# Fundamental Symmetries in Nuclei: Tackling the Strong Interaction and Hunting for New Physics

#### M.J. Ramsey-Musolf

- T.D. Lee Institute/Shanghai Jiao Tong Univ.
- UMass Amherst
- Caltech

- mjrm@umass.edu
- <u>mjrm@sjtu.edu.cn</u>
- 微信:mjrm-china
  - https://michaelramseymusolf.com/

#### About MJRM:



Science



Family

#### *My pronouns: he/him/his # MeToo*



Friends

USTC Colloquium June 4, 2024

### T. D. Lee Institute / Shanghai Jiao Tong U.



#### MJRM: Scientist & "Ambassador"





#### Global effort: ~ 20 researchers

- Foster scientific connections
- Science First ! 科学 第一 !



## Key Theme for This Talk

- Fundamental symmetry tests with nuclei & hadrons address compelling questions about the fundamental laws of nature both within and beyond the Standard Model
- Advances in experimental sensitivities challenge theory to push the state-of-the-art in Standard Model computations and delineate the broader implications of of these experiments for our understanding of the strong interaction and beyond Standard Model physics
- Theoretical developments are meeting this challenge head on, uncovering new puzzles, and pointing toward the next horizon in experimental sensitivity

## **Outline**

#### I. Context

В. С.

#### II. Four Quests

Today

Another time Parity-violation with electrons Lepton Number:  $0\nu\beta\beta$ -Decay  $\beta$ -Decay: 65 years after Wu et al CP: Electric Dipole Moments & the Origin of Matter

#### III. Concluding Remarks

#### I. Context

#### Nuclear Physics Today



Hadron structure & dynamics: "cold QCD"



Rare isotopes: nuclear structure & astrophysics



Fundamental symmetries & neutrinos: "Intensity Frontier"



Relativistic heavy ions: "hot & dense QCD"

#### **Fundamental Questions**

#### Matter, Energy & Mass





Origin of m<sub>f</sub> Beyond Standard Model

#### **Nucleon & Nuclear Structure**



How does QCD build nucleons and nuclei with quarks & gluons ?



#### **Fundamental Symmetries**

• Discrete: parity (P), charge conjugation (C), time-reversal (T),...

Parity:
$$\vec{x} \rightarrow -\vec{x}$$
 $\vec{S} \rightarrow \vec{S}$ 

Continuous: QED U(1), weak isospin SU(2)<sub>L</sub>, color SU(3)<sub>C</sub>, chiral, …

SU(N): 
$$\psi \rightarrow U \psi$$
 ,  $U = \exp\left[i ec{lpha}(x) \cdot ec{T}
ight]$ 

### **Standard Model**

#### $SU(3)_C \times SU(2)_L \times U(1)_Y$ : Strong, EM, & Weak

#### **Standard Model of Elementary Particles**



#### Nuclei & Hadrons as Laboratories

	EDM searches: BSM CPV, Origin of Matter	<i>Ονββ</i> decay searches: Nature of neutrino, Lepton number violation, Origin pftion Matter
	Electron & muon prop's & interactions:	Radioactive decays & other tests
Today	SM Precision Tests, BSM "diagnostic" probes Parity Violation	SM Precision Tests, BSM "diagnostic" probes Parity Violation



### Low-Energy QCD Is Strong









- How reliably can we interpret electroweak processes at the nuclear and hadronic scales in terms of
  - nucleon & nuclear structure ?
  - beyond Standard Model physics ?
- What is the theoretical error bar ?



## **IIA. Parity-Violation with Electrons**

## **Symmetries Score Card**

Force	Р	С	т	СРТ
Gravity	Yes	Yes	Yes	Yes
E.M.	Yes	Yes	Yes	Yes
Strong	Yes	Yes	Yes	Yes
Weak	No	No	No	Yes

C:  $e^+ \leftrightarrow e^-$  T:  $t \leftrightarrow -t$ 

#### **Exploit Parity Symmetry**



### Fermion Electroweak Interactions & PV



Weak interaction flavor basis: "primordial" force carriers

#### **Parity-Violation: Scattering & Atoms**



#### **Parity-Violation & Weak Charges**



Parity-Violating electron scattering Sensitive to weak mixing  $A_{PV} = \frac{N_{\uparrow\uparrow} - N}{N_{\uparrow\uparrow} + N} \sim 10^{-6} \left(\frac{Q}{M_p}\right)^2 \left[Q_W + F(Q^2, \theta)\right]$ 

