

第一届Lambda超子自旋极化跨系统研讨会

北京谱仪上Lambda超子自旋极 化理论进展

Jia-Jun Wu (UCAS)

Collaborator: Shu-Ming Wu, Bing-Song Zou

Phys. Rev. D 104 (2021) 5, 054018

第一届Lambda超子自旋极化跨系统研讨会

2025. 03. 22.

合肥，中科大

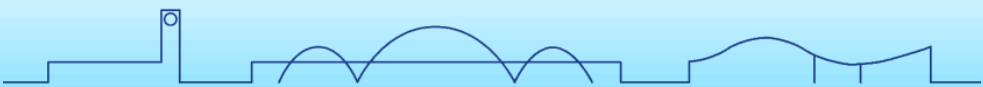


中国科学院大学
University of Chinese Academy of Sciences



Content

- 现状和问题
- 利用L-S scheme方法抽取 $\psi \rightarrow \bar{B}B$ 过程的L
- 衰变的有效半径
- 小结



现状和问题

nature physics

Explore content ▾ About the journal ▾ Publish with us ▾ Subscribe

[nature](#) > [nature physics](#) > [letters](#) > article

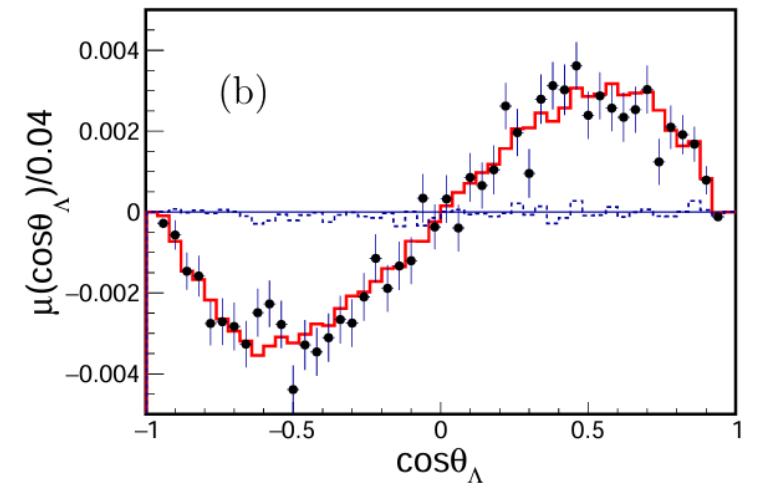
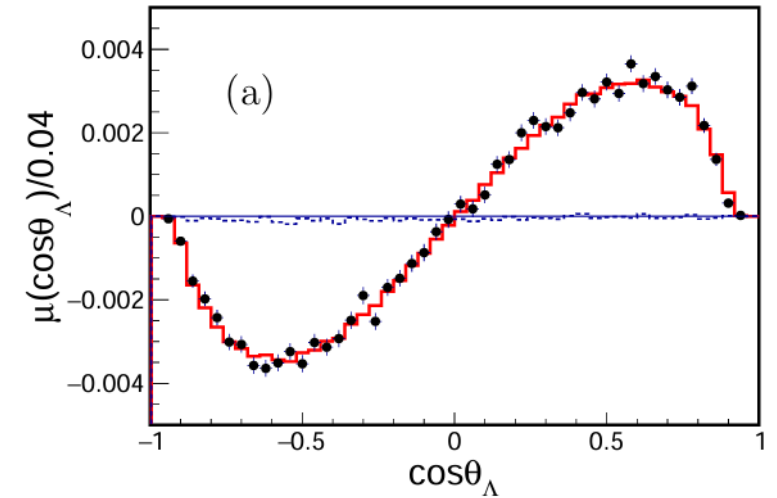
Letter | Published: 06 May 2019

Polarization and entanglement in baryon–antibaryon pair production in electron–positron annihilation

[The BESIII Collaboration](#)

[Nature Physics](#) **15**, 631–634 (2019) | [Cite this article](#)

7492 Accesses | 139 Citations | 64 Altmetric | [Metrics](#)

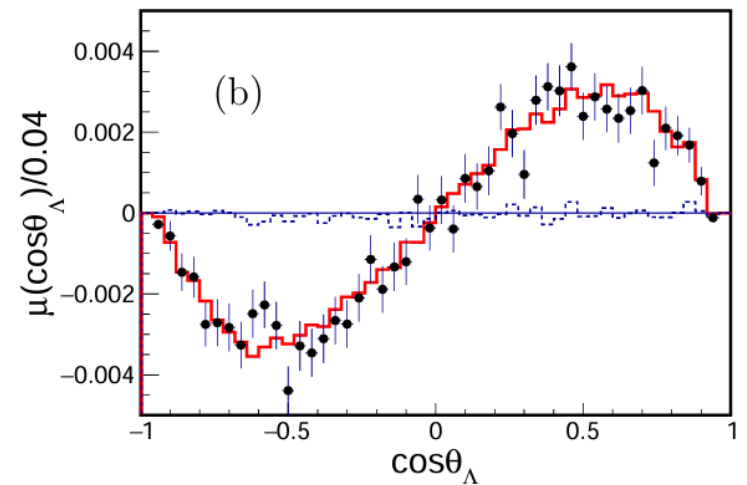
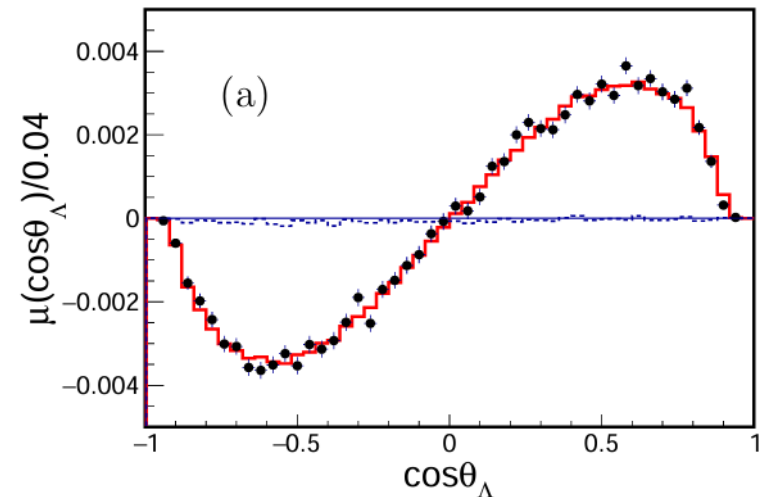


现状和问题

$$e^+e^- \rightarrow J/\psi \rightarrow \Lambda\bar{\Lambda} \rightarrow p\pi^- \bar{p}\pi^+ / p\pi^- \bar{n}\pi^0$$

$$\begin{aligned} \mathcal{W}(\xi; \alpha_\psi, \Delta\Phi, \alpha_-, \alpha_+) = & 1 + \alpha_\psi \cos^2\theta_\Lambda \\ & + \alpha_- \alpha_+ [\sin^2\theta_\Lambda (n_{1,x}n_{2,x} - \alpha_\psi n_{1,y}n_{2,y}) + (\cos^2\theta_\Lambda + \alpha_\psi) n_{1,z}n_{2,z}] \\ & + \alpha_- \alpha_+ \sqrt{1 - \alpha_\psi^2} \cos(\Delta\Phi) \sin\theta_\Lambda \cos\theta_\Lambda (n_{1,x}n_{2,z} + n_{1,z}n_{2,x}) \\ & + \sqrt{1 - \alpha_\psi^2} \sin(\Delta\Phi) \sin\theta_\Lambda \cos\theta_\Lambda (\alpha_- n_{1,y} + \alpha_+ n_{2,y}), \end{aligned}$$

