

$\phi(2170)$: a strangeonium or exotic state ?

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PDG2018 $\phi(2170)$ DECAY MODES

Mode	Fraction (Γ_i/Γ)
Γ_1 e^+e^-	seen
Γ_2 $\phi\eta$	
Γ_3 $\phi\pi\pi$	
Γ_4 $\phi f_0(980)$	seen
Γ_5 $K^+K^-\pi^+\pi^-$	
Γ_6 $K^+K^-f_0(980) \rightarrow K^+K^-\pi^+\pi^-$	seen
Γ_7 $K^+K^-\pi^0\pi^0$	
Γ_8 $K^+K^-f_0(980) \rightarrow K^+K^-\pi^0\pi^0$	seen
Γ_9 $K^{*0}K^\pm\pi^\mp$	not seen
Γ_{10} $K^*(892)^0\bar{K}^*(892)^0$	not seen



$\phi(2170)$ PDG2024 $J^{PC} = 0^-(1^{--})$

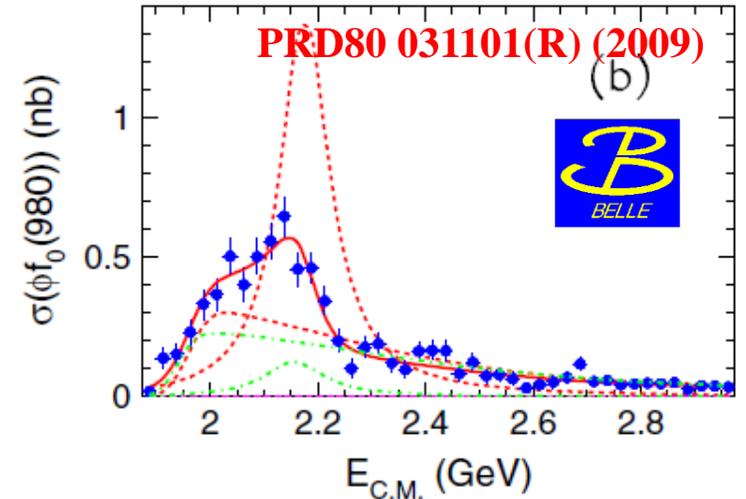
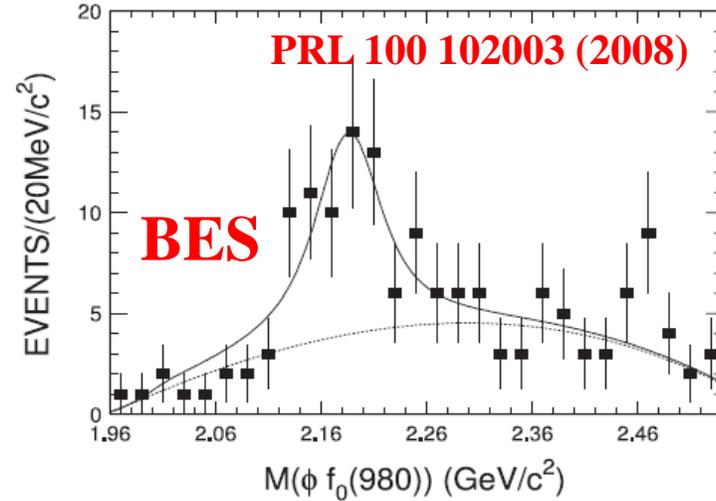
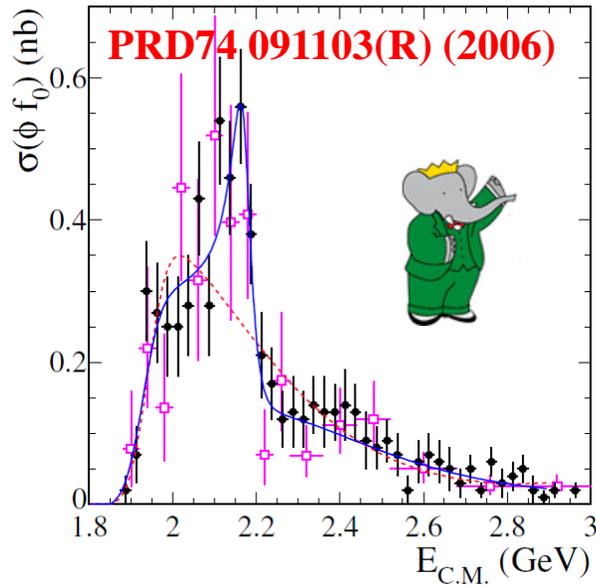
See the review on "Spectroscopy of Light Meson Resonances."

$\phi(2170)$ MASS

VALUE (MeV)	EVTS	DOCUMENT ID	TECN	COMMENT
2164 ± 6 OUR AVERAGE				
2178 ± 20 ± 5	1	ABLIKIM	23AX BES3	$e^+e^- \rightarrow \phi\pi^+\pi^-$
2190 ± 19 ± 37	2	ABLIKIM	22L BES3	$2.0-3.08 e^+e^- \rightarrow K^+K^-\pi^0$
2176 ± 24 ± 3	3	ABLIKIM	21A BES3	$e^+e^- \rightarrow \omega\eta$
2163.5 ± 6.2 ± 3.0	4	ABLIKIM	21T BES3	$e^+e^- \rightarrow \phi\eta$
2177.5 ± 4.8 ± 19.5	5	ABLIKIM	20M BES3	$e^+e^- \rightarrow \eta'\phi$
2126.5 ± 16.8 ± 12.4	6	ABLIKIM	20S BES3	$e^+e^- \rightarrow K^+K^-\pi^0\pi^0$
••• We do not use the following data for averages, fits, limits, etc. •••				
2215.7 ± 8.3	7	LICHARD	23 RVUE	$e^+e^- \rightarrow \Upsilon(nS) \rightarrow \phi\eta\gamma$
2273.7 ± 5.7 ± 19.3	9	ABLIKIM	21AP BES3	$e^+e^- \rightarrow K_S^0 K_L^0$
2239.2 ± 7.1 ± 11.3	10	ABLIKIM	19L BES3	$e^+e^- \rightarrow \eta\phi(980)$
2200 ± 6 ± 5	471	ABLIKIM	15H BES3	$J/\psi \rightarrow \eta\phi\pi^+\pi^-$
2180 ± 8 ± 8	11,12	LEES	12F BABR	$10.6 e^+e^- \rightarrow \phi\pi^+\pi^-\gamma$
2079 ± 13 +79 -28	4.8k	13 SHEN	09 BELL	$10.6 e^+e^- \rightarrow K^+K^-\pi^+\pi^-\gamma$
2186 ± 10 ± 6	52	ABLIKIM	08F BES	$J/\psi \rightarrow \eta\phi f_0(980)$
2125 ± 22 ± 10	483	AUBERT	08S BABR	$10.6 e^+e^- \rightarrow \phi\eta\gamma$
2192 ± 14	116	14 AUBERT	07AK BABR	$10.6 e^+e^- \rightarrow K^+K^-\pi^+\pi^-\gamma$
2169 ± 20	149	14 AUBERT	07AK BABR	$10.6 e^+e^- \rightarrow K^+K^-\pi^0\pi^0\gamma$
2175 ± 10 ± 15	201	12,15 AUBERT, BE	06D BABR	$10.6 e^+e^- \rightarrow K^+K^-\pi\pi\gamma$

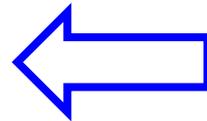
第八届BESIII R值与QCD强子结构研讨会, 2024.07.20, 哈尔滨

$\phi(2170)/Y(2175)$

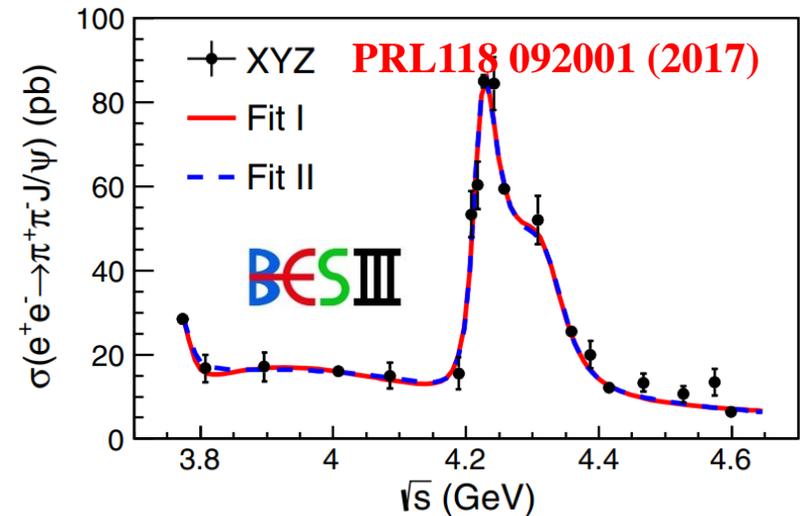


Eur. Phys. J. C72 2008 (2012)

$$e^+e^- \Rightarrow \begin{cases} Y(2175) \rightarrow \phi(1020)\pi^+\pi^- & \text{strange,} \\ Y(4260) \rightarrow J/\psi\pi^+\pi^- & \text{charm,} \\ \Upsilon(10860) \rightarrow \Upsilon(1S, 2S)\pi^+\pi^- & \text{bottom,} \end{cases}$$



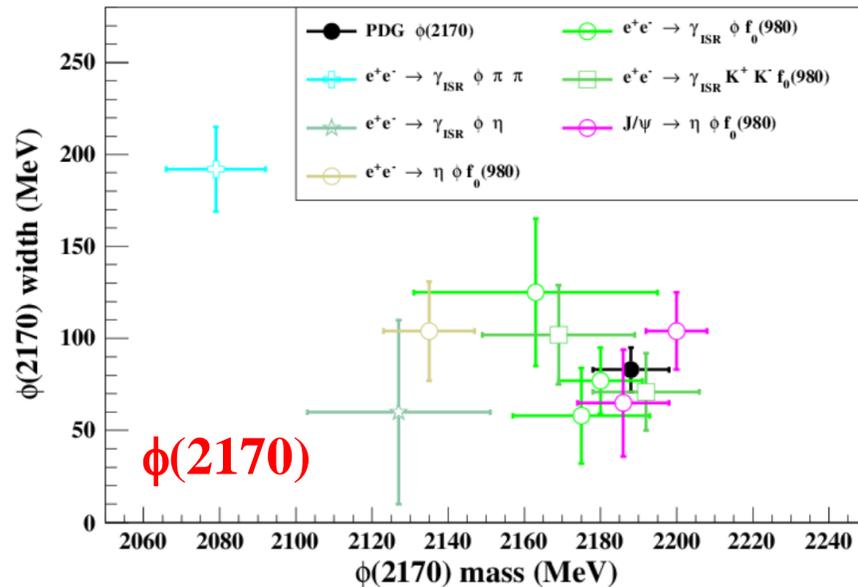
$\phi(2170)$ as strange analogue of $Y(4230)$



$\phi(2170)$

PDG2018 $\phi(2170)$ DECAY MODES

Mode	Fraction (Γ_i/Γ)
Γ_1 $e^+ e^-$	seen
Γ_2 $\phi \eta$	
Γ_3 $\phi \pi \pi$	
Γ_4 $\phi f_0(980)$	seen
Γ_5 $K^+ K^- \pi^+ \pi^-$	
Γ_6 $K^+ K^- f_0(980) \rightarrow K^+ K^- \pi^+ \pi^-$	seen
Γ_7 $K^+ K^- \pi^0 \pi^0$	
Γ_8 $K^+ K^- f_0(980) \rightarrow K^+ K^- \pi^0 \pi^0$	seen
Γ_9 $K^{*0} K^\pm \pi^\mp$	not seen
Γ_{10} $K^*(892)^0 \bar{K}^*(892)^0$	not seen



- Published experimental information
 - ✓ limited decay modes
 - ✓ inconsistency on mass & width
- @ 2018: Theorists explain $\phi(2170)$ as
 - ✓ 2^3D_1 or 3^3S_1 $s\bar{s}$
 - ✓ $s\bar{s}g$ hybrid
 - ✓ tetraquark
 - ✓ molecular state $\Lambda\bar{\Lambda}$
 - ✓ $\phi f_0(980)$ resonance with FSI
 - ✓ three body system ϕKK
 - ✓ estimated or ruled out: not yet
- Nature of $\phi(2170)$: open question ?

Difficulty @ $\phi(2170)$

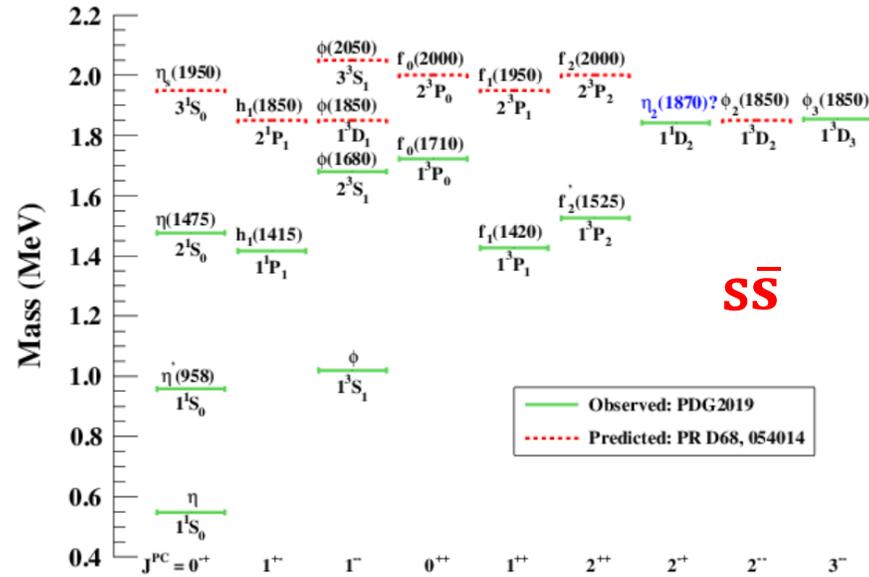
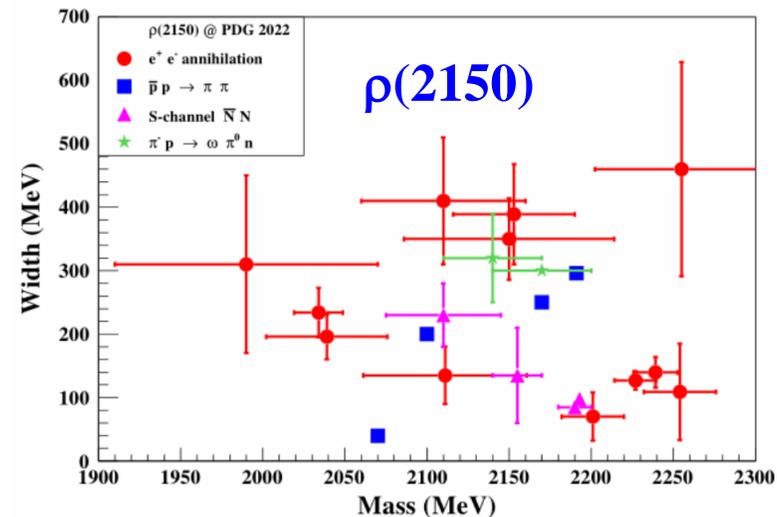


TABLE XII. Decay amplitudes squared (excluding the decay strength constants).