Atomic parity-violation

$$E_1^{PV} / \beta = i \ e \ \mathcal{M} \times 10^{-11} a_0 \ Q_W / N) / \beta$$

# Weak Charge & Weak Mixing Near cancellation $Q_W^P = -Q_W^e = 1 - 4\sin^2\theta_W$



Weak mixing depends on scale

#### Weak Mixing Depends on Energy Scale



Marciano & Czarnecki '00 Erler & MJRM '05 Erler & Ferro-Hernandez '18

#### **Parity-Violation & Weak Charges**



Parity-Violating electron scattering

$$A_{PV} = \frac{N_{\uparrow\uparrow} - N}{N_{\uparrow\uparrow} + N} \sim 10^{-6} \left(\frac{Q}{M_p}\right)^2 \left(Q_W + F(Q^2, \theta)\right)$$

"Weak Charge" ~ 0.1 in SM

Enhanced transparency to beyond Standard Model physics

Small QCD uncertainties (Marciano & Sirlin; Erler & R-M) Nucleon internal structure: strong interaction (QCD) dynamics at low energy

## **PV Electron Scattering**



27

## **PV Electron Scattering**



28

#### SLAC '77: PV Deep Inelastic Scattering



Glashow-Weingerg-Salam: Standard Model

PARITY NON-CONSERVATION IN INELASTIC ELECTRON SCATTERING <sup>☆</sup>

C.Y. PRESCOTT, W.B. ATWOOD, R.L.A. COTTRELL, H. DESTAEBLER, Edward L. GARWIN, A. GONIDEC<sup>1</sup>, R.H. MILLER, L.S. ROCHESTER, T. SATO<sup>2</sup>, D.J. SHERDEN, C.K. SINCLAIR, S. STEIN and R.E. TAYLOR Stanford Linear Accelerator Center, Stanford University, Stanford, CA 94305, USA

J.E. CLENDENIN, V.W. HUGHES, N. SASAO<sup>3</sup> and K.P. SCHÜLER Yale University, New Haven, CT 06520, USA

M.G. BORGHINI CERN, Geneva, Switzerland

K. LÜBELSMEYER Technische Hochschule Aachen, Aachen, West Germany

#### and

W. JENTSCHKE II. Institut für Experimentalphysik, Universität Hamburg, Hamburg, West Germany

Received 14 July 1978

terium and hydrogen. For deuterium near  $Q^2 = 1.6$  (GeV/c)<sup>2</sup> the asymmetry is  $(-9.5 \times 10^{-5})Q^2$  with statistical and systematic uncertainties each about 10%.



Phys. Lett. B84, 524 (1979)

#### Phys. Lett. B77, 347 (1977)

## **PV Electron Scattering**



#### The Spin Crisis





#### **The Spin Crisis**



#### The Constituent Quark Model gives a successful description

![](_page_32_Figure_1.jpeg)

![](_page_33_Figure_0.jpeg)

Constituent quarks (QM)

 $Q^{\mathsf{P}} \;,\;\; \mu^{\mathsf{P}}$ 

Current quarks (QCD)

 $F^{P_2}(x)$ 

#### We can uncover the sea with the Z<sup>0</sup>

![](_page_34_Figure_1.jpeg)

Heavy QCD quarks:

- $c \qquad m_c \sim 1500 \; MeV$
- $b \qquad m_b \sim 4500 \ MeV$
- $t \qquad m_t \sim 175,000 \; MeV$

![](_page_34_Figure_6.jpeg)

#### **Weak Neutral Current is a Probe**

Nuclear Physics B310 (1988) 527-547 North-Holland, Amsterdam

#### STRANGE MATRIX ELEMENTS IN THE PROTON FROM NEUTRAL-CURRENT EXPERIMENTS

David B KAPLAN<sup>1</sup>

Department of Physics, Harvard University, Cambridge, MA 02138, USA

Ancesh MANOHAR<sup>2</sup>

Center for Theoretical Physics, Laboratory for Nuclear Science and Department of Physics, Massachusetts Institute of Technology, Cambridge, MA 02139, USA