Parameters	This work	Previous results
α_ψ	$0.461 \pm 0.006 \pm 0.007$	0.469 ± 0.027 [25]
$\Delta\Phi$	$(42.4 \pm 0.6 \pm 0.5)^\circ$	—
α_-	$0.750 \pm 0.009 \pm 0.004$	0.642 ± 0.013 [27]
α_+	$-0.758 \pm 0.010 \pm 0.007$	-0.71 ± 0.08 [27]
$\bar{\alpha}_0$	$-0.692 \pm 0.016 \pm 0.006$	—
A_{CP}	$-0.006 \pm 0.012 \pm 0.007$	0.006 ± 0.021 [27]
$\bar{\alpha}_0/\alpha_+$	$0.913 \pm 0.028 \pm 0.012$	—



现状和问题

标准公式，通过末态的衰变
来抽取粒子的极化信息。

$$e^+e^- \rightarrow J/\psi \rightarrow \Lambda\bar{\Lambda} \rightarrow p\pi^- \bar{p}\pi^+ / p\pi^- \bar{n}\pi^0$$



现状和问题

Zhe Zhang, Rong-Gang Ping, Tianbo Liu, Jiao Jiao Song,
Weihua Yang, Ya-jin Zhou PRD 110 034034(2024) $e^+e^- \rightarrow B_1\bar{B}_2$

标准公式，通过末态的衰变
来抽取粒子的极化信息。

G. Fäldt, EPJA 52 141(2016)
G. Fäldt and A. Kupsc, PLB 772 16(2017)

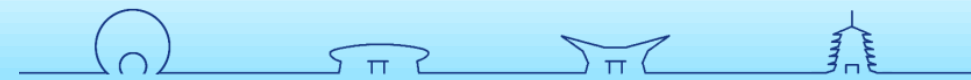
$$e^+e^- \rightarrow J/\psi \rightarrow \Lambda\bar{\Lambda} \rightarrow p\pi^- \bar{p}\pi^+ / p\pi^- \bar{n}\pi^0$$

Johann Haidenbauer, Ulf-G. Meißner, Ling-Yun Dai
PRD 103 (2021) 1, 014028 Study the formfactor
Jian-Ping Dai, Xu Cao, Horst Lenske PLB 846 138192
(2023) isospin assignment and data driven
Prof. He's talk, about CP and EDM

? 为什么极化是这样的?

反应的机制是什么?

如何通过极化信息抽取反应的内部信息，从而帮助我们理解强子过程



现状和问题

Zhe Zhang, Rong-Gang Ping, Tianbo Liu, Jiao Jiao Song,
Weihua Yang, Ya-jin Zhou PRD 110 034034(2024) $e^+e^- \rightarrow B_1\bar{B}_2$

标准公式，通过末态的衰变
来抽取粒子的极化信息。

G. Fäldt, EPJA 52 141(2016)
G. Fäldt and A. Kupsc, PLB 772 16(2017)

$$e^+e^- \rightarrow J/\psi \rightarrow \Lambda\bar{\Lambda} \rightarrow p\pi^- \bar{p}\pi^+ / p\pi^- \bar{n}\pi^0$$

通过极化信息了解其轨道角动量，
然后据此来了解产生端的衰变尺度

Shu-ming Wu, Jia-jun Wu, Bing-song Zou,
PRD 104 (2021) 5, 054018

？为什么极化是这样的？

反应的机制是什么？

如何通过极化信息抽取反应的内部信息，从而帮助我们理解强子过程



L-S scheme

$$\psi \rightarrow \bar{B}(1/2-)B(1/2+) \xrightarrow{L: \text{ S and D wave}} r_{eff} \sim \frac{\bar{L}}{p}$$



L-S scheme

$$\psi \rightarrow \bar{B}(1/2-)B(1/2+) \xrightarrow{L: S \text{ and } D \text{ wave}} r_{eff} \sim \frac{\bar{L}}{p}$$

This is a very useful PWA tool

PHYSICAL REVIEW C 67, 015204 (2003)

Lorentz covariant orbital-spin scheme for the effective N^*NM couplings

B. S. Zou^{1,2,3,*} and F. Hussain^{3,†}



L-S scheme

$$\psi \rightarrow \bar{B}(1/2-)B(1/2+) \xrightarrow{L: \text{ S and D wave}} r_{eff} \sim \frac{\bar{L}}{p}$$

This is a very useful PWA tool

PHYSICAL REVIEW C 67, 015204 (2003)

Lorentz covariant orbital-spin scheme for the effective N^*NM couplings

B. S. Zou^{1,2,3,*} and F. Hussain^{3,†}

Here I mainly introduce it for $\psi \rightarrow \bar{N}N^*$ case



L-S scheme

$$\psi \rightarrow \bar{N}N^*$$

$$J = S_\psi = S_{\bar{N}N^*} + L_{\bar{N}N^*}$$

$$S_{\bar{N}} = \frac{1}{2}, \quad S_{N^*} = \frac{2n+1}{2}$$
$$r = p_{N^*} - p_N$$



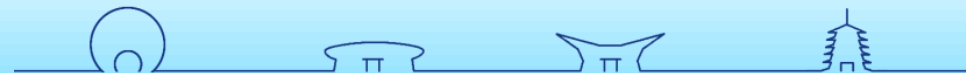
L-S scheme

$$S_{\bar{N}} = \frac{1}{2}, \quad S_{N^*} = \frac{2n+1}{2}$$
$$r = p_{N^*} - p_N$$

$$\psi \rightarrow \bar{N}N^*$$

$$J = S_\psi = S_{\bar{N}N^*} + L_{\bar{N}N^*}$$

$$S_{\bar{N}N^*} \left\{ \begin{array}{l} n: \\ \psi_{\mu_1, \mu_2, \dots, \mu_n}^{(n)} = \bar{u}_{\mu_1, \mu_2, \dots, \mu_n}(p_{N^*}, S_{N^*}) \gamma_5 v(p_N, S_N) \end{array} \right.$$



L-S scheme

$$S_{\bar{N}} = \frac{1}{2}, \quad S_{N^*} = \frac{2n+1}{2}$$

$$r = p_{N^*} - p_N$$

$$\psi \rightarrow \bar{N}N^*$$

$$J = S_\psi = S_{\bar{N}N^*} + L_{\bar{N}N^*}$$

$$S_{\bar{N}N^*} \left\{ \begin{array}{l} n: \quad \psi_{\mu_1, \mu_2, \dots, \mu_n}^{(n)} = \bar{u}_{\mu_1, \mu_2, \dots, \mu_n}(p_{N^*}, S_{N^*}) \gamma_5 v(p_N, S_N) \\ n+1: \quad \psi_{\mu_1, \mu_2, \dots, \mu_{n+1}}^{(n+1)} = \bar{u}_{\mu_1, \mu_2, \dots, \mu_n}(p_{N^*}, S_{N^*}) \left(\gamma_{\mu_{n+1}} - \frac{r_{\mu_{n+1}}}{m_\psi + m_{N^*} + m_N} \right) v(p_N, S_N) + (\mu_i \leftrightarrow \mu_j) \end{array} \right.$$



L-S scheme

$$S_{\bar{N}} = \frac{1}{2}, \quad S_{N^*} = \frac{2n+1}{2}$$

$$r = p_{N^*} - p_N$$

$$\psi \rightarrow \bar{N}N^*$$

$$J = S_\psi = S_{\bar{N}N^*} + L_{\bar{N}N^*}$$

$$S_{\bar{N}N^*} \left\{ \begin{array}{l} n: \quad \psi_{\mu_1, \mu_2, \dots, \mu_n}^{(n)} = \bar{u}_{\mu_1, \mu_2, \dots, \mu_n}(p_{N^*}, S_{N^*}) \gamma_5 v(p_N, S_N) \\ n+1: \quad \psi_{\mu_1, \mu_2, \dots, \mu_{n+1}}^{(n+1)} = \bar{u}_{\mu_1, \mu_2, \dots, \mu_n}(p_{N^*}, S_{N^*}) \left(\gamma_{\mu_{n+1}} - \frac{r_{\mu_{n+1}}}{m_\psi + m_{N^*} + m_N} \right) v(p_N, S_N) + (\mu_i \leftrightarrow \mu_j) \end{array} \right.$$

$$L_{\bar{N}N^*} \sim \tilde{t}_{\mu_1, \mu_2, \dots, \mu_L}^{(L)}(r, p_\psi)$$

$$\tilde{t}^{(0)}(r, p_\psi) = 1; \quad \tilde{t}^{(1)}_\mu(r, p_\psi) = \tilde{r}_\mu \equiv \tilde{g}_{\mu\nu}(p_\psi) r^\nu$$

$$\tilde{t}^{(2)}_{\mu\nu}(r, p_\psi) = \tilde{r}_\mu \tilde{r}_\nu - \frac{1}{3}(\tilde{r} \cdot \tilde{r}) \tilde{g}_{\mu\nu}(p_\psi); \quad \dots$$



