles of both  $Z$  boson systems, providing additional CP sensitivity from shape differences between the SM and aNTGC predictions. The CP-sensitive polar angles  $\theta_1(\theta_3)$  for the  $Z_1(Z_2)$  boson are already defined in Section 6.1. The CP-sensitive azimuthal angles  $\phi_1$  and  $\phi_3$  are reconstructed in a reference frame that allows a direct measure of the  $Z$  boson spin as discussed in Ref. [24, 89] and are illustrated in Figure 2. The CP-sensitive azimuthal angle  $\phi_1(\phi_3)$  is the azimuthal angle of the negative lepton in the  $Z_1(Z_2)$  rest frame in this new axis system. The differential cross-sections for  $\theta_1(\theta_3)$  and  $\phi_1(\phi_3)$  are symmetric in the SM but asymmetric in the presence of the two CP-odd aNTGC.

**However,  
we are not  
always  
sensitive to  
interference  
yet!**

# Example 1: ATLAS VBF Z+2Jets

- Select events consistent with EW Zjj topology
  - Opposite charge, same flavor lepton pair
  - Dijet system:  $m_{jj} > 1 \text{ TeV}$ ,  $|\Delta y_{jj}| > 2.0$
  - Z boson centrally produced relative to dijet
  - Z boson & dijet required to be approximately balanced in transverse momentum



# Example 1: ATLAS VBF Z+2 Jets

- Constraints are placed on dimension-6 operators in Warsaw basis

- CP-even: ( $O_W, O_{HWB}$ )

- CP-odd: ( $\tilde{O}_W, \tilde{O}_{HWB}$ )

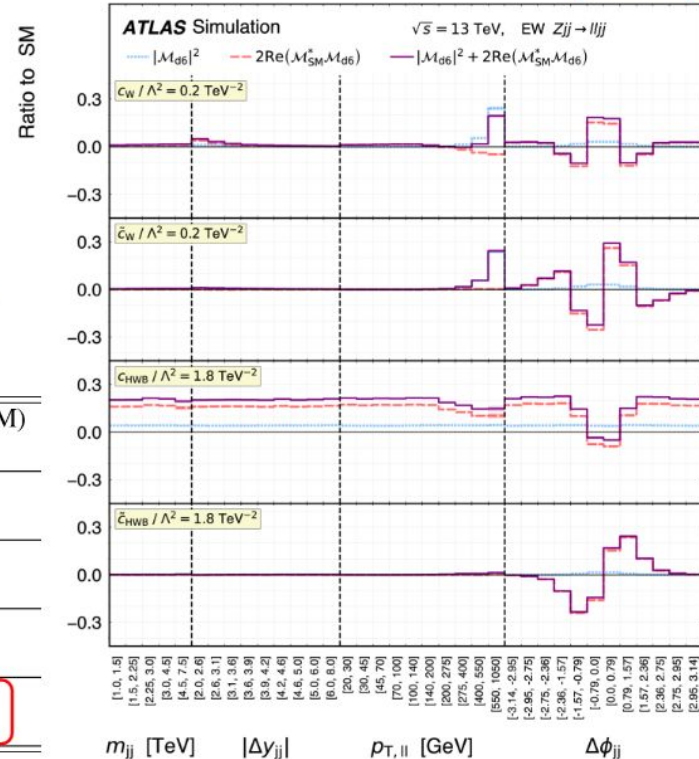
- $\Delta\phi_{jj}$  is more sensitive to anomalous interactions and therefore used to constrain Wilson coefficients

- Constraints on dimension-6 operators, derived with and without pure dimension-6 terms, show much less sensitivity from the pure dimension-6 terms

Wilson coefficient	Includes $ \mathcal{M}_{d6} ^2$	95% confidence interval [TeV <sup>-2</sup> ]		p-value (SM)
		Expected	Observed	
$c_W/\Lambda^2$	no	[-0.30, 0.30]	[-0.19, 0.41]	45.9%
	yes	[-0.31, 0.29]	[-0.19, 0.41]	43.2%
$\tilde{c}_W/\Lambda^2$	no	[-0.12, 0.12]	[-0.11, 0.14]	82.0%
	yes	[-0.12, 0.12]	[-0.11, 0.14]	81.8%
$c_{HWB}/\Lambda^2$	no	[-2.45, 2.45]	[-3.78, 1.13]	29.0%
	yes	[-3.11, 2.10]	[-6.31, 1.01]	25.0%
$\tilde{c}_{HWB}/\Lambda^2$	no	[-1.06, 1.06]	[0.23, 2.34]	1.7%
	yes	[-1.06, 1.06]	[0.23, 2.35]	1.6%

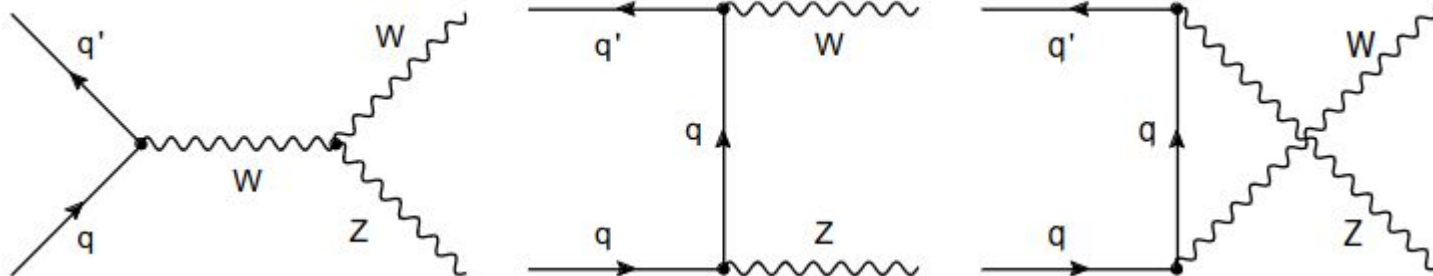
**EFT:**  $\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{c_i}{\Lambda^2} O_i$

$$|\mathcal{M}|^2 = |\mathcal{M}_{\text{SM}}|^2 + 2 \text{Re}(\mathcal{M}_{\text{SM}}^* \mathcal{M}_{d6}) + |\mathcal{M}_{d6}|^2$$





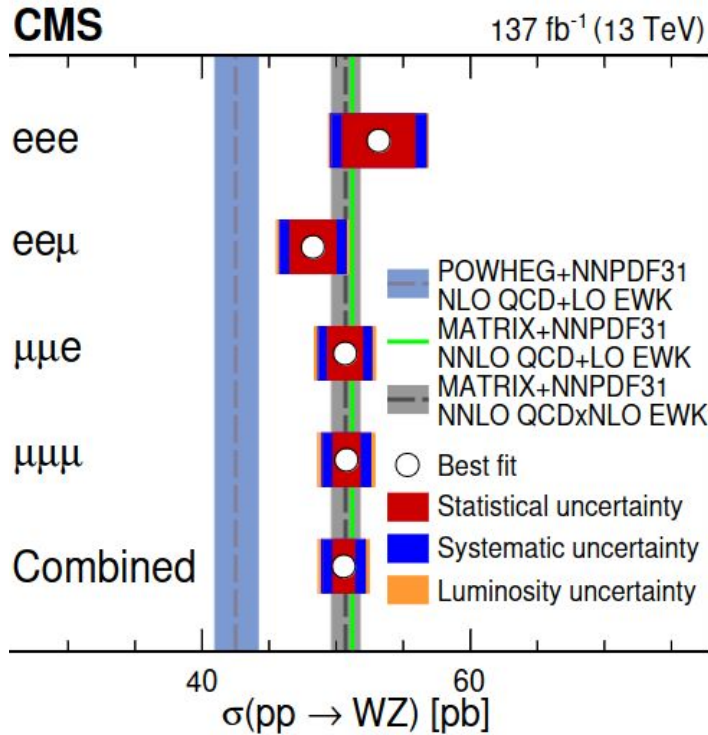
# Example 2: CMS WZ



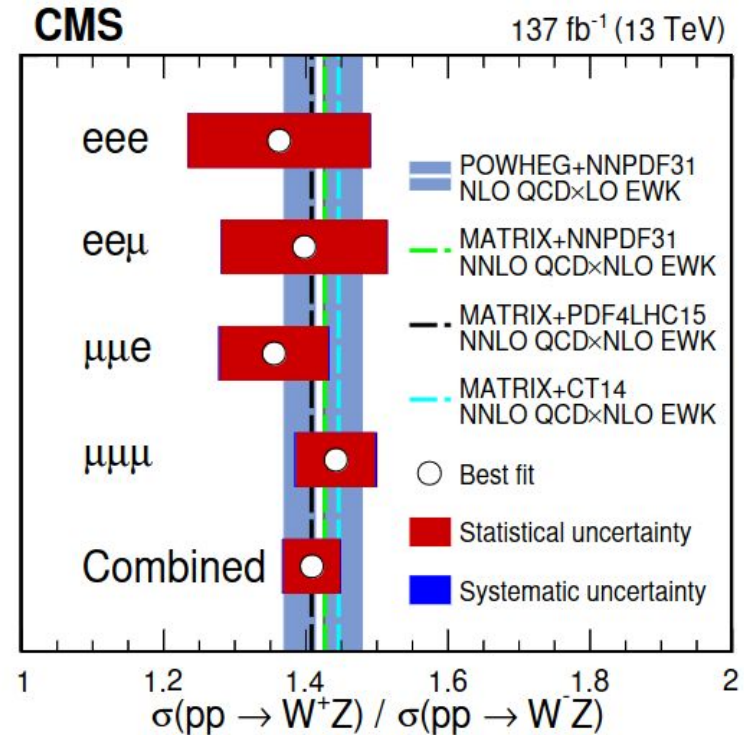
Signal: powheg box (v2.0) NLO (nominal); MadGraph5\_amc@nlo 0+1jet FxFx (alternative)