Received 19 May 1988

Volume 219, number 2,3

PHYSICS LETTERS B

16 March 1989

![](_page_35_Picture_11.jpeg)

#### SENSITIVITY OF POLARIZED ELASTIC ELECTRON-PROTON SCATTERING TO THE ANOMALOUS BARYON NUMBER MAGNETIC MOMENT

R.D. McKEOWN

W.K. Kellogg Radiation Laboratory, California Institute of Technology, Pasader PHYSICA

Received 20 August 1988

#### PHYSICAL REVIEW D

VOLUME 39, NUMBER 11

1 JUNE 1989

#### Strange-quark vector currents and parity-violating electron scattering from the nucleon and from nuclei

The anomalous baryon number magnetic moment may be a useful quantity in It is shown that this quantity can be determined quite precisely in the elastic protons at low momentum transfer.

#### D. H. Beck

W.K. Kellogg Radiation Laboratory, California Institute of Technology, Pasadena, California 91125 (Received 3 January 1989)

Measurements of the processes  $p(\pi,\pi)$ ,  $p(v,v)/p(\bar{v},\bar{v})$ , and deep-inelastic  $\vec{p}(\vec{x},\mu')$  can be interpreted in a manner which requires a significant strange-quark contribution to proton matrix elements. In this paper some implications of strange-quark contributions to proton vector currents and their manifestation in parity-violating electron-scattering experiments are examined. It is found that strange-quark currents of plausible magnitude significantly affect the parity-violating elastic electron scattering from the nucleon in certain kinematic regimes. It is also shown that, while the effects in on-going parity-violating experiments on <sup>9</sup>Be and <sup>12</sup>C are small, significant strange-quark contributions might be expected in experiments with nuclear targets at higher-momentum transfer.
Proceedings of the workshop held at the California Institute of Technology

# PARITY VIOLATION in ELECTRON SCATTERING

California Institute of Technology February 23 – 24, 1990



Editors E. J. Beise R. D. McKeown



# **Theoretical Challenges**



### **Electroweak Radiative Corrections**

Volume 242, number 3,4

PHYSICS LETTERS B

#### ELECTROWEAK CORRECTIONS TO PARITY-VIOLATING NEUTRAL CURRENT SCATTERING

#### M.J. MUSOLF

Center For Theoretical Physics, Laboratory for Nuclear Science and Department of Physics, Massachusetts Institute of Technology, Cambridge, MA 02139, USA

and

Barry R. HOLSTEIN Department of Physics and Astronomy, University of Massachusetts, Amherst, MA 01003, USA

#### PHYSICAL REVIEW D, VOLUME 65, 033001

#### Electroweak radiative corrections to parity-violating electroexcitation of the $\Delta$

 Shi-Lin Zhu,<sup>1,2</sup> C. M. Maekawa,<sup>2</sup> G. Sacco,<sup>1,2</sup> B. R. Holstein,<sup>3</sup> and M. J. Ramsey-Musolf<sup>1,2,4</sup>
 <sup>1</sup>Department of Physics, University of Connecticut, Storrs, Connecticut 06,
 <sup>2</sup>Kellogg Radiation Laboratory, California Institute of Technology, Pasadena, Calif
 <sup>3</sup>Department of Physics, University of Massachusetts, Amherst, Massachusetts
 <sup>4</sup>Theory Group, Thomas Jefferson National Accelerator Facility, Newport News, Vin (Received 10 July 2001; published 20 December 2001)

#### PHYSICAL REVIEW D

14 June 1990

#### VOLUME 43, NUMBER 9

1 MAY 1991

#### Observability of the anapole moment and neutrino charge radius

M. J. Musolf Center for Theoretical Physics, Laboratory for Nuclear Science and Department of Physics, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139

> Barry R. Holstein Astronomy, University of Massachusetts, Amherst, Massachusetts 01003 (Received 25 September 1990)

> > PHYSICAL REVIEW D 72, 073003 (2005)