L-S scheme

$$S_{\bar{N}} = \frac{1}{2}, \quad S_{N^*} = \frac{2n+1}{2}$$

$$r = p_{N^*} - p_N$$

$$\psi \rightarrow \bar{N}N^*$$

$$J = S_\psi = S_{\bar{N}N^*} + L_{\bar{N}N^*}$$

$$S_{\bar{N}N^*} \begin{cases} n: & \psi_{\mu_1, \mu_2, \dots, \mu_n}^{(n)} = \bar{u}_{\mu_1, \mu_2, \dots, \mu_n}(p_{N^*}, S_{N^*}) \gamma_5 v(p_N, S_N) \\ n+1: & \psi_{\mu_1, \mu_2, \dots, \mu_{n+1}}^{(n+1)} = \bar{u}_{\mu_1, \mu_2, \dots, \mu_n}(p_{N^*}, S_{N^*}) \left(\gamma_{\mu_{n+1}} - \frac{r_{\mu_{n+1}}}{m_\psi + m_{N^*} + m_N} \right) v(p_N, S_N) + (\mu_i \leftrightarrow \mu_j) \end{cases}$$

$$L_{\bar{N}N^*} \sim \tilde{t}_{\mu_1, \mu_2, \dots, \mu_L}^{(L)}(r, p_\psi)$$

$$\tilde{t}^{(0)}(r, p_\psi) = 1; \quad \tilde{t}^{(1)}_\mu(r, p_\psi) = \tilde{r}_\mu \equiv \tilde{g}_{\mu\nu}(p_\psi) r^\nu$$

$$\tilde{t}^{(2)}_{\mu\nu}(r, p_\psi) = \tilde{r}_\mu \tilde{r}_\nu - \frac{1}{3}(\tilde{r} \cdot \tilde{r}) \tilde{g}_{\mu\nu}(p_\psi); \quad \dots$$

S. Dulat, J.-J. Wu, B. S. Zou PRD 83 (2011) 094032

$$\tilde{t}_{\mu_1 \mu_2 \dots \mu_L}^{(L)} = \tilde{r}_{\mu_1} \tilde{r}_{\mu_2} \dots \tilde{r}_{\mu_L} + \sum_{l=1}^{[L/2]} \sum_{i_1 < i_2 < \dots < i_{2l}=1}^L \frac{(-\tilde{r} \cdot \tilde{r})^l}{(2L-1)(2L-3)\dots(2L-2l+1)}$$

$$\times \frac{1}{2^l l!} (\tilde{g}_{\mu_1 \mu_2} \tilde{g}_{\mu_3 \mu_4} \dots \tilde{g}_{\mu_{2l-1} \mu_{2l}} + \mu_{i_1}, \mu_{i_2}, \dots, \mu_{i_{2l}} \text{ permutation}, (2l)! \text{ term})$$

$$\times (\tilde{r}_{\mu_1} \tilde{r}_{\mu_2} \dots \tilde{r}_{\mu_{i_1-1}} \tilde{r}_{\mu_{i_1+1}} \dots \tilde{r}_{\mu_{i_2-1}} \tilde{r}_{\mu_{i_2+1}} \dots \tilde{r}_{\mu_{i_{2l-1}-1}} \tilde{r}_{\mu_{i_{2l-1}+1}} \dots \tilde{r}_{\mu_L}), \quad (12)$$



L-S scheme

$$S_{\bar{N}} = \frac{1}{2}, \quad S_{N^*} = \frac{2n+1}{2}$$

$$r = p_{N^*} - p_N$$

$$\psi \rightarrow \bar{N}N^*$$

$$J = S_\psi = S_{\bar{N}N^*} + L_{\bar{N}N^*}$$

$$S_{\bar{N}N^*} \begin{cases} n: & \psi_{\mu_1, \mu_2, \dots, \mu_n}^{(n)} = \bar{u}_{\mu_1, \mu_2, \dots, \mu_n}(p_{N^*}, S_{N^*}) \gamma_5 v(p_N, S_N) \\ n+1: & \psi_{\mu_1, \mu_2, \dots, \mu_{n+1}}^{(n+1)} = \bar{u}_{\mu_1, \mu_2, \dots, \mu_n}(p_{N^*}, S_{N^*}) \left(\gamma_{\mu_{n+1}} - \frac{r_{\mu_{n+1}}}{m_\psi + m_{N^*} + m_N} \right) v(p_N, S_N) + (\mu_i \leftrightarrow \mu_j) \end{cases}$$

$$L_{\bar{N}N^*} \sim \tilde{t}_{\mu_1, \mu_2, \dots, \mu_L}^{(L)}(r, p_\psi)$$

$$\tilde{t}^{(0)}(r, p_\psi) = 1; \quad \tilde{t}^{(1)}_\mu(r, p_\psi) = \tilde{r}_\mu \equiv \tilde{g}_{\mu\nu}(p_\psi) r^\nu$$

$$\tilde{t}^{(2)}_{\mu\nu}(r, p_\psi) = \tilde{r}_\mu \tilde{r}_\nu - \frac{1}{3}(\tilde{r} \cdot \tilde{r}) \tilde{g}_{\mu\nu}(p_\psi); \quad \dots$$

S. Dulat, J.-J. Wu, B. S. Zou PRD 83 (2011) 094032

$$\tilde{t}_{\mu_1 \mu_2 \dots \mu_L}^{(L)} = \tilde{r}_{\mu_1} \tilde{r}_{\mu_2} \dots \tilde{r}_{\mu_L} + \sum_{l=1}^{[L/2]} \sum_{i_1 < i_2 < \dots < i_{2l}=1}^L \frac{(-\tilde{r} \cdot \tilde{r})^l}{(2L-1)(2L-3)\dots(2L-2l+1)}$$

$$\times \frac{1}{2^l l!} (\tilde{g}_{\mu_1 \mu_2} \tilde{g}_{\mu_3 \mu_4} \dots \tilde{g}_{\mu_{2l-1} \mu_{2l}} + \mu_{i_1}, \mu_{i_2}, \dots, \mu_{i_{2l}} \text{ permutation}, (2l)! \text{ term})$$

$$\times (\tilde{r}_{\mu_1} \tilde{r}_{\mu_2} \dots \tilde{r}_{\mu_{i_1-1}} \tilde{r}_{\mu_{i_1+1}} \dots \tilde{r}_{\mu_{i_2-1}} \tilde{r}_{\mu_{i_2+1}} \dots \tilde{r}_{\mu_{i_{2l-1}-1}} \tilde{r}_{\mu_{i_{2l-1}+1}} \dots \tilde{r}_{\mu_L}), \quad (12)$$

$$S_\psi = S_{\bar{N}N^*} + L_{\bar{N}N^*}$$

$$\psi_{\mu_1, \mu_2, \dots, \mu_S}^{(S)}, \quad \tilde{t}_{\mu_1, \mu_2, \dots, \mu_L}^{(L)}, \quad \varepsilon_{\mu_1, \dots, \mu_J}(p_\psi, S_\psi)$$



