

Introduction of Helix Corrections

Yijing Wang

University of Science and technology of China

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Motivation

- Obvious difference between MC and data on the distribution of χ_{4c}^2 and pulls are observed in most analysis.
- **The traditional method:** using control samples to estimate the systematic error of this difference.
- **Disadvantages: Firstly** for most channels, it is hard to find appropriate reference channel with the final states and momentum distribution similar to the analysis process. **Furthermore,** it is difficult to select pure control sample without using kinematic constraints or selection criteria correlated with kinematic constraints such as total energy, total momentum and so on.
- **Method:** Correct the track helix parameters to reduce the difference between MC and data.
- The control samples used for μ and K corrections are:
 $e^+e^- \rightarrow j/\psi\pi^+\pi^- \rightarrow \mu^+\mu^-\pi^+\pi^-$ and $e^+e^- \rightarrow K^*K^\pm\pi^\mp \rightarrow K^+K^-\pi^+\pi^-$

Selection of $e^+e^- \rightarrow j/\psi\pi^+\pi^- \rightarrow \mu^+\mu^-\pi^+\pi^-$

Event selection

- Charged Track

$d_{xy} < 1.0$ cm, $d_z < 10.0$ cm, $\cos\theta < 0.93$;

nGood == 4, nCharged == 0;

- Lepton and pion identify

$P > 1.0$ GeV : lepton

$P < 1.0$ GeV : π

npion+ = npion-, nlepton+ = nlepton-

$E/P > 0.7$: e

$E < 0.45$ GeV : μ

- Kinematic fit : $\chi_{4C}^2 < 60$

- J/ψ mass window cut

$|M(J/\psi) - 3.097| < 0.02$

- open angle cut

$\cos\theta(\pi^+\pi^-) < 0.98$

$\cos\theta(l^+\pi^-) < 0.98$

$\cos\theta(l^-\pi^+) < 0.98$

Selection of $e^+e^- \rightarrow K^*K^\pm\pi^\mp \rightarrow K^+K^-\pi^+\pi^-$

Good charged tracks:

- $|V_z| < 10$ cm, $V_r < 1$ cm and $|\cos\theta| < 0.93$
- $N_{Good} = 4, \sum Q_{track} = 0$

PID:

- For K :
 $Prob_K > Prob_\pi \&\& Prob_K > Prob_p \&\& Prob_K > 0.001, N_{K^+} = N_{K^-} = 1$
- For π :
 $Prob_\pi > Prob_K \&\& Prob_\pi > Prob_p \&\& Prob_\pi > 0.001, N_{\pi^+} = N_{\pi^-} = 1$

Vertex Fit:

- Successful vertex fit for the two charge tracks

Kinematic Fit:

- Successful 4c kinematic fit, $\chi_{4c}^2 < 60$
- One of $M_{K^\pm\pi^\mp}$ should in the K^* window: $[0.8, 1]$ GeV/ c^2 .

The pull distribution

- d_0 : 螺旋线于x-y平面投影与IP的距离
- ϕ_0 : x-y平面内, POCA的方位角
- κ : 横动量的倒数 ($1/P_T$), 其符号反映粒子电荷的正负
- z_0 : POCA的z坐标
- $\tan\lambda$: λ 为螺旋线与x-y平面的夹角
- IP (Initial Point): 正负电子对撞点
- POCA (Point of closest approach)

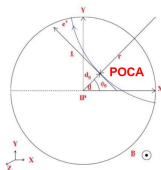
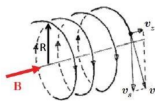
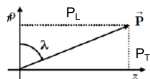


图 3.3 螺旋线径迹参数示意图



$$\mathbf{P} \equiv (d_0, \phi_0, \kappa, z_0, \tan\lambda)^T.$$

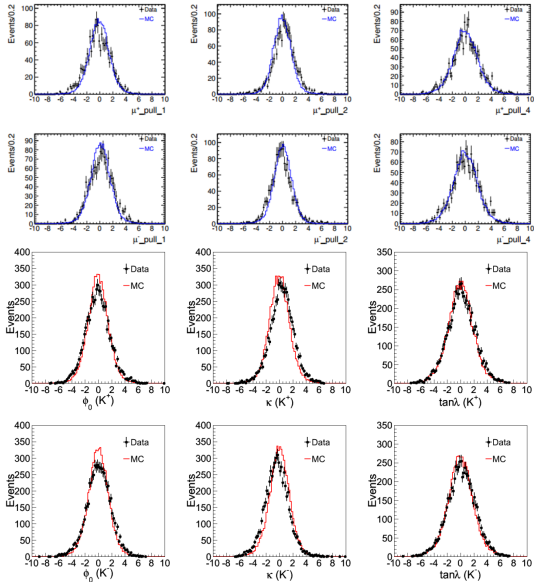


- One charge track of BESIII can be described by 5 parameters.