#### Weak mixing angle at low energies

Jens Erler<sup>1</sup> and Michael J. Ramsey-Musolf<sup>2</sup>

<sup>1</sup>Instituto de Física, Universidad Nacional Autónoma de México, 01000 México D.F., Mexico <sup>2</sup>Kellogg Radiation Laboratory, California Institute of Technology, Pasadena, California 91125, USA (Received 21 October 2004; revised manuscript received 11 July 2005; published 13 October 2005)

### "Quantum corrections"



# Strange Quarks: $G_M^P$ & $G_E^P$

Interpreting the asymmetry

Nuclear Physics A546 (1992) 509-587 North-Holland NUCLEAR PHYSICS A

# The interpretation of parity-violating electron-scattering experiments\*

M.J. Musolf and T.W. Donnelly

Center for Theoretical Physics, Laboratory for Nuclear Science and Department of Physics, Massachusetts Institute of Technology, Cambridge, MA 02139, USA

Received 3 February 1992

# Strange Magnetism vs Electroweak Radiative Corrections> Interpreting the asymmetry 3.1.1. Backward angles. In the $\theta \rightarrow 180^\circ$ limit, $\varepsilon \rightarrow 0$ and we have $\frac{W^{(n)}}{F^2} \rightarrow (1 - 4\sin^2\theta_W)(1 + R_V^p) - \frac{1}{G_M^p} \left[ (1 + R_V^n)G_M^n + (1 + R_V^{(0)})G_M^{(s)} \right]$ $+\sqrt{\frac{1}{\tau}+1}(-1+4\sin^2\theta_{\rm W})\frac{\tilde{G}^{\rm p}_{\rm A}}{G^{\rm p}_{\rm M}}.$

$$\tilde{G}_{A}^{p} = -g_{A}G_{D}^{A}[1+R_{A}^{p}] + (1+R_{A}^{(0)})\eta], \qquad \eta = \frac{G_{A}^{(s)}(0)}{g_{A}}$$

Radiative correction

Non-perturbative strong interactions

## Strange Quarks: Radiative Corrections



# **EW Radiative Corrections & EFT**

### Chiral pert theory: "effective field theory" for low-energy QCD

PHYSICAL REVIEW D, VOLUME 62, 033008

#### Nucleon anapole moment and parity-violating ep scattering

Hadronic Weak Interaction

 Shi-Lin Zhu,<sup>1</sup> S. J. Puglia,<sup>1</sup> B. R. Holstein,<sup>3</sup> and M. J. Ramsey-Musolf<sup>1,2</sup>
 <sup>1</sup>Department of Physics, University of Connecticut, Storrs, Connecticut 06269
 <sup>2</sup>Theory Group, Thomas Jefferson National Laboratory, Newport News, Virginia
 <sup>3</sup>Department of Physics and Astronomy, University of Massachusetts, Amherst, Massachusetts 01003 (Received 29 February 2000; published 12 July 2000)











-	·	
Source	$R_A^{T=1}$	$R_A^{T=0}$
One-quark (SM)	-0.35	0.05
Anapole	$-0.06\pm0.24$	0.01 ± 0.14
Total	−0.41±0.24	0.06±0.14

### **Quantify theoretical uncertainty**

### **SAMPLE Results**

### R. Hasty et al., Science 290, 2117 (2000).



### **SAMPLE Results**

### R. Hasty et al., Science 290, 2117 (2000).



### at $Q^2 = 0.1 \, (\text{GeV/c})^2$

 s-quarks contribute less than 5% (1 $\sigma$ ) to the proton's magnetic moment.

200 MeV update 2003: Improved EM radiative corr. Improved acceptance model Correction for  $\pi$  background

125 MeV: no  $\pi$  background similar sensitivity to  $G_A^e(T=1)$ 

**Radiative corrections** 

E. Beise, U Maryland

### **SAMPLE Results**

### R. Hasty et al., Science 290, 2117 (2000).



# Strange Quarks: Proton Magnetism & Charge Distribution

If strange quarks – not part of the quark model picture – give a sizeable contribution to the nucleon spin and mass, what about their effects on electromagnetic properties ?



