



Measurements of Light Nuclei Femtoscopy at High Baryon Density

Ke Mi (米柯)

Central China Normal University

STAR区域研讨会

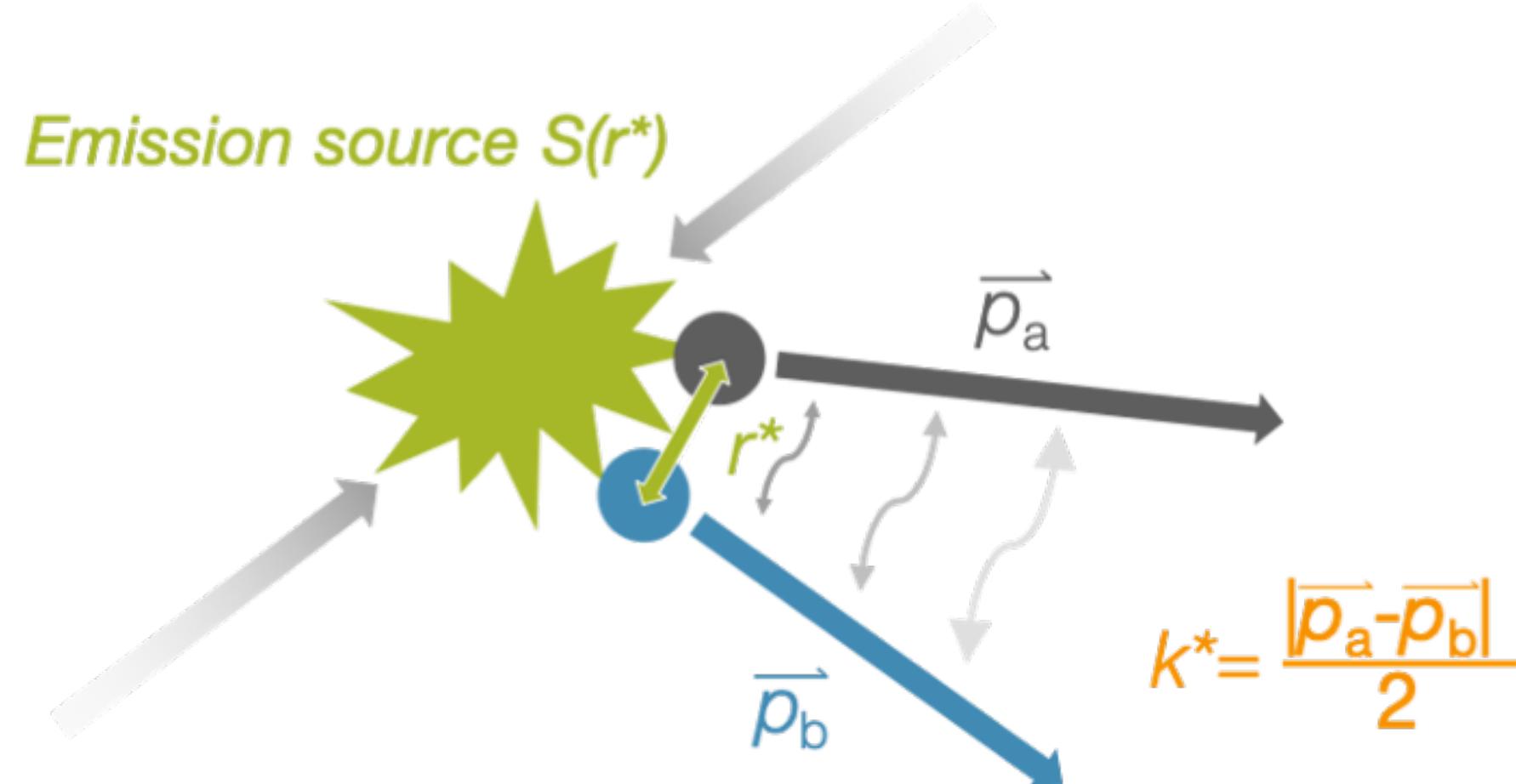
2024年10月10-15日，重庆，中国

Outline



- 1. Femtoscopy and Two-particle Correlation Function**
- 2. Lednicky-Lyuboshitz (L-L) Model**
- 3. Motivation**
- 4. STAR Experiment**
- 5. Results**
 - **p-d, d-d correlation at 3 GeV**
 - **d- Λ correlation at 3 GeV**
- 6. Summary & Outlook**

Femtoscopy

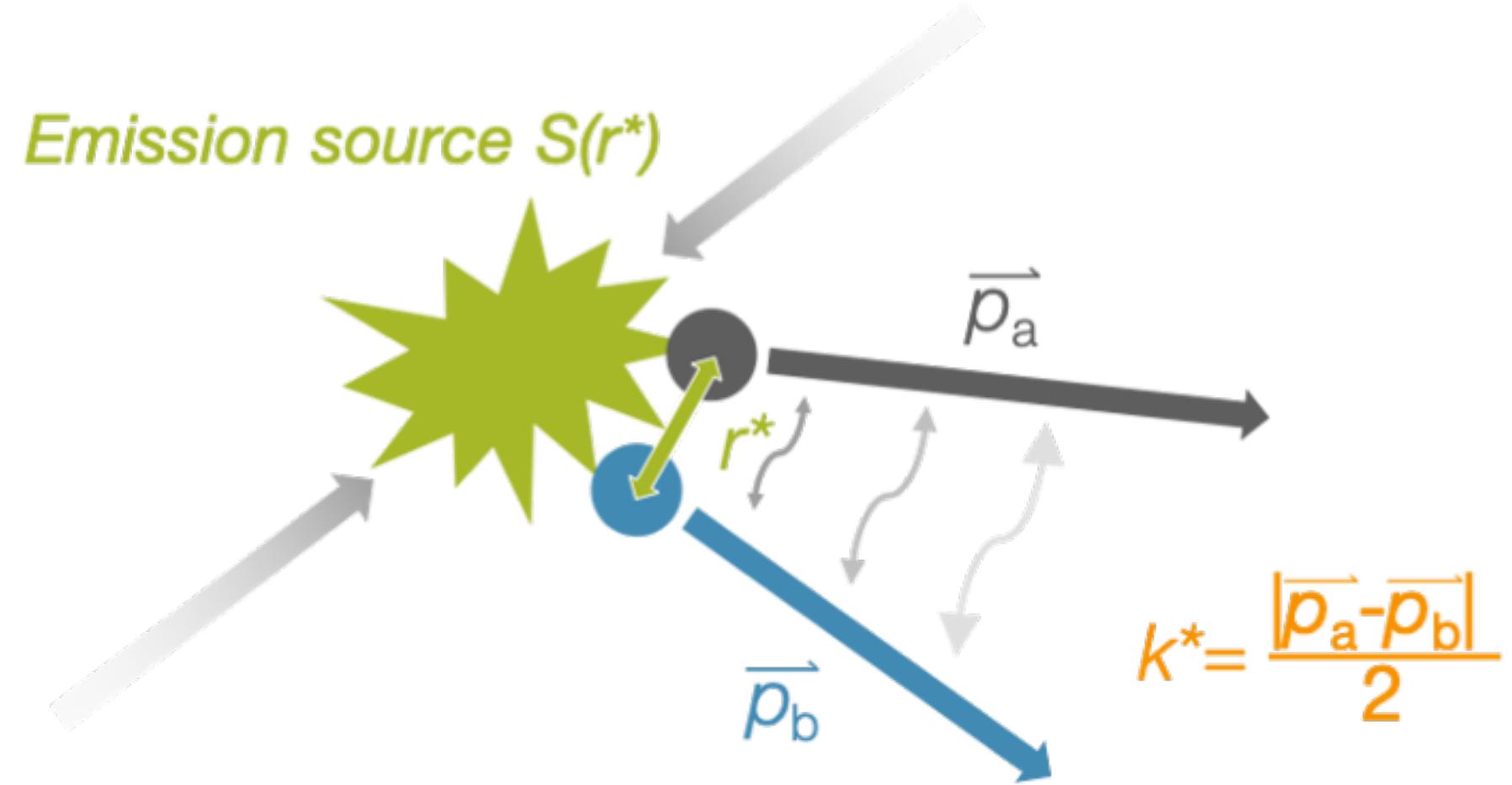


⇒ Femtoscopy is inspired by Hanbury Brown and Twiss (HBT) interferometry, but different scale (~several fm)

- Spatial and temporal extent of emission source
- Final-state Interactions (Coulomb, Strong interaction)
- Bound state

Nature 178 1046-1048(1956)
ALICE Coll. Nature 588, 232–238 (2020)

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✓ Two-particle correlation function:

Model

$$C(k^*) = \int S(\vec{r}) |\Psi(\vec{k}^*, \vec{r})|^2 d^3\vec{r} = \frac{N_{\text{same}}(k^*)}{N_{\text{mixed}}(k^*)}$$