- The pull distribution is defined as: $pull_i = \frac{\alpha_i - \alpha_{0i}}{\sqrt{|(V_{a0})_{ii} - (V_a)_{ii}|}}$
- α_i : the i^{th} track parameter. V : the covariance matrix.

- Theoretically, the distribution of pull is a standard Normal distribution.

The pull distribution



Correction of the track parameters of MC simulation

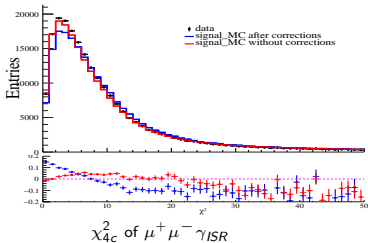
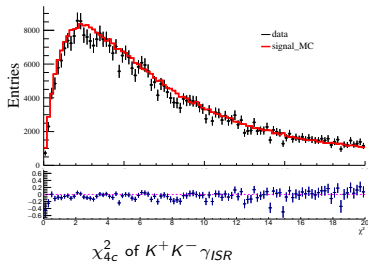
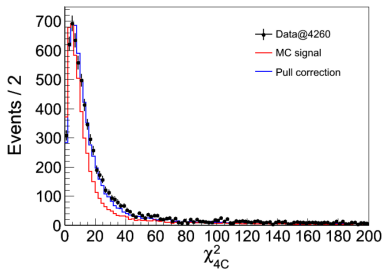
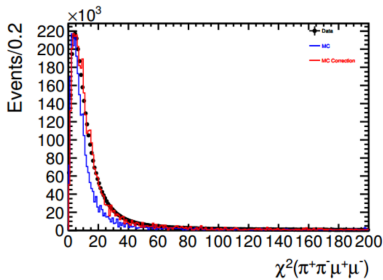
- Actually the pull distribution obeys a Normal distribution with mean μ_i and standard deviation σ_i .
- To reduce the difference between data and MC: enlarge the resolution of α_{0i} by smearing it with a Gaussian, and the mean and sigma of the smeared Gaussian is:

$$\alpha_{0i} + (\mu_i^{data} - \mu_i^{MC}) * (V_{a0})_{ii} \text{ and } \sqrt{((\sigma_i^{data}/\sigma_i^{MC})^2 - 1) * (V_{a0})_{ii}}$$

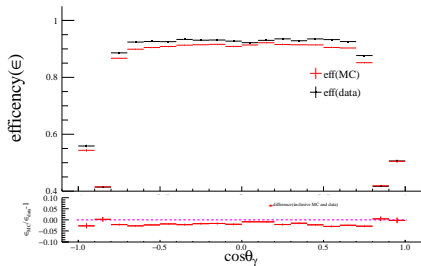
	ϕ_0		κ		$\text{tg}\lambda$	
	$m^{data} - m^{MC}$	$\sigma^{data}/\sigma^{MC}$	$m^{data} - m^{MC}$	$\sigma^{data}/\sigma^{MC}$	$m^{data} - m^{MC}$	$\sigma^{data}/\sigma^{MC}$
π^+	-0.007	1.087	0.362	1.178	0.168	1.178
π^-	-0.060	1.162	-0.361	1.131	0.211	1.253
μ^+	-0.045	1.277	0.499	1.103	0.184	1.129
μ^-	0.031	1.269	-0.464	1.057	0.233	1.138

	ϕ_0		κ		$\text{tg}\lambda$	
	$m^{data} - m^{MC}$	$\sigma^{data}/\sigma^{MC}$	$m^{data} - m^{MC}$	$\sigma^{data}/\sigma^{MC}$	$m^{data} - m^{MC}$	$\sigma^{data}/\sigma^{MC}$
π^+	-0.02±0.03	1.15±0.02	0.42±0.03	1.14±0.02	0.07±0.03	1.09±0.02
π^-	-0.01±0.03	1.16±0.02	-0.36±0.03	1.13±0.02	0.08±0.03	1.09±0.02
K^+	-0.08±0.03	1.17±0.02	0.37±0.03	1.12±0.02	0.06±0.03	1.07±0.02
K^-	0.06±0.03	1.16±0.02	-0.43±0.03	1.11±0.02	0.07±0.03	1.09±0.02

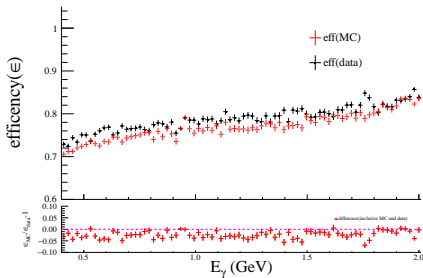
χ_{4c}^2 distributions after distribution



efficiency after corrections of $\mu^+\mu^-$



(a)



(b)

- The situation of kinematic fit efficiency still exists.