- Small s-quark effects on E.M. properties
- We wouldn't have known this w/o enormous exp't effort and rigorous precision EW calculations & reliable statement of theoretical uncertainty

# **PV Electron Scattering**



49

### **Parity-Violation & Weak Charges**



Parity-Violating electron scattering

$$A_{PV} = \frac{N_{\uparrow\uparrow} - N}{N_{\uparrow\uparrow} + N} \sim 10^{-6} \left(\frac{Q}{M_p}\right)^2 \left(Q_W + F(Q^2, \theta)\right)$$

"Weak Charge" ~ 0.1 in SM

Enhanced transparency to BSM physics

Small QCD uncertainties (Marciano & Sirlin; Erler & R-M) QCD effects (s-quarks): measured (MIT-Bates, Mainz, JLab)

# **Theoretical Challenges**



# Intensity Frontier: BSM Footprints



High energy searches: does the observed BSM "species" fit the footprints ?



Fundamental symmetry tests: draw inferences about BSM scenarios from a variety of measurements

### Higgs Boson: EW Precision + Direct Observation



### **Electroweak Radiative Corrections**

#### PHYSICAL REVIEW D 68, 016006 (2003)

#### Weak charge of the proton and new physics

Jens Erler,<sup>1,2,\*</sup> Andriy Kurylov,<sup>3,†</sup> and Michael J. Ramsey-Musolf<sup>2,3,4,‡</sup> <sup>1</sup>Instituto de Física, Universidad Nacional Autónoma de México, 04510 México D.F., Mexico <sup>2</sup>Institute for Nuclear Theory, University of Washington, Seattle, Washington 98195, USA <sup>3</sup>Kellogg Radiation Laboratory, California Institute of Technology, Pasadena, California 91125, USA <sup>4</sup>Department of Physics, University of Connecticut, Storrs, Connecticut 06269, USA (Received 27 February 2003; published 17 July 2003)

#### PHYSICAL REVIEW D 72, 073003 (2005)

#### Weak mixing angle at low energies

Jens Erler<sup>1</sup> and Michael J. Ramsey-Musolf<sup>2</sup>

<sup>1</sup>Instituto de Física, Universidad Nacional Autónoma de México, 01000 México D.F., Mexico <sup>2</sup>Kellogg Radiation Laboratory, California Institute of Technology, Pasadena, California 91125, USA (Received 21 October 2004; revised manuscript received 11 July 2005; published 13 October 2005)

### Strong interaction



Strong interaction: inside proton





#### Pertrubative

$$\Box_{WW} = \frac{\hat{\alpha}}{4\pi\hat{s}^2} \left[ 2 + 5 \left( 1 - \frac{\alpha_s(M_W^2)}{\pi} \right) \right],$$

#### Non-pertrubative

$$\Box_{\gamma Z} = \frac{5 \hat{\alpha}}{2\pi} (1 - 4 \hat{s}^2) \left[ \ln \left( \frac{M_Z^2}{\Lambda^2} \right) \underbrace{C_{\gamma Z}(\Lambda)}_{\gamma Z} \right],$$



# Deviations: BSM "Footprints"



SUSY footprints ?

# **Theoretical Challenges**





# **PV Electron Scattering**



# Deviations: BSM "Footprints"



# **Two-Loop EW Radiative Corrections**

### Closed fermion loops: gauge invariant



# **Two-Loop EW Radiative Corrections**

$\delta(Q^{e}w) = \pm 2.1 \% (stat.) \pm 1.1 \% (syst.)$ Exp't precision (goal) $PSM Probe$				
Quantity	Contribution $(\times 10^{-3})$	% shift		
$1-4\sin^2\theta_W$	+74.4			
$\Delta Q^{e}_{W(1,1)}$	-29.0	- 39%		
$\Delta Q^e_{W(1,0)}$	+ 3.1	+ 4%		
$\Delta Q^e_{W(2,2)}$	$-2.12_{-0.024}^{+0.014}$	- 4.4%	Must !	
$\Delta Q^e_{W(2,1)}$	$+ 1.65^{+0.010}_{-0.007}$	+ 3.4%		
$\Delta Q^e_{W(2,0)}$	$\pm$ 0.18 (estimate)	+/- 0.4%	Safe !	
		·		
	<pre> # of closed * Relative to p </pre>	receding order		
l oon order				