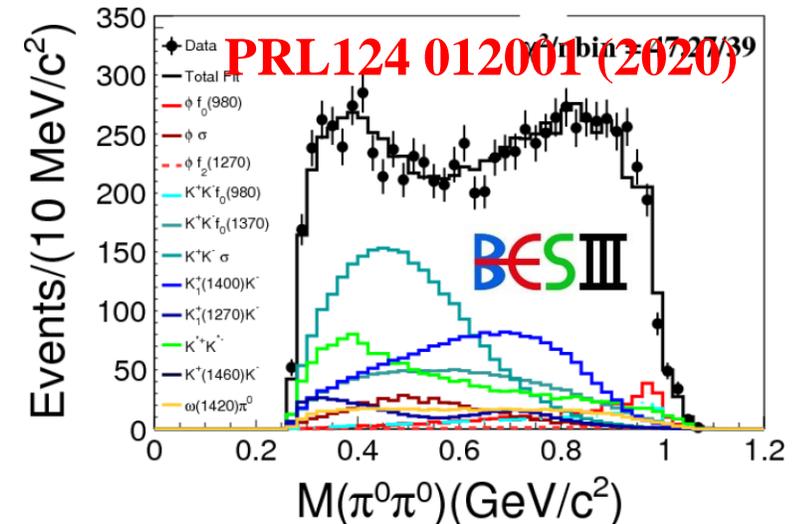
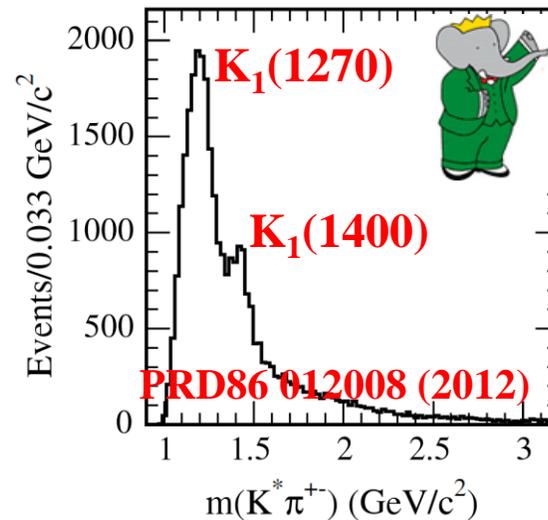
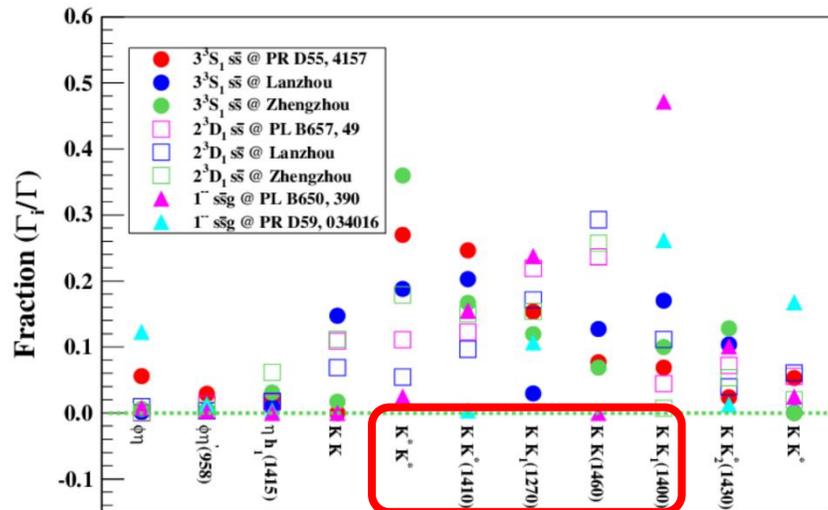
Decay	Products	Squared amplitude
$\rho^* \rightarrow PP$	$K\bar{K}$	$\frac{4}{2}$
$\rho^* \rightarrow VP$	$\pi\pi$	$\frac{4}{2}$
	\bar{K}^*K	$\frac{4}{2}$
	$\rho\eta$	$2\cos^2\phi_P$
	$\rho\eta'$	$2\sin^2\phi_P$
	$\omega\pi$	$2\sin^2\phi_V$
	$\phi\pi$	$2\cos^2\phi_V$
$\omega^* \rightarrow PP$	$K\bar{K}$	$12\sin^2\theta_V^*$
$\omega^* \rightarrow VP$	$\phi\eta$	$2(\sqrt{2}\cos\phi_V^*\sin\phi_V\sin\phi_P + \sin\phi_V^*\cos\phi_V\cos\phi_P)^2$
	$\phi\eta'$	$2(\sqrt{2}\cos\phi_V^*\sin\phi_V\cos\phi_P - \sin\phi_V^*\cos\phi_V\sin\phi_P)^2$
	$\omega\eta$	$2(\sqrt{2}\cos\phi_V^*\cos\phi_V\sin\phi_P - \sin\phi_V^*\sin\phi_V\cos\phi_P)^2$
	$\omega\eta'$	$2(\sqrt{2}\cos\phi_V^*\cos\phi_V\cos\phi_P + \sin\phi_V^*\sin\phi_V\sin\phi_P)^2$
	$\rho\pi$	$6\sin^2\phi_V^*$
	$K^*\bar{K}$	$2(\sin\phi_V^* + \sqrt{2}\cos\phi_V^*)^2$
$\phi^* \rightarrow PP$	$K\bar{K}$	$12\cos^2\theta_V^*$
$\phi^* \rightarrow VP$	$\phi\eta$	$2(-\sqrt{2}\sin\phi_V^*\sin\phi_V\sin\phi_P + \cos\phi_V^*\cos\phi_V\cos\phi_P)^2$
	$\phi\eta'$	$2(\sqrt{2}\sin\phi_V^*\sin\phi_V\cos\phi_P + \cos\phi_V^*\cos\phi_V\sin\phi_P)^2$
	$\omega\eta$	$2(\sqrt{2}\sin\phi_V^*\cos\phi_V\sin\phi_P + \cos\phi_V^*\sin\phi_V\cos\phi_P)^2$
	$\omega\eta^*$	$2(-\sqrt{2}\sin\phi_V^*\cos\phi_V\cos\phi_P + \cos\phi_V^*\sin\phi_V\sin\phi_P)^2$
	$\rho\pi$	$6\cos^2\phi_V^*$
	$K^*\bar{K}$	$2(\cos\phi_V^* - \sqrt{2}\sin\phi_V^*)^2$

PRD79 014036 (2009)

- Better understanding $s\bar{s}$ spectrum ?
 - ✓ unobserved $1^- s\bar{s}$ mesons
- OZI rule and isospin
 - ✓ contribution of $\rho^*/\omega^*/\phi^*$
- ρ^*/ω^* @ [2-3] GeV: “omitted from summary table” or “further states”



$\phi(2170)$ decay \Leftarrow PWA for multi \sqrt{s}

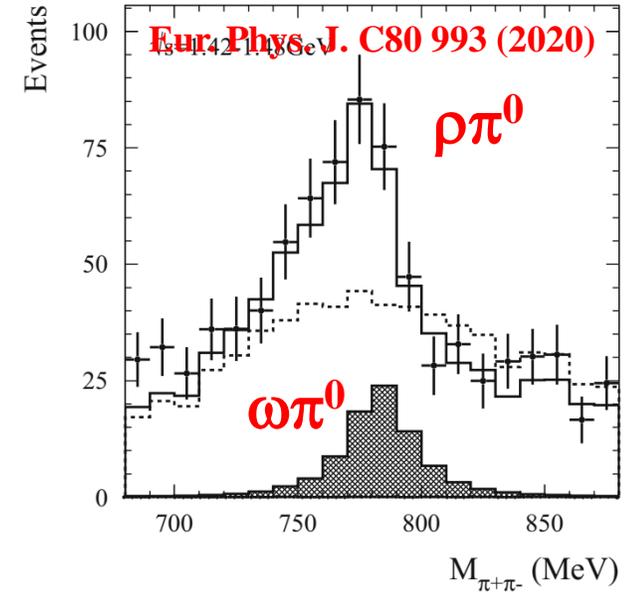


- $e^+e^- \rightarrow K K \pi \pi$: important to distinguish $\phi(2170)$ theory models
 - ✓ K^*K^* : $s\bar{s}g$ (unfavored), 3^3S_1 (favored)
 - ✓ $KK_1(1400)$: $s\bar{s}g$ (favored)
 - ✓ $KK(1460)$: $s\bar{s}g$ (unfavored), 2^3D_1 (favored)
- PWA for multi \sqrt{s} points
 - ✓ (only) focus on dominant components
 - ✓ fraction and phase angle: smoothness and continuity



Why PWA ? a lesson @ $e^+ e^- \rightarrow \pi^+ \pi^- \pi^0$

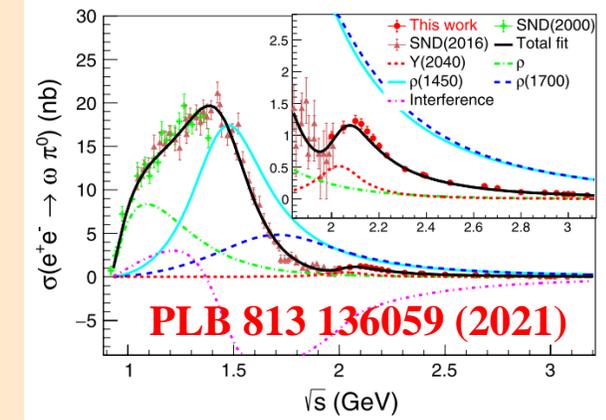
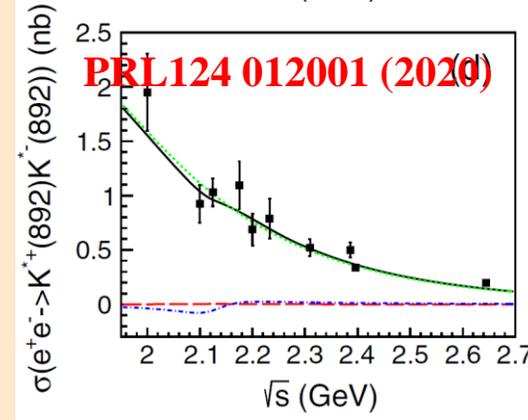
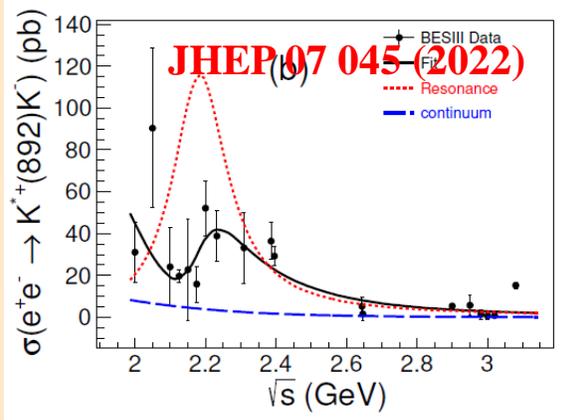
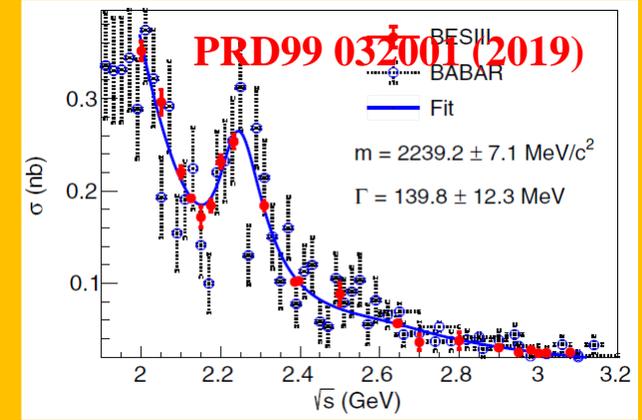
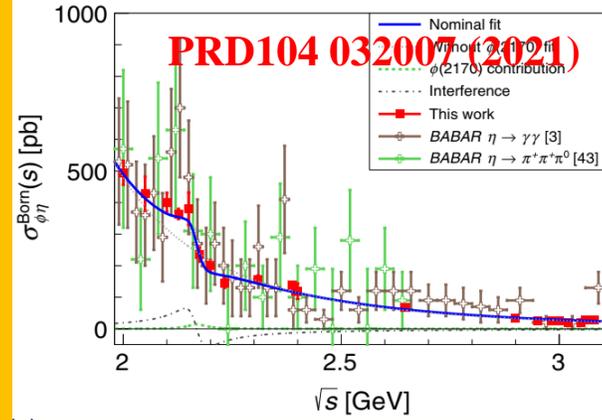
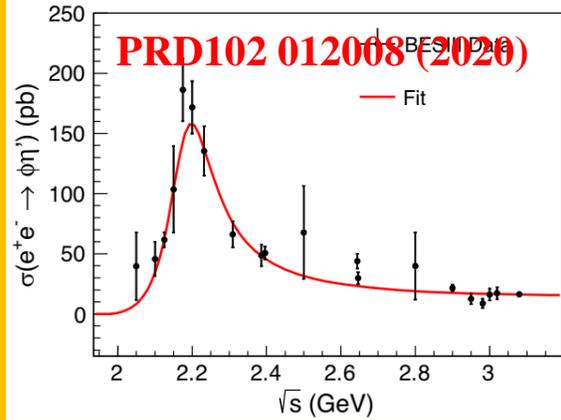
- **Isospin & G-parity: ω^*/ϕ^***
 - ✓ ϕ^* : OZI-suppressed
 - ✓ ρ^* : ignored
- $\omega\pi^0$ with $\omega \rightarrow \pi^+ \pi^-$ events: **16% @ 1.45 GeV**
- ρ^* @ $\omega\pi^0 \Leftarrow \rho(1450)$ & $\rho(1700)$ contribution
- **SND: $\omega, \phi, \omega(1420)$ and $\omega(1650)$, without ρ^***



VALUE (MeV)	EVTS	DOCUMENT ID	TECN	COMMENT
290 ± 190	OUR ESTIMATE	$\omega(1420)$ @ PDG2022		
• • We do not use the following data for averages, fits, limits, etc. • •				
440 ± 125	267	¹ ACHASOV	2020B	SND $e^+ e^- \rightarrow \omega\eta \rightarrow \eta\pi^0\gamma$
104 ± 35 ± 10	824	² AKHMETSHIN	2017A	CMD3 $1.4 - 2.0 e^+ e^- \rightarrow \omega\eta$
880 ± 170	13.1k	³ AULCHENKO	2015A	SND $1.05 - 1.80 e^+ e^- \rightarrow \pi^+\pi^-\pi^0$
480 ± 180		⁴ ACHASOV	2010D	SND $1.075 - 2.0 e^+ e^- \rightarrow \pi^0\gamma$
130 ± 50 ± 100		AUBERT	2007AU	BABR $10.6 e^+ e^- \rightarrow \omega\pi^+\pi^-\gamma$
450 ± 70 ± 70		AUBERT,B	2004N	BABR $10.6 e^+ e^- \rightarrow \pi^+\pi^-\pi^0\gamma$
870 $^{+500}_{-300}$ ± 450	1.2M	⁵ ACHASOV	2003D	RVUE $0.44 - 2.00 e^+ e^- \rightarrow \pi^+\pi^-\pi^0$
199 ± 15		⁶ HENNER	2002	RVUE $1.2 - 2.0 e^+ e^- \rightarrow \rho\pi, \omega\pi\pi$
188 ± 45	177	⁷ AKHMETSHIN	2000D	CMD2 $1.2 - 1.38 e^+ e^- \rightarrow \omega\pi^+\pi^-$
360 $^{+100}_{-60}$	5095	ANISOVICH	2000H	SPEC $0.0 p\bar{p} \rightarrow \omega\pi^0\pi^0\pi^0$
240 ± 70		⁸ CLEGG	1994	RVUE
174 ± 59	315	⁹ ANTONELLI	1992	DM2 $1.34 - 2.4 e^+ e^- \rightarrow \rho\pi$

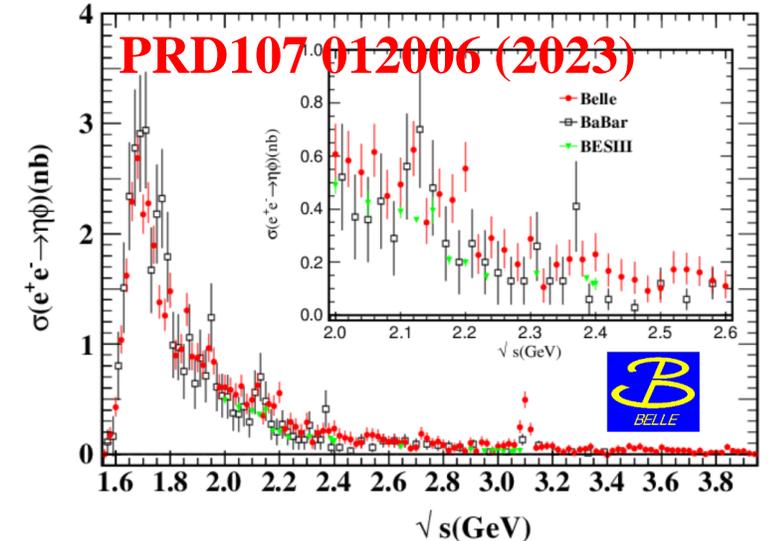
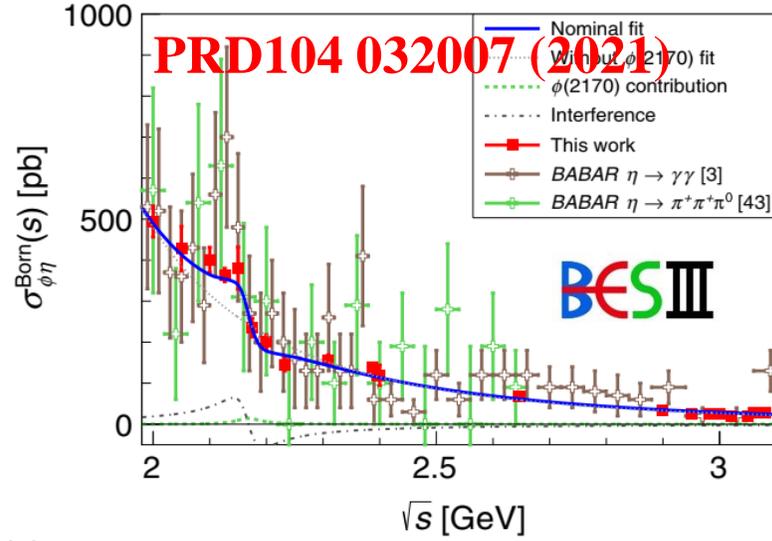
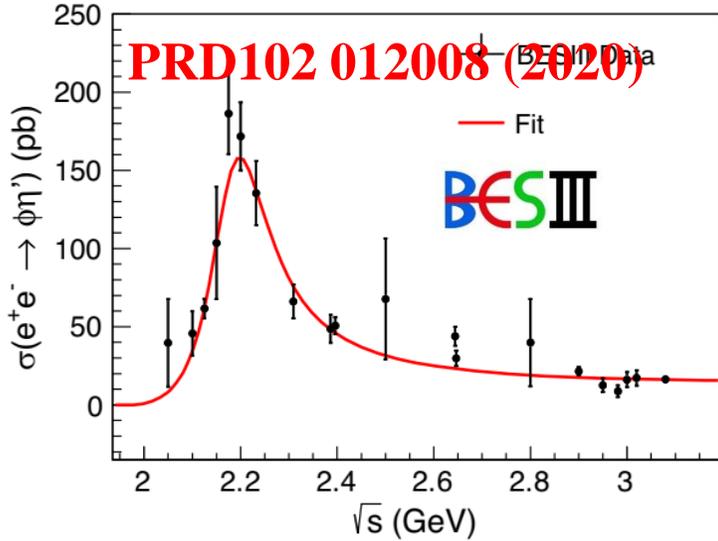
	SND 2003	BABAR	This work
$m_{\omega'}$, MeV	1400 ± 50 ± 130	1350 ± 20 ± 20	1470 ± 50
$\Gamma_{\omega'}$, MeV	870 ± $^{500}_{200}$ ± 450	450 ± 70 ± 70	880 ± 170
$B(\omega' \rightarrow e^+e^-)B(\omega' \rightarrow \pi^+\pi^-\pi^0) \times 10^6$	0.65 ± 0.13 ± 0.21	0.82 ± 0.05 ± 0.06	0.73 ± 0.08
$m_{\omega''}$, MeV	1770 ± 50 ± 60	1660 ± 10 ± 2	1680 ± 10
$\Gamma_{\omega''}$, MeV JETP 121 27 (2015)	490 ± $^{200}_{150}$ ± 130	230 ± 30 ± 20	310 ± 30
$B(\omega'' \rightarrow e^+e^-)B(\omega'' \rightarrow \pi^+\pi^-\pi^0) \times 10^6$	1.15 ± $^{0.44}_{0.09}$ ± 0.83	1.3 ± 0.1 ± 0.1	1.56 ± 0.23