L-S scheme

$$S_{\bar{N}} = \frac{1}{2}, \quad S_{N^*} = \frac{2n+1}{2}$$

$$r = p_{N^*} - p_N$$

$$\psi \rightarrow \bar{N}N^*$$

$$J = S_\psi = S_{\bar{N}N^*} + L_{\bar{N}N^*}$$

$$S_{\bar{N}N^*} \left\{ \begin{array}{l} n: \quad \psi_{\mu_1, \mu_2, \dots, \mu_n}^{(n)} = \bar{u}_{\mu_1, \mu_2, \dots, \mu_n}(p_{N^*}, S_{N^*}) \gamma_5 v(p_N, S_N) \\ n+1: \quad \psi_{\mu_1, \mu_2, \dots, \mu_{n+1}}^{(n+1)} = \bar{u}_{\mu_1, \mu_2, \dots, \mu_n}(p_{N^*}, S_{N^*}) \left(\gamma_{\mu_{n+1}} - \frac{r_{\mu_{n+1}}}{m_\psi + m_{N^*} + m_N} \right) v(p_N, S_N) + (\mu_i \leftrightarrow \mu_j) \end{array} \right.$$

$$L_{\bar{N}N^*} \sim \tilde{t}_{\mu_1, \mu_2, \dots, \mu_L}^{(L)}(r, p_\psi)$$

$$\tilde{t}^{(0)}(r, p_\psi) = 1; \quad \tilde{t}^{(1)}_\mu(r, p_\psi) = \tilde{r}_\mu \equiv \tilde{g}_{\mu\nu}(p_\psi) r^\nu$$

$$\tilde{t}^{(2)}_{\mu\nu}(r, p_\psi) = \tilde{r}_\mu \tilde{r}_\nu - \frac{1}{3}(\tilde{r} \cdot \tilde{r}) \tilde{g}_{\mu\nu}(p_\psi); \quad \dots$$

S. Dulat, J.-J. Wu, B. S. Zou PRD 83 (2011) 094032

$$\begin{aligned} \tilde{t}_{\mu_1 \mu_2 \dots \mu_L}^{(L)} &= \tilde{r}_{\mu_1} \tilde{r}_{\mu_2} \dots \tilde{r}_{\mu_L} + \sum_{l=1}^{[L/2]} \sum_{i_1 < i_2 < \dots < i_{2l}=1}^L \frac{(-\tilde{r} \cdot \tilde{r})^l}{(2L-1)(2L-3)\dots(2L-2l+1)} \\ &\times \frac{1}{2^l l!} (\tilde{g}_{\mu_1 \mu_2} \tilde{g}_{\mu_3 \mu_4} \dots \tilde{g}_{\mu_{2l-1} \mu_{2l}} + \mu_{i_1}, \mu_{i_2}, \dots, \mu_{i_{2l}} \text{ permutation, } (2l)! \text{ term}) \\ &\times (\tilde{r}_{\mu_1} \tilde{r}_{\mu_2} \dots \tilde{r}_{\mu_{i_1-1}} \tilde{r}_{\mu_{i_1+1}} \dots \tilde{r}_{\mu_{i_2-1}} \tilde{r}_{\mu_{i_2+1}} \dots \tilde{r}_{\mu_{i_{2l-1}-1}} \tilde{r}_{\mu_{i_{2l-1}+1}} \dots \tilde{r}_{\mu_L}), \end{aligned} \quad (12)$$

$$S_\psi = S_{\bar{N}N^*} + L_{\bar{N}N^*}$$

$$\psi_{\mu_1, \mu_2, \dots, \mu_S}^{(S)}, \quad \tilde{t}_{\mu_1, \mu_2, \dots, \mu_L}^{(L)}, \quad \varepsilon_{\mu_1, \dots, \mu_J}(p_\psi, S_\psi)$$

If $S+L+J=\text{odd}$, $M \sim \varepsilon^{\alpha\beta\gamma\sigma} \psi_{\mu_i \mu_j, \alpha}^{(S)} \tilde{t}'_{\mu'_i \mu'_k, \beta} \varepsilon_{\mu'_j \mu'_k, \gamma} p_{\psi, \sigma} g^{\mu_i \mu'_i} g^{\mu_j \mu'_j} g^{\mu_k \mu'_k}$

If $S+L+J=\text{even}$, $M \sim \psi_{\mu_i \mu_j}^{(S)} \tilde{t}'_{\mu'_i \mu'_k} \varepsilon_{\mu'_j \mu'_k} g^{\mu_i \mu'_i} g^{\mu_j \mu'_j} g^{\mu_k \mu'_k}$

We also need to consider Parity conservation.



L-S scheme

$$\psi \rightarrow \bar{B}(1/2-)B(1/2+) \xrightarrow{L: S \text{ and } D \text{ wave}} r_{eff} \sim \frac{\bar{L}}{p}$$

This is a very useful PWA tool

PHYSICAL REVIEW C 67, 015204 (2003)

Lorentz covariant orbital-spin scheme for the effective N^*NM couplings

B. S. Zou^{1,2,3,*} and F. Hussain^{3,†}

$\psi \rightarrow \bar{N}^*N^*$
Such as $\Sigma^*\bar{\Sigma}^*$

Here I mainly introduce it for $\psi \rightarrow \bar{N}N^*$ case

Update: Recently, we propose a new method based on Group theory to write down **covariant** partial wave amplitudes within **L-S scheme** for three-particle vertex with **any spin**. And we also show that it is equivalent with usual helicity amplitude.

Covariant orbital-spin scheme for any spin based on irreducible tensor

#43

Hao-Jie Jing (Beijing, GUCAS), Di Ben (Beijing, Inst. Theor. Phys. and Beijing, GUCAS), Shu-Ming Wu (Beijing, GUCAS and Beijing, Inst. Theor. Phys.), Jia-Jun Wu (Beijing, GUCAS), Bing-Song Zou (Beijing, Inst. Theor. Phys. and Central South U., Changsha) (Jan 4, 2023)

Published in: *JHEP* 06 (2023) 039, *JHEP* 06 (2023) 039 • e-Print: 2301.01575 [hep-ph]

Algorithms for partial wave amplitudes in the covariant L - S scheme

#22

Hao-Jie Jing (Beijing, GUCAS), Shu-Ming Wu (Beijing, GUCAS), Jia-Jun Wu (Beijing, GUCAS and Lanzhou, Inst. Modern Phys.) (May 10, 2024)

Published in: *Phys.Rev.D* 110 (2024) 1, 016014 • e-Print: 2405.06576 [hep-ph]



Two ways for the amplitude of $\psi \rightarrow \bar{B}B$

Method 1, using G_E^ψ and G_M^ψ , the amplitude,

$$M = -ie_g \bar{u}_B \left(G_E^\psi \gamma_\mu - \frac{2m_B}{r^2} (G_M^\psi - G_E^\psi) r_\mu \right) v_{\bar{B}} \epsilon^\mu$$

$$r^2 = q^2 = \frac{s}{4} - m_B^2$$

G. Fäldt, EPJA 52 141(2016)

G. Fäldt and A. Kupsc, PLB 772 16(2017)



Two ways for the amplitude of $\psi \rightarrow \bar{B}B$

Method 1, using G_E^ψ and G_M^ψ , the amplitude,

$$M = -ie_g \bar{u}_B \left(G_E^\psi \gamma_\mu - \frac{2m_B}{r^2} (G_M^\psi - G_E^\psi) r_\mu \right) v_{\bar{B}} \epsilon^\mu$$

G. Fäldt, EPJA 52 141(2016)

G. Fäldt and A. Kupsc, PLB 772 16(2017)

$$r^2 = q^2 = \frac{s}{4} - m_B^2$$

Method 2, using L-S scheme, the amplitude,

$$M = \psi_\mu^{(1)} (g_S g^{\mu\nu} + g_D e^{i\delta} \tilde{t}^{(2)\mu\nu}) \epsilon_\nu = \bar{u}_B \left(\gamma_\mu - \frac{(p_B - p_{\bar{B}})}{m_\psi + 2m_B} \right) v_{\bar{B}} (g_S g^{\mu\nu} + g_D e^{i\delta} \tilde{t}^{(2)\mu\nu}) \epsilon_\nu$$

$$\psi(1^-) \rightarrow \bar{B}(1/2^-) B(1/2^+)$$

$$S_\psi = S_{\bar{N}N^*} + L_{\bar{N}N^*}$$

$$1 = 1 + (0, 2)$$

Including S- and D-wave



Two ways for the amplitude of $\psi \rightarrow \bar{B}B$

Method 1, using G_E^ψ and G_M^ψ , the amplitude,

$$M = -ie_g \bar{u}_B \left(G_E^\psi \gamma_\mu - \frac{2m_B}{r^2} (G_M^\psi - G_E^\psi) r_\mu \right) v_{\bar{B}} \epsilon^\mu$$