Region	$N_\ell$	$p_T\{\ell_{Z1}, \ell_{Z2}, \ell_W, \ell_4\}$	$N_{\text{OSSF}}$	$ M(\ell_{Z1}, \ell_{Z2}) - m_Z $	$p_T^{\text{miss}}$	$N_{\text{b tag}}$	$\min(M(\ell\ell'))$	$M(\ell_{Z1}, \ell_{Z2}, \ell_W)$
SR	=3	$>\{25, 10, 25, -\}$ GeV	$\geq 1$	$<15$ GeV	$>30$ GeV	=0	$>4$ GeV	$>100$ GeV
CR-ZZ	=4	$>\{25, 10, 25, 10\}$ GeV	$\geq 1$	$<15$ GeV	—	=0	$>4$ GeV	$>100$ GeV
CR-t $\bar{t}$ Z	=3	$>\{25, 10, 25, -\}$ GeV	$\geq 1$	$<15$ GeV	$>30$ GeV	$>0$	$>4$ GeV	$>100$ GeV
CR-conv	=3	$>\{25, 10, 25, -\}$ GeV	$\geq 1$	—	$\leq 30$ GeV	=0	$>4$ GeV	$<100$ GeV

# Example 2: CMS WZ



**Total cross section** measured in a total phase space: 3 light leptons and  $60 \text{ GeV} < m_Z < 120 \text{ GeV}$  at gen level phase space.



**Asymmetry ratio** driven by the statistical precision. Effects on PDF also studied using the Bayesian reweighting technique.

## Example 2: CMS WZ

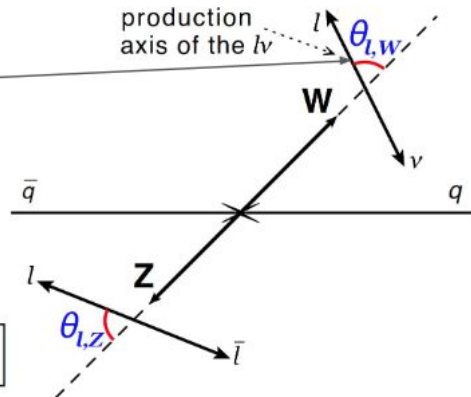
→ Instead of measuring the spin density matrix, experimental searches have focused on the -related- polarization fractions  $f_L, f_R, f_0$  (left, right, longitudinal).

→ The key observable is the “polarization angle”  $\theta_V$ .

→ At LO in EWK, a quadratic dependance of the differential cross-section with respect to  $\cos(\theta_V)$  is expected:

$$\frac{d\sigma}{\sigma d \cos \theta^{W\pm}} = \frac{3}{8} \left[ (1 \mp \cos(\theta^{W\pm}))^2 f_L^W + (1 \pm \cos(\theta^{W\pm}))^2 f_R^W + 2 \sin^2(\theta^{W\pm}) f_0^W \right]$$

$$\frac{d\sigma}{\sigma d \cos \theta^Z} = \frac{3}{8} \left[ (1 + \cos^2(\theta^Z) + 2c \cos(\theta^Z)) f_L^Z + (1 + \cos^2(\theta^Z) - 2c \cos(\theta^Z)) f_R^Z + 2 \sin^2(\theta^Z) f_0^Z \right]$$



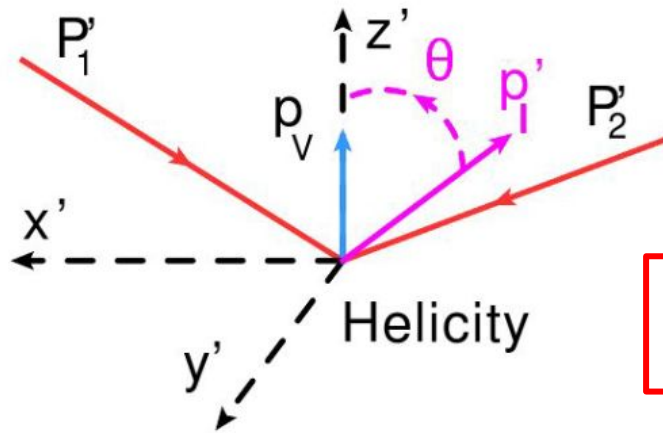
- $f_0$  (longitudinal), and  $f_L$ , and  $f_R$  (transversal) polarization fractions are the measurable quantities.
- The additional constant “c” for the Z accounts for its couplings to both left and right handed fermions.
- Polarization fractions are frame-dependant for massive particles, so **the frame needs to be fixed**.

## Example 2: CMS WZ

- The helicity frame defined in the centre-of mass of the measured gauge boson (W or Z) is used to perform the measurements of the gauge boson polarization fractions.
- Strictly speaking a different frame for the measurement of each of the bosons, as only singly polarized states are studied.

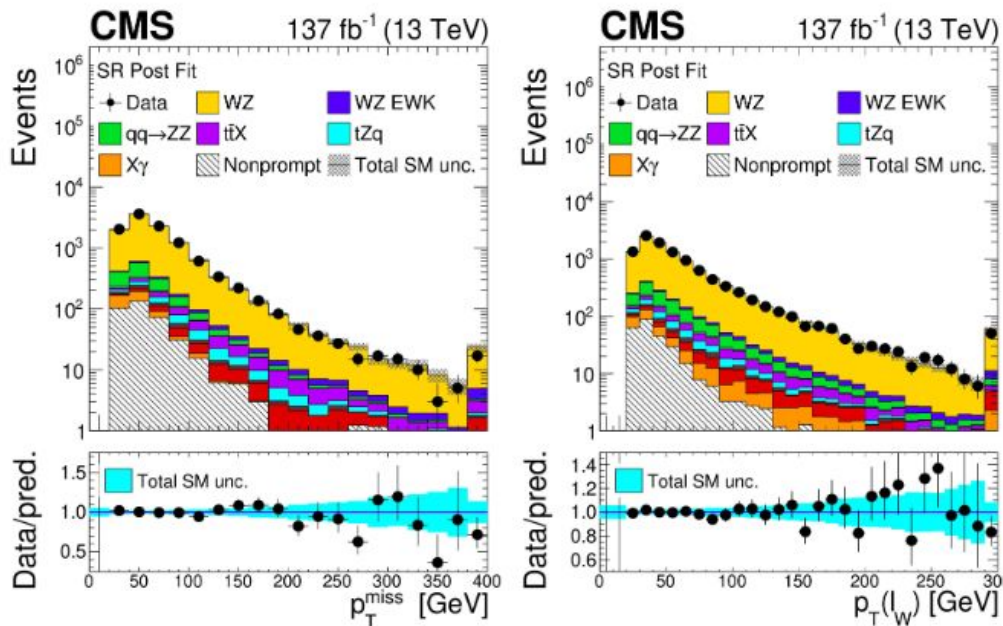
*The helicity frame is obtained in two transformations:*

- 1) Start at the  $pp$  frame ( $O$  frame), and rotate it so the  $W$  ( $Z$ ) boson momentum goes along the  $z$  axis ( $O'$  frame).
- 2) The  $O'$  frame is then boosted so the  $W$  ( $Z$ ) boson is at rest ( $O''$  frame)



-  $\theta$  is then the angle between the lepton and the  $Z$  axis in the  $O''$  frame (helicity frame).

# Example 2: CMS WZ: W reconstruction

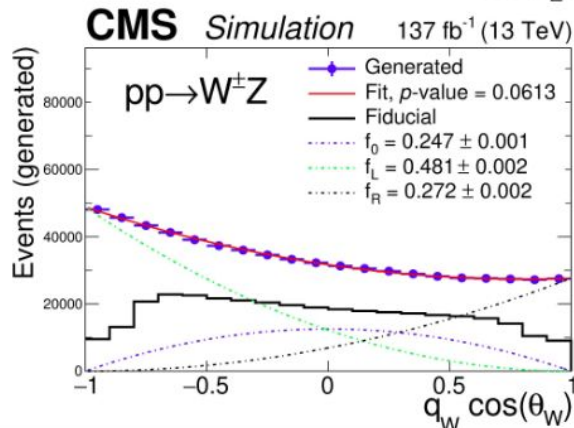
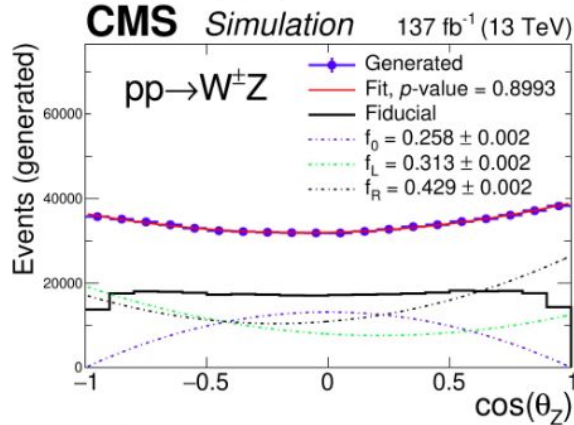


In cases where two real solutions are compatible with the W mass constrain, the one resulting in a lower magnitude of the longitudinal momentum of the neutrino is chosen. If both solutions are complex, their real part is chosen instead.

→ W boson is reconstructed from  $l_W$  and  $p_T^{\text{miss}}$ . →  
 The constraint of  $m(l_W, p_T^{\text{miss}}) = m_W$  is used to  
 solve for the neutrino's  $p_Z$ .