Roadmap for $\phi(2170)$: two body decay

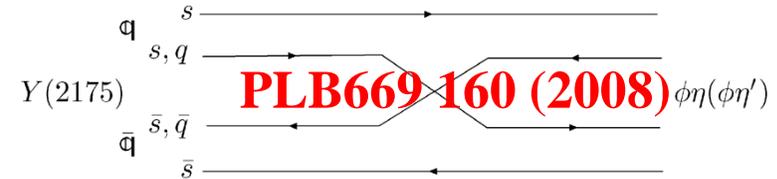


- OZI & isospin **favoured**: $\phi\eta$, $\phi\eta'$, $\phi f_0(980)$ and so on
- KK , K^*K and $K^*K^* \leftarrow \rho^*/\omega^*$ contribution
- OZI & isospin **un-favoured**: $\rho\pi^0$, $\omega\pi^0$ and so on

$e^+ e^- \rightarrow \phi\eta'$ and $\phi\eta$



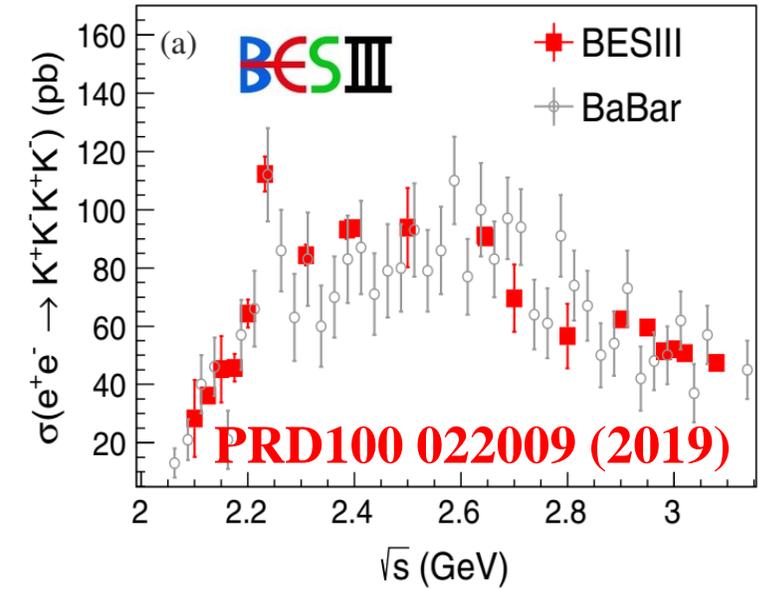
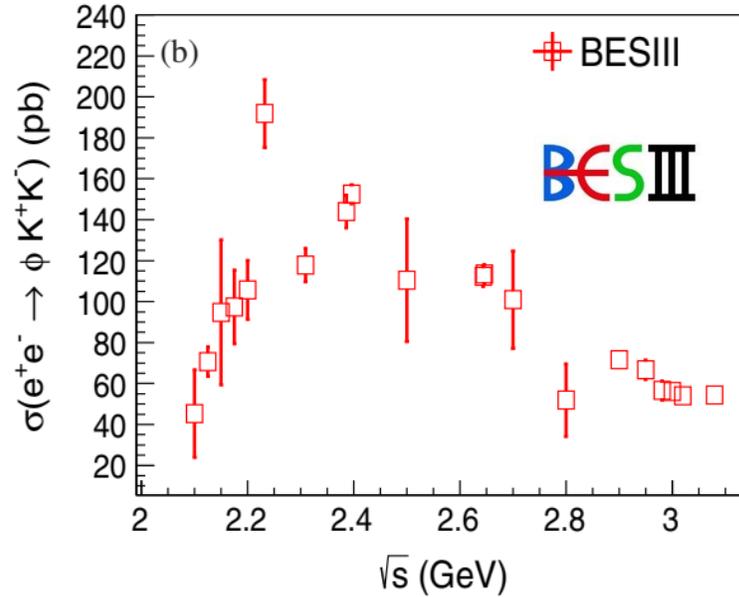
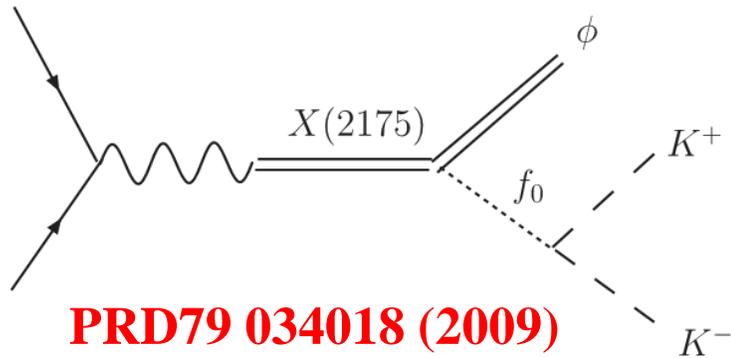
- $\phi\eta$ and $\phi\eta'$ modes: isoscalar
 - ✓ ϕ^* and ω^* (OZI suppressed)
 - ✓ useful to measure parameters
- tetraquark favorites $\phi\eta$ and $\phi\eta'$
- $1^{--} s\bar{s}g$ hybrid has large $\Gamma_{\phi\eta}$ and smaller $\Gamma_{\phi\eta'}$
- BESIII data vs. Belle data
 - ✓ Belle II data ?



$1^{--} s\bar{s}g$	PRD59 034016				PLB650 390
$\phi\eta$	2	19	11	3	1.2
$\phi\eta'$	0.01	2	0.1	0.02	0.4
Ratio	200	9.5	110	150	3

$e^+ e^- \rightarrow \phi K^+ K^-$ and $2(K^+ K^-)$

- $\phi(2170)$: resonant of $\phi K K$

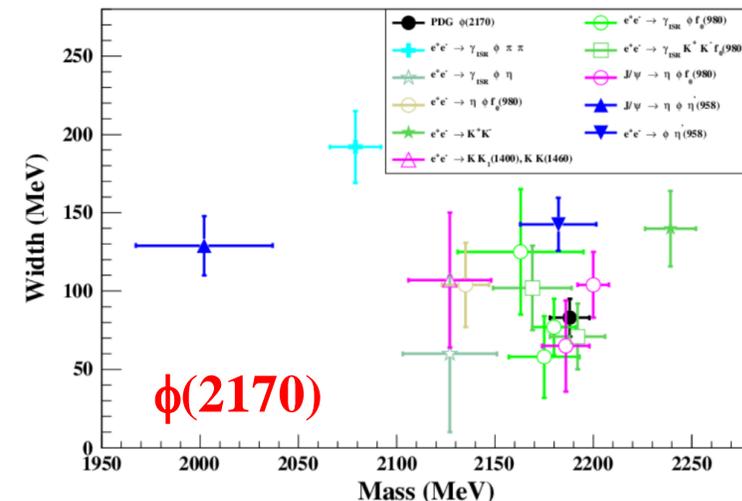


- $\phi K^+ K^-$ & $2(K^+ K^-)$: similar enhancement around 2.2324 GeV

- hint for a narrow resonance around $\Lambda \bar{\Lambda}$ threshold

✓ Width < 20 MeV

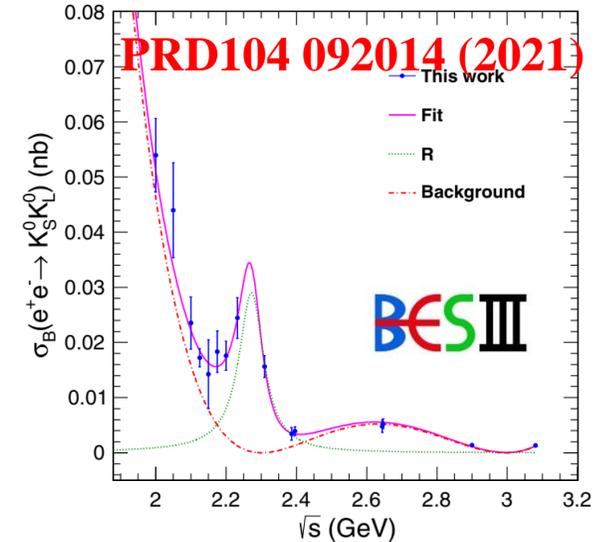
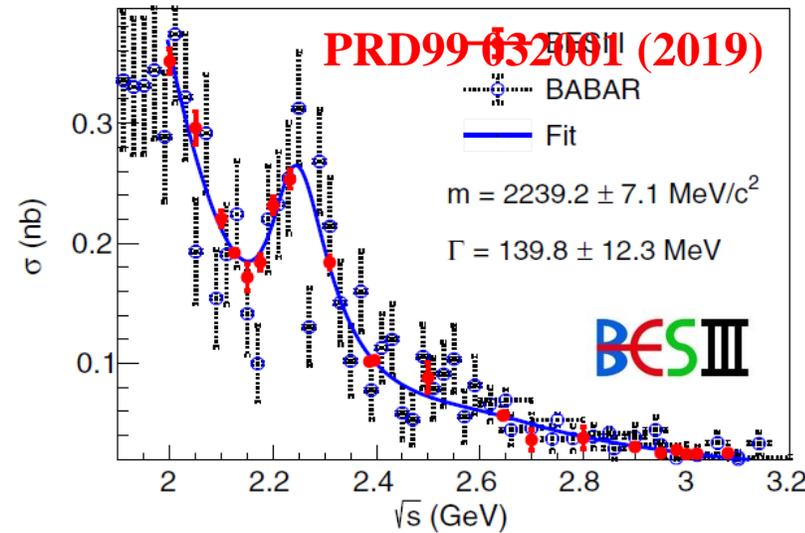
- three body system $\phi K K$???



$e^+ e^- \rightarrow K^+ K^- \text{ \& } K_S K_L$

● $\phi(2170)$: molecular state $\Lambda\bar{\Lambda}$

$\phi(2170)$ decay	This work	3P_0 model	Data [5]
	$^3S_1 \Lambda\bar{\Lambda}$	within $s\bar{s}$ [10]	
KK	73.8–87.7
$\phi f_0(980)$	0.25–0.3	<10	Seen
$\omega\sigma$	4.2–4.9
$K^* K_0^*(800)$	1.8–2.1		PRD96 074027 (2017)
Total	80.1–95		83 ± 12



● dominant KK mode @ $\phi(2170)$?

✓ iso-scalar: ω^*/ϕ^* ; iso-vector: ρ^*

✓ extract isospin component

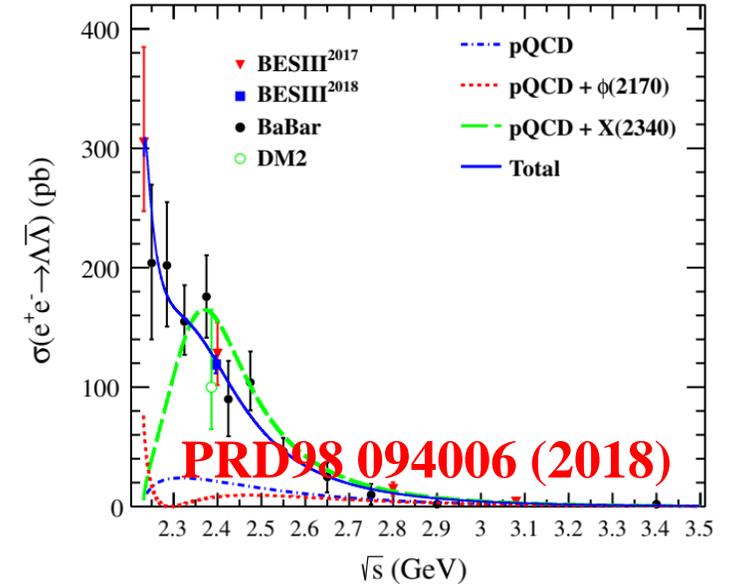
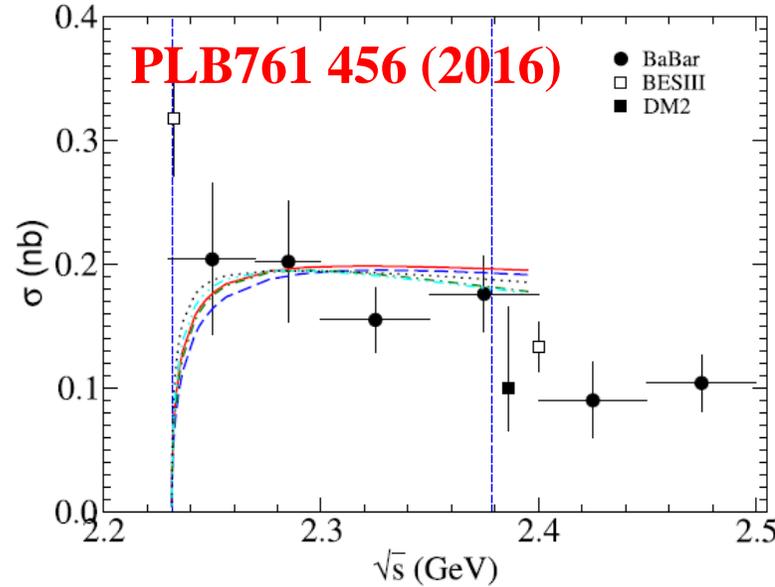
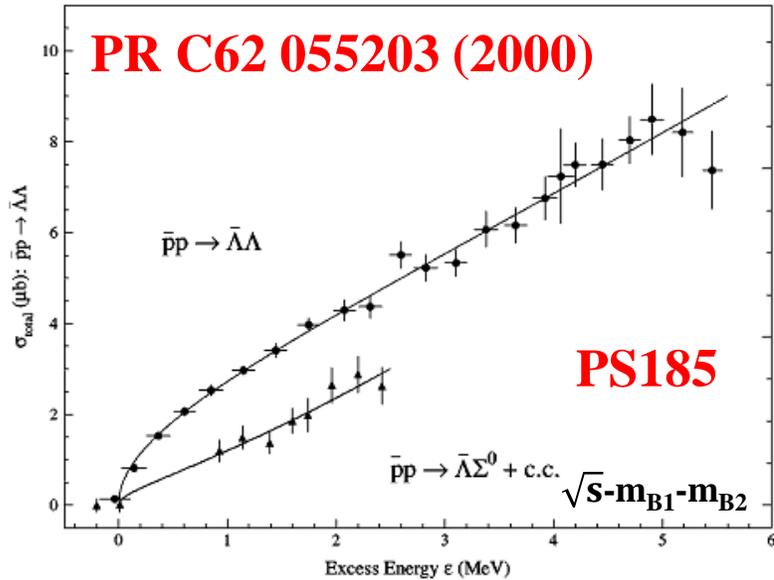
● one resonance @ K^+K^- & $K_S K_L$

● $\Gamma(K^+K^-) \approx 10 \Gamma(K_S K_L)$

✓ PRC 102 015201: valence quark charge

	K^+K^-	$K_S K_L$
Mass (MeV/c ²)	$2239.2 \pm 7.1 \pm 11.3$	$2273.7 \pm 5.7 \pm 19.3$
Width (MeV)	$139.8 \pm 12.3 \pm 20.6$	$86 \pm 44 \pm 51$
$\Gamma_{ee} \text{Br}$ (eV)		$0.9 \pm 0.6 \pm 0.7$

$e^+e^- \rightarrow \Lambda\bar{\Lambda}$



- $\phi(2170)$: molecular state $\Lambda\bar{\Lambda}$

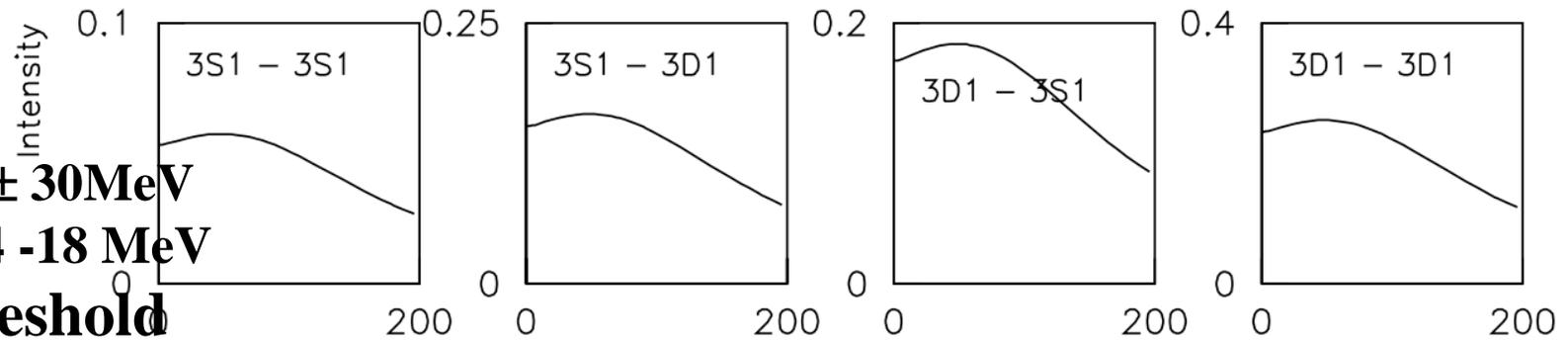
- **Fitting @ EPJ C36 161 (2004)**

✓ 1^- $M = 2290 \pm 20 \text{ MeV}$; $\Gamma = 275 \pm 30 \text{ MeV}$

✓ $\phi(2170)$: $2164 \pm 6 \text{ MeV}$; $106 +24 -18 \text{ MeV}$

- non-zero behavior around threshold

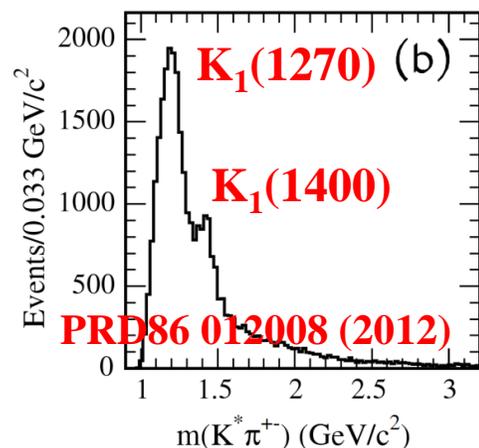
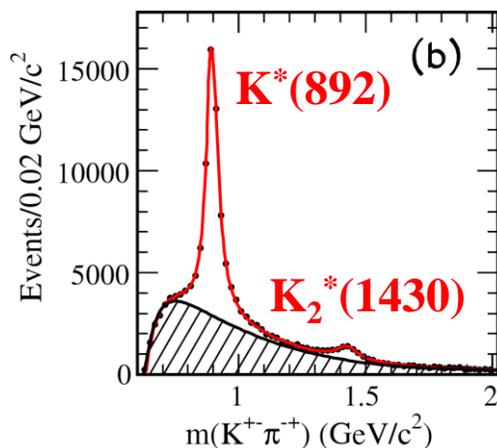
- A resonance @ $\Lambda\bar{\Lambda}$?