G. Fäldt, EPJA 52 141(2016)

G. Fäldt and A. Kupsc, PLB 772 16(2017)

$$r^2 = q^2 = \frac{s}{4} - m_B^2$$

$\psi(1^-) \rightarrow \bar{B}(1/2^-)B(1/2^+)$

Method 2, using L-S scheme, the amplitude,

$$M = \psi_\mu^{(1)} (g_S g^{\mu\nu} + g_D e^{i\delta} \tilde{t}^{(2)\mu\nu}) \epsilon_\nu = \bar{u}_B \left(\gamma_\mu - \frac{(p_B - p_{\bar{B}})}{m_\psi + 2m_B} \right) v_{\bar{B}} (g_S g^{\mu\nu} + g_D e^{i\delta} \tilde{t}^{(2)\mu\nu}) \epsilon_\nu$$

$$S_\psi = S_{\bar{N}N^*} + L_{\bar{N}N^*}$$

$$1 = 1 + (0, 2)$$

Including S- and D-wave

Relationship, there are three free parameters in both cases, we can define them as: an overall

coupling constant, $\left| \frac{g_D}{g_S} \right| \left(\left| \frac{G_E^\psi}{G_M^\psi} \right| \right)$, and $\delta \left(\Delta\Phi \equiv \text{Arg} \left(\frac{G_E^\psi}{G_M^\psi} \right) \right)$, typically,

$$e^{i\delta} \frac{g_D}{g_S} = - \frac{3}{2r^2} \frac{2m_B - r^2 / (m_\psi + 2m_B) - 2m_B \left(G_E^\psi / G_M^\psi \right)}{2m_B - r^2 / (m_\psi + 2m_B) + 2m_B \left(G_E^\psi / G_M^\psi \right)}$$



Two ways for the amplitude of $\psi \rightarrow \bar{B}B$

Method 1, using G_E^ψ and G_M^ψ , the amplitude, $M = -ie_g \bar{u}_B \left(G_E^\psi \gamma_\mu - \frac{2m_B}{r^2} (G_M^\psi - G_E^\psi) r_\mu \right) v_{\bar{B}} \epsilon^\mu$

Method 2, using PAW, the amplitude, $M = \bar{u}_B \left(\gamma_\mu - \frac{(p_B - p_{\bar{B}})}{m_\psi + 2m_B} \right) v_{\bar{B}} (g_S g^{\mu\nu} + g_D e^{i\delta} \tilde{t}^{(2)\mu\nu}) \epsilon_\nu$

Experimentally,

(1) an overall coupling constant can be obtained from the partial width Γ .

(2) $t = \left| \frac{g_D}{g_S} \right|$ and δ can be determined by angular distribution, $\frac{d\Gamma}{d\cos\theta} \sim (1 + \alpha \cos^2\theta)$,

and $\Delta\Phi \equiv \text{Arg} \left(\frac{G_E^\psi}{G_M^\psi} \right)$

$$\alpha = \frac{-3t^2 r^2 / 8 - 9tr^2 \cos\delta}{9 + 5t^2 r^2 / 8 - 3tr^2 \cos\delta}$$

$$e^{i\Delta\Phi} = \sqrt{\frac{1 + \alpha \left(\frac{2m_B}{m_\psi} - \frac{r^2}{m_\psi(m_\psi + 2m_B)} \right) \frac{3 + 2r^2 t e^{i\delta}}{3 - r^2 t e^{i\delta}}}{1 - \alpha \left(\frac{2m_B}{m_\psi} - \frac{r^2}{m_\psi(m_\psi + 2m_B)} \right) \frac{3 + 2r^2 t e^{i\delta}}{3 - r^2 t e^{i\delta}}}}$$



Two ways for the amplitude of $\psi \rightarrow \bar{B} B$

Method 1, using G_E^ψ and G_M^ψ , the amplitude, $M = -ie_g \bar{u}_B \left(G_E^\psi \gamma_\mu - \frac{2m_B}{r^2} (G_M^\psi - G_E^\psi) r_\mu \right) v_{\bar{B}} \epsilon^\mu$

Method 2, using PAW, the amplitude, $M = \bar{u}_B \left(\gamma_\mu - \frac{(p_B - p_{\bar{B}})}{m_\psi + 2m_B} \right) v_{\bar{B}} (g_S g^{\mu\nu} + g_D e^{i\delta} \tilde{t}^{(2)\mu\nu}) \epsilon_\nu$

Experimentally,

(1) an overall coupling constant can be obtained from the partial width Γ .

(2) $t = \left| \frac{g_D}{g_S} \right|$ and δ can be determined by angular distribution, $\frac{d\Gamma}{d \cos \theta} \sim (1 + \alpha \cos^2 \theta)$,

and $\Delta\Phi \equiv \text{Arg} \left(\frac{G_E^\psi}{G_M^\psi} \right)$

$$\alpha = \frac{-3t^2 r^2 / 8 - 9tr^2 \cos \delta}{9 + 5t^2 r^2 / 8 - 3tr^2 \cos \delta}$$

$$e^{i\Delta\Phi} = \sqrt{\frac{1 + \alpha \left(\frac{2m_B}{m_\psi} - \frac{r^2}{m_\psi(m_\psi + 2m_B)} \right) \frac{3 + 2r^2 t e^{i\delta}}{3 - r^2 t e^{i\delta}}}{1 - \alpha \left(\frac{2m_B}{m_\psi} - \frac{r^2}{m_\psi(m_\psi + 2m_B)} \right) \frac{3 + 2r^2 t e^{i\delta}}{3 - r^2 t e^{i\delta}}}}$$



Two ways for the amplitude of $\psi \rightarrow \bar{B} B$

Method 1, using G_E^ψ and G_M^ψ , the amplitude, $M = -ie_g \bar{u}_B \left(G_E^\psi \gamma_\mu - \frac{2m_B}{r^2} (G_M^\psi - G_E^\psi) r_\mu \right) v_{\bar{B}} \epsilon^\mu$

Method 2, using PAW, the amplitude, $M = \bar{u}_B \left(\gamma_\mu - \frac{(p_B - p_{\bar{B}})}{m_\psi + 2m_B} \right) v_{\bar{B}} (g_S g^{\mu\nu} + g_D e^{i\delta} \tilde{t}^{(2)\mu\nu}) \epsilon_\nu$

Experimentally,

(1) an overall coupling constant can be obtained from the partial width Γ .

(2) $t = \left| \frac{g_D}{g_S} \right|$ and δ can be determined by angular distribution, $\frac{d\Gamma}{d \cos \theta} \sim (1 + \alpha \cos^2 \theta)$,

and $\Delta\Phi \equiv \text{Arg} \left(\frac{G_E^\psi}{G_M^\psi} \right)$

$$\alpha = \frac{-3t^2 r^2 / 8 - 9tr^2 \cos \delta}{9 + 5t^2 r^2 / 8 - 3tr^2 \cos \delta};$$

$$e^{i\Delta\Phi} = \sqrt{\frac{1 + \alpha}{1 - \alpha}} \left(\frac{2m_B}{m_\psi} - \frac{r^2}{m_\psi(m_\psi + 2m_B)} \right) \frac{3 + 2r^2 t e^{i\delta}}{3 - r^2 t e^{i\delta}}$$