Experimental

$S(\vec{r})$: Source function

$\Psi(\vec{k}^*, \vec{r})$: Pair wave function

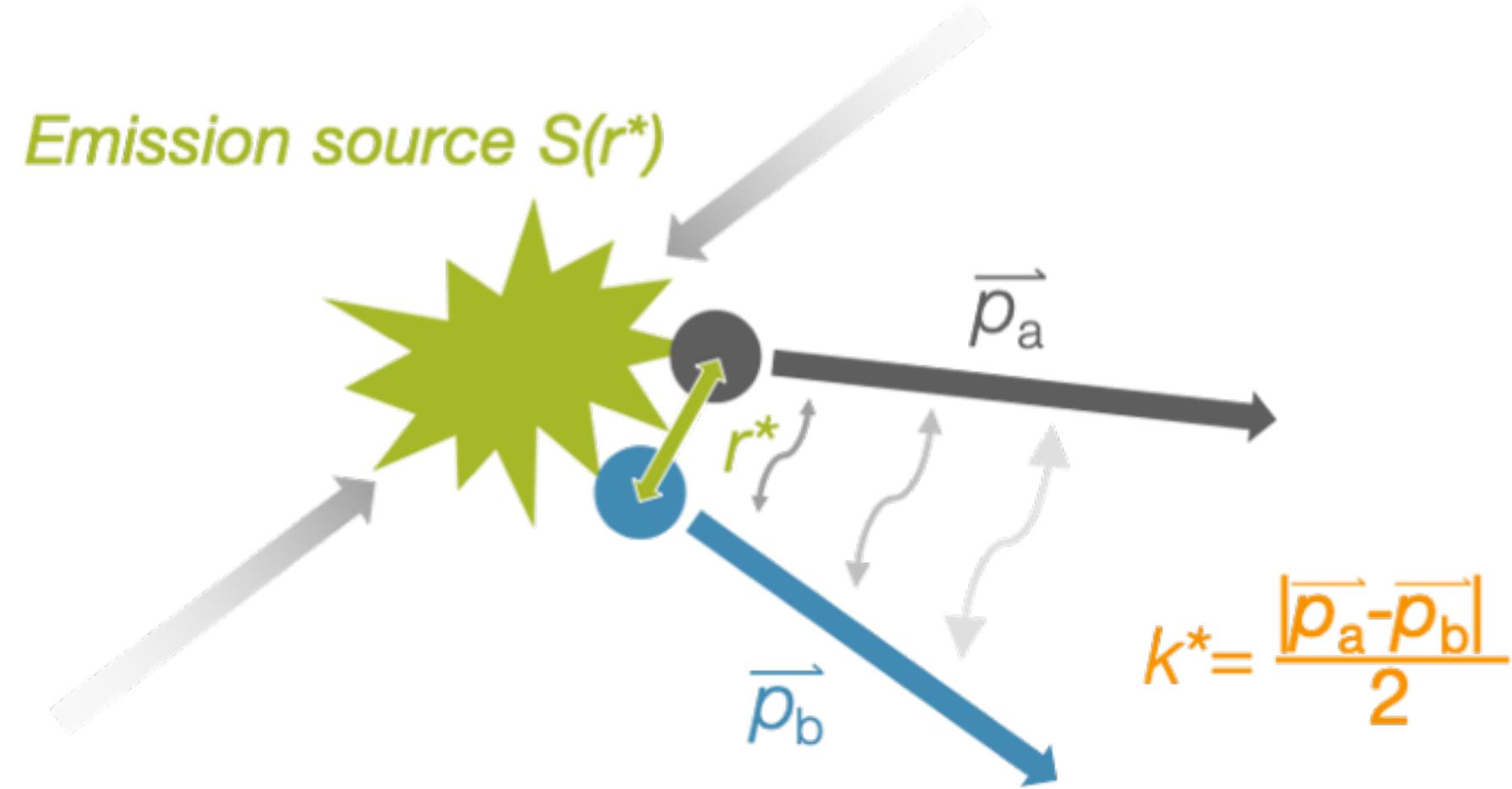
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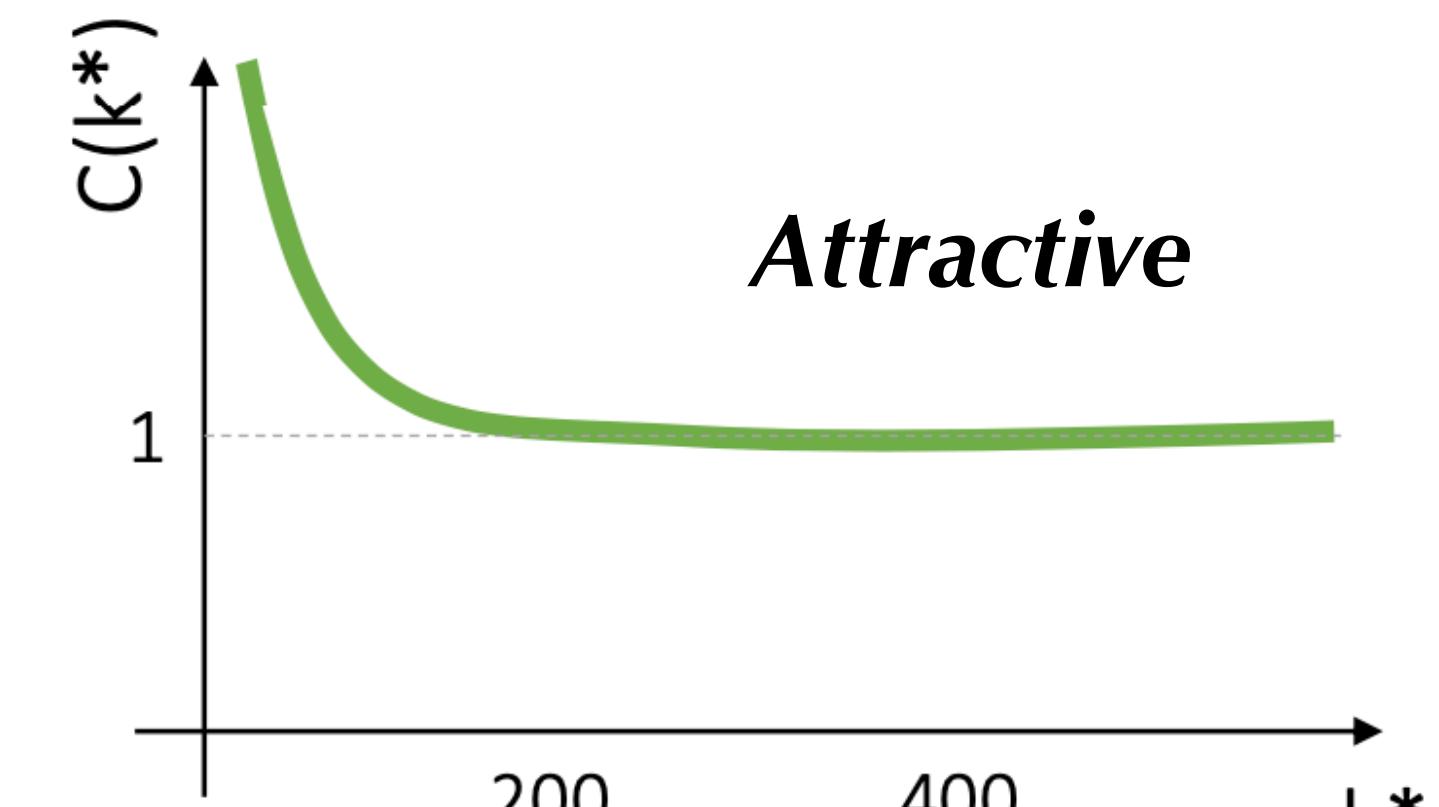
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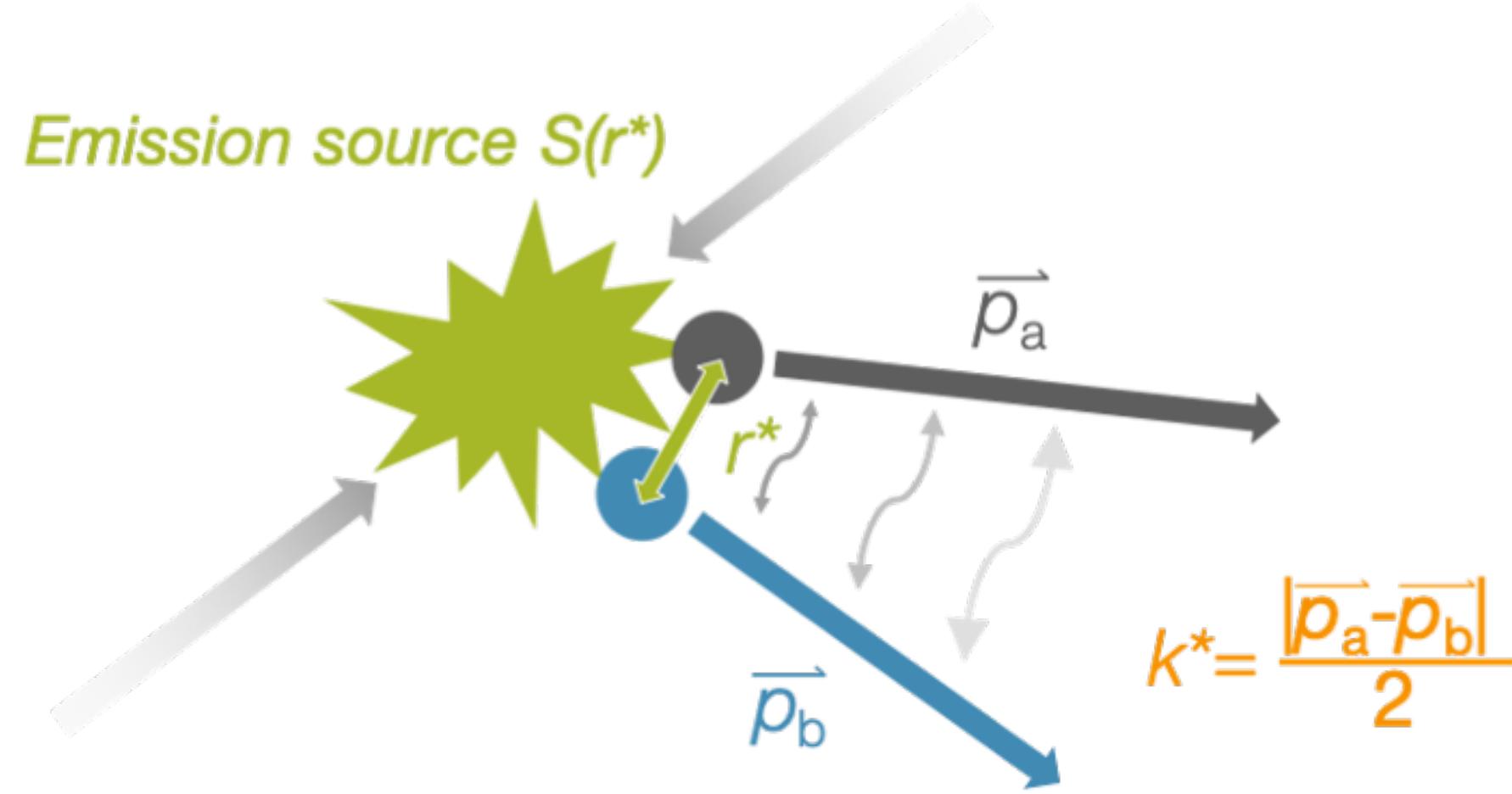
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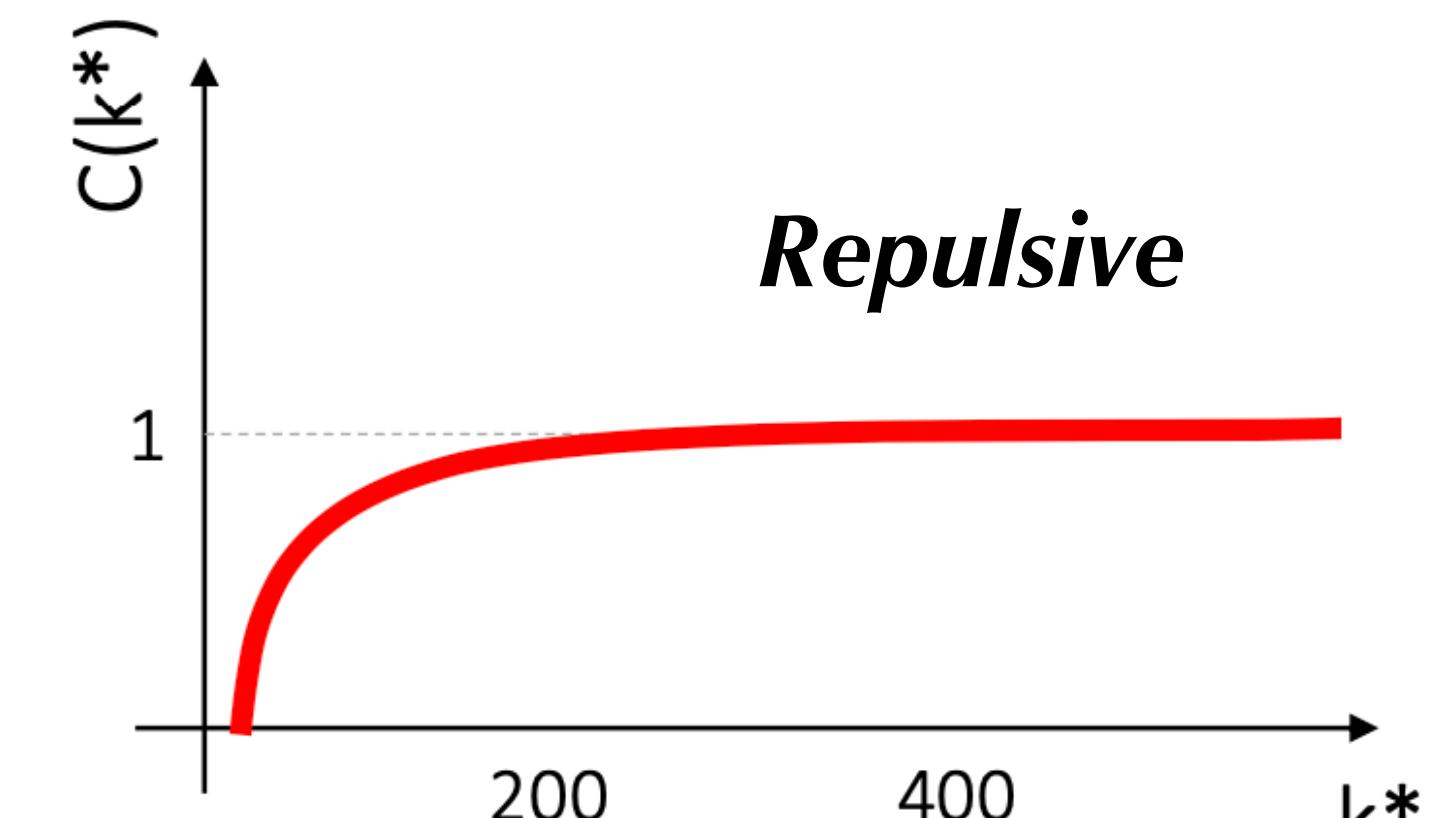
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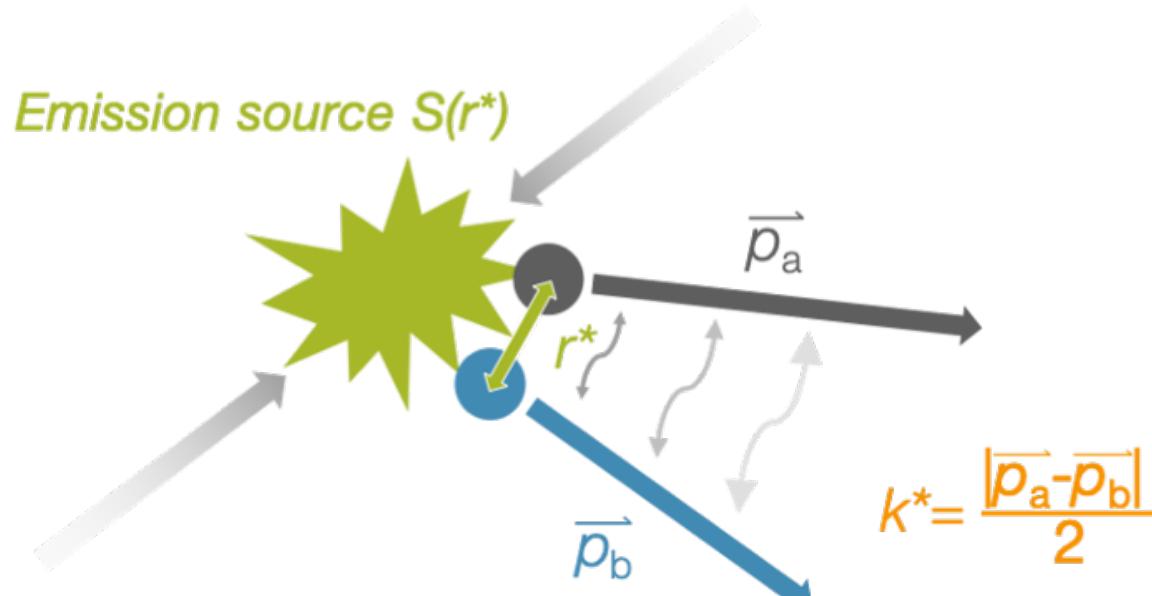
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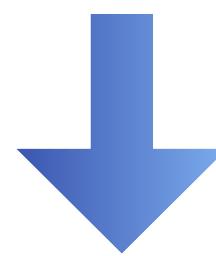
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Femtoscopy — Lednicky-Lyuboshitz approach