$e^+ e^- \rightarrow K^+ K^- \pi^0 \pi^0$

● $e^+e^- \rightarrow K K \pi \pi$: important to distinguish $\phi(2170)$ theory models

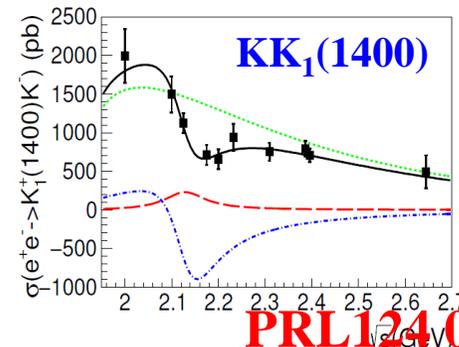
- ✓ K^*K^* : $s\bar{s}g$ (unfavored), 3^3S_1 (favored)
- ✓ $KK_1(1400)$: $s\bar{s}g$ (favored)
- ✓ $KK(1460)$: $s\bar{s}g$ (unfavored), 2^3D_1 (favored)



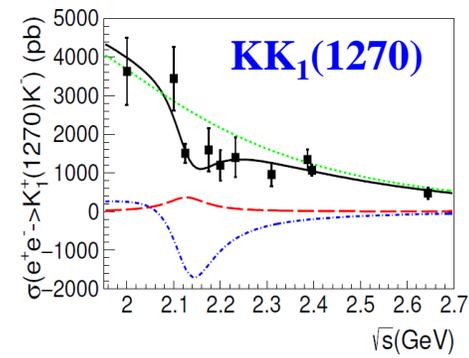
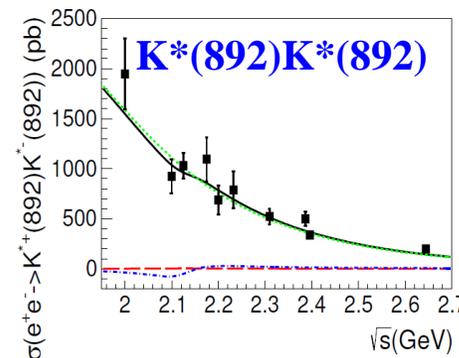
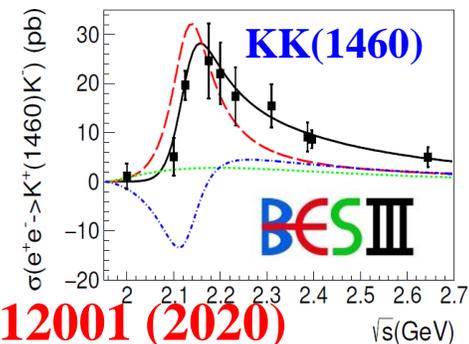
PRD86 012008 (2012)

Table 22: Fitting parameters.

channel	$e^+e^- \rightarrow K_1^+(1400)K^-$	$e^+e^- \rightarrow K^+(1460)K^-$	$e^+e^- \rightarrow K_1^+(1270)K^-$	$e^+e^- \rightarrow K^{*+}K^{*-}$
Mass (MeV/c ²)	2126.5 ± 16.8			
Width (MeV)	106.9 ± 32.1			
	Solution1	Solution2	Solution1	Solution2
$\mathcal{B}_R \Gamma^{e^+e^-}$ (eV)	7.6 ± 3.7	152.6 ± 14.2	1.0 ± 1.3	4.7 ± 3.3
ϕ (rad)	3.7 ± 0.4	4.5 ± 0.3	5.6 ± 1.5	98.8 ± 7.8
Significance(σ)	4.8		1.4	
			1.2	

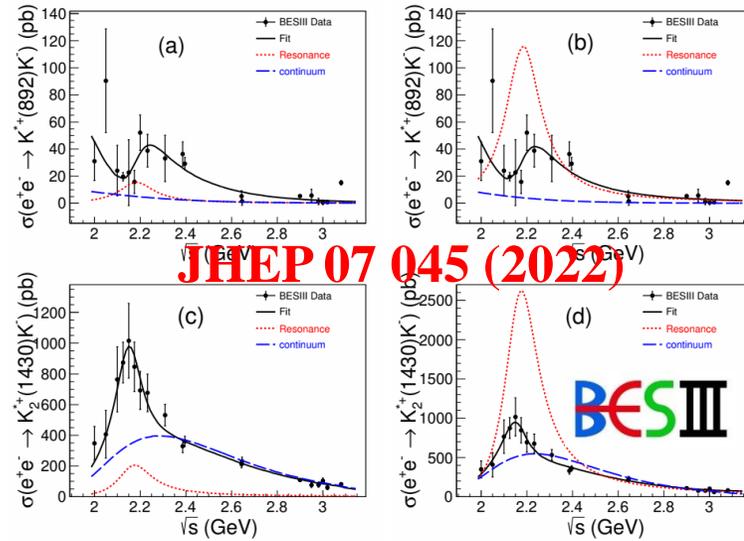
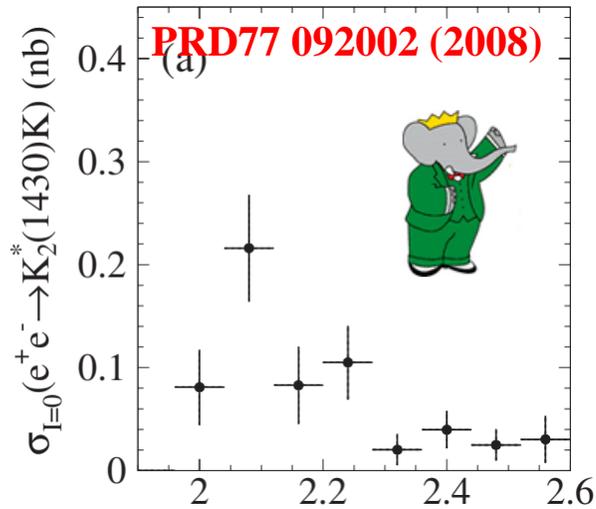


PRL124 012001 (2020)



- ✓ dots: BESIII data
- ✓ black curves: fit results
- ✓ red long-dashed: $\phi(2170)$
- ✓ green shot-dashed: $1/s^n$
- ✓ blue dash-dotted: interference

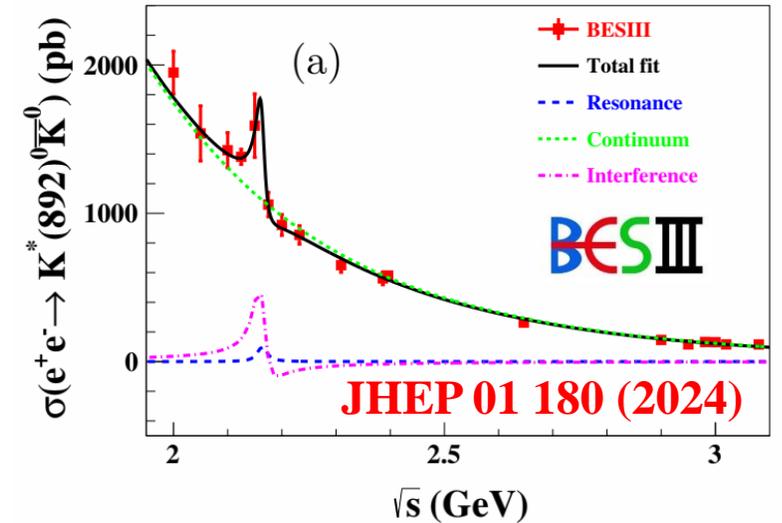
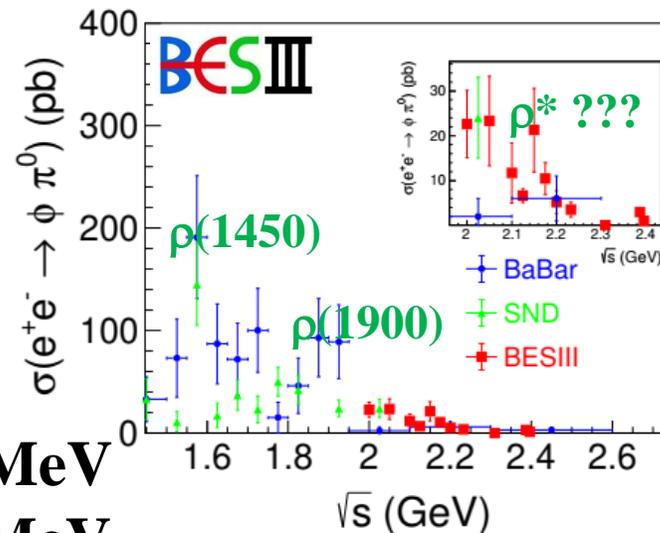
$e^+ e^- \rightarrow K^+ K^- \pi^0$ & $e^+ e^- \rightarrow K_S^0 K_L^0 \pi^0$



	$K_2^*(1430)K$	$K^*(892)K$
Mass	$2190 \pm 19 \pm 37 \text{ MeV}/c^2$	
Width	$191 \pm 28 \pm 60 \text{ MeV}$	
$\Gamma_{ee} \text{Br}$	$12.6 \pm 2.4 \text{ eV}$	$1.0 \pm 0.3 \text{ eV}$
	$161.1 \pm 20.6 \text{ eV}$	$7.1 \pm 0.9 \text{ eV}$

$$\frac{\mathcal{B}(\phi(2170) \rightarrow K^{*+}(1430)K^-)}{\mathcal{B}(\phi(2170) \rightarrow K^{*+}(892)K^-)} = \frac{12.6 \pm 4.5}{22.7 \pm 4.1}$$

- $K_2^*(1430)K$ @ $\phi(2170)$?
 - ✓ BaBar: hint @ 2.1 GeV
- Vector state @ $\phi\pi^0$
 - ✓ ρ^* : OZI-suppressed
 - ✓ ω/ϕ^* : isospin-violated
- Vector state @ $K_S^0 K_L^0 \pi^0$
 - ✓ Mass: $2164.7 \pm 9.1 \pm 3.1 \text{ MeV}$
 - ✓ Width: $32.4 \pm 21.0 \pm 1.8 \text{ MeV}$



$e^+ e^- \rightarrow K^+ K^- \pi^0$ vs. $e^+ e^- \rightarrow K_S^0 K_L^0 \pi^0$

Process	Fraction (%) (2.125 GeV)	Fraction (%) (2.396 GeV)
$\phi\pi^0$	1.8 ± 0.4	0.7 ± 0.3
$\rho(1450)\pi^0$	3.8 ± 0.7	0.2 ± 0.2
$\phi(1680)\pi^0$	14.6 ± 2.3	13.6 ± 2.9
$\rho(1900)\pi^0$	2.1 ± 0.3	3.0 ± 1.0
$\rho_3(2250)$	0.9 ± 0.5	0.9 ± 0.6
$K^*(892)K$	2.8 ± 0.3	9.3 ± 1.2
$K^*(1410)K$	1.1 ± 0.8	3.6 ± 1.4
$K_2^*(1430)K$	73.0 ± 3.7	64.6 ± 3.2
$K_3^*(1780)K$	1.3 ± 0.5	2.1 ± 1.4

JHEP 07 045 (2022)

Process	Fraction (%)		
	2.125 GeV	2.396 GeV	2.900 GeV
$\phi\pi^0$	1.75 ± 0.66	0.87 ± 0.66	1.82 ± 1.11
$\phi(1680)\pi^0$	2.39 ± 1.23	5.96 ± 2.10	5.22 ± 1.50
$K^*(892)^0 \bar{K}^0$	79.89 ± 1.12	86.01 ± 1.38	72.65 ± 2.11
$K_2^*(1430)^0 \bar{K}^0$	7.42 ± 0.83	1.93 ± 0.57	1.85 ± 0.82
$K(1680)^0 \bar{K}^0$	3.00 ± 1.11	6.73 ± 1.91	5.82 ± 1.96

JHEP 01 180 (2024)

● $KK\pi$ system

✓ $K_2^*(1430)K @ K^+K^-\pi^0$

✓ $K^*(892)^0 \bar{K}^0 @ K_S^0 K_L^0 \pi^0$

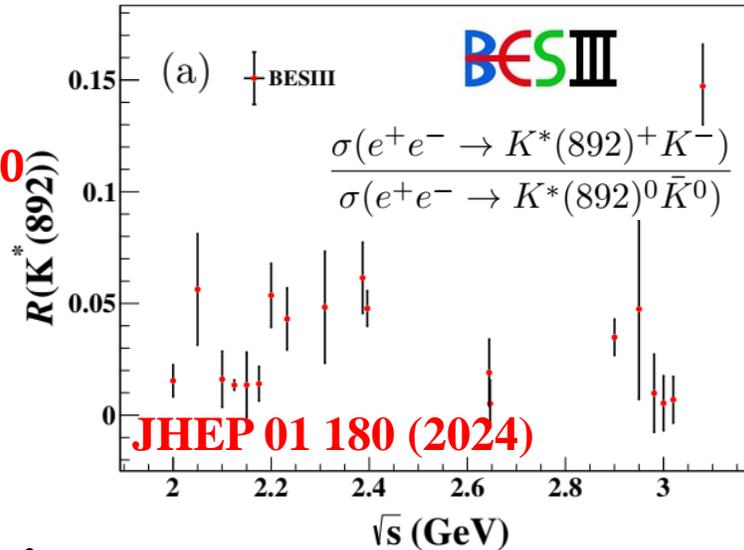
✓ Missing $K_S^0 K^\pm \pi^\mp$

● $\Gamma(K^+K^-) \approx 10 \Gamma(K_S K_L)$

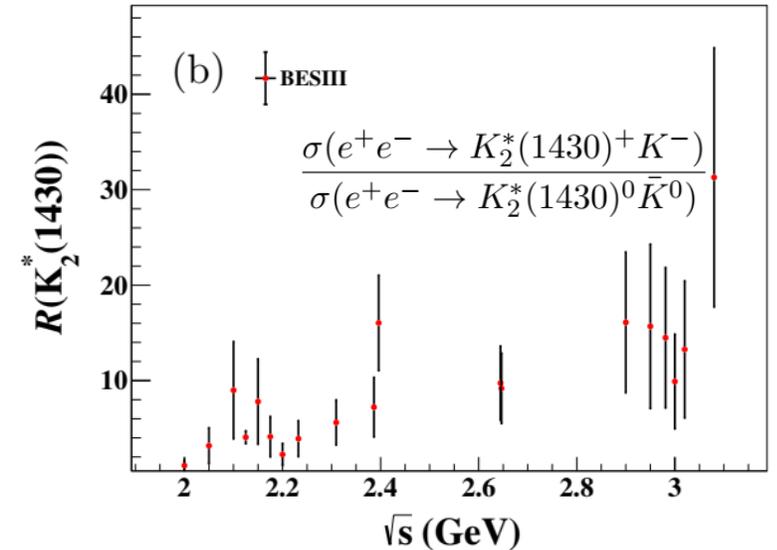
✓ valence quark charge

● K^*K : isospin \rightarrow one

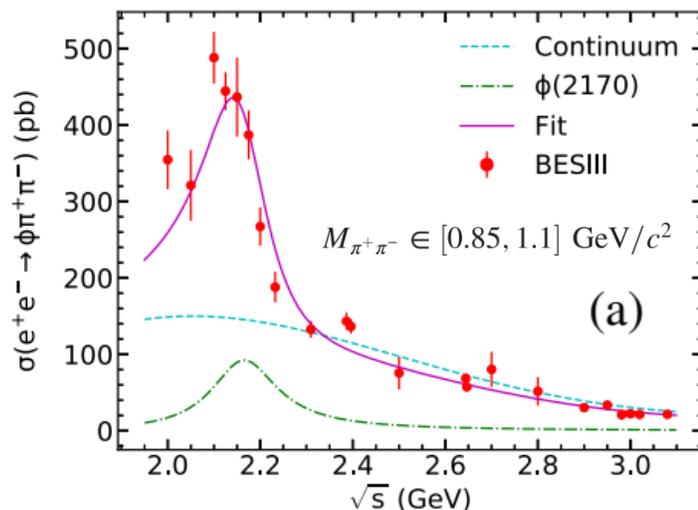
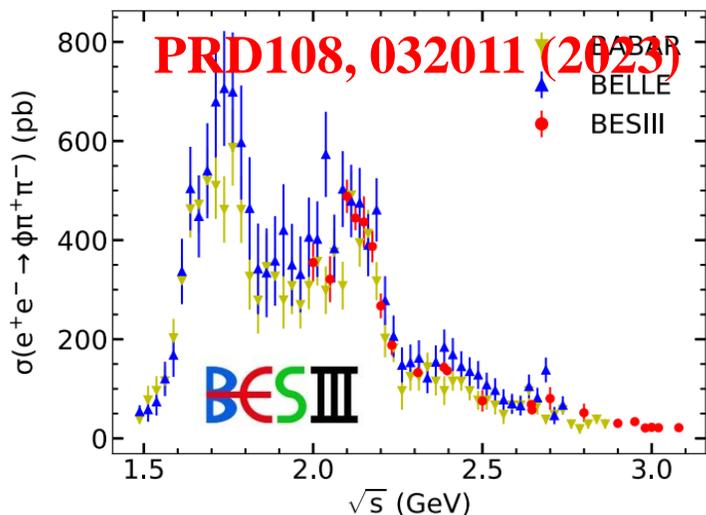
✓ electromagnetic interaction



JHEP 01 180 (2024)



$e^+ e^- \rightarrow \phi \pi^+ \pi^-$



$\phi f_0(980)$	Mass (MeV)	Width (MeV)
BaBar (2006)	$2175 \pm 10 \pm 15$	$58 \pm 16 \pm 20$
BES (2008)	$2186 \pm 10 \pm 6$	$65 \pm 23 \pm 17$
Belle (2009)	2163 ± 32	125 ± 40
BaBar (2012)	$2172 \pm 10 \pm 8$	$96 \pm 19 \pm 12$
BESIII (2015)	$2200 \pm 6 \pm 5$	$104 \pm 15 \pm 15$
BESIII (2019)	$2135 \pm 8 \pm 9$	$104 \pm 24 \pm 12$
PDG2024	2163 ± 7	$103 \pm 28 \pm 21$

● Belle & Babar results: general consistency, small systematic difference around 2.4 GeV.