Du, Freitas, Patel, MJRM PRL 126 (2021) 131801 [1912.08220]

Loop order

### **III. Concluding Remarks**

# Nuclei & Hadrons as Laboratories

EDM searches: BSM CPV, Origin of Matter	<i>Ονββ</i> decay searches: Nature of neutrino, Lepton number violation, Origin oftion Matter Lepton Number
Electron & muon prop's &	Radioactive decays & other
interactions:	tests
SM Precision Tests, BSM	SM Precision Tests, BSM
"diagnastia" probas	"diagnastia" probas
"diagnostic" probes	"diagnostic" probes
Parity Violation	Parity Violation

# **Theoretical Challenges** Connecting physics at multiple scales Eau

Early Universe



**BSM** Physics

### **Precision Electroweak Studies**

- **Perturbation theory**
- **Effective Field Theory**
- Non-equilibrium QFT
- **Dispersion Relations**
- Collider simulations & phenomenology



# Career-long teamwork Theory & Exp't: Close Collaboration

Global analysis of nucleon strange form factors at low  $Q^2$ 

Jianglai Liu,\* Robert D. McKeown, and Michael J. Ramsey-Musolf<sup>†</sup> W. K. Kellogg Radiation Laboratory, California Institute of Technology, Pasadena, California 91125, USA (Received 1 June 2007; published 2 August 2007)



ECHNOLOG



# **Exciting Challenges Remain**

### Atomic EDMs



### Future Circular e<sup>+</sup>e<sup>-</sup> & pp



### Electron-nucleus interaction

A former
$T_{\mu,\mu_{2}}^{(n),\varepsilon} = \sum_{\mu,\mu_{2}} \left[ dk_{3} dk_{4} dQ_{2} dQ_{2} - e^{-\varepsilon} \left( \tilde{k}_{3}, \pi_{2} \right) \cdot \varepsilon \right] \tilde{k}_{4} \right]$
* (1M/1M, 2M2) Jo (k3 K) J. (ky K2)
$\left[ \sqrt{\frac{2}{5}} \frac{7}{7} \frac{0}{100} + \left[ \frac{3}{5} \frac{7}{7} \frac{2}{100} \right]^{\frac{1}{2}} \left[ \sqrt{\frac{2}{5}} \frac{7}{7} \frac{1}{200} + \left[ \frac{3}{2} \frac{7}{7} \frac{3}{200} \right]^{\frac{1}{2}} \right]^{\frac{1}{2}}$
now is tas now is the
- Z Jak, ak, dab, dar, 15,1 / (hor) ), (ur), (u)
} 1417) Z (-1) NOTI Je (KST) [ TEGENIG TE(FI) ) ]
* [ (471 ] [-] & John je (hur) [ [ [ (hu ) @ [ [ (f) ] ] ]
× [ [= tw(k) ∂r, + (= , LY2(k,) @ ê ).m. ]
* [ J= [Y, (h.) @ e) = + [ = [Y (h.) @ e) = 1
= (477) 2 Z Gi) 2011 /2011 /211 (14) (14, 2M-3)
r Jakes to (15 x1) je (1000) Jake to (1000) to (1000) that
* [d] 2 mg [Yelling) ( +e(i) ) [ [ (tolki We) , + ( ] [ ]
(d 2 m, 18/6, 10/8/17) 13 [1/6, 100] 1, + [7]

Welcome to join !

"Old School" theoretical physics

### Electroweak precision calc's







# Fermion Electroweak Interactions & PV



### Weak interaction flavor basis

### **Electroweak Radiative Corrections**

#### PHYSICAL REVIEW D 68, 016006 (2003)

#### Weak charge of the proton and new physics

Jens Erler,<sup>1,2,\*</sup> Andriy Kurylov,<sup>3,†</sup> and Michael J. Ramsey-Musolf<sup>2,3,4,‡</sup> <sup>1</sup>Instituto de Física, Universidad Nacional Autónoma de México, 04510 México D.F., Mexico <sup>2</sup>Institute for Nuclear Theory, University of Washington, Seattle, Washington 98195, USA <sup>3</sup>Kellogg Radiation Laboratory, California Institute of Technology, Pasadena, California 91125, USA <sup>4</sup>Department of Physics, University of Connecticut, Storrs, Connecticut 06269, USA (Received 27 February 2003; published 17 July 2003) PHYSICAL REVIEW D 72, 073003 (2005)