<u>Model</u>	<u>Experimental</u>
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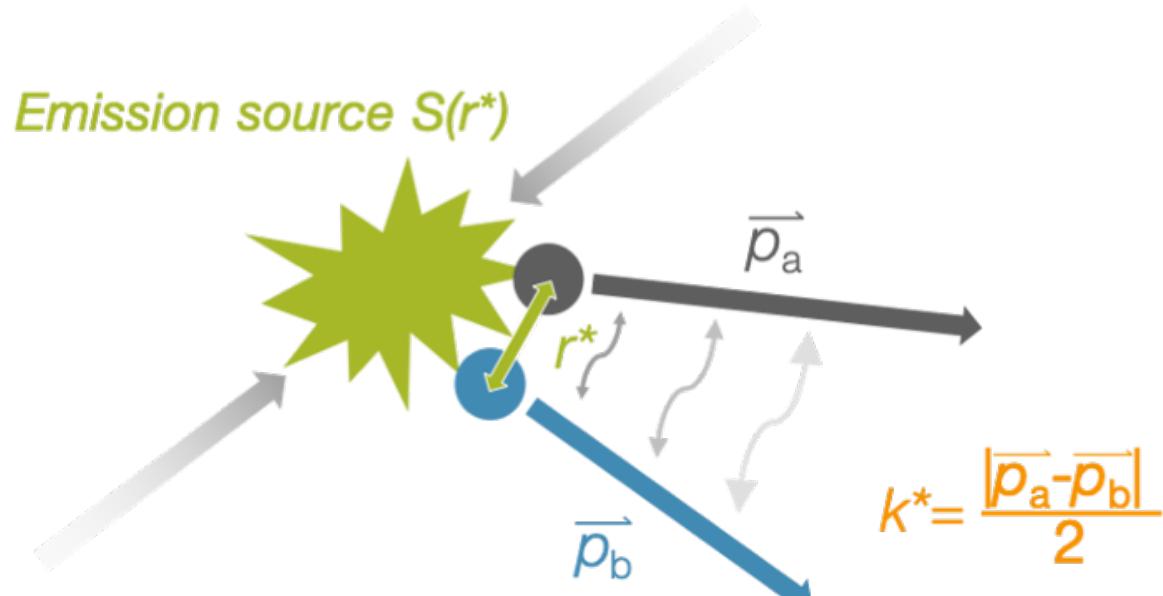


⇒ Formalism with Lednicky-Lyuboshitz (L-L) approach

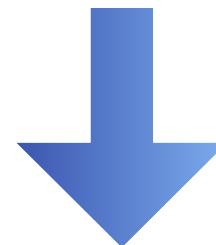
- Only consider s-wave
- Smoothness approximation for source function
- Static and spherical Gaussian source assumed
- Effective range expansion for $\Psi(r^*, k^*)$

R. Lednicky, et al, Sov.J.Nucl.Phys. 35 (1982) 770

Femtoscopy — Lednicky-Lyuboshitz approach

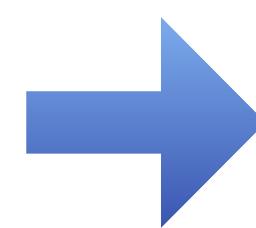


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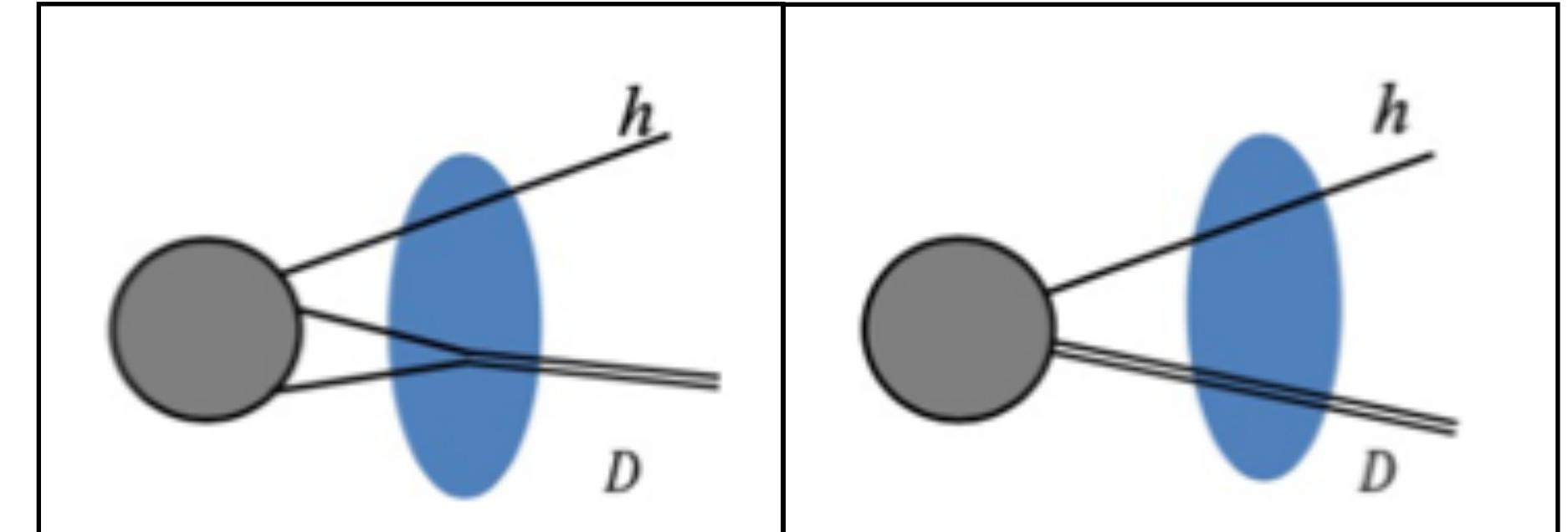
Physics quantity:

1. R_G : Spherical Gaussian source size
2. f_0 : Scattering length
3. d_0 : Effective range

R. Lednicky, et al, Sov.J.Nucl.Phys. 35 (1982) 770

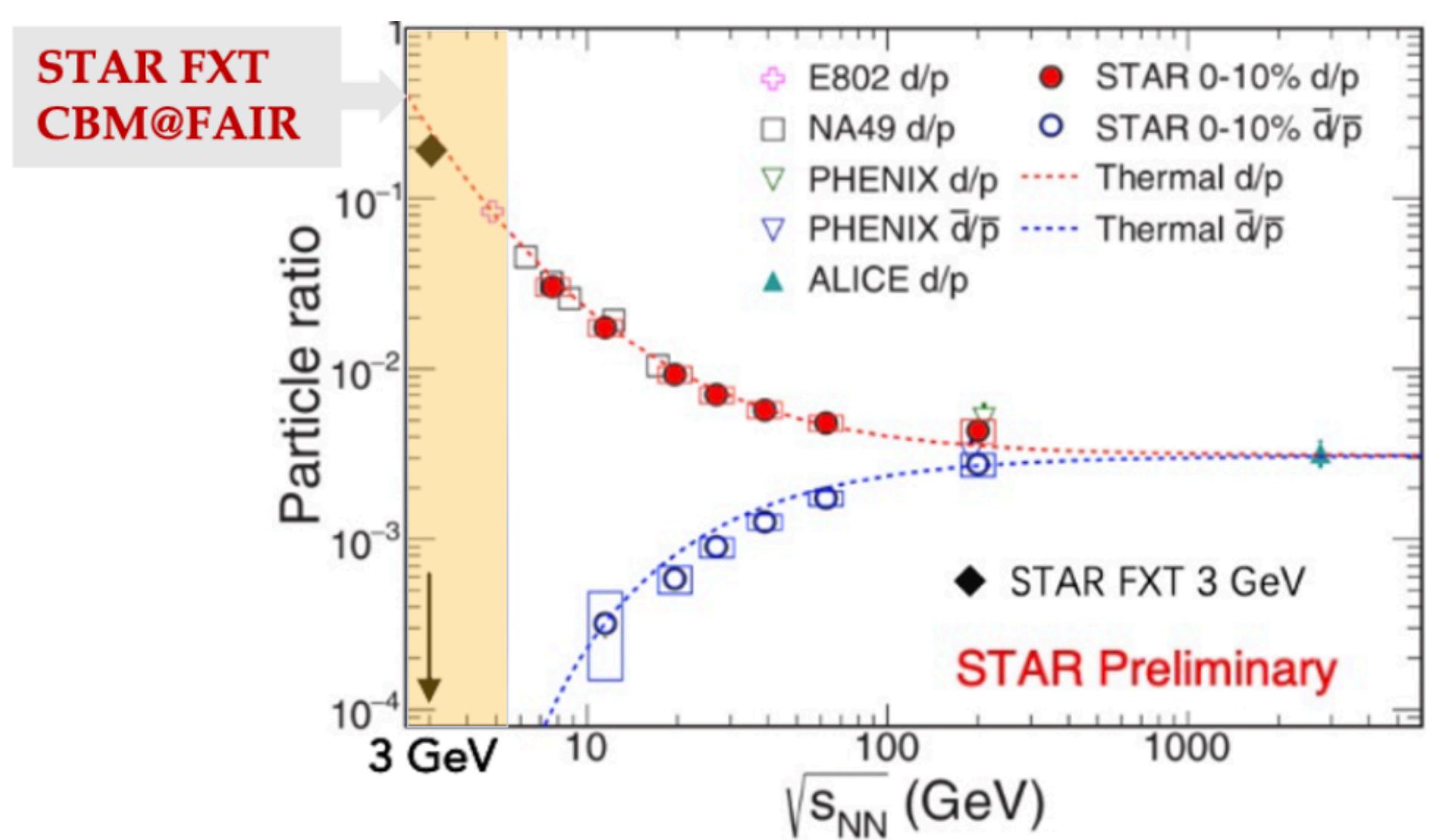
Motivation

- Formation mechanism of light nuclei are under debate
 - ⇒ Coalescence : final-state interaction
 - ⇒ Thermal : produced directly from fireball
- Indirect approach of three-body and four-body interactions



Coalescence

Direct production



J.Cleymans et al, Phys.Rev.C 74, 034903 (2006)

K. Blum et al, Phys.Rev.C 99, 04491 (2019)

St. Mrówczyński and P. Słoń, Acta Physica Polonica B 51, 1739 (2020)

St. Mrówczyński and P. Słoń, Physical Review C 104, 024909 (2021)