# Example 2: CMS WZ

## Building polarized templates



→ The procedure is based on the reweighting of a POWHEG+Pythia sample based on the generator-level  $\cos(\theta_V)$  distributions to obtain “pure” polarized templates:

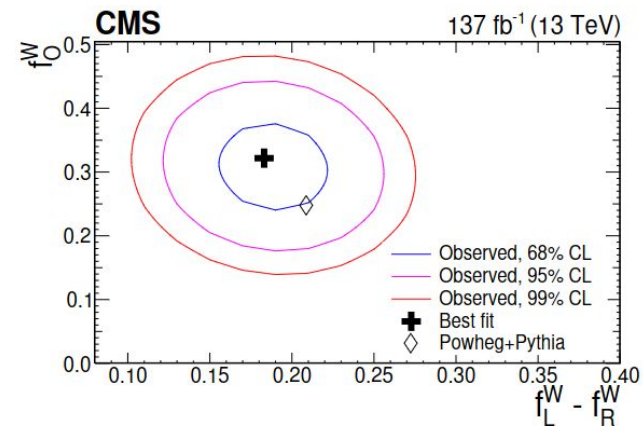
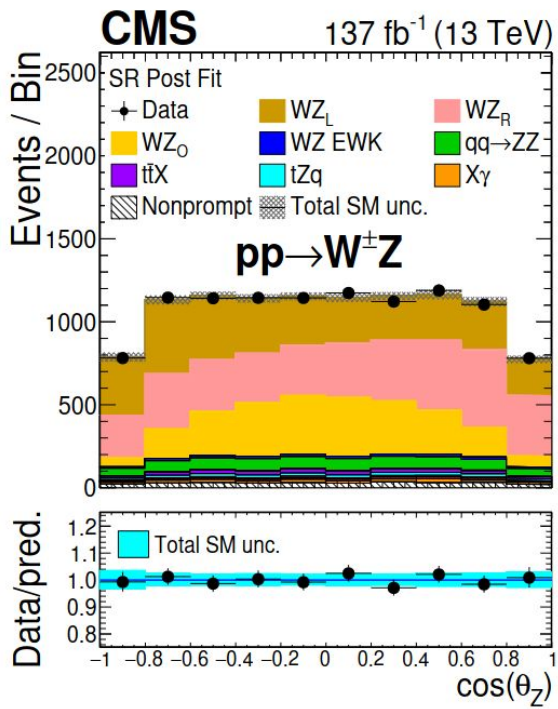
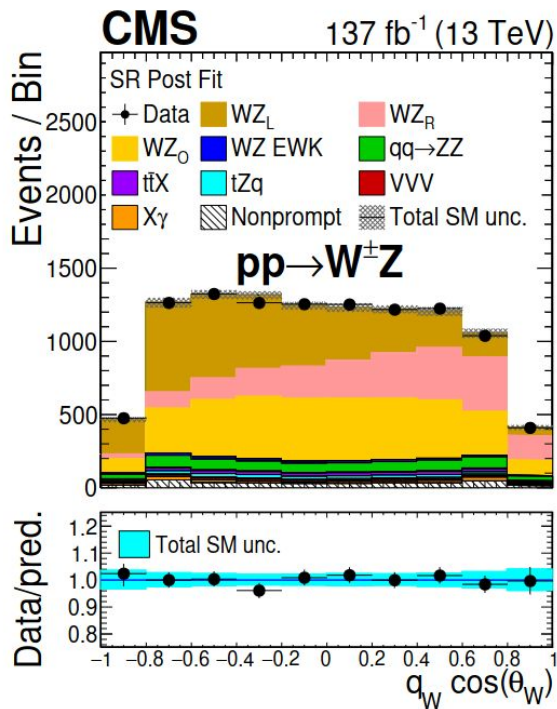
→ For example, the event weight for the left-handed W templates:

$$\frac{\frac{3}{8} (1 \mp \cos \theta_{\ell, W})^2}{\frac{3}{8} f_L^{\text{gen.}} (1 \mp \cos \theta_{\ell, W})^2 + \frac{3}{8} f_R^{\text{gen.}} (1 \pm \cos \theta_{\ell, W})^2 + \frac{3}{4} f_0^{\text{gen.}} \sin^2 \theta_{\ell, W}}$$

→ The  $f_0^{\text{gen.}}$ ,  $f_L^{\text{gen.}}$ ,  $f_R^{\text{gen.}}$  quantities can be obtained directly by fitting the  $\cos(\theta_V)$  distribution of the whole sample.

→ Fiducial requirements break the quadratic dependance! This fit is not possible at the reco-level.

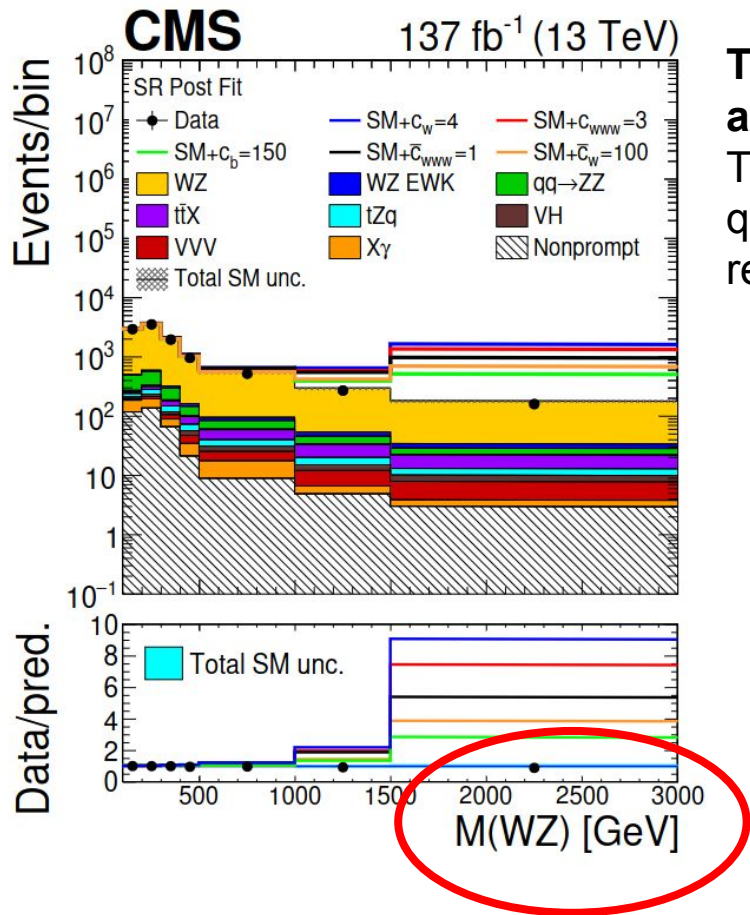
# Example 2: CMS WZ



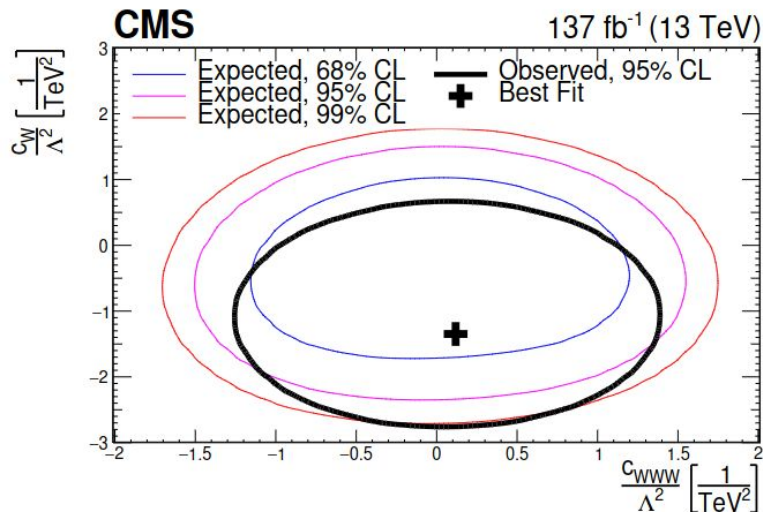
The  $\cos(\theta)$  distributions at the reconstructed are fitted separately for W/Z production.

**First observation of single longitudinally polarized W bosons in WZ production!  $5.6 \sigma$  ( $4.3\sigma$ ) obs (exp).**

# Example 2: CMS WZ: aGCs



The longitudinal momentum and mass of the neutrino are assumed to be zero in the computation of  $M(WZ)$ . This choice aims to avoid further correlation of the  $M(WZ)$  quantity with the MET variable, which has a worse resolution than the leptonic momenta.