#### Weak mixing angle at low energies

Jens Erler<sup>1</sup> and Michael J. Ramsey-Musolf<sup>2</sup>

<sup>1</sup>Instituto de Física, Universidad Nacional Autónoma de México, 01000 México D.F., Mexico <sup>2</sup>Kellogg Radiation Laboratory, California Institute of Technology, Pasadena, California 91125, USA (Received 21 October 2004; revised manuscript received 11 July 2005; published 13 October 2005)



# Weak Mixing in the SM: Uncertainties

Erler & R-M

### Full SU(2)<sub>L</sub> x U(1)<sub>Y</sub> Renormalization Group

$$\hat{s}^2 \frac{d\hat{\alpha}}{dt} - \hat{\alpha} \frac{d\hat{s}^2}{dt} = \frac{b_2}{\pi} \hat{\alpha}^2 + \sum_j \frac{b_{2j}}{\pi^2} \hat{\alpha}^2 \hat{\alpha}_j + \cdots$$

$$\sin^2 \hat{\theta}_W(\mu) = \frac{\hat{\alpha}(\mu)}{\hat{\alpha}(\mu_0)} \sin^2 \hat{\theta}_W(\mu_0) + \frac{\sum_i N_i^c \gamma_i Q_i T_i}{\sum_i N_i^c \gamma_i Q_i^2} \bigg[ 1 - \frac{\hat{\alpha}(\mu)}{\hat{\alpha}(\mu_0)} \bigg],$$

- 1. Relate running of  $\sin^2 \theta_W$  to running of  $\alpha$
- 2. Run  $\alpha$  & sin<sup>2</sup> $\theta_W$  to  $\mu \sim m_c$
- 3. Bound s-quark contribution to  $\alpha(m_c)$  -relative to u and d contributions -- using **symmetry limits:** heavy quark and  $SU(3)_f$  limits

$$\Delta \alpha_{\rm HAD}(M_Z^2) = \frac{\alpha \, M_Z^2}{3 \, \pi} P \int_{4m_\pi^2}^\infty \frac{R(s)}{s(M_Z^2 - s)} ds$$

 $R = \sigma (e^+e^- \rightarrow had) / \sigma (e^+e^- \rightarrow \mu^+\mu^-)$ 




# *0vββ-Decay: LNV? Mass Term?*

$$\mathcal{L}_{\text{mass}} = y \bar{L} \tilde{H} \nu_R + \text{h.c.}$$

Dirac

#### Impact of observation

- Total lepton number not
  conserved at classical level
- New mass scale in nature A
- Key ingredient for standard baryogenesis via leptogenesis



## *Ονββ-Decay* & *PVES*

 $\partial v \beta \beta$  Decay, PV e<sup>-</sup>e<sup>-</sup>  $\rightarrow$  e<sup>-</sup>e<sup>-</sup>, e<sup>+</sup>e<sup>-</sup>  $\rightarrow$  e<sup>+</sup>e<sup>-</sup> & pp collisions



G. Li, MJRM, S. Urrutia-Quiroga, J.C. Vasquez

### *Ονββ-Decay* & *PVES*

 $\partial v \beta \beta$  Decay, PV e<sup>-</sup>e<sup>-</sup>  $\rightarrow$  e<sup>-</sup>e<sup>-</sup>, e<sup>+</sup>e<sup>-</sup>  $\rightarrow$  e<sup>+</sup>e<sup>-</sup> & pp collisions



### **NLDBD Experimental Horizons**



- Global effort to deply "ton scale" expt's
  → 100 x better lifetime sensitivity
- Top priority for U.S. nuclear science

# *0vββ-Decay: LNV? Mass Term?*

$$\mathcal{L}_{\text{mass}} = y \bar{L} \tilde{H} \nu_R + \text{h.c.}$$

Dirac

#### Impact of observation

- Total lepton number not conserved at classical level
- New mass scale in nature, A
- Key ingredient for standard baryogenesis via leptogenesis