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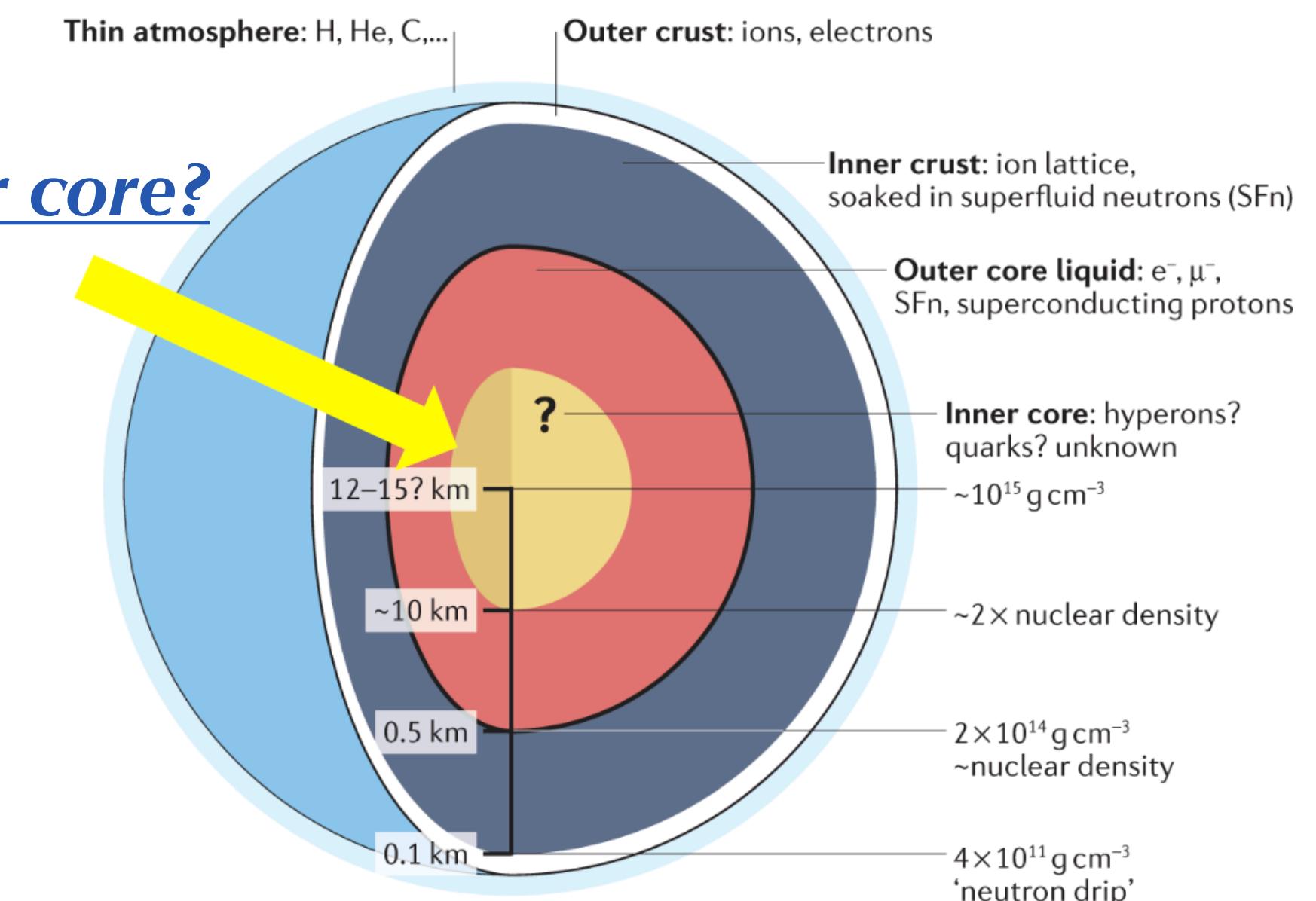
- Indirect approach of three-body and four-body interactions

- Role of Nucleon-Nucleon (N-N) and Hyperon-Nucleon (Y-N)

interactions in the Equation-of-State

⇒ Inner structures of neutron star

⇒ Light nuclei + hyperon: provide the insights to hypernuclei
structure and properties



Phys.Rev.C 99, 064905 (2019)

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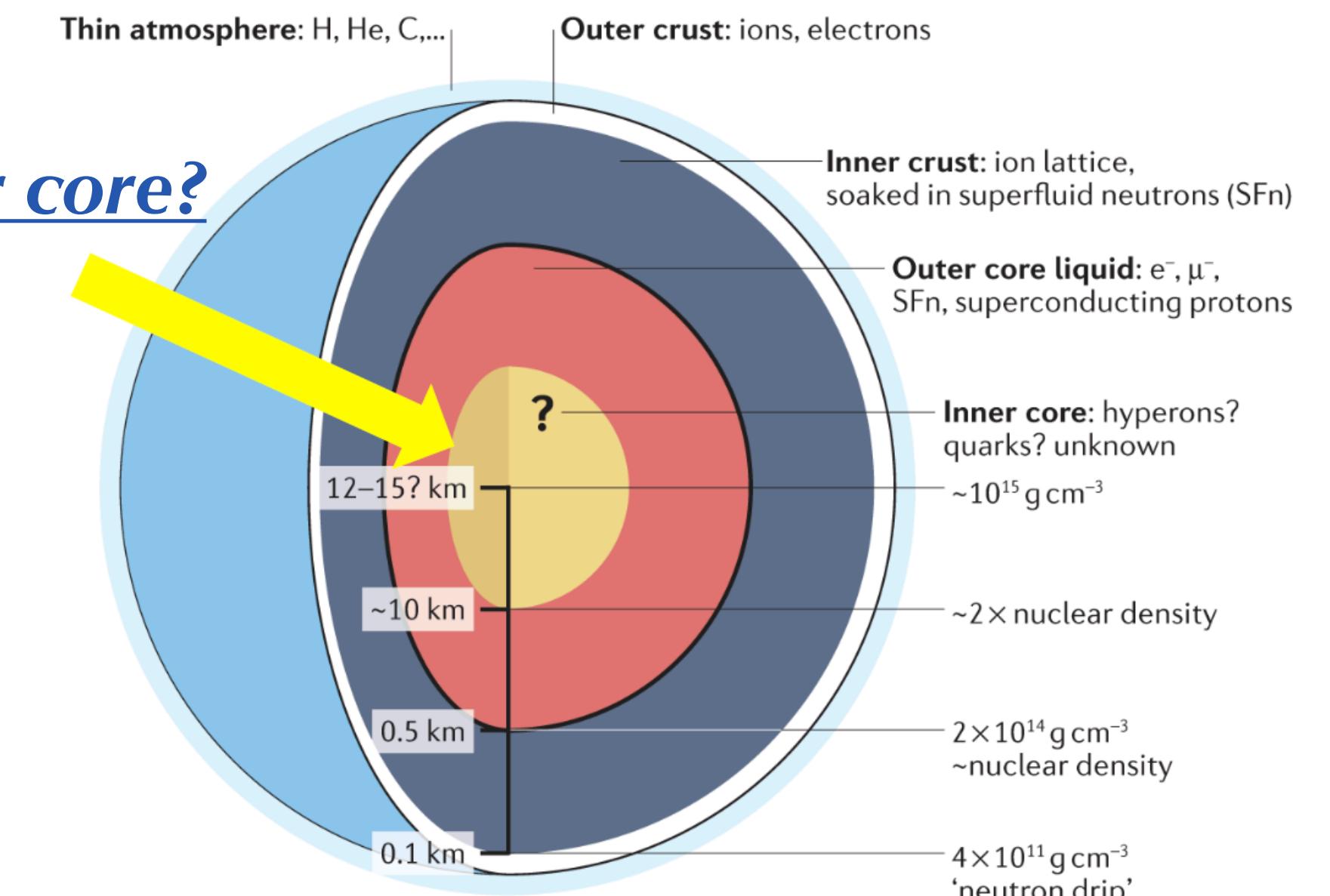
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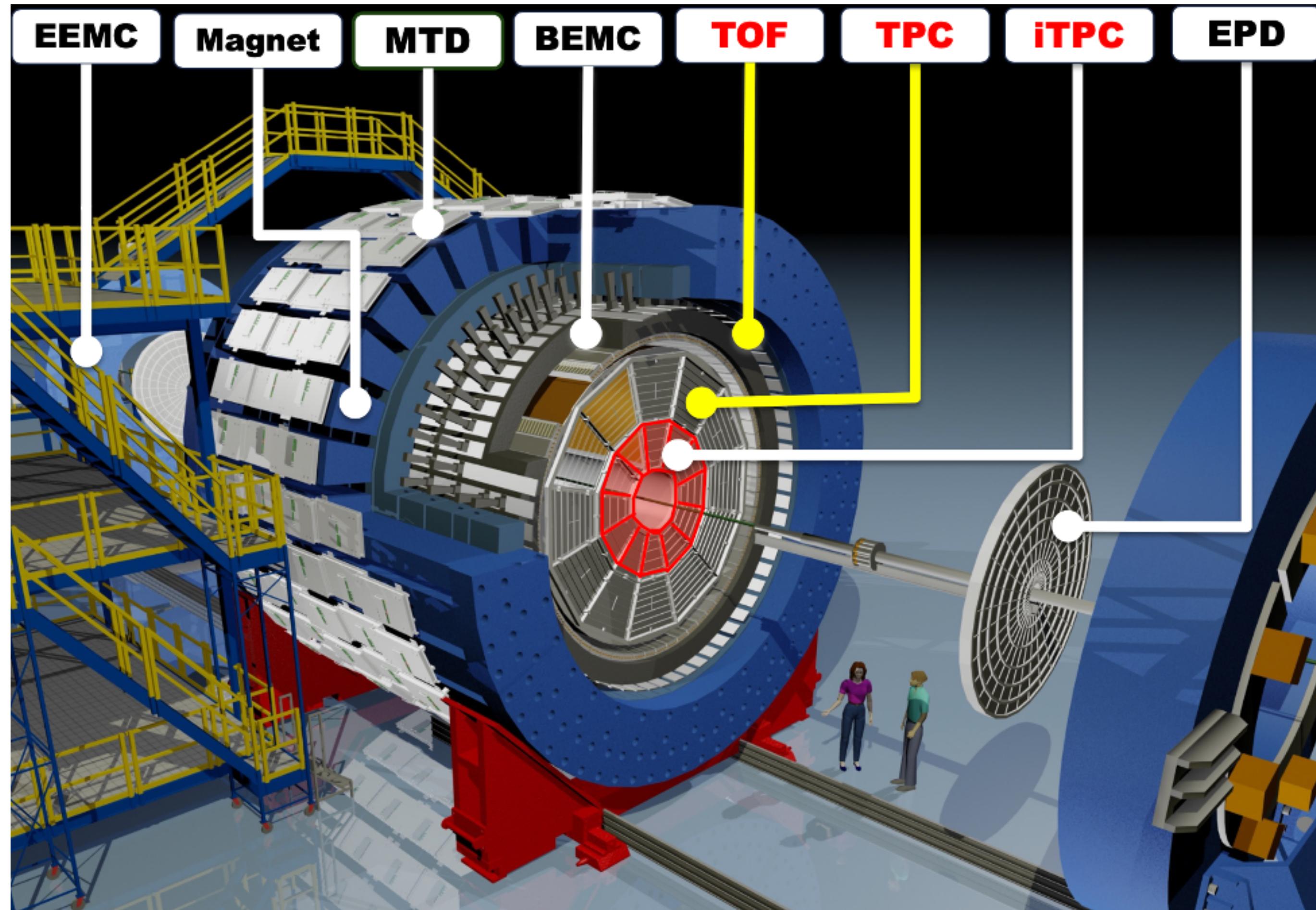
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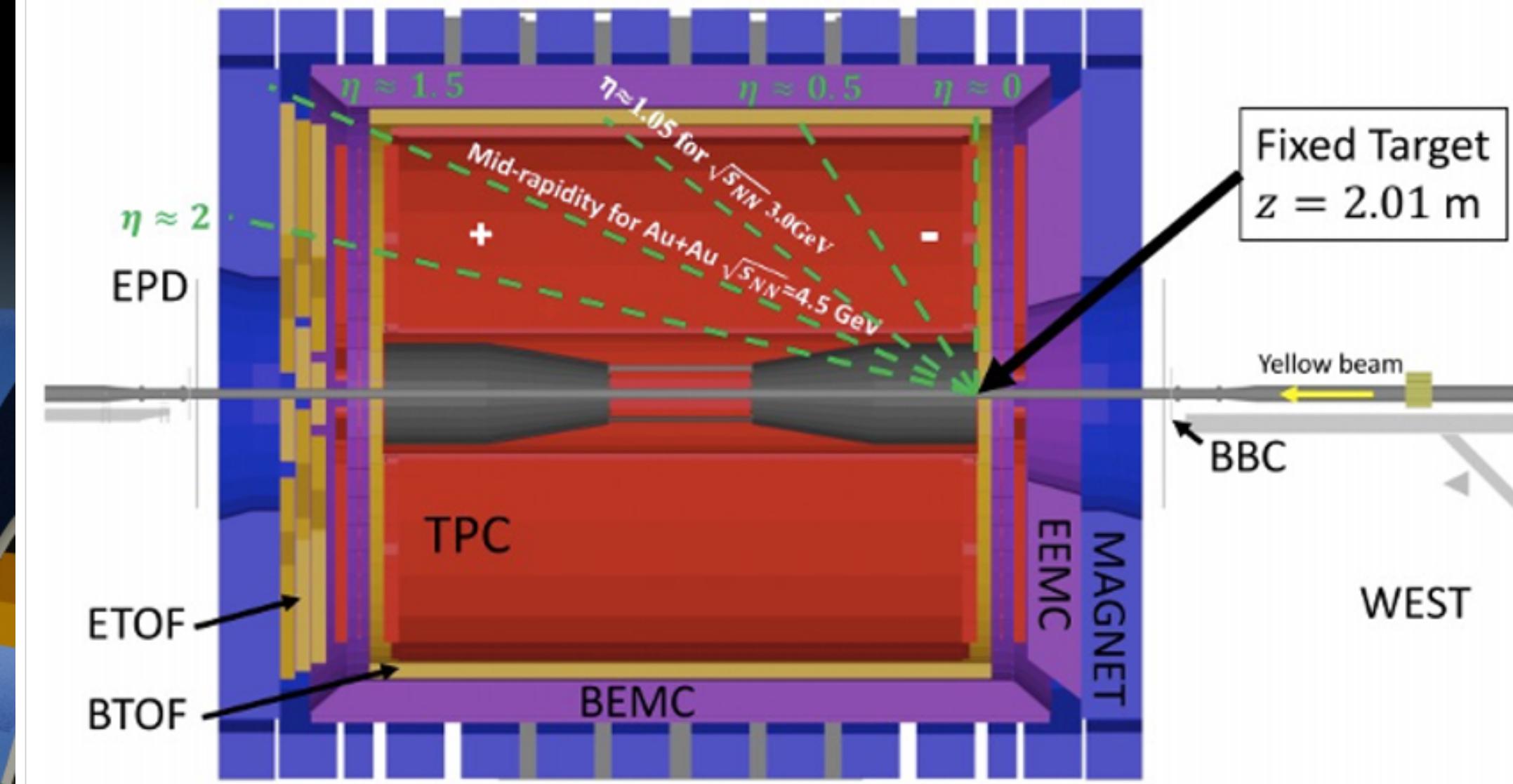
In this talk:
p-d, d-d, d-Λ correlation @ 3 GeV