✓ Belle data: structure @ 2.4 GeV with 1.5σ

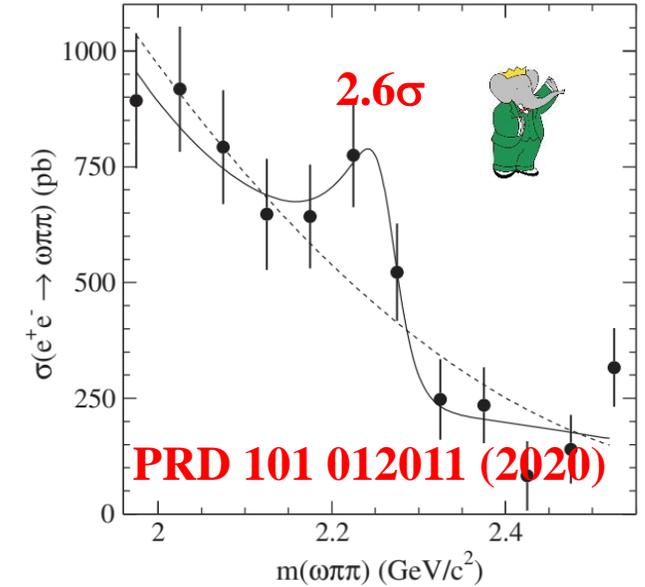
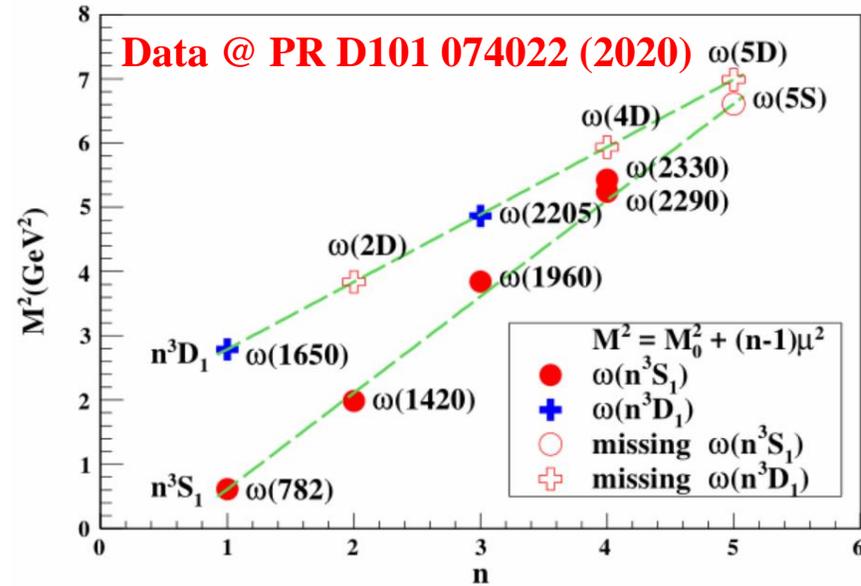
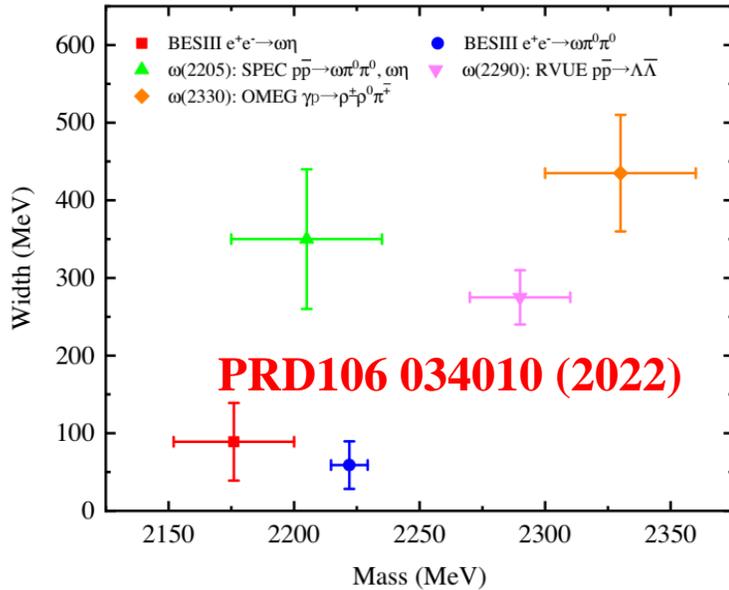
● $\phi \pi^+ \pi^-$ @ $M_{\pi\pi} [0.85, 1.1] \text{ GeV}/c^2$

✓ Really $\phi f_0(980)$? ✗

✓ $\phi(2170)$?

Parameter	σ	σ^*
$M_r(\phi(2170))$	2171 ± 12	2178 ± 20
$\Gamma_r(\phi(2170))$	115 ± 28	140 ± 36
ϕ_P^D	1.01 ± 0.14	1.13 ± 0.06
ϕ_P^C	-1.87 ± 0.16	-1.71 ± 0.12
χ^2/ndf	$28/15$	$23/15$

ω^* spectrum



● ω^* vector states

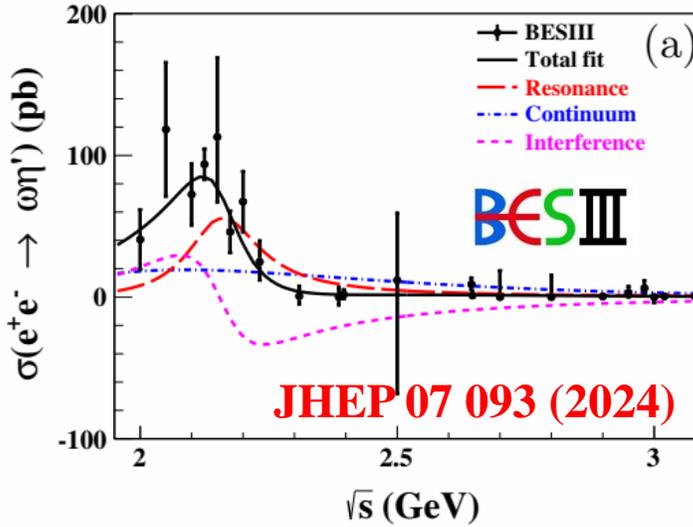
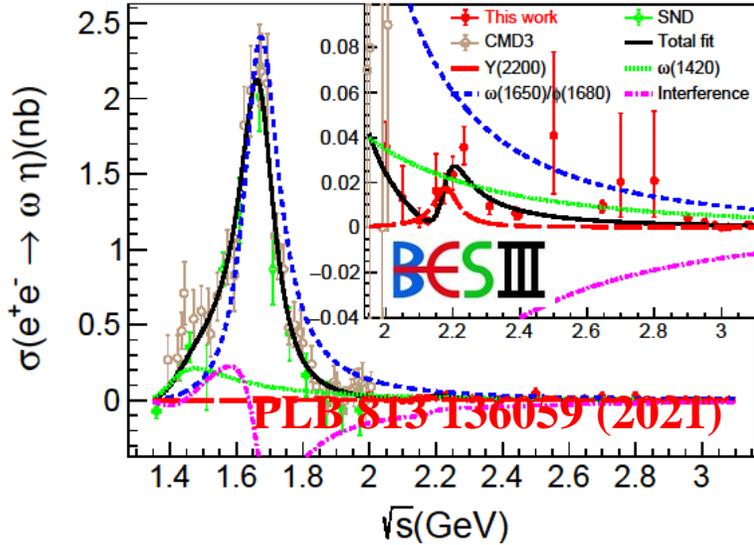
- ✓ $\omega(2205)$: possible 3D/4S, further states
- ✓ $\omega(2290)$: possible 4S, further states
- ✓ $\omega(2330)$: possible 4S, further states

● ω^* @ $e^+ e^-$ collision ?

Mode	$\omega(2205)$	$\omega(2290)$
	Width (MeV)	Width (MeV)
$b_1(1235)\pi$	24	35
$\rho(1450)\pi$	30	26
$\rho\pi$	4	16
$\omega\eta'$	0.4	0.4
$\omega\eta$	0	0.1
Total	141	138
Experiment	350 ± 90 (SPEC 02)	

PRD 104 054027 (2020)

$e^+ e^- \rightarrow \omega \eta$ & $\omega \eta'$



Parameters	Solution I	Solution II
$m_{Y(2180)}$ (MeV/ c^2)		2176 ± 24
$\Gamma_{Y(2180)}$ (MeV)		89 ± 50
$\Gamma^{ee} \cdot \mathcal{B}^{\omega\eta}$ (eV)	0.43 ± 0.15	1.25 ± 0.48
ϕ	2.6 ± 0.3	1.9 ± 0.2
significance		6.2σ

Parameter	Solution 1	Solution 2
M_R (MeV/ c^2)	$2153 \pm 30(\text{stat.}) \pm 31(\text{syst.})$	
Γ_R (MeV)	$167 \pm 77(\text{stat.}) \pm 7(\text{syst.})$	
ϕ (rad)	$3.78 \pm 0.24(\text{stat.}) \pm 0.12(\text{syst.})$	$3.16 \pm 0.4(\text{stat.}) \pm 0.2(\text{syst.})$
$\Gamma_R^{e^+e^-} \mathcal{B}_R^{\omega\eta'}$ (eV)	$5.72 \pm 1.68(\text{stat.}) \pm 1.5(\text{syst.})$	$2.99 \pm 1.68(\text{stat.}) \pm 1.2(\text{syst.})$
Significance	9.6σ	

PDG	Mass	Width
$\omega(2205)$	2205 ± 30	350 ± 90
$\omega(2290)$	2290 ± 20	375 ± 35
$\omega(2330)$	2330 ± 30	435 ± 75

PDG2024 $\omega(2220)$ WIDTH

VALUE (MeV)	DOCUMENT ID	TECN	COMMENT
$93 \pm 53 \pm 20$	⁵ ABLIKIM	23G BES3	$2.0\text{--}3.1 e^+e^- \rightarrow \omega\pi\pi$
••• We do not use the following data for averages, fits, limits, etc. •••			
$125 \pm 43 \pm 15$	⁶ ABLIKIM	23G BES3	$2.0\text{--}3.1 e^+e^- \rightarrow \omega\pi^+\pi^-$
$59 \pm 30 \pm 6$	⁷ ABLIKIM	22I BES3	$2.0\text{--}3.8 e^+e^- \rightarrow \omega\pi^0\pi^0$
350 ± 90	⁸ ANISOVICH	02B SPEC	$0.6\text{--}1.9 p\bar{p} \rightarrow \omega\eta, \omega\pi^0\pi^0$

- Isospin zero: ω^* and ϕ^* ?
- $\omega(2220)$ width
 - ✓ ~ 100 MeV @ BESIII
 - ✓ ~ 350 MeV @ SPEC

$$\begin{pmatrix} \eta \\ \eta' \end{pmatrix} = \begin{pmatrix} \cos\phi & -\sin\phi \\ \sin\phi & \cos\phi \end{pmatrix} \begin{pmatrix} \eta_q \\ \eta_s \end{pmatrix}$$



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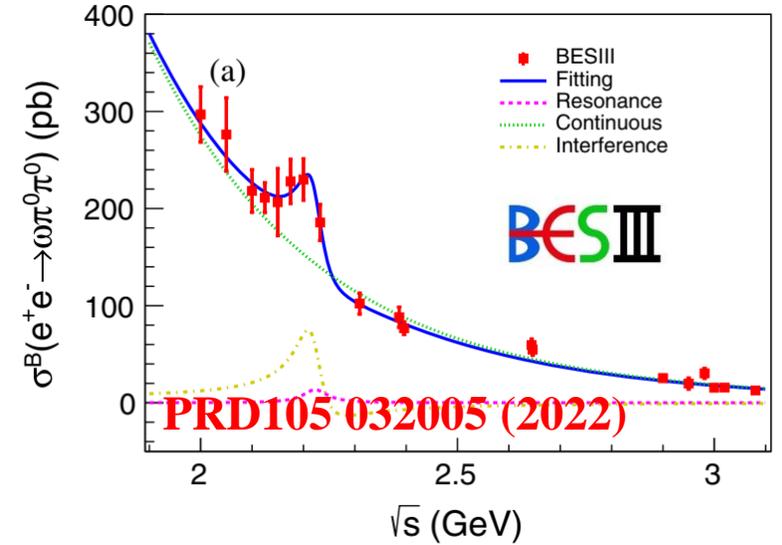
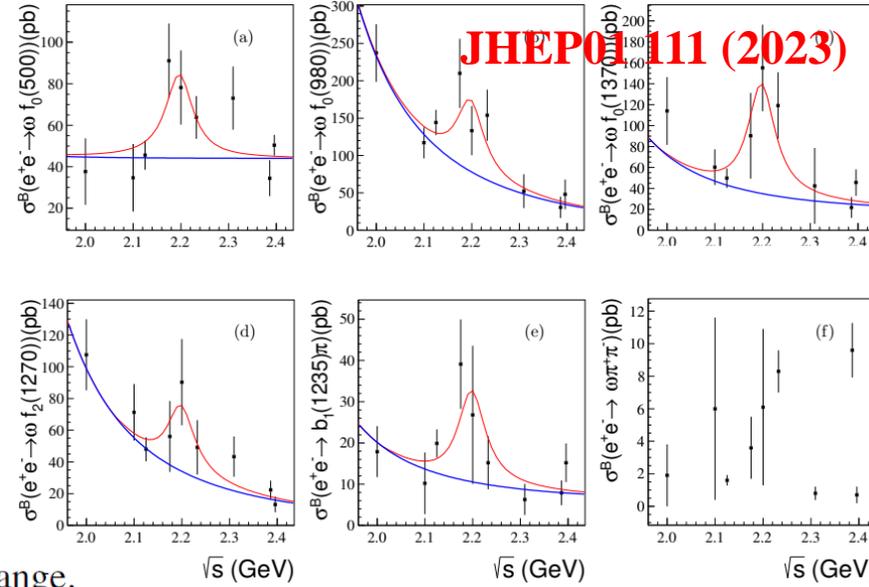
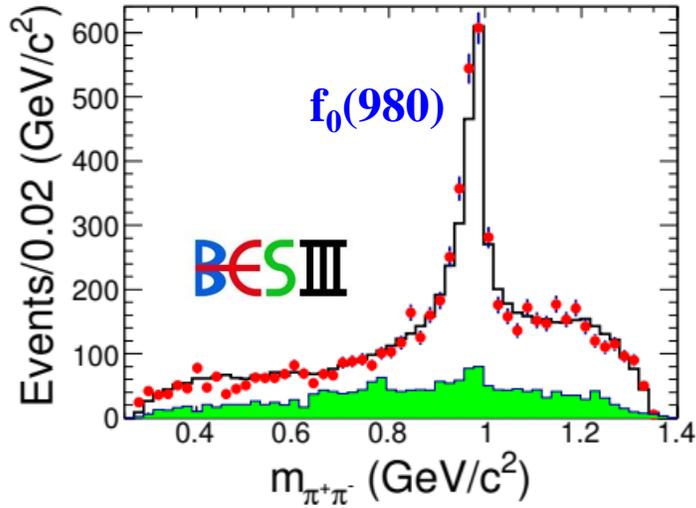
Physics Letters B 542 (2002) 19–28

www.elsevier.com/locate/nucphysb

$I = 0, C = -1$ mesons from 1940 to 2410 MeV

A.V. Anisovich^d, C.A. Baker^a, C.J. Batty^a, D.V. Bugg^c, L. Montanet^b, V.A. Nikonov^d,
A.V. Sarantsev^d, V.V. Sarantsev^d, B.S. Zou^{c,1}

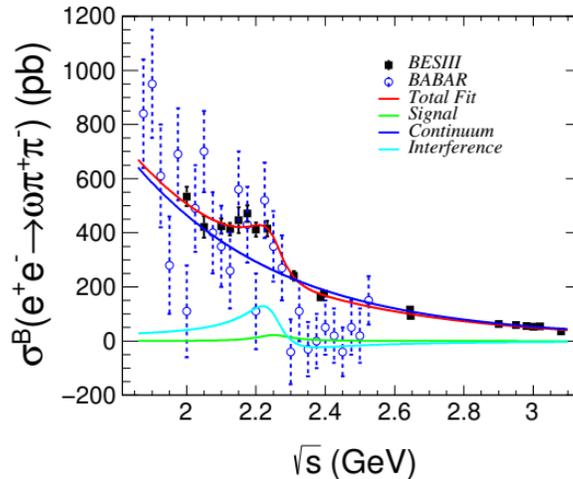
$e^+ e^- \rightarrow \omega \pi^+ \pi^-$ & $\omega \pi^0 \pi^0$



$$e^+ e^- \Rightarrow \begin{cases} Y(2175) \rightarrow \phi(1020) \pi^+ \pi^- & \text{strange,} \\ Y(4260) \rightarrow J/\psi \pi^+ \pi^- & \text{charm,} \\ \Upsilon(10860) \rightarrow \Upsilon(1S, 2S) \pi^+ \pi^- & \text{bottom,} \end{cases}$$