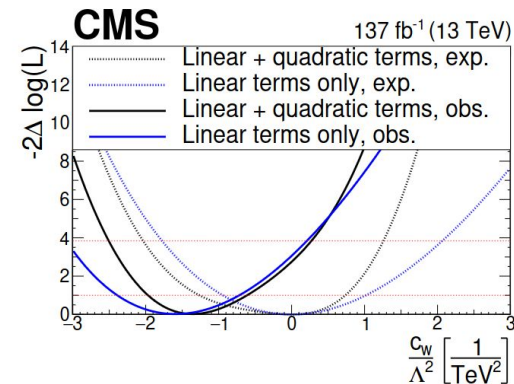


# Example 2: CMS WZ:aGCs

Parameter	95% CI, exp. ( $\text{TeV}^{-2}$ )	95% CI, obs. ( $\text{TeV}^{-2}$ )	Best fit, obs. ( $\text{TeV}^{-2}$ )
$c_w/\Lambda^2$	[-2.0, 1.3]	[-2.5, 0.3]	-1.3
$c_{www}/\Lambda^2$	[-1.3, 1.3]	[-1.0, 1.2]	0.1
$c_b/\Lambda^2$	[-86, 125]	[-43, 113]	44
$\tilde{c}_{www}/\Lambda^2$	[-0.76, 0.65]	[-0.62, 0.53]	-0.03
$\tilde{c}_w/\Lambda^2$	[-46, 46]	[-32, 32]	0

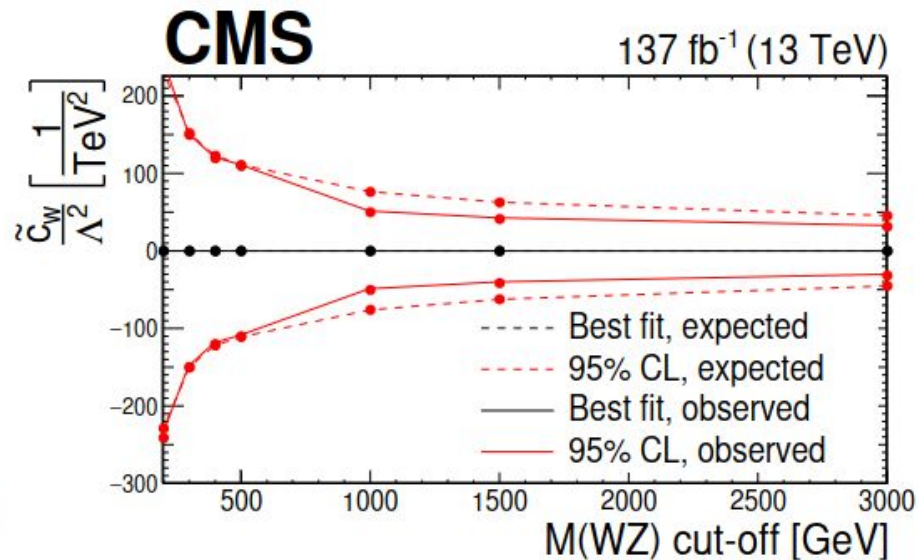
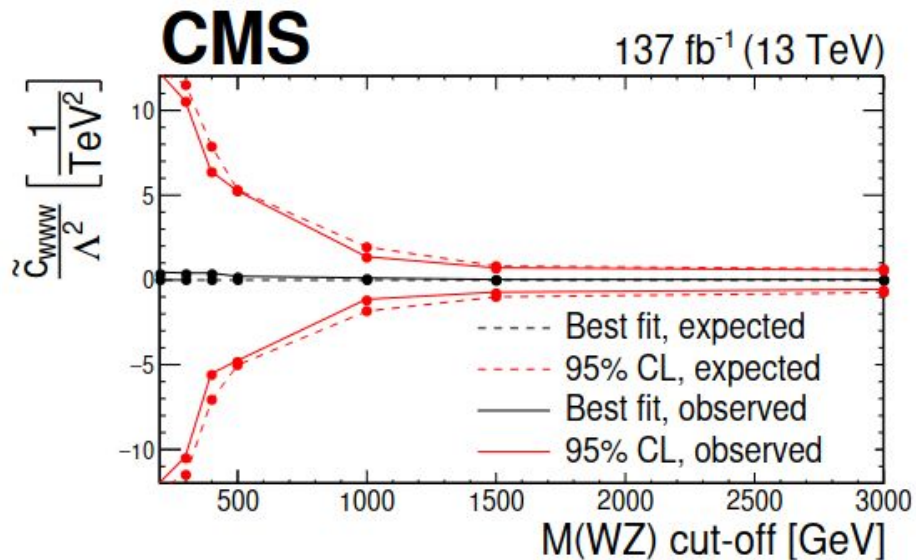
Parameter	95% CI, exp. ( $\text{TeV}^{-2}$ )	95% CI, obs. ( $\text{TeV}^{-2}$ )	Best fit, obs. ( $\text{TeV}^{-2}$ )
$c_w/\Lambda^2$	[-1.8, 2.1]	[-3.1, 0.3]	-1.6
$c_{www}/\Lambda^2$	[-8.5, 8.5]	[-4.2, 14.2]	5.5
$c_b/\Lambda^2$	[-200, 180]	[10, 380]	200
$\tilde{c}_{www}/\Lambda^2$	[-3.3, 4.1]	[-4.0, 3.6]	-0.6
$\tilde{c}_w/\Lambda^2$	—	—	—

**Both the purely dimension-eight BSM contribution as well as the dimension-six interference term are included**



**Only the dimension-six interference term is included**

## Example 2: CMS WZ:aGCs



# Example 3: ATLAS WZ

**WZ rest frame** for joint-polarisation and single boson polarisation (so-called Modified Helicity frame)

- Allow to meaningfully **compare** both
- **Longitudinal fractions** of both bosons have **maximum decorrelation**

**Defined from the joint spin density matrix:**

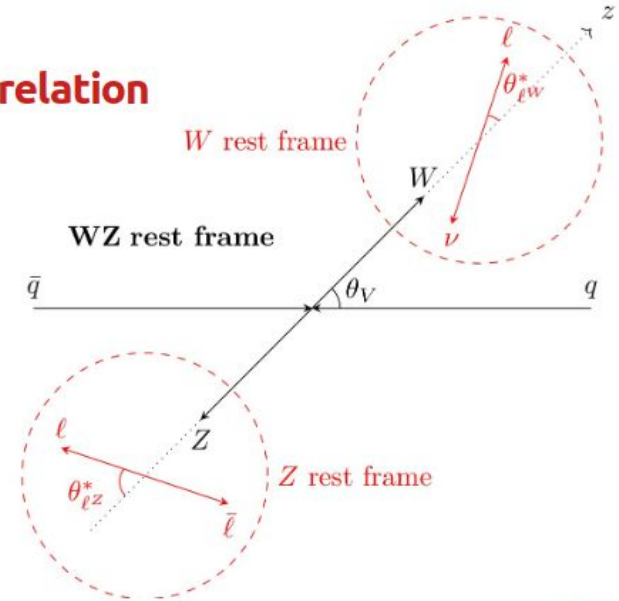
$$\rho_{\lambda_W \lambda'_W \lambda_Z \lambda'_Z} \equiv \frac{1}{C} \times \sum_{\mu_q \mu_{\bar{q}}} F_{\lambda_W \lambda_Z}^{(\mu_q \mu_{\bar{q}})} F_{\lambda'_W \lambda'_Z}^{(\mu_q \mu_{\bar{q}})*} \quad C = \sum_{\mu_q \mu_{\bar{q}} \lambda_W \lambda_Z} |F_{\lambda_W \lambda_Z}^{(\mu_q \mu_{\bar{q}})}|^2$$

$$f_{00} = \rho_{0000},$$

$$f_{TT} = \rho_{++--} + \rho_{--++} + \rho_{----} + \rho_{++++},$$

$$f_{0T} = \rho_{00--} + \rho_{00++},$$

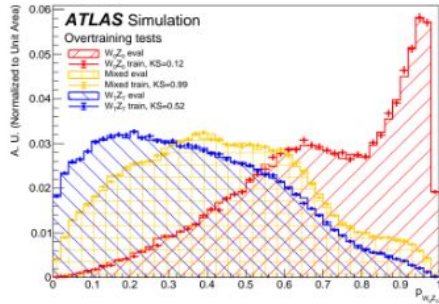
$$f_{T0} = \rho_{--00} + \rho_{++00}.$$



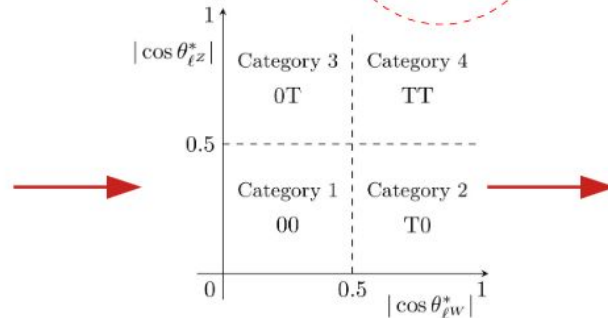
# Example 3: ATLAS WZ

## Joint-polarisation fraction measurement:

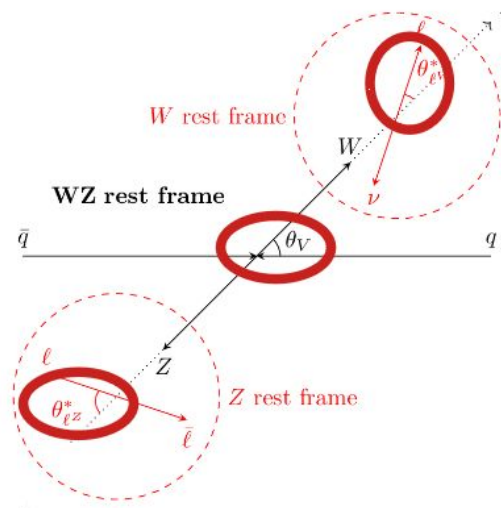
- Analytical variable  $|\cos\theta_v|$  not discriminant enough
- **Classification DNN** between all 4 joint-polarisation states: still **poorly discriminant between 0T and T0**
- Split DNN score for 00 in **4 categories** based on  $\cos\theta^*$