Phys.Rev.C 99, 064905 (2019)

STAR Detector & Datasets



- ⇒ Excellent particle identification
- ⇒ Large, uniform acceptance at mid-rapidity

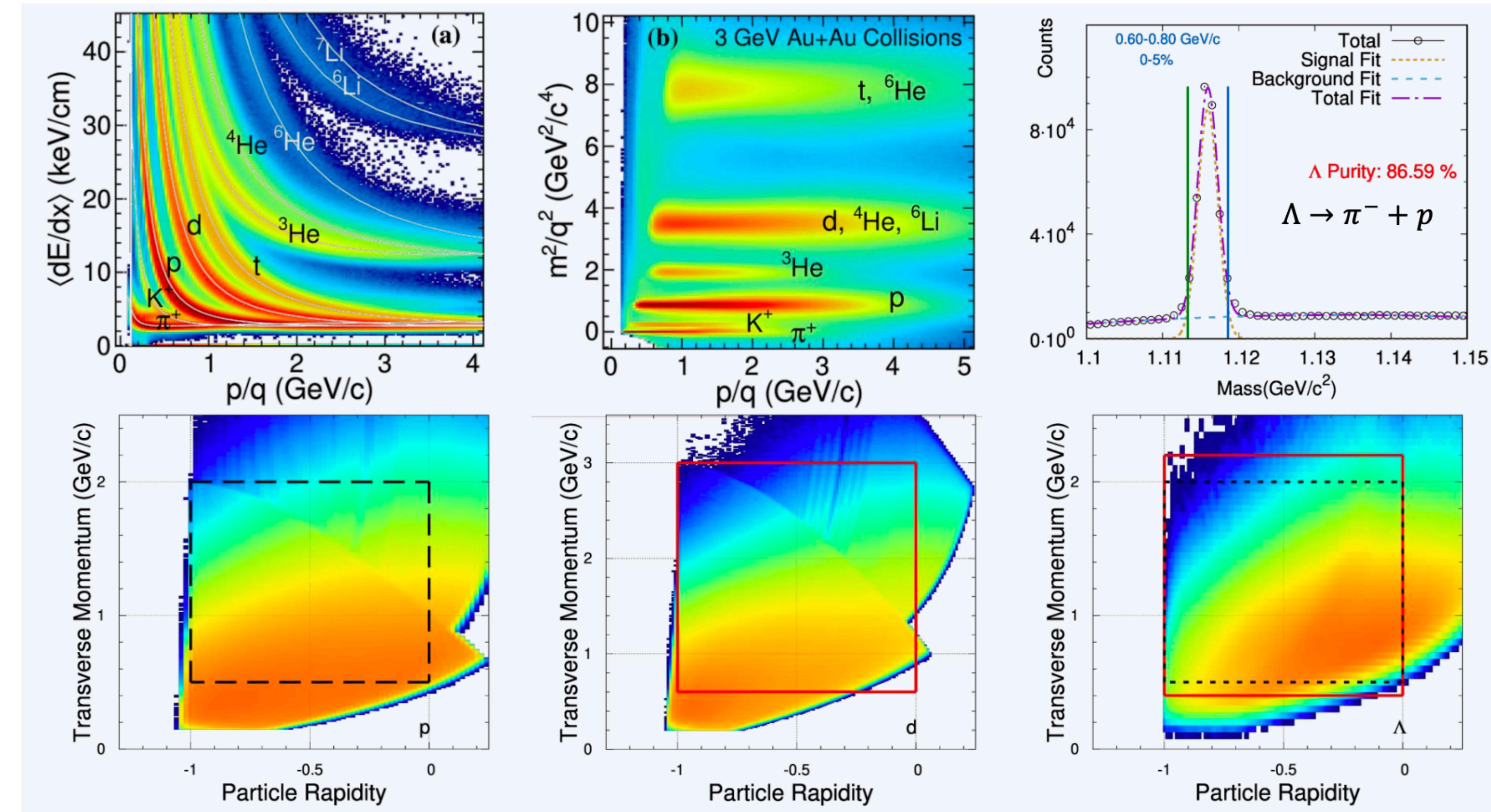


⇒ 3 GeV Au+Au collisions @ 2018

$$\rightarrow \mu_B \sim 720 \text{ MeV}$$

⇒ 0-60% centrality

Particle Identification & Reconstruction

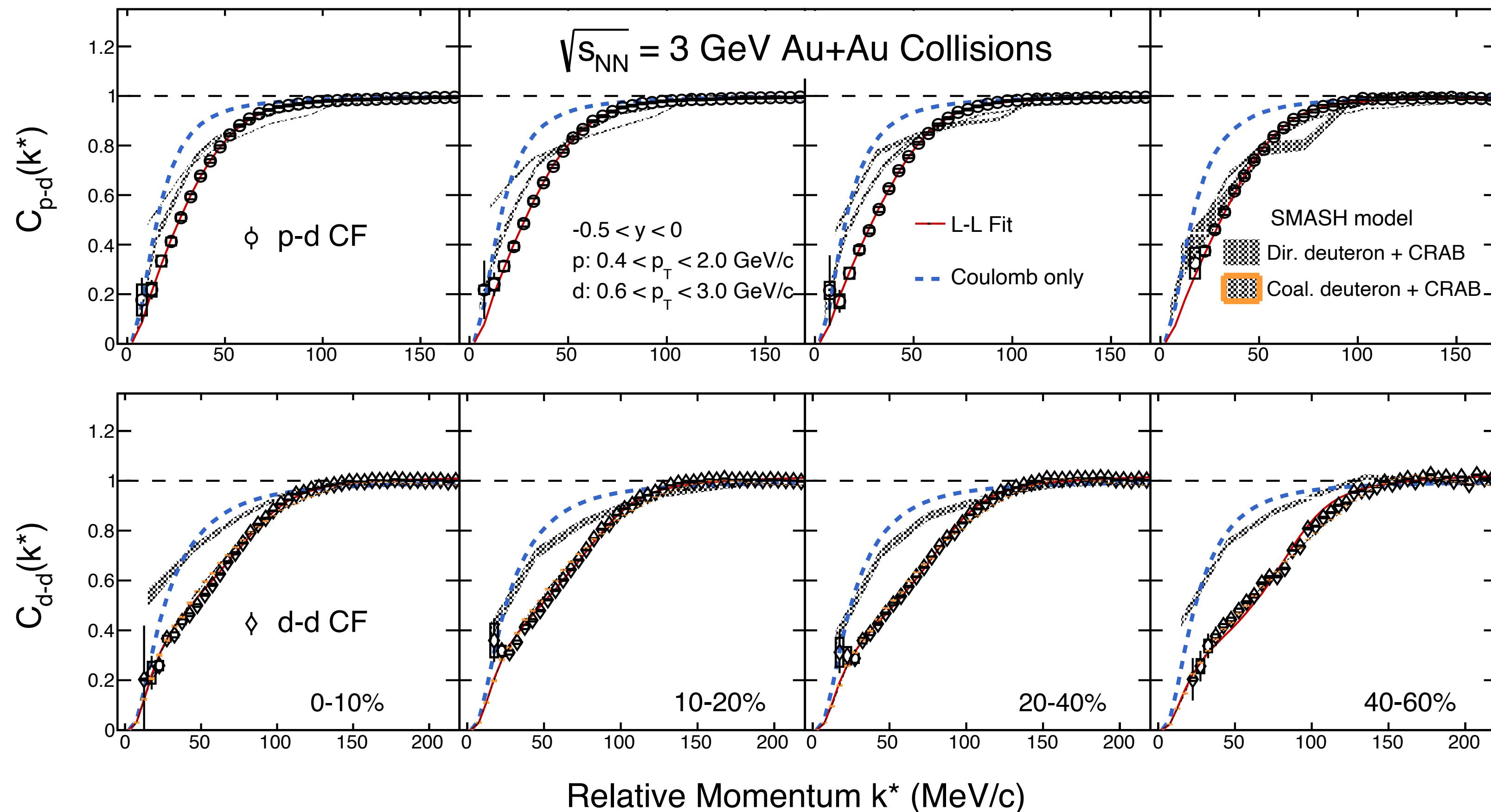


$\Rightarrow \pi^-$, p and d are identified by Time Projection Chamber (TPC) and Time-Of-Flight (TOF)

\Rightarrow Reconstruct Λ candidates with KFParticle package -> Improve significance

Phys. Lett. B 827 (2022) 136941

Results — p-d, d-d Correlation



⇒ First measurements of p-d/d-d correlation functions in HIC

⇒ Clear depletion in low k^*

- Coulomb repulsive & strong interaction

⇒ Fitted with L-L model simultaneously, assuming in different centrality:

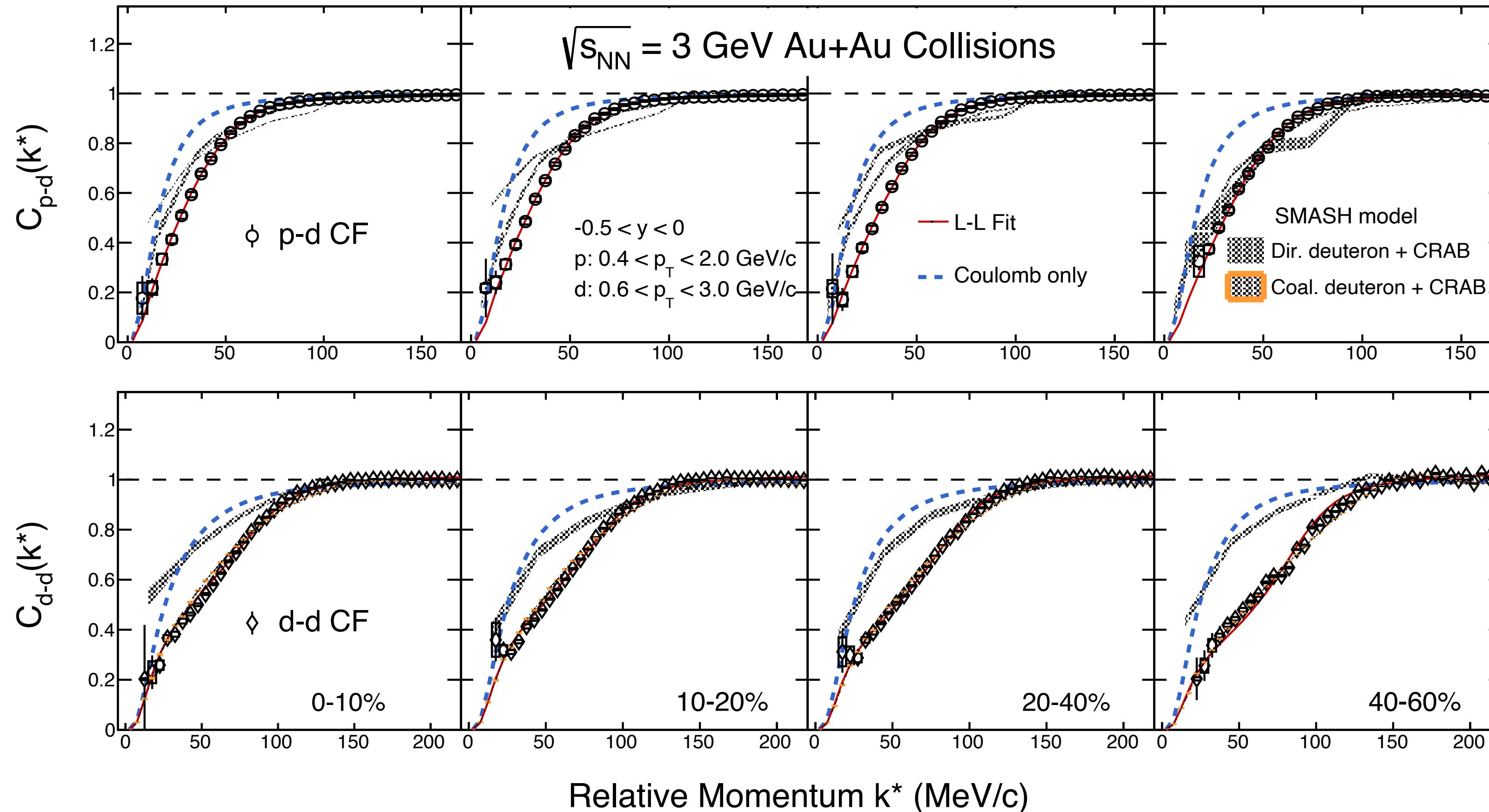
- Different R_G
- Common f_0 and d_0

STAR: arXiv:2410.03436v1

SMASH: J. Weil et al. Phys. Rev. C 94 (2016) 5, 054905

Coalescence: W.Zhao et al. Phys. Rev. C 98 (2018) 5, 054905

Results — p-d, d-d Correlation



⇒ Simulated with SMASH model, consider two deuteron formation mechanism:

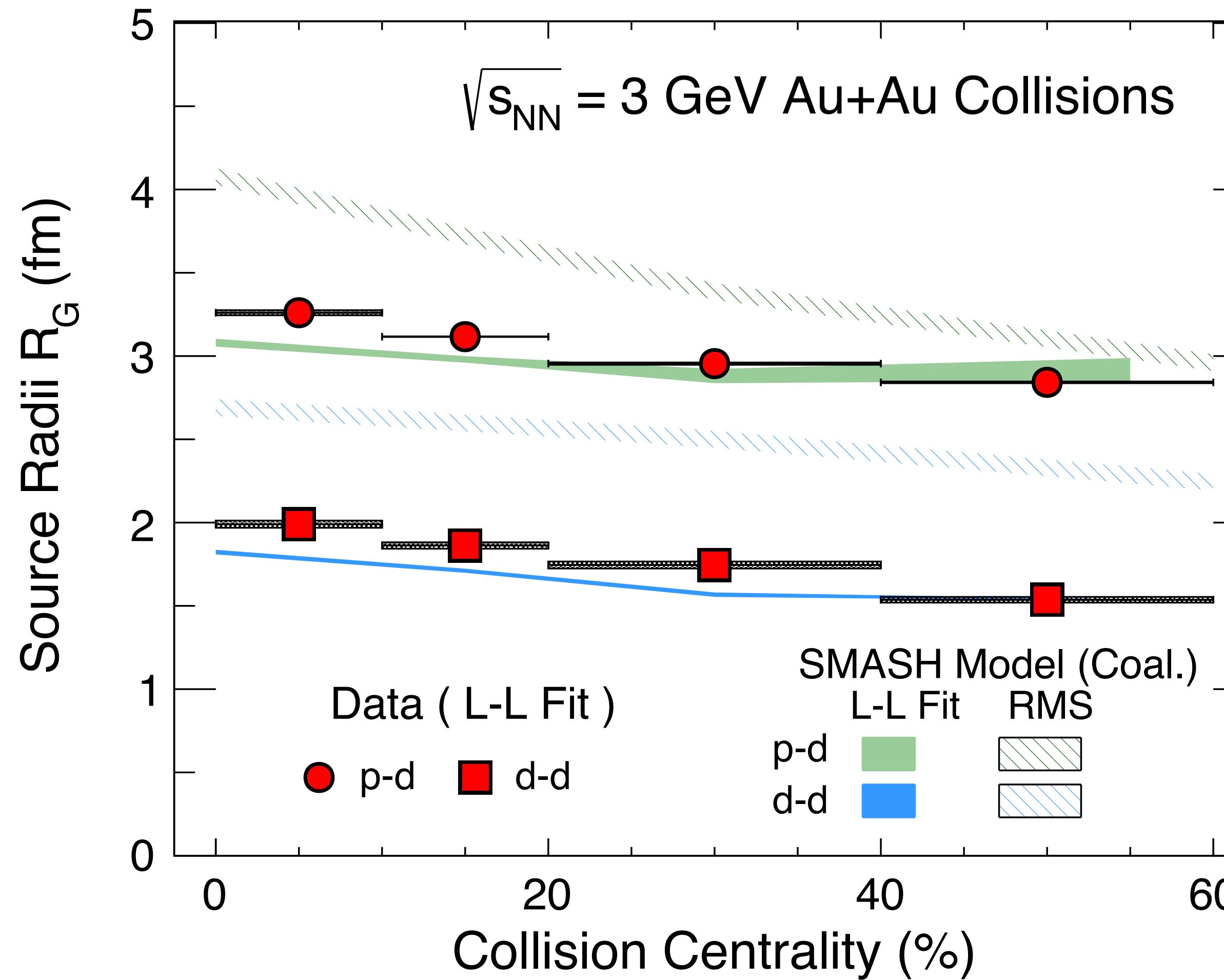
- Direct production
 - Hadronic scattering
 - Fail to describe data at certain k^*
- Coalescence production
 - Wigner function
 - Well description to data
 - Coalescence is the dominant process for deuteron formation in the high-energy nuclear collisions

STAR: arXiv:2410.03436v1

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Results — p-d, d-d Correlation



⇒ Extracted source size (R_G) with LL model

- Centrality dependence: $R_G^{\text{central}} > R_G^{\text{peripheral}}$
- $\langle m_T \rangle$ dependence: $R_G^{\text{p-d}} > R_G^{\text{d-d}}$

⇒ Using same fit, source size from SMASH (R_G^{SMASH})

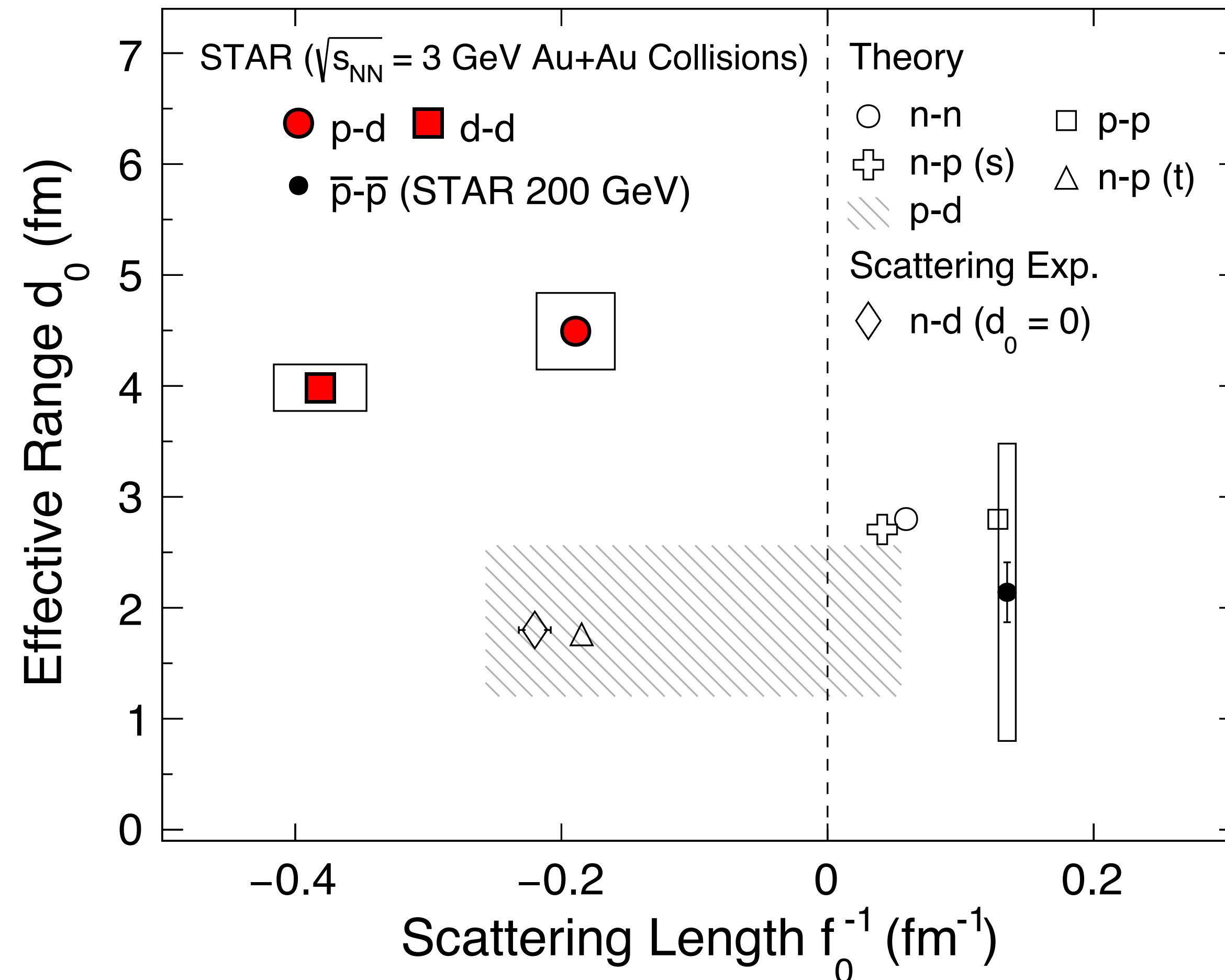
is closely match the data

⇒ The root mean square (RMS) values from SMASH

are larger than R_G

- Dynamical expansion of the system

Results — p-d, d-d Interaction



⇒ Extracted spin-averaged final state interaction

parameters (f_0 , d_0) with LL model

⇒ For both p-d and d-d interaction, the spin-averaged f_0 is negative

- Combination of repulsive interactions in quartet (quintet) spin state for p-d (d-d) along with the presence of bound states (${}^3\text{He}$ for p-d and ${}^4\text{He}$ for d-d)

⇒ For p-d interaction, the result is consistent with theory calculation and low-energy scattering experiment measurement