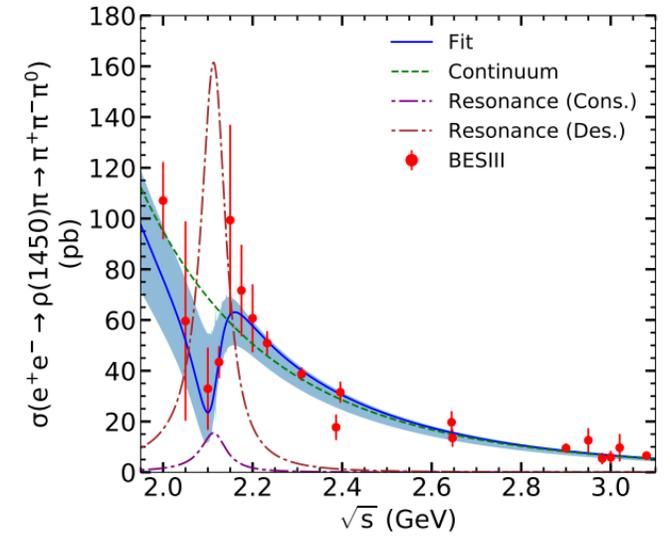
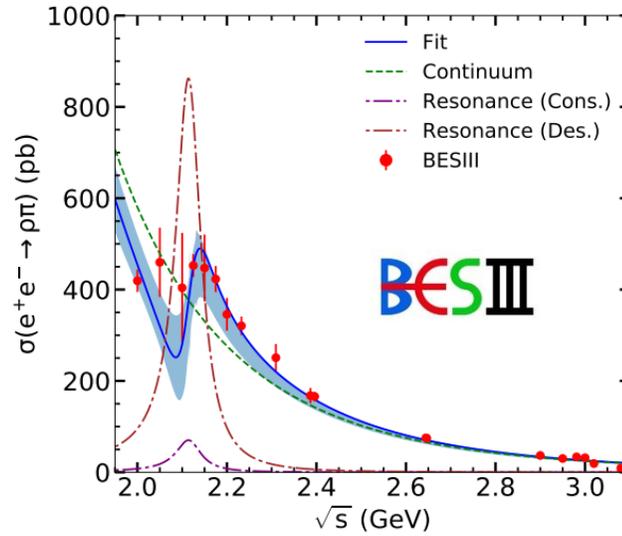
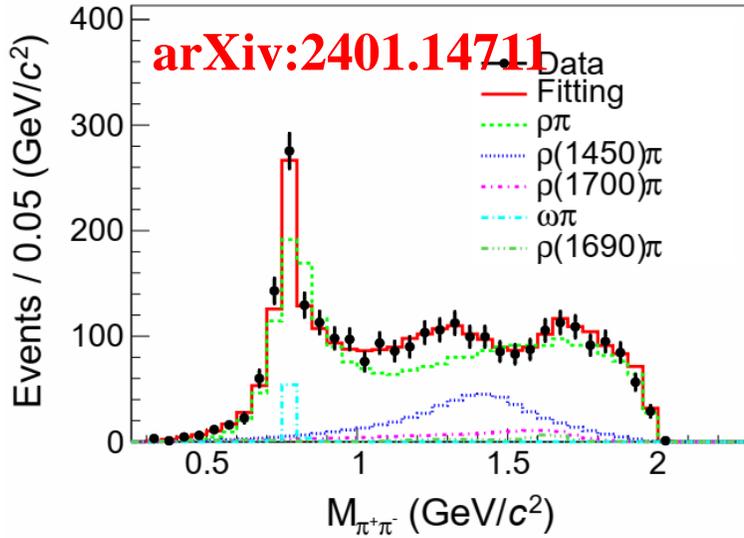
Eur. Phys. J. C72, 2008 (2012)

- $e^+ e^- \rightarrow \omega \rho \pi^+ \pi^-$?
- $\pi^+ \pi^-$: $f_0(980)$ signal
- G parity = -, ω^* state ?



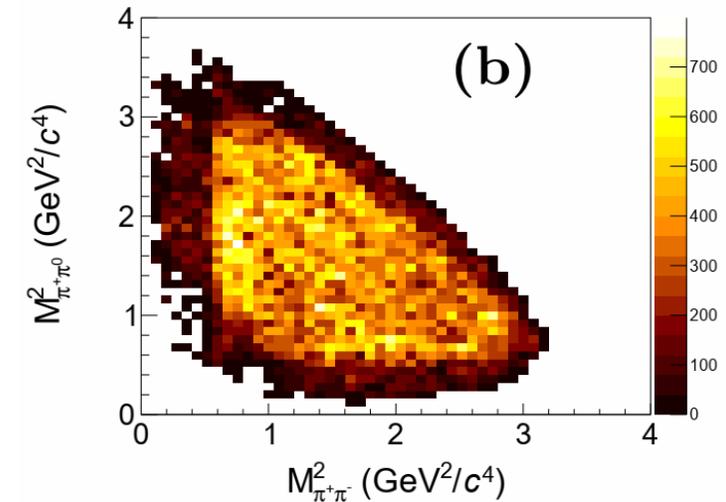
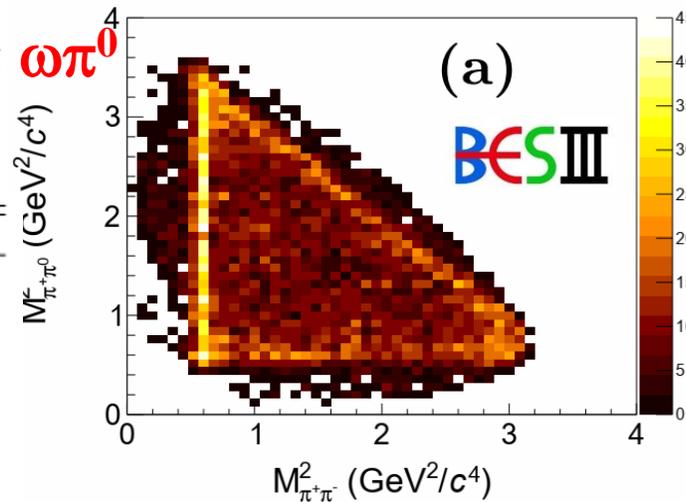
Parameter	Solution I	Solution II
m_r (MeV/ c^2)	2250 ± 25	
Γ_r (MeV)	125 ± 23	
$\Gamma_r^{ee} \cdot Br$ (eV)	0.9 ± 0.4	52.9 ± 17.0
ϕ (rad.)	2.4 ± 0.3	-1.8 ± 0.1
$a(10^3)(\text{pb}^{1/2})$	1.1 ± 0.2	
b	4.4 ± 0.1	
Significance	10.3σ	

$e^+ e^- \rightarrow \pi^+ \pi^- \pi^0$

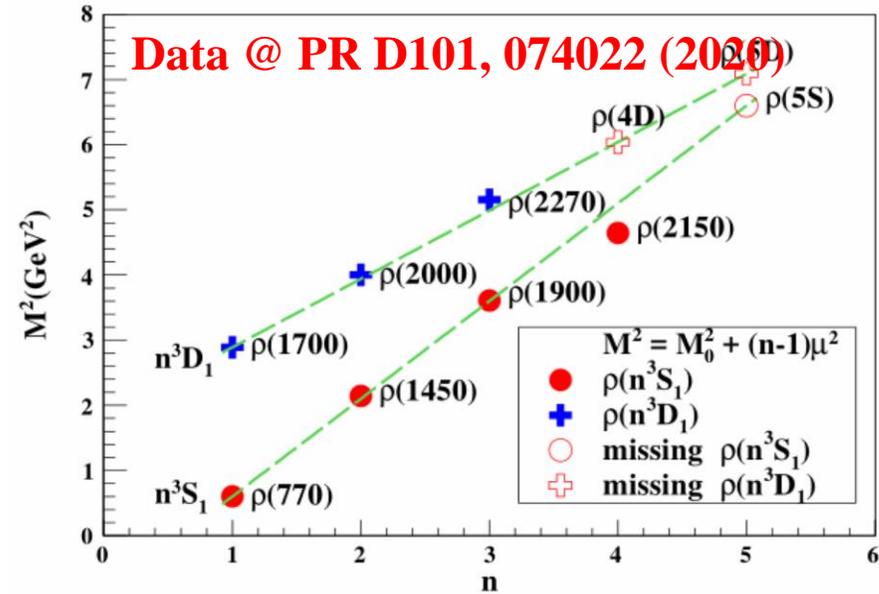
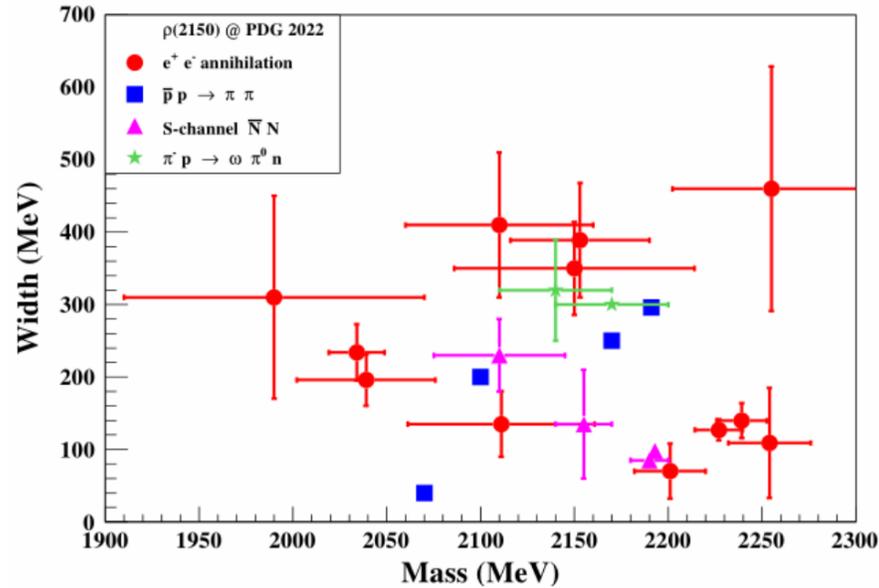


- $\rho^0 \pi^0$: G parity -, OZI, ω^* state
- Dominant $\rho^0 \pi^0$, visible $\rho(1450) \pi^0$ & $\omega \pi^0$
- PHOKHARA MC fails @ BESIII

	Nominal fit	Alternative fit
Mass	$2119 \pm 11 \text{ MeV}/c^2$	$2134 \pm 14 \text{ MeV}/c^2$
Width	$69 \pm 30 \text{ MeV}$	$74 \pm 31 \text{ MeV}$
χ^2	41.9	73.3
Number of free parameters	10	18
Degrees of freedom (ndf)	28	48
χ^2/ndf	1.50	1.53
Significance	5.9σ	5.2σ



ρ^* spectrum



- $\rho(2000)$: possible 2D, **further states**
- $\rho(2150)$: possible 2D or 4S
 ✓ $\rho(2150)$: inconsistent results between e^+e^- , $\bar{p}p$, s-channel $\bar{N}N$ and πp
- $\rho(2270)$: possible 3D, **further states**
- $\rho(2000)$ & $\rho(2270)$ @ e^+e^- collision ?

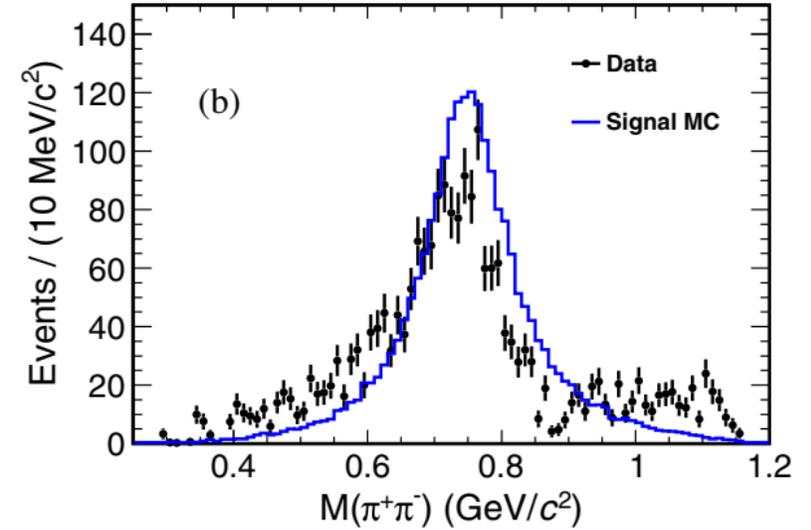
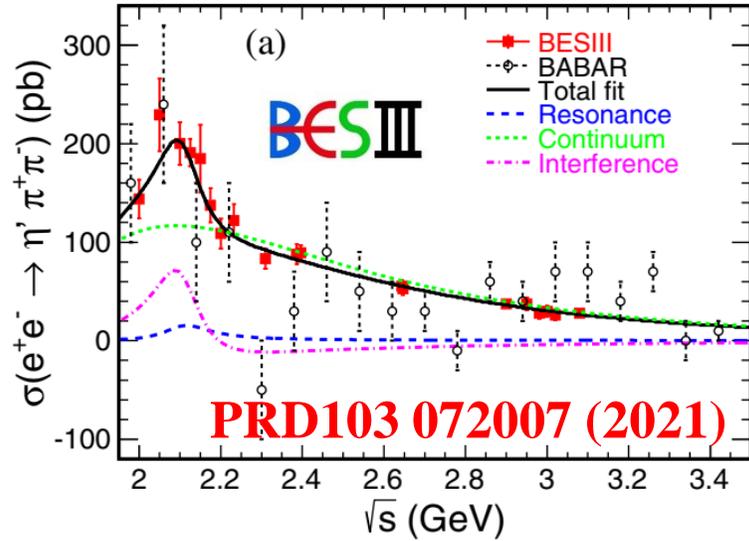
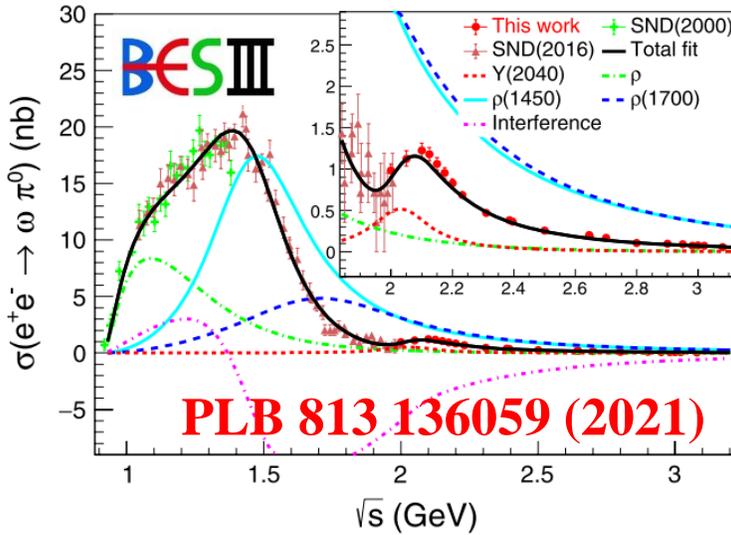
$\rho(2000)$		$I^G(J^{PC}) = 1^+(1^{--})$		PDG2022	
MASS (MeV)	WIDTH (MeV)	DOCUMENT ID	TECN	COMMENT	
2000 ± 30	260 ± 45	²³ BUGG	04c	RVUE	Compilation
~ 1988	~ 244	HASAN	94	RVUE	$\bar{p}p \rightarrow \pi\pi$

²³ From the combined analysis of ANISOVICH 00J, ANISOVICH 01D, ANISOVICH 01E, and ANISOVICH 02.

$\rho(2270)$		$I^G(J^{PC}) = 1^+(1^{--})$			
MASS (MeV)	WIDTH (MeV)	DOCUMENT ID	TECN	COMMENT	
2265 ± 40	325 ± 80	⁵⁰ ANISOVICH	02	SPEC	$0.6-1.9 \bar{p}p \rightarrow \omega\pi^0, \omega\eta\pi^0, \pi^+\pi^-$
2280 ± 50	440 ± 110	ATKINSON	85	OMEG	$20-70 \gamma p \rightarrow p\omega\pi^+\pi^-\pi^0$

⁵⁰ From the combined analysis of ANISOVICH 00J, ANISOVICH 01D, ANISOVICH 01E, and ANISOVICH 02.