DNN score



**4-categories DNN score**



**Classification DNN input variables (by importance)**

$$|y_{l^* w} - y_{l^* z}| \sim |\cos\theta_v|$$

$$P_T^{WZ}$$

$$P_T^{l^* w}$$

$$\Delta\phi(l^* w, v)$$

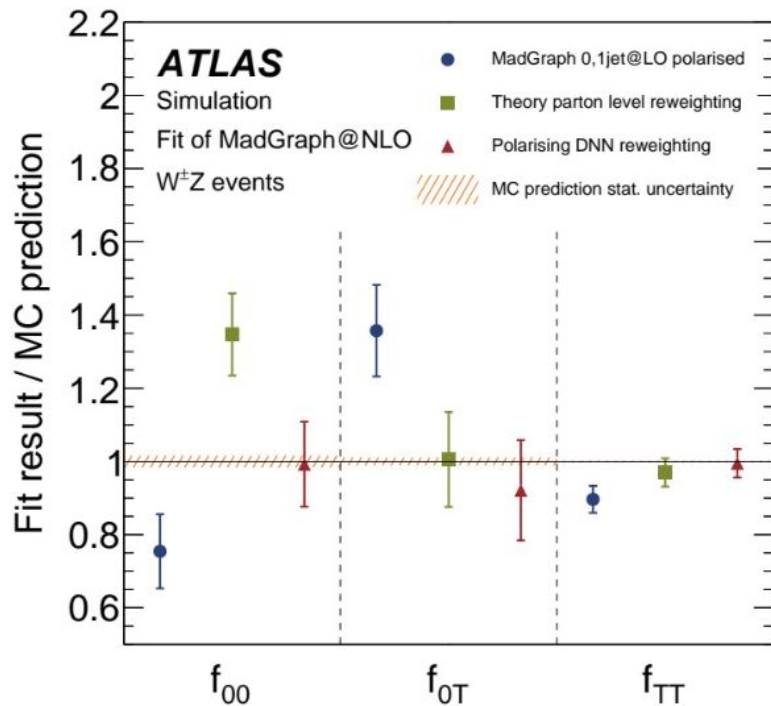
$$\Delta\phi(l_1^* z, l_2^* z)$$

$$E_T^{\text{miss}}$$

$$P_T^{l_2^* z}$$

$$P_T^{l_1^* z}$$

# Choice of NLO accurate template set



## Madgraph polarised generation:

- Big **bias**, from **10% to 40%** of the fractions values

## Theory parton level reweighting:

- Still some **bias**, but generally reduced **~15%** of the fractions values
- Used as the alternative method for modelling uncertainty

## Polarising DNN reweighting:

- Found to be the **least biased method** of all tried (almost no bias)
- **Baseline**

# Example 3: ATLAS WZ



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Physics Letters B

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Observation of gauge boson joint-polarisation states in  $W^{\pm}Z$  production from  $pp$  collisions at  $\sqrt{s} = 13$  TeV with the ATLAS detector



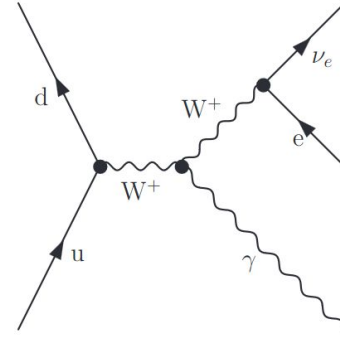
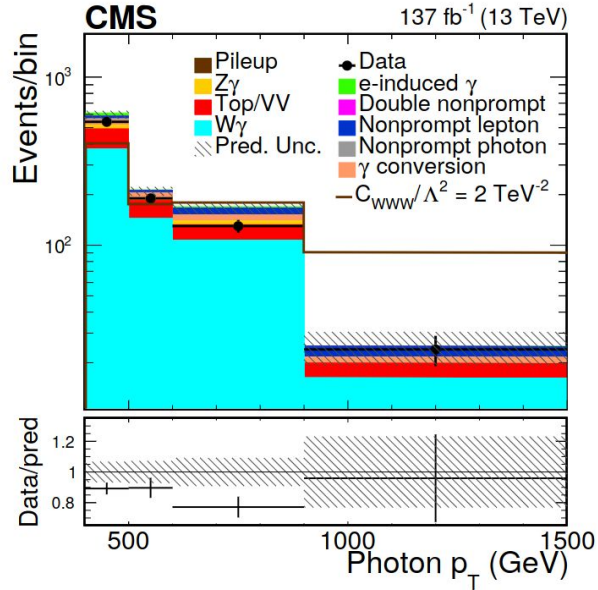
The ATLAS Collaboration \*

<b><math>W+Z</math> &amp; <math>W-Z</math></b>		<b><math>W+Z</math></b>		<b><math>W-Z</math></b>	
$f_{00}$	$0.067 \pm 0.010$	$f_{00}$	$0.072 \pm 0.016$	$f_{00}$	$0.063 \pm 0.016$
$f_{0T}$	$0.110 \pm 0.029$	$f_{0T}$	$0.119 \pm 0.034$	$f_{0T}$	$0.11 \pm 0.04$
$f_{T0}$	$0.179 \pm 0.023$	$f_{T0}$	$0.153 \pm 0.033$	$f_{T0}$	$0.21 \pm 0.04$
$f_{TT}$	$0.644 \pm 0.032$	$f_{TT}$	$0.66 \pm 0.04$	$f_{TT}$	$0.62 \pm 0.05$

**Measurement performed as well separating by the W charge**

- Significance on  $f_{00}$  at  **$6.9\sigma$  in  $W+Z$**
- Significance on  $f_{00}$  at  **$4.1\sigma$  in  $W-Z$**

# Example 4: CMS $W\gamma$

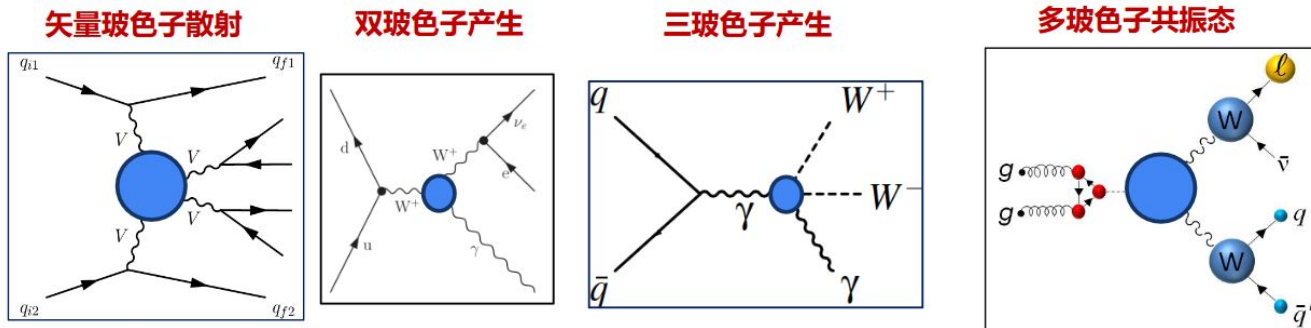


Coefficient	Exp. lower	Exp. upper	Obs. lower	Obs. upper
$c_{WWW}/\Lambda^2$	-0.85	0.87	-0.90	0.91
$c_B/\Lambda^2$	-46	45	-40	41
$c_{\bar{W}W}/\Lambda^2$	-0.43	0.43	-0.45	0.45
$c_{\bar{W}}/\Lambda^2$	-23	22	-20	20

Figure 3: The photon  $p_T$  distribution used for the extraction of limits on dimension-six EFT operators. The expected yields correspond to the estimates made before the fit. The uncertainty in the prediction (the hatched band) is the quadratic sum of the systematic uncertainties. The uncertainty in the data is statistical. The last bin includes the overflow.

# Summary and Outlook

- Rich progress and potential from Multiboson Measurements/Probes
  - Precise measurements, Rare process discovery...
  - Polarization, interference, correlation ...
  - Anomalous coupling, EFT, and even Higgs properties...
- High energy, High Luminosity, High multiplicity, High opportunities!
- Rich space for improvement!
  - CP-odd either ignored, or treated same as CP-even





***Backup***

# Higgs without Higgs



TABLE I. Each effect (left-hand column) can be measured as an on-shell Higgs coupling (diagram in the HC column) or in a high-energy process (diagram in the HwH column), where it grows with energy as indicated in the last column.

	HC	HwH	Growth
$\kappa_t$ $\mathcal{O}_{y_t}$			$\sim(E^2/\Lambda^2)$
$\kappa_\lambda$ $\mathcal{O}_6$			$\sim(vE/\Lambda^2)$
$\kappa_{Z\gamma}$ $\mathcal{O}_{WW}$ $\kappa_{\gamma\gamma}$ $\mathcal{O}_{BB}$ $\kappa_V$ $\mathcal{O}_r$			$\sim(E^2/\Lambda^2)$
$\kappa_g$ $\mathcal{O}_{gg}$			$\sim(E^2/\Lambda^2)$

HCs are associated with an EFT Lagrangian  $\mathcal{L} = \sum_i c_i \mathcal{O}_i / \Lambda^2$ , consisting in particular of the dimension-six operators [12,13],

$$\begin{aligned}
 \mathcal{O}_r &= |H|^2 \partial_\mu H^\dagger \partial^\mu H, & \mathcal{O}_{y_\psi} &= Y_\psi |H|^2 \psi_L H \psi_R, \\
 \mathcal{O}_{BB} &= g^2 |H|^2 B_{\mu\nu} B^{\mu\nu}, & \mathcal{O}_{WW} &= g^2 |H|^2 W_{\mu\nu}^a W^{a\mu\nu}, \\
 \mathcal{O}_{GG} &= g_s^2 |H|^2 G_{\mu\nu}^a G^{a\mu\nu}, & \mathcal{O}_6 &= |H|^6,
 \end{aligned} \tag{1}$$

with  $Y_\psi$  the Yukawa coupling for the fermion  $\psi$ . [Note that the parameters in Eq. (3) can be put in correspondence with other parametrizations of HCs: via partial widths  $\kappa_i^2 = \Gamma_{h \rightarrow ii} / \Gamma_{h \rightarrow ii}^{\text{SM}}$  [14], via Lagrangian couplings in the unitary gauge  $g_{hii}$  [13,15], or via pseudo-observables [16].]