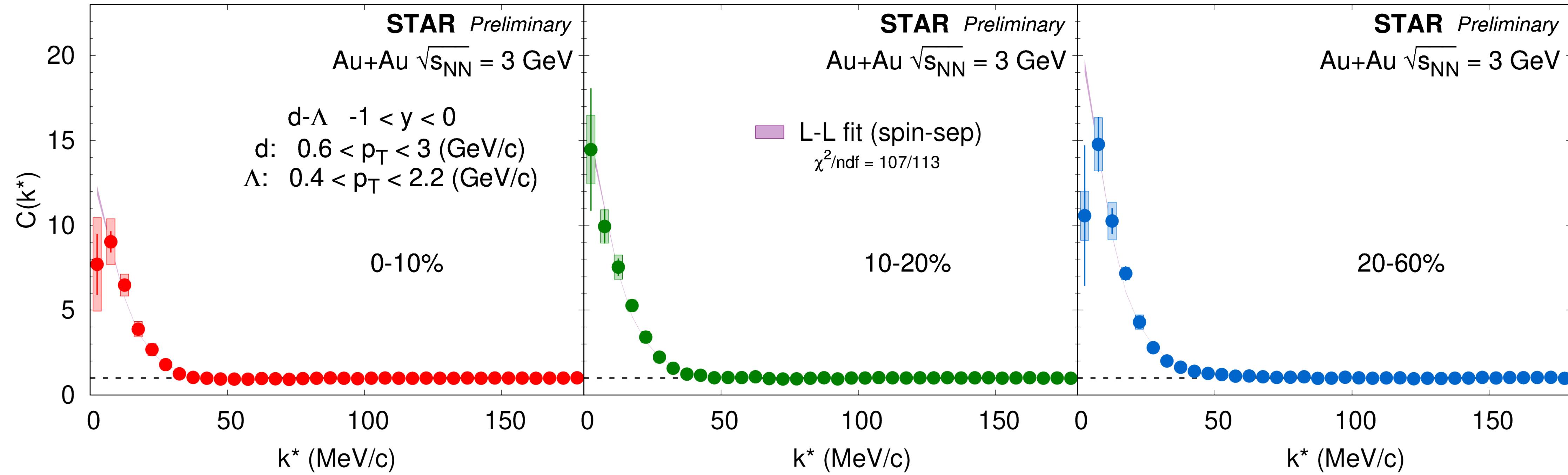
- Support the feasibility of extracting interaction parameters with Femtoscopy technique

STAR: arXiv:2410.03436v1

Results — d- Λ Correlation



First measurement of d- Λ CF at STAR



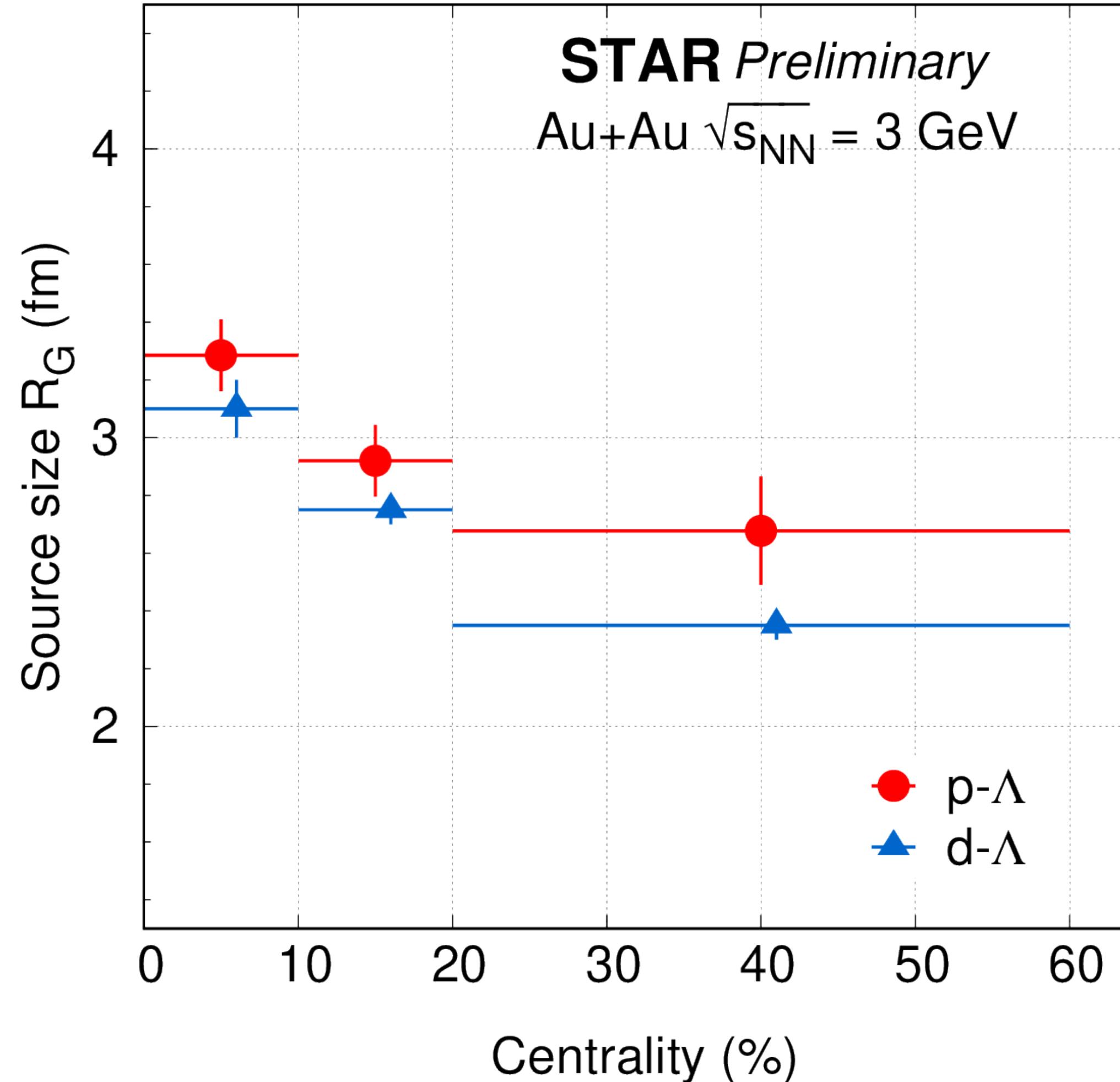
⇒ Strong enhancements at small k^* range -> Attractive interactions

⇒ Simultaneously fit to data in different centralities with L-L approach

- Consider two-spin components: D (doublet, $S = 1/2$), Q (quartet, $S=3/2$)

* Λ feed-down correction not applied

Results — d- Λ Correlation



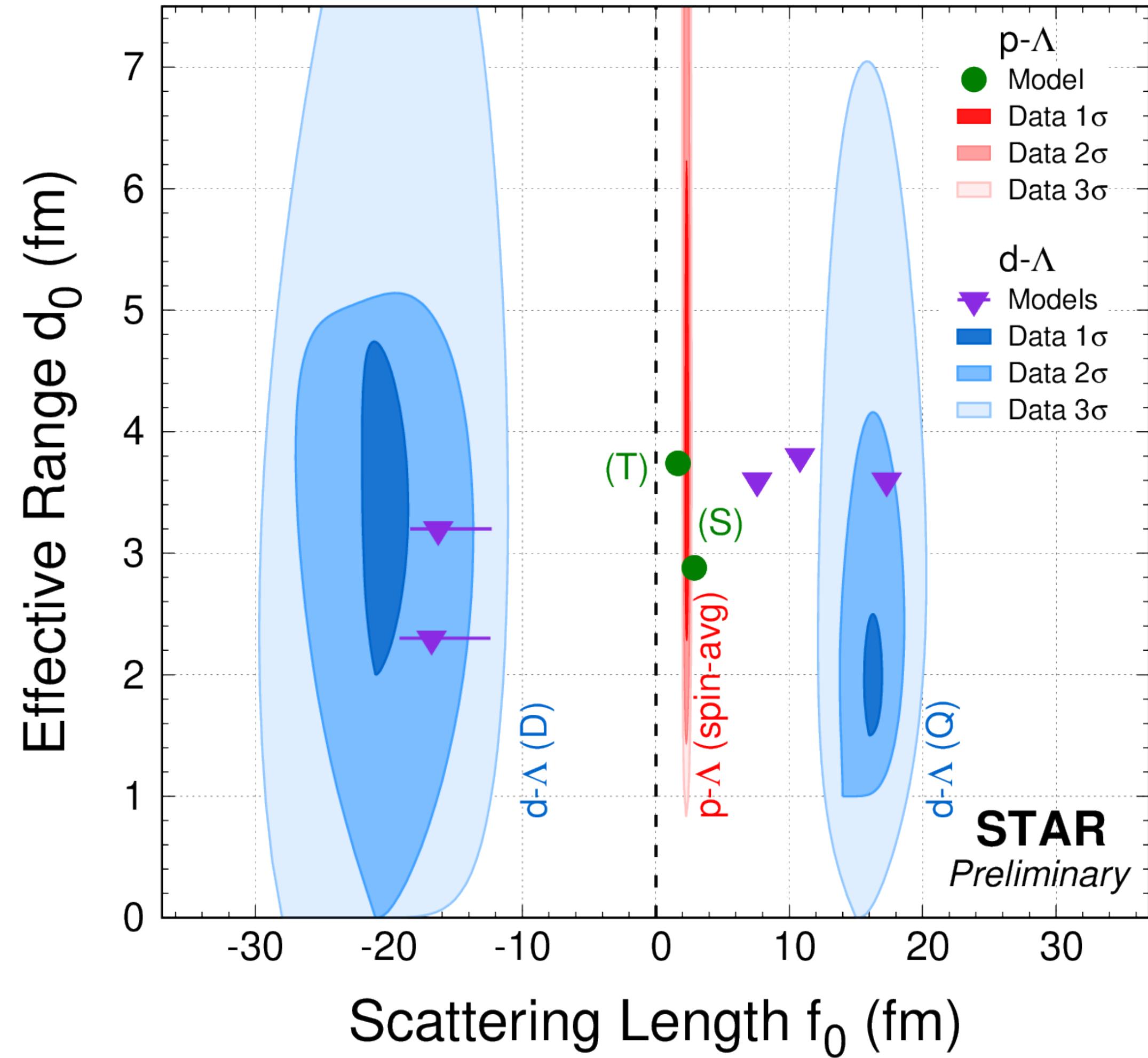
⇒ Collision dynamics as expected

- Centrality dependence: $R_G^{\text{central}} > R_G^{\text{peripheral}}$
- $\langle m_T \rangle$ dependence: $R_G(p - \Lambda) > R_G(d - \Lambda)$

$p - \Lambda$ correlation at 3 GeV: [backup](#)

EPJ Web Conf. 296 (2024) 14010

Results — d- Λ Interaction



$p - \Lambda$ correlation at 3 GeV: [backup](#)

⇒ First experimental extraction of strong interaction parameters of $d - \Lambda$