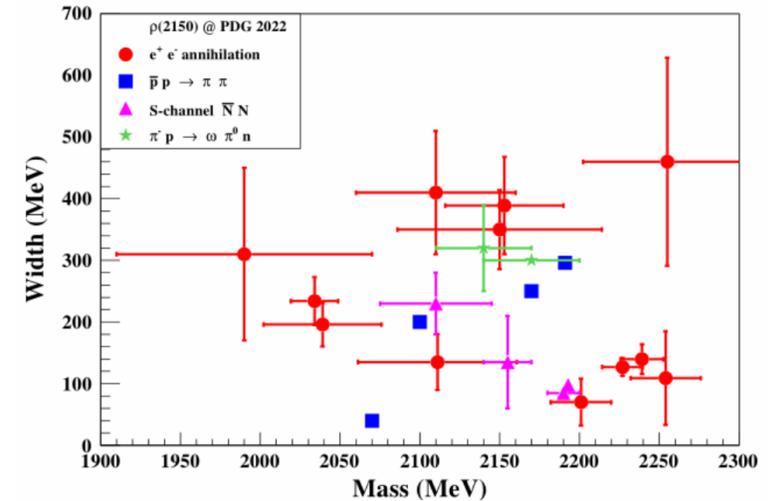
$e^+ e^- \rightarrow \omega \pi^0$ & $\eta' \pi^+ \pi^-$



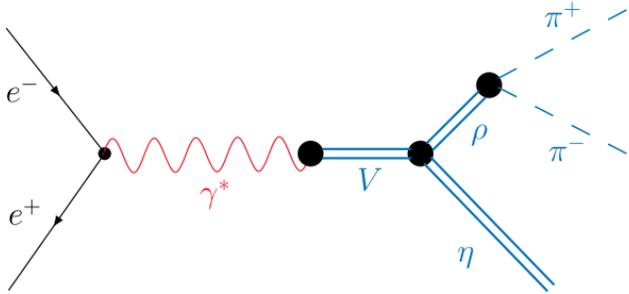
Parameters	Solution I	Solution II
$m_{Y(2180)}$ (MeV/ c^2)	2176 ± 24	
$\Gamma_{Y(2180)}$ (MeV)	89 ± 50	
$\Gamma^{ee} \cdot B^{\omega\eta}$ (eV)	0.43 ± 0.15	1.25 ± 0.48
ϕ	2.6 ± 0.3	1.9 ± 0.2
significance		6.2σ

Parameter	Solution 1	Solution 2
M_R (MeV/ c^2)	$2111 \pm 43 \pm 25$	
Γ_R^{tot} (MeV)	$135 \pm 34 \pm 30$	
$B_R \Gamma_R^{ee}$ (eV)	$0.64 \pm 0.49 \pm 0.42$	$23.3 \pm 5.3 \pm 3.3$
ϕ (rad)	$2.24 \pm 0.73 \pm 0.48$	$4.46 \pm 0.06 \pm 0.10$
$n(n')$	$4.42 \pm 0.22 \pm 0.20$	$(1.66 \pm 0.12 \pm 0.07)$
$C_0(C'_0)$	$921 \pm 240 \pm 114$	$(53.0 \pm 13.2 \pm 0.1)$

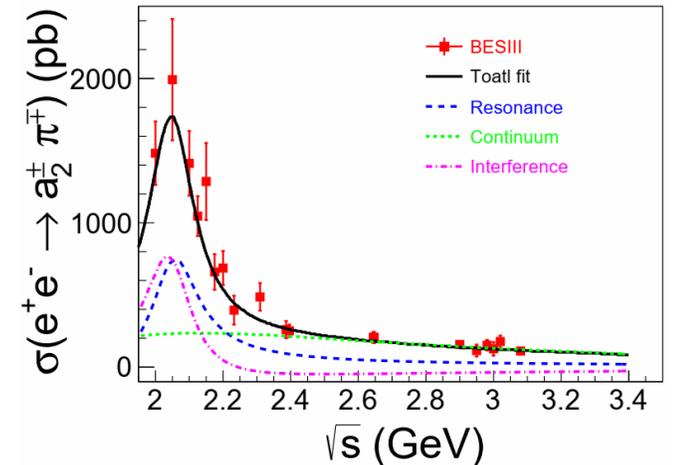
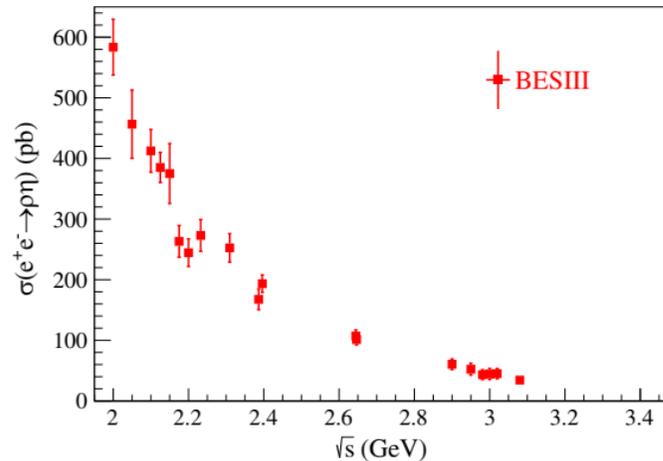
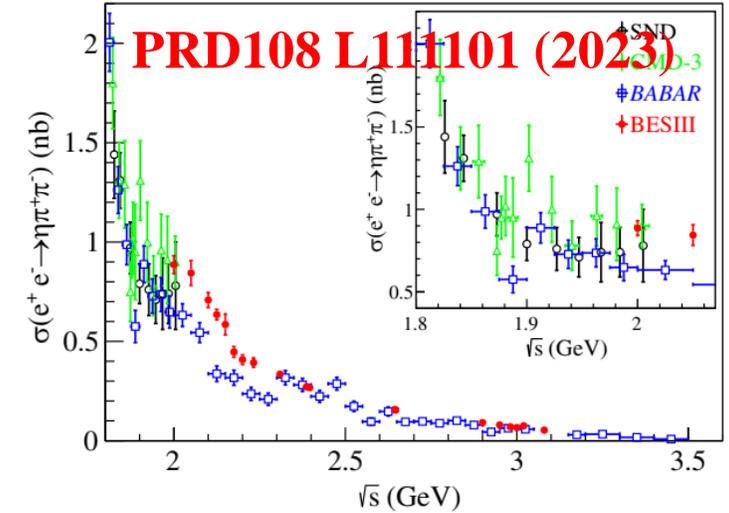
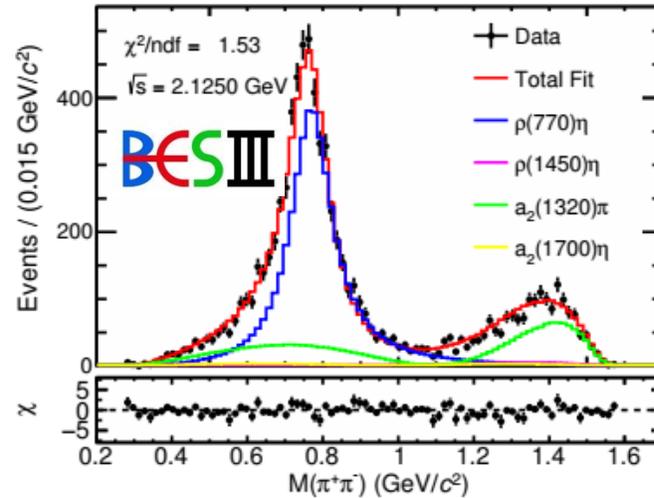
- $\omega\pi^0$ & $\rho\eta'$: G parity = +, ρ^* state $\rho(2000)$ or $\rho(2150)$?
- **dominant component $\rho\eta'$** , non- ρ contribution < 10%.



$e^+ e^- \rightarrow \pi^+ \pi^- \eta$

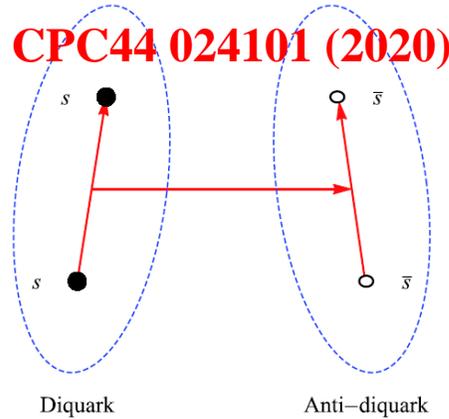
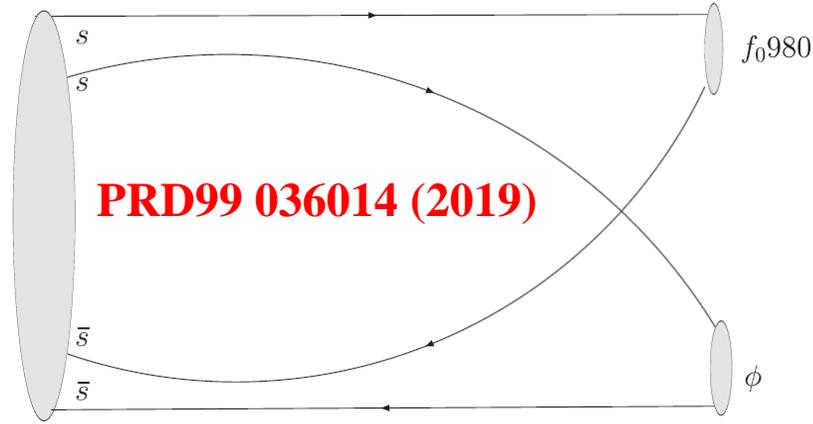


- $\rho \eta$ mode: G parity = +, ρ^* state
- Default MC $e^+ e^- \rightarrow \rho \eta$ for $\eta \pi^+ \pi^-$
- BESIII results vs. BABAR results
 - ✓ Systematically 30% higher
- Dominant component $\rho\eta$ @ $\pi^+ \pi^- \eta$
 - ✓ A dip around 2.18 GeV, hint ?
- A resonance @ $a_2(1320)\pi$



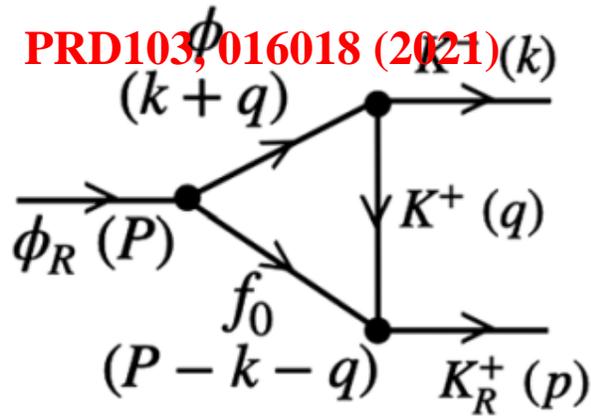
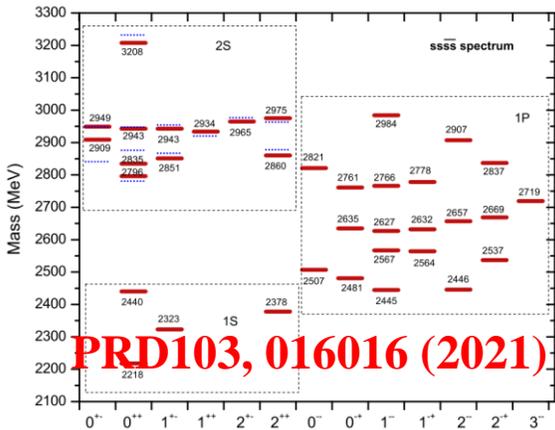
Parameter	Solution 1	Solution 2
M_R (MeV/ c^2)	$2044 \pm 31 \pm 4$	
Γ_{tot}^R (MeV)	$163 \pm 69 \pm 24$	
$\mathcal{B}_R \Gamma_{e^+e^-}^R$ (eV)	$34.6 \pm 17.1 \pm 6.0$	$137.1 \pm 73.3 \pm 2.1$
ϕ (rad)	$1.95 \pm 0.97 \pm 0.06$	$4.35 \pm 0.48 \pm 0.43$

Nature of $\phi(2170)$



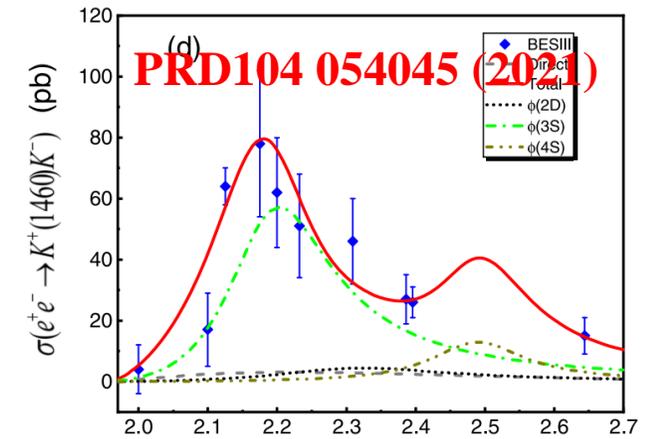
	$\phi(3S)$		$s\bar{s}$ hybrid	$\phi(4S)$	
Mass	2188	2002	2000 [29]	2498	
Channel	Value	Value	Value [29]	Channel	Value
Total	217	133	120	Total	942
$KK^*(1410)$	48.4	45.2	9	$KK_3^*(1780)$	178
KK^*	60	26.9	16	$K^*K_2^*(1430)$	160
KK_1'	4.36	21.4	64	KK_1'	123
KK_1	23.6	19.3	26	K^*K^*	94.9
KK	11.9	10.8	...	$KK_2^*(1430)$	84.6
$KK_2^*(1430)$	39.8	4.48	2	$KK^*(1410)$	80.9
K^*K^*	22.7	4.40	...	KK^*	67.5
$\eta\phi$	6.66	0.363	3	KK_1	54.2
$\eta'\phi$	0.0862	0.0729	0.02	$KK_1^*(2045)$	54.8
				$KK^*(1680)$	29.0
				$KK^*(1680)$	14.9

PRD99 074015 (2019)



Mode	$\phi(2170)$	$\phi(2050)$
	Width (MeV)	Width (MeV)
$K_1(1400)K$	120	64
$K_1(1270)K$	111	71
KK	77	51
K^*K	41	41
K^*K^*	20	25
$h_1(1415)\eta$	15	8
$\phi\eta$	4	0.4
$K_2^*(1430)K$	3	0
$K^*(1410)K$	3	37
$K(1460)K$	2	6
$\phi\eta'$	0.6	0.4
Total	410	277
Experiment	125 ± 65	

PRD104, 054027 (2021)



tetraquark ? $s\bar{s}$ state ? $\phi f_0(980)$ molecular state ? mixing state ?

Nature of $\phi(2170)$

PHYSICAL REVIEW D **101**, 074012 (2020)

Nature of the vector resonance $Y(2175)$

S. S. Agaev,¹ K. Azizi^{2,3}, and H. Sundu⁴

PHYSICAL REVIEW D **101**, 074045 (2020)

Reconciling the $X(2240)$ with the $Y(2175)$

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²Department of Physics, Hunan Normal University, Changsha 410081, China
PHYSICAL REVIEW D **100**, 034012 (2019)

Is the $Y(2175)$ a strangeonium hybrid meson?

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Chinese Physics C Vol. 45, No. 1 (2021) 013112

Strangeonium-like hybrids on the lattice*

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Chinese Physics C Vol. 45, No. 2 (2021) 023116

Mass spectrum and strong decays of strangeonium in a constituent quark model*

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Qi-Fang Lü(吕齐放)^{1,2,3} Xian-Hui Zhong(钟显辉)^{1,2,3†}

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Chinese Physics C Vol. 43, No. 11 (2019) 113105

A possible explanation of the threshold enhancement in the process

$$e^+e^- \rightarrow \Lambda\bar{\Lambda}^*$$

Li-Ye Xiao(肖立叶)^{1,2,1)} Xin-Zhen Weng(翁新震)^{1,2)} Xian-Hui Zhong(钟显辉)^{3,4,3)} Shi-Lin Zhu(朱世琳)^{1,2,5,4)}

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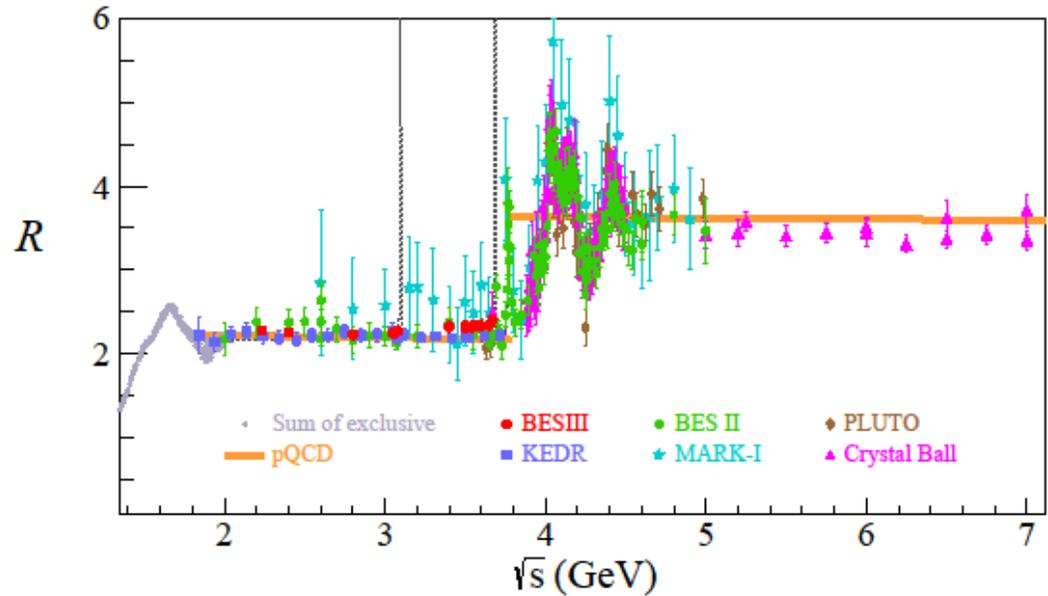
⁵Collaborative Innovation Center of Quantum Matter, Beijing 100871, China

need more experimental data ? \Rightarrow Belle II

$\phi(2170)$ @ 2015 R scan data

16 published paper + 1 draft

- ① $e^+e^- \rightarrow K^+ K^-$: PRD 99, 032001 (2019)
- ② $e^+e^- \rightarrow \phi K^+ K^-$: PRD 100, 032009 (2019)
- ③ $e^+e^- \rightarrow K^+ K^- \pi^0 \pi^0$: **PRL 124, 112001 (2020)**
- ④ $e^+e^- \rightarrow \phi \eta'$: PRD 102, 012008 (2020)
- ⑤ $e^+e^- \rightarrow \omega \eta$ & $\omega \pi^0$: PLB 813, 136059 (2021)
- ⑥ $e^+e^- \rightarrow \eta' \pi^+ \pi^-$: PRD 103, 072007 (2021)
- ⑦ $e^+e^- \rightarrow \phi \eta$: PRD 104, 032007 (2021)
- ⑧ $e^+e^- \rightarrow K_S K_L$: PRD 104, 092014 (2021)
- ⑨ $e^+e^- \rightarrow \omega \pi^0 \pi^0$: PRD 105, 032005 (2022)
- ⑩ $e^+e^- \rightarrow K^+ K^- \pi^0$: JHEP 07, 045 (2022)
- ⑪ $e^+e^- \rightarrow \phi \pi^+ \pi^-$: PRD 108, 032011 (2023)
- ⑫ $e^+e^- \rightarrow \eta \pi^+ \pi^-$: PRD 108, L111101 (2023)
- ⑬ $e^+e^- \rightarrow \omega \pi^+ \pi^-$: JHEP 01, 111 (2023)
- ⑭ $e^+e^- \rightarrow K_S K_L \pi^0$: JHEP 01, 180 (2024)
- ⑮ $e^+e^- \rightarrow \omega \eta'$: JHEP 07, 093 (2024)
- ⑯ $e^+e^- \rightarrow \pi^+ \pi^- \pi^0$: [arXiv:2401.14711](https://arxiv.org/abs/2401.14711), PRD
- ⑰ $e^+e^- \rightarrow \omega \eta \pi^0$: draft @ Wenbiao



BESIII

$e^+ e^- \rightarrow \omega \eta \pi^0$

Memo version 2.3

BESIII Analysis Memo

November 15, 2022

Measurement of the Born cross sections for $e^+e^- \rightarrow \omega\eta\pi^0$ at center-of-mass energies between 2.00 and 3.08 GeV