The operators of Eq. (1) have the form  $|H|^2 \times \mathcal{O}^{\text{SM}}$ , with  $\mathcal{O}^{\text{SM}}$  a dimension-four SM operator (i.e., kinetic terms, Higgs potential, and Yukawa couplings) times

## Combinations

$$p_{\perp}(p_e, p_q) = \vec{p}_e \cdot (\vec{p}_{Z/\gamma} \times \vec{p}_q)$$

- Different possibilities for the lepton in  $WZ$ .
- Explore substitutes of  $\vec{p}_{Z/\gamma}$ .
- Need to find a substitute to the unobservable  $\vec{p}_q$  :
  - $\hat{z}$ -axis :  $[0, 0, 1]$ ,
  - lepton :  $[0, 0, p_l^z]$ ,
  - neutral boson  $Z/\gamma$  :  $[0, 0, p_{Z/\gamma}^z]$ ,
  - sum of visible particles :  $[0, 0, p_{\Sigma}^z]$ .

Triple products configurations	$\mathcal{O}_{\widetilde{WWW}}$	$\mathcal{O}_{\widetilde{WB}}$
$(\vec{p}_q, \vec{p}_Z, \vec{p}_e)$	-1.612(4)	-0.3888(7)
$(\vec{p}_q, \vec{p}_Z, \vec{p}_{\mu^-})$	-0.184(4)	-0.0271(7)
$([0, 0, p_{\Sigma}^z], \vec{p}_Z, \vec{p}_e)$	-0.628(4)	-0.1207(7)
$(\vec{p}_W, \vec{p}_{\mu^-}, \vec{p}_e)$	0.535(4)	0.0965(7)
$(\vec{p}_W, \vec{p}_{\mu^+}, \vec{p}_e)$	0.511(4)	0.1009(7)
$([0, 0, p_{\widetilde{W}}^z], \vec{p}_e, \vec{p}_{\mu^-})$	-0.227(4)	-0.0594(7)
$(\vec{p}_W, \vec{p}_{\mu^-}, \vec{p}_{\mu^+})$	-0.080(4)	-0.0110(7)
$([0, 0, p_{\Sigma}^z], \vec{p}_W, \vec{p}_Z)$	-0.045(4)	-0.0086(7)
$([0, 0, p_e^z], \vec{p}_{\mu^-}, \vec{p}_W)$	0.028(4)	0.0061(7)
$(\vec{p}_e, \vec{p}_{\mu^-}, \vec{p}_{\mu^+})$	-0.025(4)	-0.004(7)
$([0, 0, p_e^z], \vec{p}_{\mu^-}, \vec{p}_{\mu^+})$	-0.029(4)	-0.0061(7)
$([0, 0, p_{\mu^-}^z], \vec{p}_e, \vec{p}_{\mu^+})$	-0.213(4)	-0.0244(7)
$([0, 0, p_{\mu^+}^z], \vec{p}_{\mu^-}, \vec{p}_e)$	0.252(4)	0.0327(7)
$([0, 0, p_{\Sigma}^z], \vec{p}_e + \vec{p}_{\mu^-}, \vec{p}_{\mu^+})$	-0.362(4)	-0.0582(7)
$([0, 0, p_{\Sigma}^z], \vec{p}_e + \vec{p}_{\mu^+}, \vec{p}_{\mu^-})$	-0.300(4)	-0.0481(7)
$([0, 0, p_{\Sigma}^z], \vec{p}_e - \vec{p}_{\mu^-}, \vec{p}_{\mu^+})$	-0.047(4)	-0.0097(7)
$([0, 0, p_{\Sigma}^z], \vec{p}_e - \vec{p}_{\mu^+}, \vec{p}_{\mu^-})$	-0.160(4)	-0.0279(7)

## Sign of the Interference

---

- 

$$\mathcal{M}_{int,i} \equiv 2\text{Re} \left\{ \frac{C_i}{\Lambda^2} \mathcal{M}_i \times \mathcal{M}_{SM}^* \right\}.$$

$\mathcal{M}_{int,i}$  is not positive-definite over the phase space but fluctuates.

- Positive and negative contributions perfectly compensates in CP-even observables of a C-even processes. Two suppression mechanisms :  $\Lambda^r$  and sign of  $\mathcal{M}_{int}$ .
- Ineffectiveness of the cross section and poor constraints on CP-odd operators.

⇒ Use asymmetries to build CP-odd observables !

## Asymmetries

---

- Differential cross section with respect to a CP-odd observable  $X$  after a CP-odd  $\mathcal{O}_i^6$  insertion is

$$\frac{d\sigma}{dX} = \frac{d\sigma(SM)}{dX} + \frac{C_i}{\Lambda^2} \frac{d\sigma(\mathcal{O}_i)}{dX} + \mathcal{O}(\Lambda^{-3}).$$

- We define the asymmetry in  $X$  as

$$\Delta X = \sigma_{X>0} - \sigma_{X<0} \approx \Delta\sigma_X(SM) + \frac{C_i}{\Lambda^2} \Delta\sigma_X(\mathcal{O}_i),$$

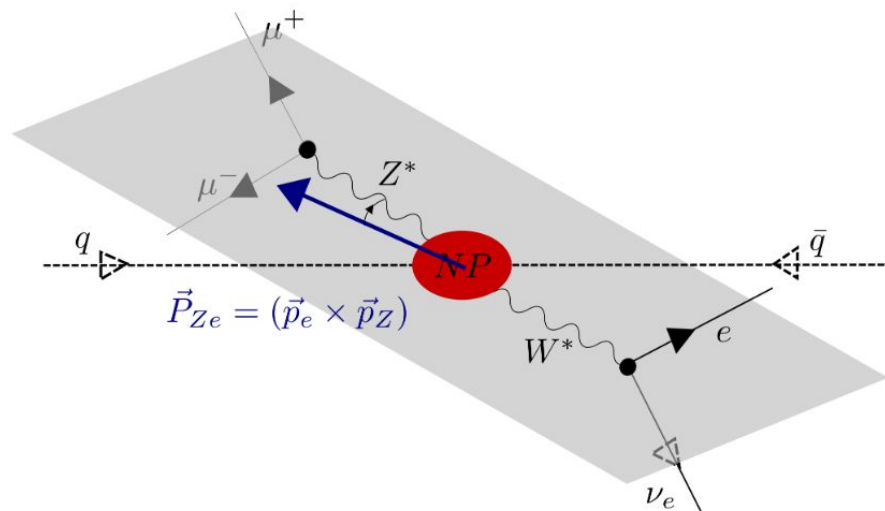
with  $\sigma_{X>0} = \int_0^{b_+} \frac{d\sigma}{dX} dX$  and  $\sigma_{X<0} = \int_{b_-}^0 \frac{d\sigma}{dX} dX$ .

$b_{\pm}$  are the upper and lower bounds of integration of  $X$ .

## Other CP-odd observables in Diboson

“Probing CP-violation at colliders through interference effects in diboson production and decay“, J. Kumar et al., arXiv 0801.2891

$$\Xi_{\pm}^Z(p_Z, p_l) = \text{sign}(p_Z^Z) \text{sign}[(p_l \times p_Z)^Z] = \text{sign}([0, 0, p_Z^Z] \cdot (\vec{p}_l \times \vec{p}_Z))$$
$$\rightarrow \Delta \Xi_{\pm}^Z = \Delta p_{\perp}(p_e, p_Z^Z)$$