The effective radius of the decay reaction

$$t = \left| \frac{g_D}{g_S} \right| \quad \alpha = \frac{-3t^2 r^2 / 8 - 9tr^2 \cos \delta}{9 + 5t^2 r^2 / 8 - 3tr^2 \cos \delta};$$
$$e^{i\Delta\Phi} = \sqrt{\frac{1 + \alpha}{1 - \alpha} \left(\frac{2m_B}{m_\psi} - \frac{r^2}{m_\psi(m_\psi + 2m_B)} \right)} \frac{3 + 2r^2 t e^{i\delta}}{3 - r^2 t e^{i\delta}}$$

$$\frac{\Gamma_S}{\Gamma_{total}} = \frac{9}{9 + 2t^2 (m_\psi^2 - 2m_B^2)^2}$$
$$\bar{l} = l_S \frac{\Gamma_S}{\Gamma_{total}} + l_D \frac{\Gamma_D}{\Gamma_{total}}$$
$$r_{\text{eff}} = \frac{\bar{l}}{p}$$



The effective radius of the decay reaction

$$t = \left| \frac{g_D}{g_S} \right| \quad \alpha = \frac{-3t^2 r^2 / 8 - 9tr^2 \cos \delta}{9 + 5t^2 r^2 / 8 - 3tr^2 \cos \delta};$$

$$e^{i\Delta\Phi} = \sqrt{\frac{1 + \alpha \left(\frac{2m_B}{m_\psi} - \frac{r^2}{m_\psi(m_\psi + 2m_B)} \right)}{1 - \alpha \left(\frac{2m_B}{m_\psi} - \frac{r^2}{m_\psi(m_\psi + 2m_B)} \right)}} \frac{3 + 2r^2 t e^{i\delta}}{3 - r^2 t e^{i\delta}}$$

$$\frac{\Gamma_S}{\Gamma_{total}} = \frac{9}{9 + 2t^2 (m_\psi^2 - 2m_B^2)^2}$$

$$\bar{l} = l_S \frac{\Gamma_S}{\Gamma_{total}} + l_D \frac{\Gamma_D}{\Gamma_{total}}$$

$$r_{eff} = \frac{\bar{l}}{p}$$

Mode	α	$\Delta\Phi$	g_D/g_S	δ	Γ_S/Γ_{Total}	r_{eff}
$J/\psi \rightarrow \Lambda \bar{\Lambda}$	$0.461 \pm 0.013[23]$	$0.74 \pm 0.019[23]$	0.180 ± 0.005	-0.804 ± 0.024	$85.7 \pm 0.6\%$	0.0488 ± 0.0021
$J/\psi \rightarrow \Sigma^+ \bar{\Sigma}^-$	$-0.508 \pm 0.010[24]$	$-0.270 \pm 0.021[24]$	0.171 ± 0.006	2.67 ± 0.04	$90.9 \pm 0.6\%$	0.0362 ± 0.0024
$\psi(2S) \rightarrow \Sigma^+ \bar{\Sigma}^-$	$0.682 \pm 0.041[24]$	$0.379 \pm 0.084[24]$	0.097 ± 0.009	-0.33 ± 0.10	$88.3 \pm 2.0\%$	0.033 ± 0.006



The effective radius of the decay reaction

$$t = \left| \frac{g_D}{g_S} \right| \quad \alpha = \frac{-3t^2 r^2 / 8 - 9tr^2 \cos \delta}{9 + 5t^2 r^2 / 8 - 3tr^2 \cos \delta};$$

$$e^{i\Delta\Phi} = \sqrt{\frac{1 + \alpha \left(\frac{2m_B}{m_\psi} - \frac{r^2}{m_\psi(m_\psi + 2m_B)} \right)}{1 - \alpha \left(\frac{2m_B}{m_\psi} - \frac{r^2}{m_\psi(m_\psi + 2m_B)} \right)}} \frac{3 + 2r^2 t e^{i\delta}}{3 - r^2 t e^{i\delta}}$$

Need further decay, such as $\Lambda \rightarrow p \pi$

$$\frac{\Gamma_S}{\Gamma_{total}} = \frac{9}{9 + 2t^2 (m_\psi^2 - 2m_B^2)^2}$$

$$\bar{l} = l_S \frac{\Gamma_S}{\Gamma_{total}} + l_D \frac{\Gamma_D}{\Gamma_{total}}$$

$$r_{eff} = \frac{\bar{l}}{p}$$

Mode	α	$\Delta\Phi$	g_D/g_S	δ	Γ_S/Γ_{Total}	r_{eff}
$J/\psi \rightarrow \Lambda \bar{\Lambda}$	$0.461 \pm 0.013[23]$	$0.74 \pm 0.019[23]$	0.180 ± 0.005	-0.804 ± 0.024	$85.7 \pm 0.6\%$	0.0488 ± 0.0021
$J/\psi \rightarrow \Sigma^+ \bar{\Sigma}^-$	$-0.508 \pm 0.010[24]$	$-0.270 \pm 0.021[24]$	0.171 ± 0.006	2.67 ± 0.04	$90.9 \pm 0.6\%$	0.0362 ± 0.0024
$\psi(2S) \rightarrow \Sigma^+ \bar{\Sigma}^-$	$0.682 \pm 0.041[24]$	$0.379 \pm 0.084[24]$	0.097 ± 0.009	-0.33 ± 0.10	$88.3 \pm 2.0\%$	0.033 ± 0.006



The effective radius of the decay reaction

Mode	α	$\Delta\Phi$	g_D/g_S	δ	$\Gamma_S/\Gamma_{\text{Total}}$	r_{eff}
$J/\psi \rightarrow \Lambda\bar{\Lambda}$	$0.461 \pm 0.013[23]$	$0.74 \pm 0.019[23]$	0.180 ± 0.005	-0.804 ± 0.024	$85.7 \pm 0.6\%$	0.0488 ± 0.0021
$J/\psi \rightarrow \Sigma^+\bar{\Sigma}^-$	$-0.508 \pm 0.010[24]$	$-0.270 \pm 0.021[24]$	0.171 ± 0.006	2.67 ± 0.04	$90.9 \pm 0.6\%$	0.0362 ± 0.0024
$\psi(2S) \rightarrow \Sigma^+\bar{\Sigma}^-$	$0.682 \pm 0.041[24]$	$0.379 \pm 0.084[24]$	0.097 ± 0.009	-0.33 ± 0.10	$88.3 \pm 2.0\%$	0.033 ± 0.006



The effective radius of the decay reaction

Mode	α	$\Delta\Phi$	g_D/g_S	δ	$\Gamma_S/\Gamma_{\text{Total}}$	r_{eff}
$J/\psi \rightarrow \Lambda \bar{\Lambda}$	$0.461 \pm 0.013[23]$	$0.74 \pm 0.019[23]$	0.180 ± 0.005	-0.804 ± 0.024	$85.7 \pm 0.6\%$	0.0488 ± 0.0021
$J/\psi \rightarrow \Sigma^+ \bar{\Sigma}^-$	$-0.508 \pm 0.010[24]$	$-0.270 \pm 0.021[24]$	0.171 ± 0.006	2.67 ± 0.04	$90.9 \pm 0.6\%$	0.0362 ± 0.0024
$\psi(2S) \rightarrow \Sigma^+ \bar{\Sigma}^-$	$0.682 \pm 0.041[24]$	$0.379 \pm 0.084[24]$	0.097 ± 0.009	-0.33 ± 0.10	$88.3 \pm 2.0\%$	0.033 ± 0.006

通过这个计算可以发现 ψ 的有效衰变半径很小。这样就会导致 $\psi \rightarrow \bar{N}N^*$ 的轨道角动量很小，即 $L = r_{\text{eff}} \times p$ ，那么就很难产生高自旋的 N^* 。所以在这类过程中， N^* 的分波分析其实只要取到 $l = 5/2$ 就基本足够分析数据了。

当然我们需要更多的数据来确认。



Motivation

Question: How many partial waves does ψ decay need ?