Linqin Huang^a, Yateng Zhang^b, and Wenbiao Yan^c, and Yuxiang Zhao^a

^aInstitute of Modern Physics, CAS

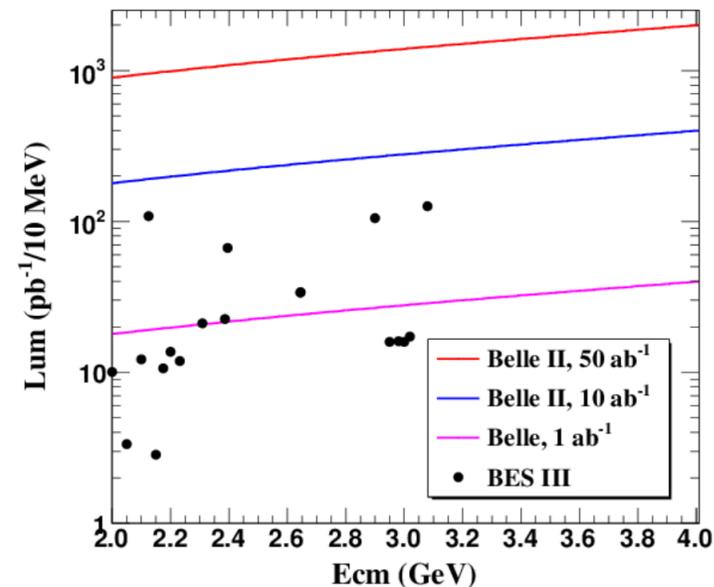
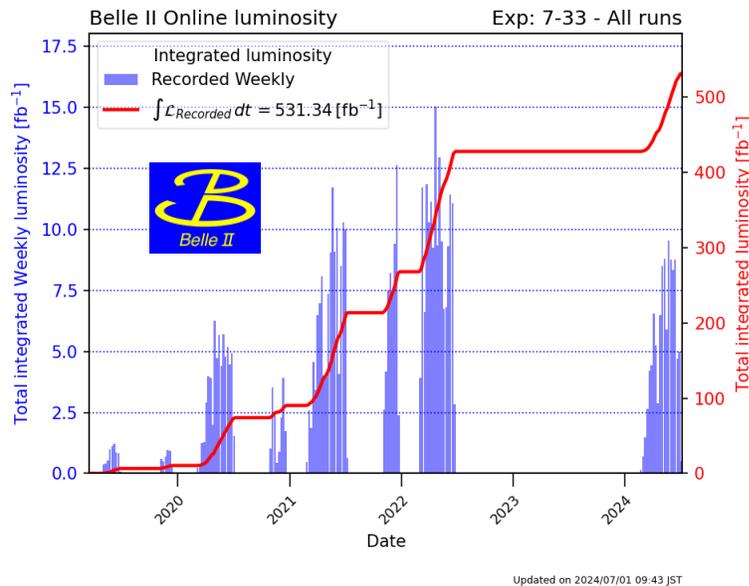
^bZhengzhou University

^cUniversity of Science and Technology of China

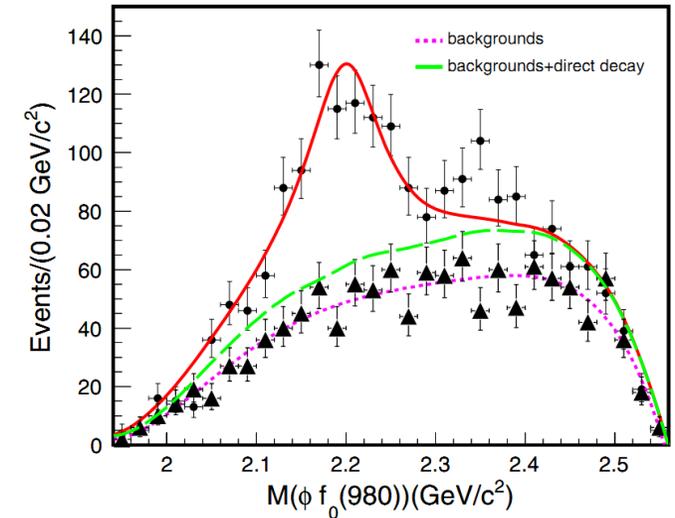
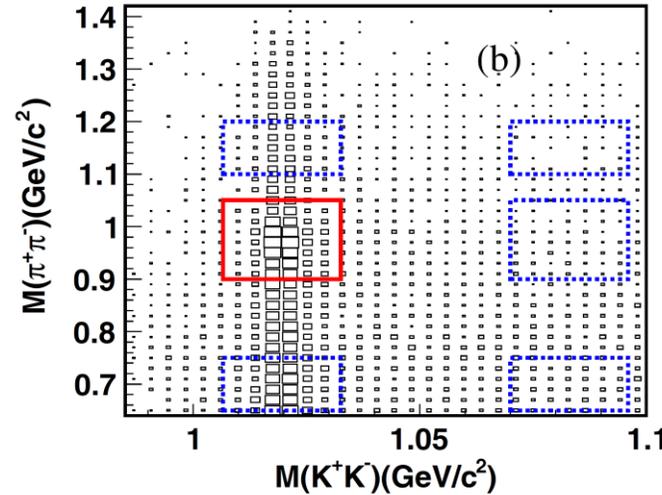
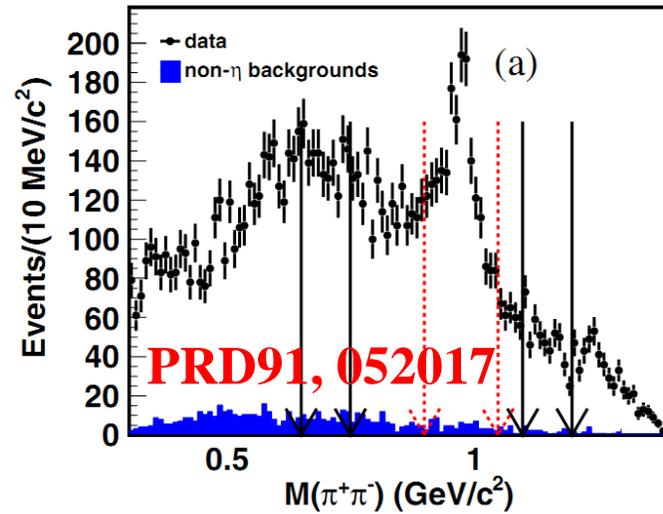


Summary and outlook

- Using BESIII R scan data, we are extensively studying $\phi(2170)$
 - ✓ $\phi(2170)$ as pure $3^3S_1 s\bar{s}$? $2^3D_1 s\bar{s}$?
 - ✓ $\phi(2170)$ as $1^- s\bar{s}g$ hybrid ? molecular state $\Lambda\bar{\Lambda}$? three body system ϕKK ?
 - ✓ $\phi(2170)$ as tetraquark: ? mixing state: ? $\phi f_0(980)$ molecular state: ?
- Need ρ^* and ω^* spectrum to understand $\phi(2170)$.
- Belle II: 50 ab^{-1} data, study $\phi(2170)$ with ISR method.



$\phi(2170) @ J/\psi \rightarrow \eta \phi \pi^+ \pi^-$



- **Fit: $\phi(2170)$ + direct decay of $J/\psi \rightarrow \eta \phi f_0(980)$ + background**
- **No interference between $\phi(2170)$ and direct decay**

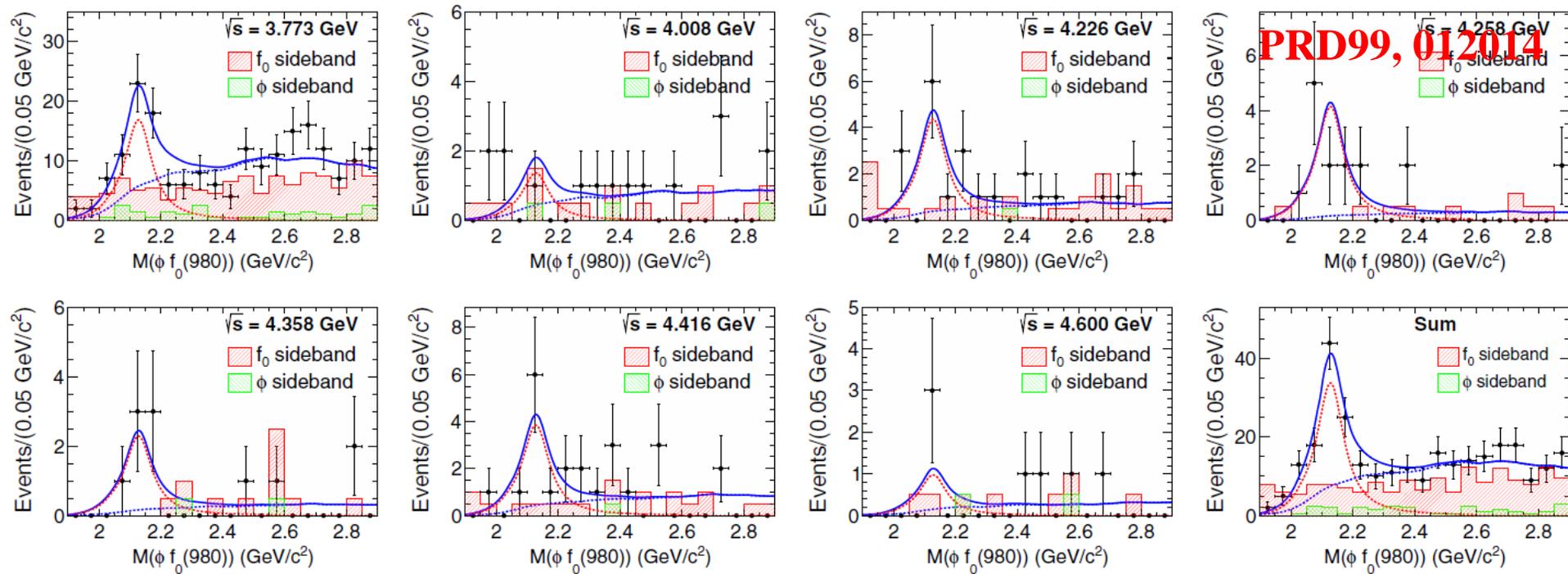
Decay mode

Branching fraction \mathcal{B}

$J/\psi \rightarrow \eta Y(2175),$
 $Y(2175) \rightarrow \phi f_0(980),$
 $f_0(980) \rightarrow \pi^+ \pi^-$

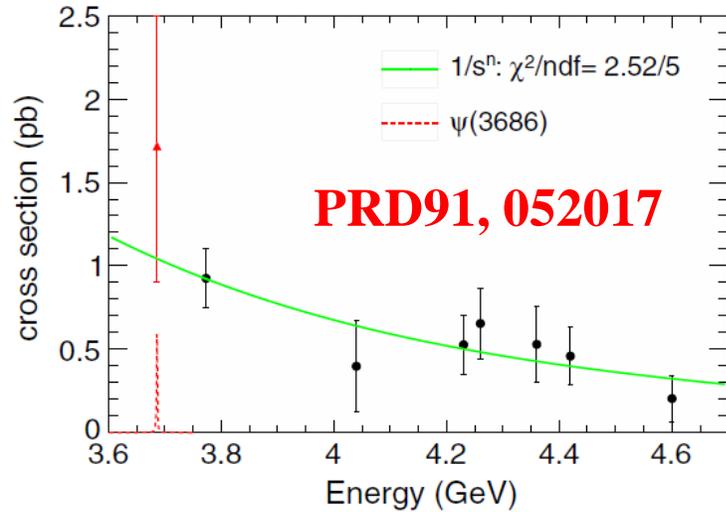
$(1.20 \pm 0.14 \pm 0.37) \times 10^{-4}$

$\phi(2170) @ e^+ e^- \rightarrow \eta \phi \pi^+ \pi^-$



- $\phi(2170) @ \phi f_0(980)$ with $\sqrt{s} = [3.773, 4.600]$ GeV data
- Limited samples for $\phi(2170)$

$e^+ e^- \rightarrow \eta \phi(2170)$



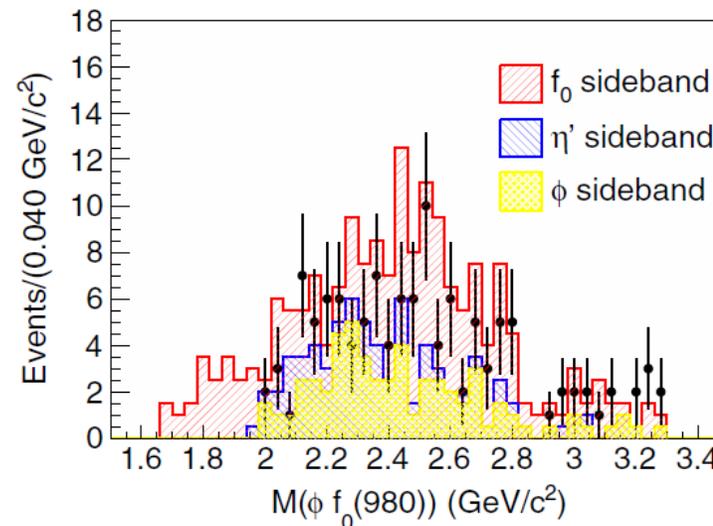
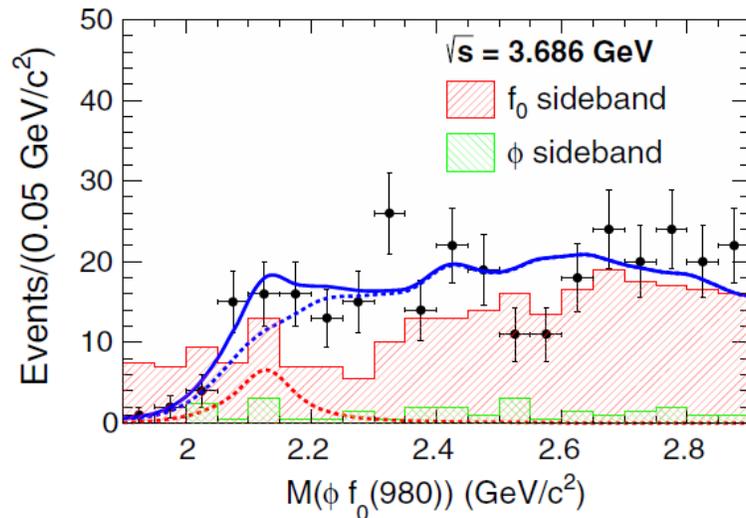
- The Born cross section varies as $1/s^n$ with $n=2.65\pm 0.86$.

- $\text{Br}[\psi(3686) \rightarrow \eta \phi(2170)] < 2.2 \cdot 10^{-6}$

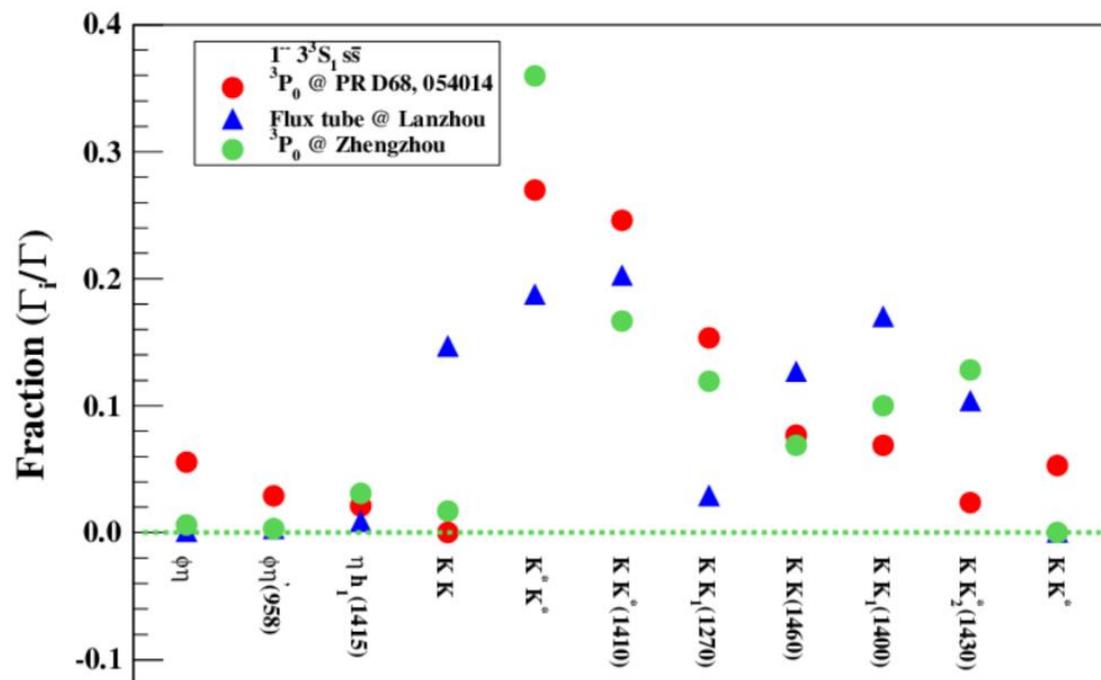
- @ 90% U.L., suppression for “12% rule”

- No significant signal $e^+e^- \rightarrow \eta' \phi(2170)$

- $\frac{\sigma[e^+e^- \rightarrow \eta' \phi(2170)]}{\sigma[e^+e^- \rightarrow \eta \phi(2170)]} < 0.43 @ 90\% \text{ U.L.}$



How ? $\phi(2170)$ as pure $3^3S_1 s\bar{s}$



- reduction to Absurdity
 - ✓ $3^3S_1 s\bar{s}$: $\Gamma_{K^*K^*} > \Gamma_{KK_1(1400)}$
 - ✓ Exp. $\phi(2170)$ @ $KK_1(1400)$
 - ✓ Exp. no $\phi(2170)$ @ K^*K^*
 - ✓ Exp. similar ε_{eff}
 - ✓ $\phi(2170)$ as pure $3^3S_1 s\bar{s}$?
- similar check for several modes
 - ✓ $KK^*(1410)$: No $\phi(2170)$
 - ✓ $KK(1460)$: Yes $\phi(2170)$
- $\phi(2170)$ as pure $3^3S_1 s\bar{s}$: No ?

- fraction Γ_i/Γ : weakly model & input parameters dependent
- dominant decay modes:
 - ✓ $KK^*(1410)$ & K^*K^*



- pure $3^3S_1 s\bar{s}$?
- pure $2^3D_1 s\bar{s}$?
- molecular state $\Lambda\bar{\Lambda}$?
- three body system ϕKK ?
- $1^- s\bar{s}g$ hybrid ?