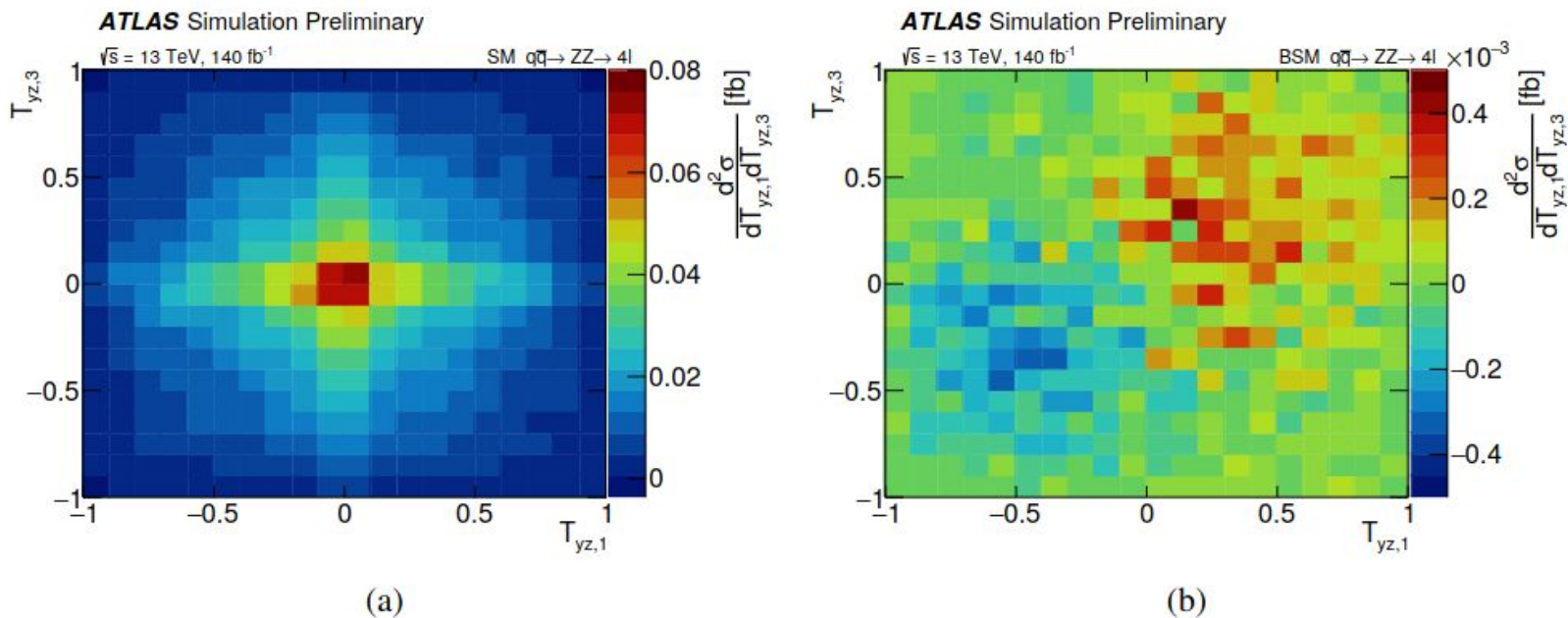
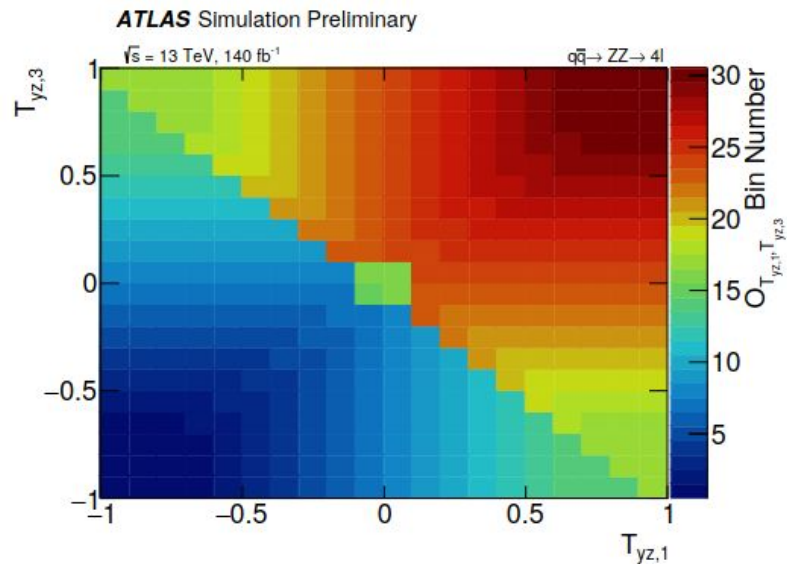
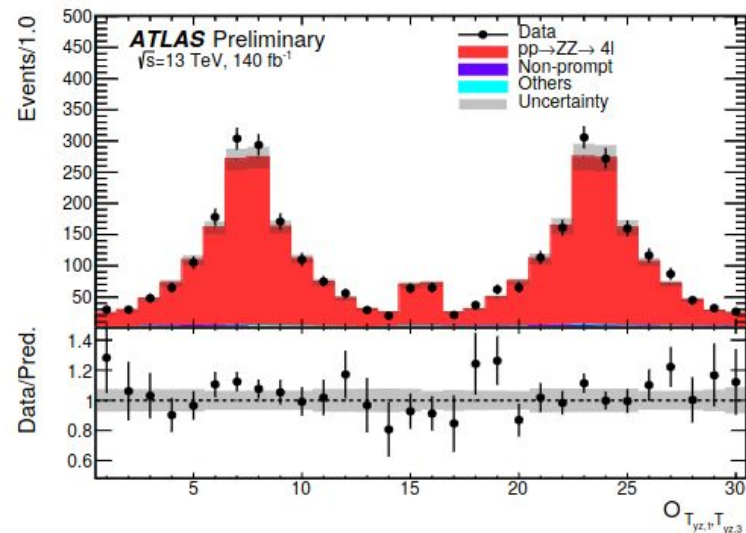


Figure 4: Particle level 2D differential cross-sections of  $T_{yz}$  of the two  $Z$  bosons for the  $q\bar{q} \rightarrow ZZ \rightarrow 4\ell$  process as predicted by (a) the SM and (b) in the presence of the BSM aNTGC vertex. The BSM prediction shows the linear only contribution when  $f_Z^4 = 1$ .



(a)



(b)

Figure 5: The  $2D \rightarrow 1D$  mapping (a) and (b) the detector level measurement of the Optimal Observable  $O_{T_{yz,1}, T_{yz,3}}$ . The measured distribution is compared to the SM signal prediction and the total background. The ‘Others’ category includes the contribution from  $t\bar{t}Z$  and  $VVZ$  processes. The non-prompt background is estimated using the fake-factor method. The grey band represents the effect of the total theoretical and experimental uncertainties for the detector-level predictions, and the vertical error bars on data represent the statistical uncertainties.



# CMS WZ

The relations described by Eqs. 9 and 10 describe the differential cross sections only when no kinematic requirements are applied to the decay products of the W and Z bosons. Since measured data are limited by the detector acceptance and trigger thresholds, this condition is not fulfilled, thus rendering impossible any direct extraction of the parameters from a fit to a quadratic distribution. Instead, the signal extraction procedure is based on the separation of the WZ process into the three different polarization components (left, right, and longitudinal) based on the generator-level information. The nominal WZ sample is split into three exclusive ones, one for each polarization fraction. Events in the sample are then weighted based on the generator-level  $\cos(\theta_W)$  ( $\cos(\theta_Z)$ ) distributions to match the expected quadratic dependence associated with the corresponding polarization state. The corresponding expected polarization fractions needed to perform this weighting are extracted from an analytical fit of the  $\cos(\theta_W)$  ( $\cos(\theta_Z)$ ) distributions with no kinematic requirements applied, as depicted in Fig. 9. These results for the expected polarization fractions have been cross-checked using an alternative derivation based on the mean and quadratic mean values of the  $\cos(\theta_W)$  ( $\cos(\theta_Z)$ ) quantity in the samples, showing consistent results within the uncertainties presented in the figure. The low  $p$ -value for the positively charged  $\cos(\theta_W)$  fit originates from a fluctuation in the 2016 MC sample. Using these weighted samples, simulation-based templates of the  $\cos(\theta_W)$  ( $\cos(\theta_Z)$ ) distributions at the reconstruction level for each of the polarization states are produced to model each of the polarized final-state contribution.

The polarization measurements are provided separately for the W and Z bosons, following a similar procedure. Since the polarization in the two different charged states can be different,

# ATLAS WZ

As observed in theory calculations [23], a strong relationship exists between NLO QCD corrections and polarisation effects. Therefore, templates for helicity states generated at LO are insufficient. The MADGRAPH 0,1j@LO MC simulation corrects for the real part of NLO QCD effects but misses virtual corrections that are also important for polarisation measurements. In order to verify that the shapes of the polarised templates are valid, a closure test is performed. Templates are used to fit pseudo-data generated using inclusive MC simulations at NLO QCD accuracy, such as with POWHEG+PYTHIA or MADGRAPH5\_AMC@NLO+PYTHIA. The fit is performed on detector-level distributions. Polarisation fractions extracted from the fit are compared with the generated polarisation fractions of the NLO MC samples. Differences from 10% to 50% depending on the polarisation state are observed between extracted and built-in fractions when using polarised templates from the MADGRAPH 0,1j@LO generation. This demonstrates the need for using polarised templates at NLO QCD accuracy for polarisation measurements.

Templates better approaching the NLO QCD accuracy are built using a DNN-based event-by-event reweighting procedure [83]. Four DNNs are trained and each of them is specialised to reweight at particle-level the inclusive MADGRAPH 0,1j@LO events to one of the four joint polarised states. Input variables of the DNNs are those of the polarisation DNN classifier augmented by the invariant mass of the WZ system  $m_{WZ}$ , and the angular variables  $\cos \theta_{\ell W}^*$ ,  $\cos \theta_{\ell Z}^*$  and  $|\cos \theta_V|$ . The four DNNs are then applied to reweight the inclusive POWHEG+PYTHIA MC events, creating four polarised MC templates with NLO-like accuracy in QCD. This method provides the best fit closure, with no bias on the extracted polarisation fractions visible within the statistical precision of the closure test.