N(2190) 7/2-	πN and γN
N(2220) 9/2+	πN and γN
N(2250) 9/2-	πN and γN
N(2300) 1/2+	$\psi(2S)$ decay
N(2570) 5/2-	$\psi(2S)$ decay
N(2600) 11/2-	πN
N(2700) 13/2+	πN

$$L = r_{eff} \times p$$

πN and γN

$$E \sim 2 \text{ GeV} \rightarrow p \sim 1 \text{ GeV}$$

$$r_{eff} \sim r_N \sim 1 \text{ fm}$$

$$L \sim 1 \text{ fm} \times 1 \text{ GeV} \sim 5$$

$$J_{N^*} \sim \left[5 - \frac{3}{2}, 5 + \frac{3}{2} \right] \sim \left[\frac{7}{2}, \frac{13}{2} \right]$$

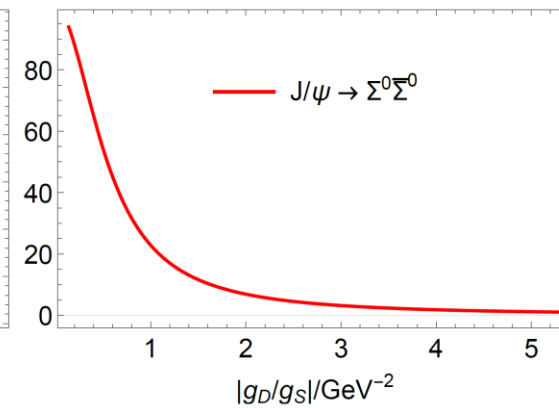
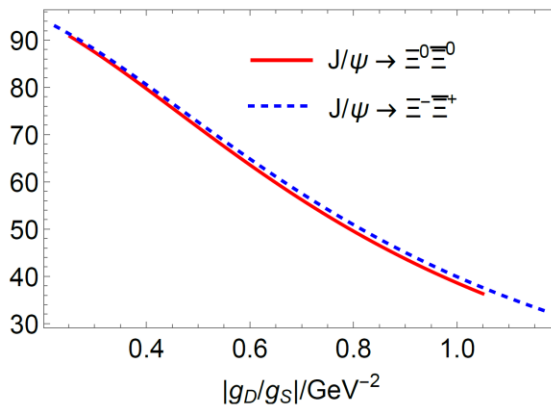
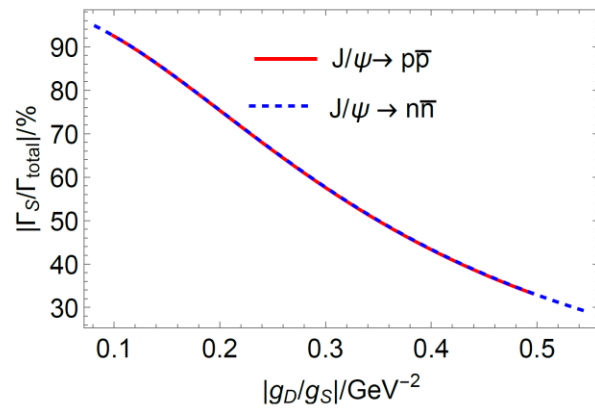
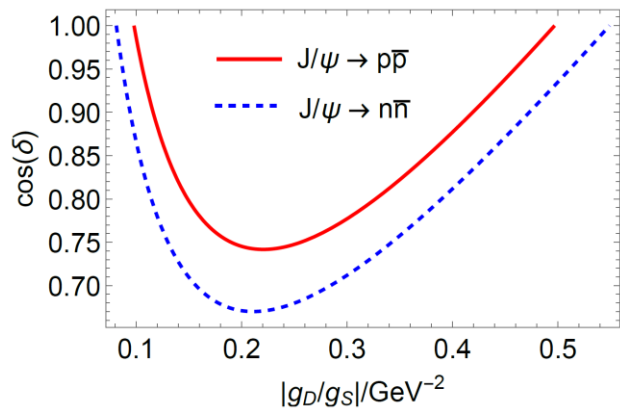
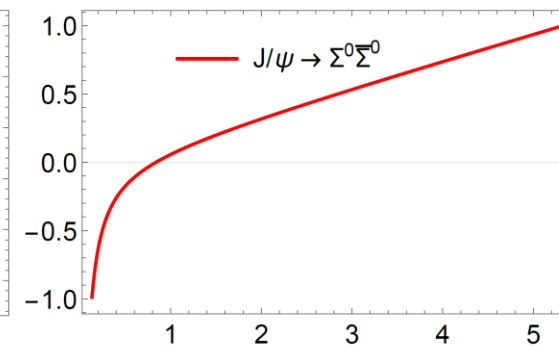
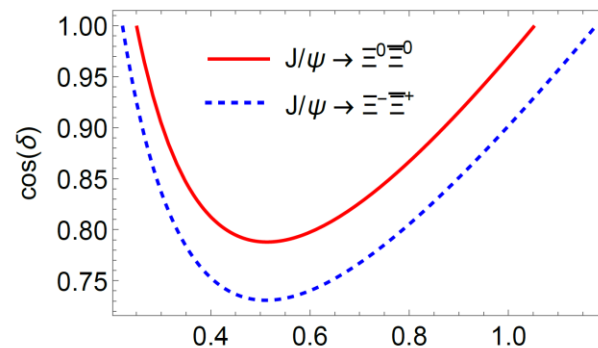
How to estimate the effective radius of the ψ decay ???

$$\psi \rightarrow \bar{B}(1/2-)B(1/2+) \longrightarrow r_{eff} \sim \frac{\bar{L}}{p}$$



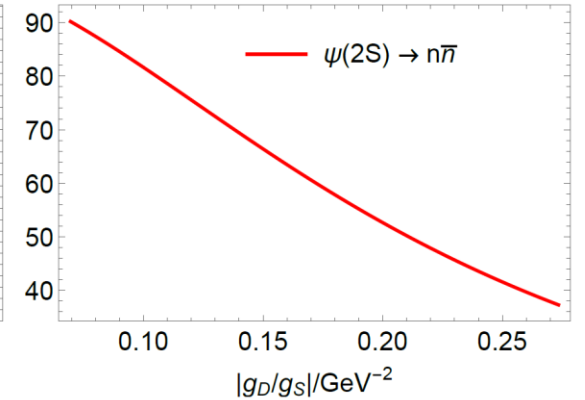
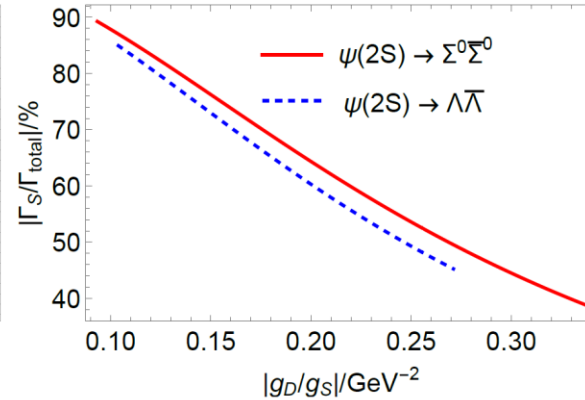
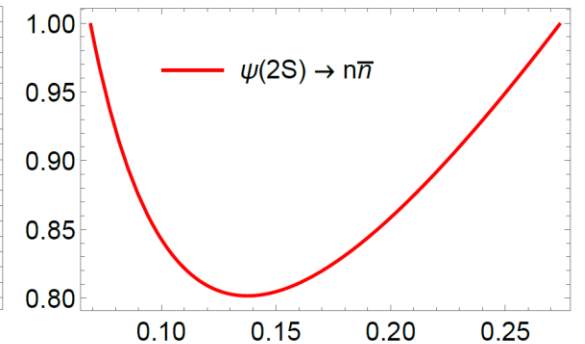
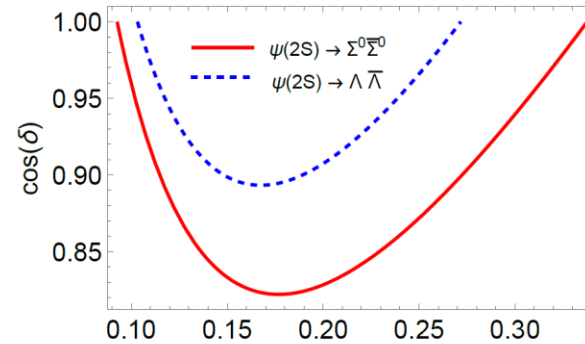
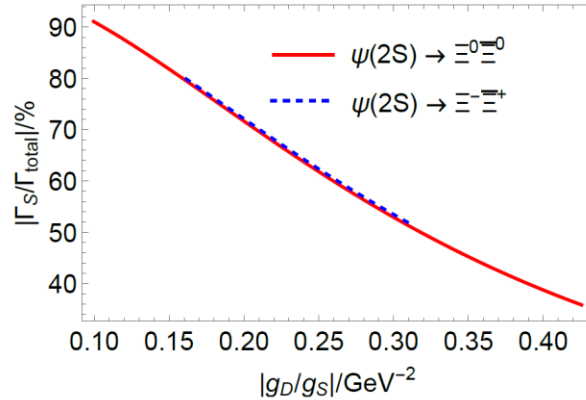
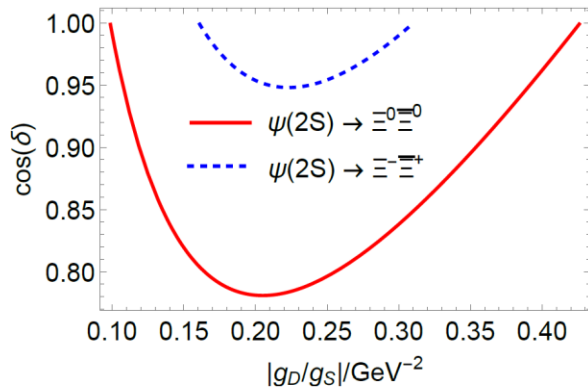
The effective radius of the decay reaction