A second method is used to create NLO QCD accurate polarised templates, based on the available fixed-order parton-level theory predictions [23]. Predicted distributions, including the output score of the DNN classifier, are calculated in the parton-level fiducial phase space [23]. Corrections for parton-shower

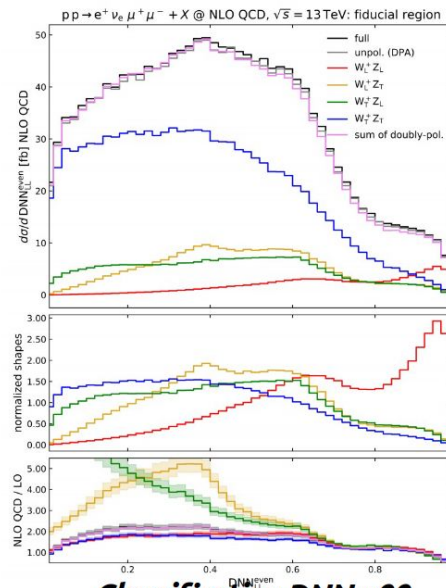
## Reweighting to theory prediction

In collaboration with theorists **A. Denner, G. Pelliccioli**:  
Theoretical calculations [arXiv:2010.07149] performed

- in the analysis **fiducial phase** space
- **NLO QCD** polarised → at **parton level**,
- Several distributions including the analysis **classification DNN score**

**Reweight** MG0,1jet polarised to NLO **at parton level**  
event-by-event with *K*-factor

$$K_{\text{MG p.s.}} = \frac{\text{MoCANLO}_{\text{pol.}}^{\text{parton}}}{\text{MADGRAPH}_{\text{ref.pol.}}^{\text{parton}}}$$



**Classification DNN  $p_0$   
polarised distribution  
at NLO QCD**

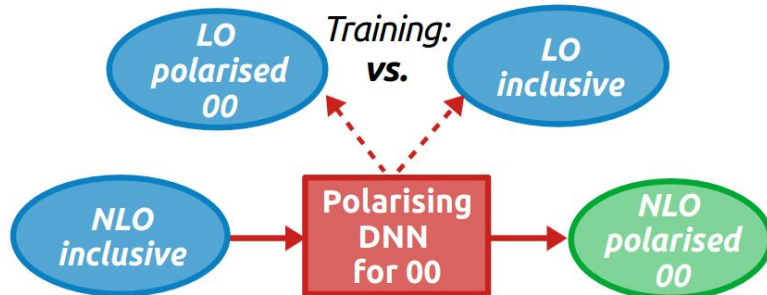
[private communication from A. Denner, G. Pelliccioli]

## DNN reweighting

Possible to reweight a distribution using a DNN [arXiv:[1907.08209](https://arxiv.org/abs/1907.08209)]

→ Acts as a **multi-dimensionnal reweighting** of the input MC sample

4 DNN **trained on polarised Madgraph samples** to discriminate one joint-polarisation states against the inclusive : event-by-event output used in **reweighting**



$$w(x) \sim \text{DNN}(x) / (1 - \text{DNN}(x))$$

$$\begin{aligned}
 &|y_{\ell, W} - y_Z| \\
 &p_T^{\ell, W} \\
 &E_T^{\text{miss}} \\
 &\Delta\phi(\ell^W, \ell^V) \\
 &p_T^{WZ} \\
 &p_{\ell 1, Z} \\
 &p_{\ell 2, Z} \\
 &p_T^{\ell 1 Z} \\
 &\Delta\phi(\ell 1^Z, \ell 2^Z) \\
 &m_{WZ} \\
 &\cos(\theta_{\ell W}^*) \\
 &\cos(\theta_{\ell Z}^*) \\
 &\cos(\theta_{\ell SS}^*) \\
 &\cos(\theta_V)
 \end{aligned}$$

**Reweighting DNNs  
input variables**

# CMS $W\gamma$

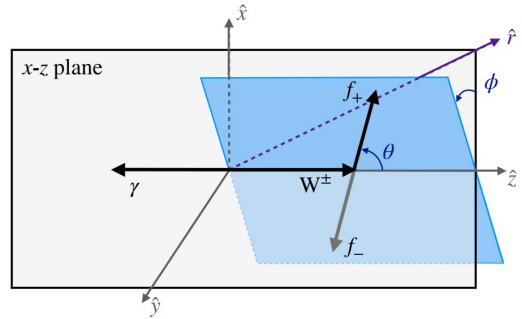
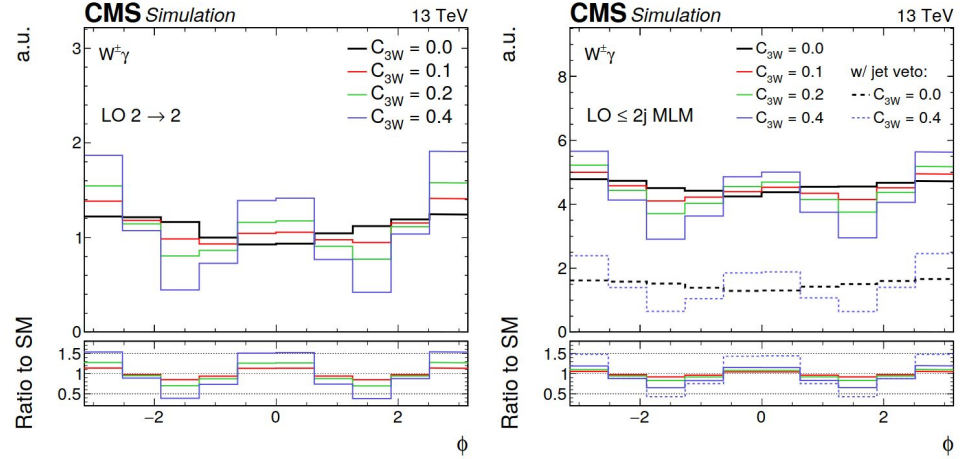


Figure 2: Scheme of the special coordinate system for  $W^\pm\gamma$  production, defined by a Lorentz boost to the center-of-mass frame along the direction  $\hat{r}$ . The  $z$  axis is chosen as the  $W^\pm$  boson direction in this frame, and  $y$  is given by  $\hat{z} \times \hat{r}$ . The  $W^\pm$  boson decay plane is indicated in blue, where the labels  $f_+$  and  $f_-$  refer to positive and negative helicity final-state fermions. The angles  $\phi$  and  $\theta$  are the azimuthal and polar angles of  $f_+$ .



$\eta^\ell$  is the pseudorapidity of the lepton, and  $m_T$  is the transverse mass of the  $\ell\nu$  system. Of the two possible solutions for  $\eta^\nu$ , only one will correspond to the unknown true value. One of the two solutions is picked at random event-by-event. In the limit of high  $W^\pm$  boson momentum, it can be demonstrated that the two solutions for  $|\phi, \phi^+|$  and  $|\phi, \phi^-|$ , are related by  $|\phi^+| = |\pi - \phi^-|$ , modulo  $2\pi$ . This intrinsic ambiguity does not, however, prevent the observation of the interference effect. This is illustrated in Fig. 3, where the deviation in the  $\phi$  distribution is unaffected by a transformation  $\phi \rightarrow \pi - \phi$ .

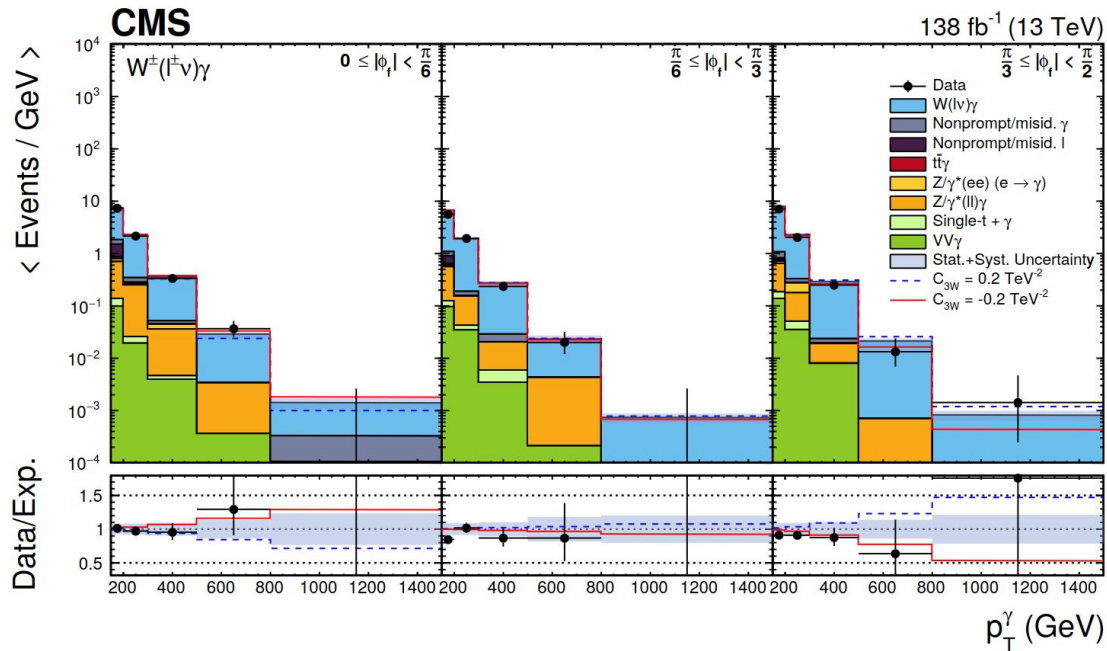


Table 4: Best fit values of  $C_{3W}$  and corresponding 95% CL confidence intervals as a function of the maximum  $p_T^\gamma$  bin included in the fit.

$p_T^\gamma$ cutoff (GeV)	Best fit $C_{3W}$ (TeV <sup>-2</sup> )		Observed 95% CL (TeV <sup>-2</sup> )		Expected 95% CL (TeV <sup>-2</sup> )	
	SM+int. only	SM+int.+BSM	SM+int. only	SM+int.+BSM	SM+int. only	SM+int.+BSM
200	-0.86	-0.24	[-2.01, 0.38]	[-0.76, 0.40]	[-1.16, 1.27]	[-0.81, 0.71]
300	-0.25	-0.17	[-0.81, 0.34]	[-0.39, 0.28]	[-0.56, 0.60]	[-0.33, 0.33]
500	-0.13	-0.025	[-0.50, 0.25]	[-0.15, 0.12]	[-0.35, 0.38]	[-0.17, 0.16]
800	-0.20	-0.033	[-0.49, 0.11]	[-0.10, 0.08]	[-0.29, 0.31]	[-0.097, 0.095]
1500	-0.13	-0.009	[-0.38, 0.17]	[-0.062, 0.052]	[-0.27, 0.29]	[-0.066, 0.065]