Mode	α	$r_{\text{eff}}(\text{fm})$
$J/\psi \rightarrow p\bar{p}$	$0.595 \pm 0.027[26]$	$[0.023 - 0.214]$
$J/\psi \rightarrow n\bar{n}$	$0.50 \pm 0.25[26]$	$[0.016 - 0.228]$
$J/\psi \rightarrow \Sigma^0\bar{\Sigma}^0$	$-0.449 \pm 0.028[25]$	$[0.022 - 0.396]$
$J/\psi \rightarrow \Xi^0\bar{\Xi}^0$	$0.66 \pm 0.08[28]$	$[0.044 - 0.308]$
$J/\psi \rightarrow \Xi^-\bar{\Xi}^+$	$0.58 \pm 0.12[29]$	$[0.034 - 0.331]$



The effective radius of the decay reaction

Mode	α	$r_{\text{eff}}(\text{fm})$
$\psi_{2S} \rightarrow \Lambda \bar{\Lambda}$	0.82 ± 0.10 [25]	[0.040 – 0.148]
$\psi_{2S} \rightarrow p \bar{p}$	1.03 ± 0.09 [27]	???
$\psi_{2S} \rightarrow n \bar{n}$	0.68 ± 0.23 [27]	[0.024 – 0.156]
$\psi_{2S} \rightarrow \Sigma^0 \bar{\Sigma}^0$	0.71 ± 0.15 [25]	[0.030 – 0.172]
$\psi_{2S} \rightarrow \Xi^0 \bar{\Xi}^0$	0.65 ± 0.23 [28]	[0.027 – 0.196]
$\psi_{2S} \rightarrow \Xi^- \bar{\Xi}^+$	0.91 ± 0.27 [29]	[0.061 – 0.148]

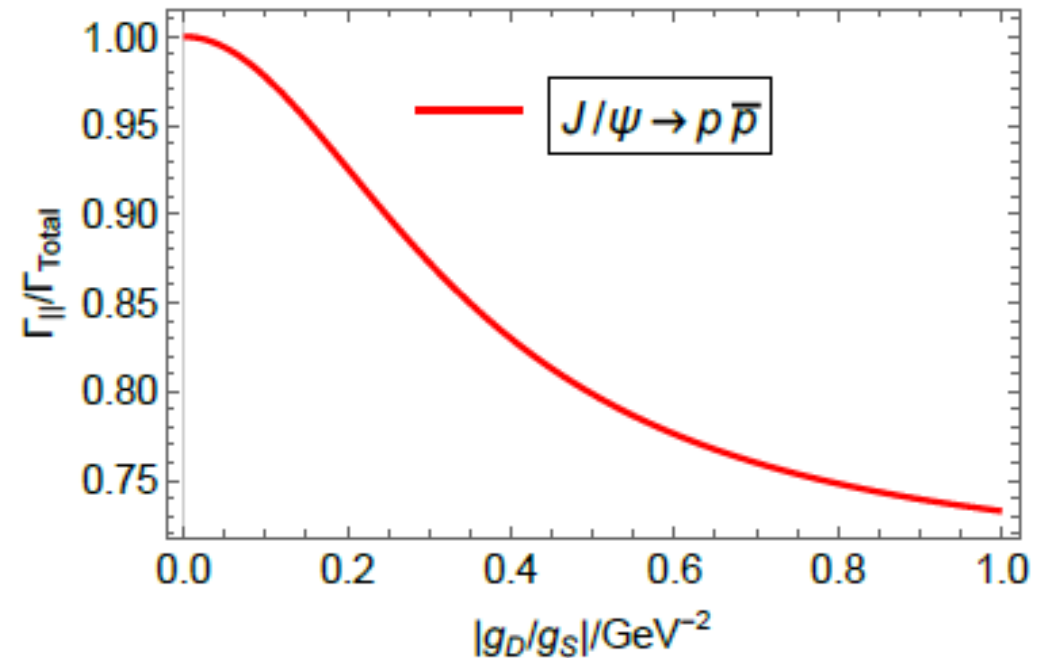


The effective radius of the decay reaction

Mode	α	$r_{\text{eff}}(\text{fm})$
$\psi_{2S} \rightarrow \Lambda \bar{\Lambda}$	0.82 ± 0.10 [25]	[0.040 – 0.148]
$\psi_{2S} \rightarrow p \bar{p}$	1.03 ± 0.09 [27]	???
$\psi_{2S} \rightarrow n \bar{n}$	0.68 ± 0.23 [27]	[0.024 – 0.156]

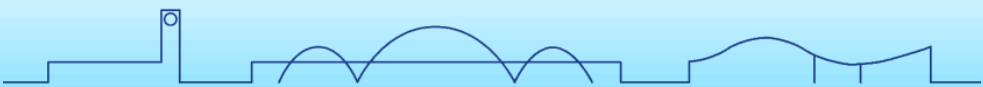
Since $p(n)$ can not further decay, thus $\Delta\Phi$ cannot be measured. We need new observable, such as $\Gamma_{//}$ to stand for the decay width of the process where $p(n)$ and $\bar{p}(\bar{n})$ have the same polarization,

$$\Gamma_{//} = \frac{|\vec{p}_B|}{32\pi^2 m_\psi^2} \int \frac{1}{2} \sum_{S_\psi, S_B=S_{\bar{B}}} |M(S_\psi, S_B, S_{\bar{B}})|^2 d\Omega = \Gamma_S + 0.7\Gamma_D$$

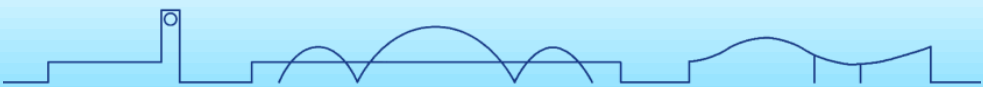


Summary

- Introduction of L-S scheme
- Through $\psi \rightarrow \bar{B}(1/2-)B(1/2+)$ to estimate the effective radius of ψ decay, around 0.05fm.
- It leads to low spin N^* dominate in the $\psi \rightarrow \bar{N}N^*$, thus, highest partial wave analysis require the total J of N^* with $l = 5/2$.
- It provides a unique window to search low spin baryon resonances with masses above 2 GeV in ψ decay.
- We need more experimental data to confirm it.



Thanks Very Much !



中国科学院大学
University of Chinese Academy of Sciences