⇒ Successfully separate two spin components in $d - \Lambda$

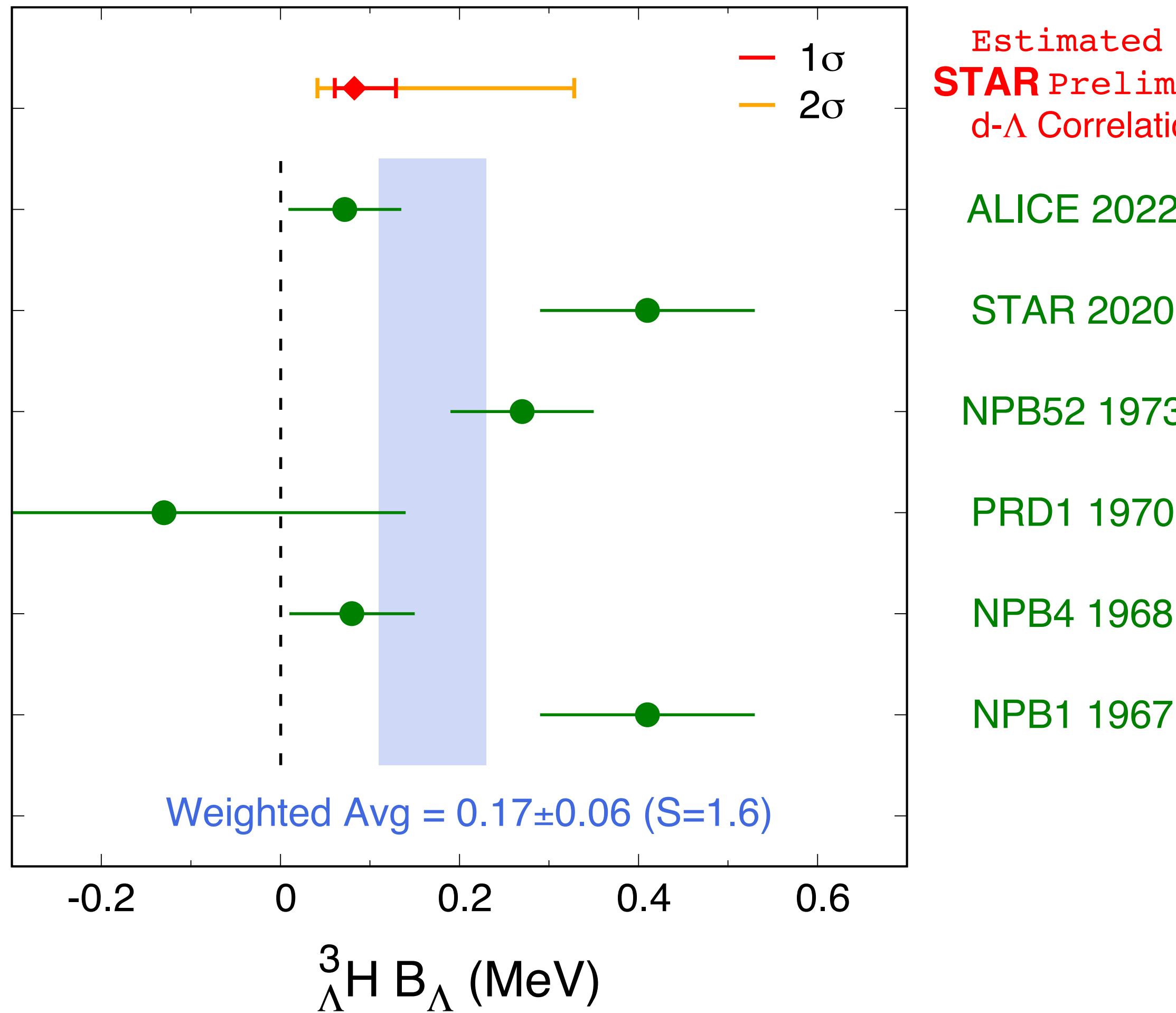
$$f_0(D) = -20^{+3}_{-3} \text{ fm}, \quad d_0(D) = 3^{+2}_{-1} \text{ fm}$$

$$f_0(Q) = 16^{+2}_{-1} \text{ fm}, \quad d_0(Q) = 2^{+1}_{-1} \text{ fm}$$

- Negative f_0 in doublet state $\rightarrow {}^3_\Lambda\text{H}$ bound state
- Positive f_0 in quartet state \rightarrow Attractive interaction

- EPJ Web Conf. 296 (2024) 14010*
H. W. Hammer, Nucl. Phys. A 805 (2002) 173
Cobis, et al. J. Phys. G 23 (1997) 401
J. Haidenbauer, Phys. Rev. C 102 (2020) 3, 034001
F. Wang, et al, Phys. Rev. Lett. 83 (1999) 3138
M. Schafer, et al, Phys. Lett. B 808 (2020) 135614
G. Alexander, et al. Phys. Rev. 173 (1968) 1452
J. Haidenbauer, et al. Nucl. Phys. A 915 (2013) 24

Results — ${}^3_{\Lambda}\text{H}$ Binding Energy



$p - \Lambda$ correlation at 3 GeV: [backup](#)

$\Rightarrow {}^3_{\Lambda}\text{H}$ binding energy (B_{Λ}):

Bethe formula from Effective Range Expansion (ERE)

$$B_{\Lambda} = \frac{\gamma^2}{2\mu_{d\Lambda}}$$

$$\frac{1}{-f_0} = \gamma - \frac{1}{2}d_0\gamma^2$$

$\mu_{d\Lambda}$: reduced mass

γ : binding momentum

$\Rightarrow {}^3_{\Lambda}\text{H } B_{\Lambda} = [0.04, 0.33] \text{ (MeV) @ 95% CL}$

-> Consistent with the world average

\Rightarrow Open a new way to constrain ${}^3_{\Lambda}\text{H}$ properties

EPJ Web Conf. 296 (2024) 14010
H.Bethe, Phys.Rev 76, 38 (1949)

Summary & Outlook



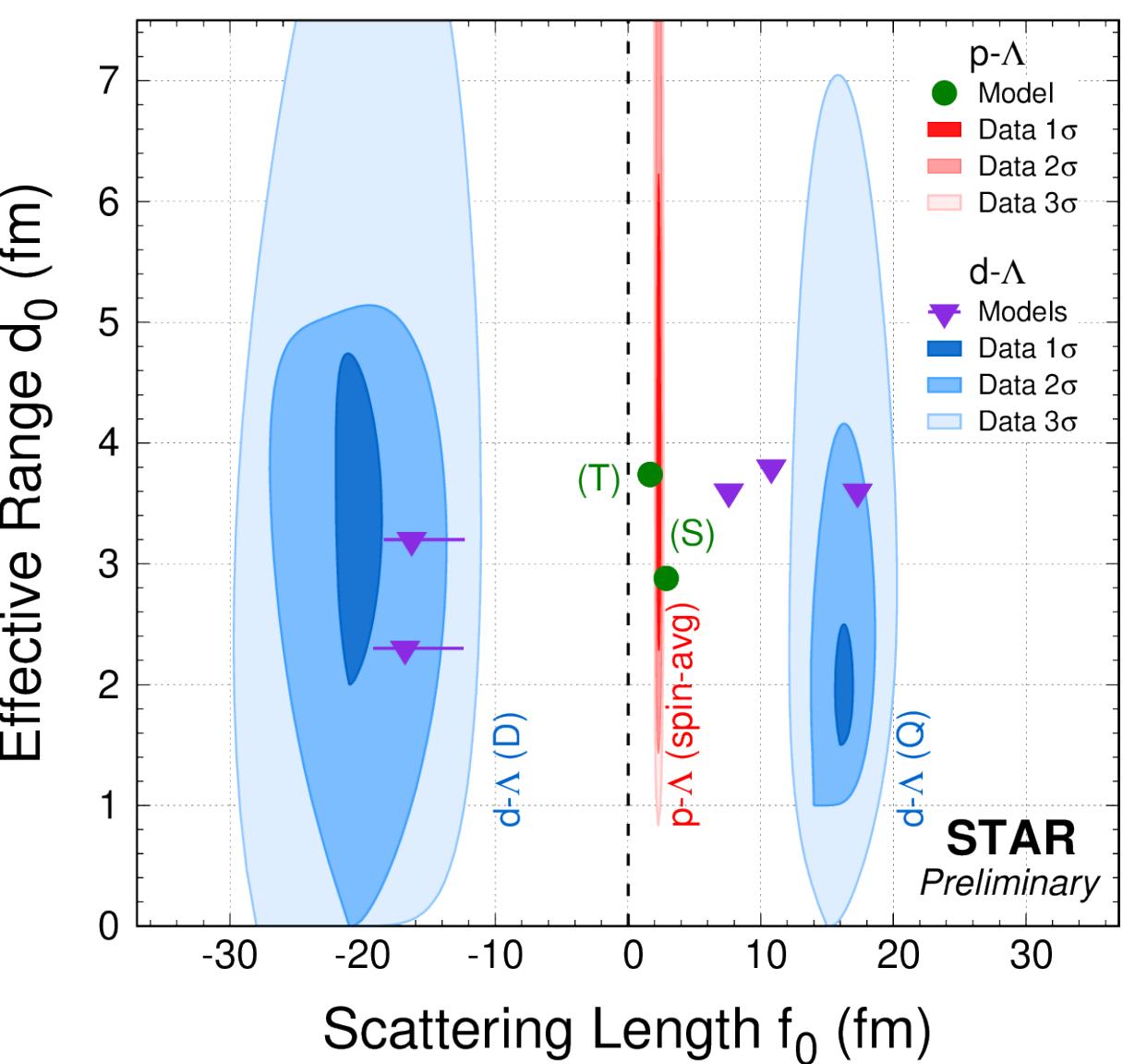
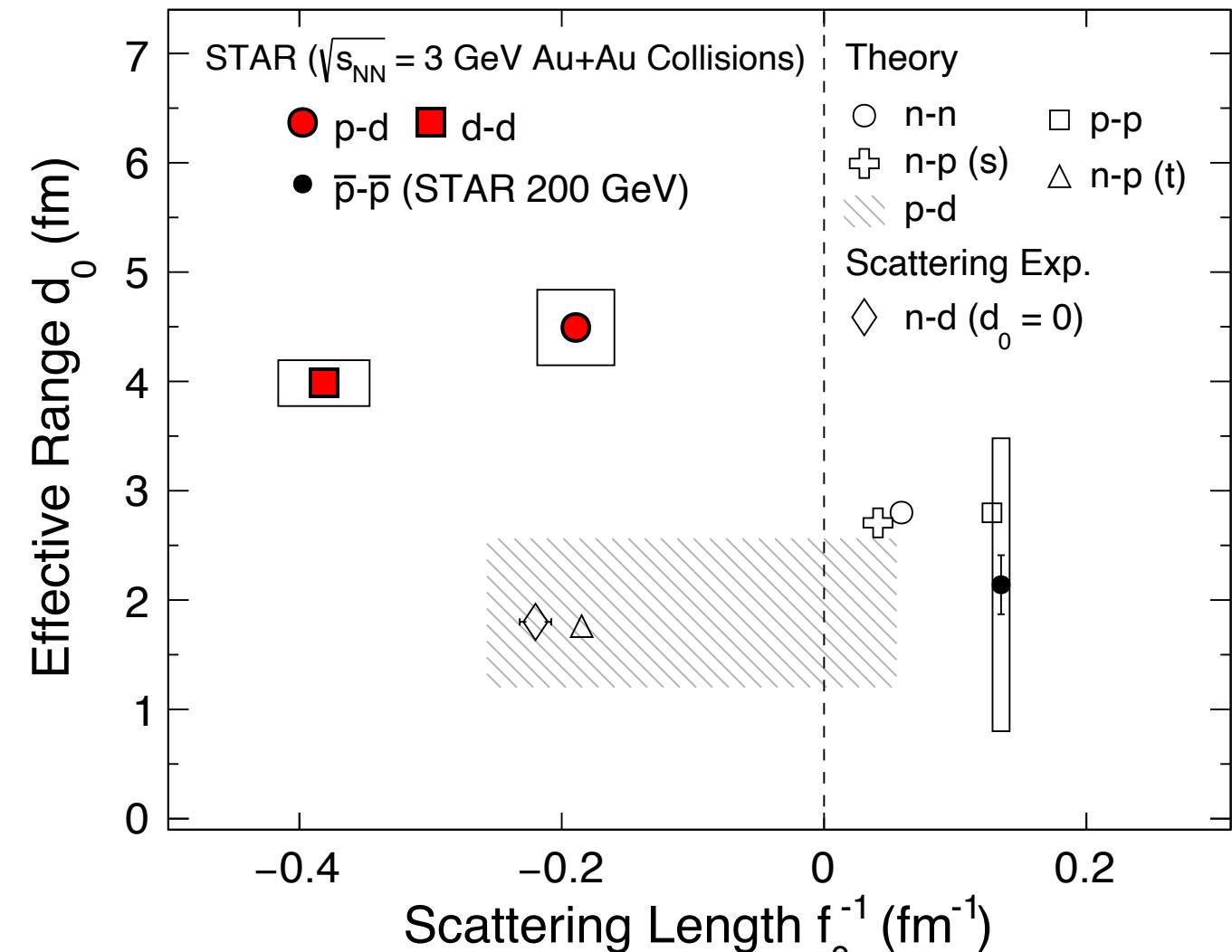
⇒ Femtoscopy measurements from heavy-ion collisions provides a unique tool to explore strong interactions and evolution dynamics

⇒ N-N interaction (p-d & d-d)

- First measurements of p-d / d-d correlation functions in STAR
- Coalescence is the dominant process for deuteron formation in the high-energy nuclear collisions
- f_0 is consistent with repulsive interaction and bound state formation in p-d / d-d pair

⇒ Y-N interaction (d- Λ)

- First experimental measurements of f_0 and d_0 in d- Λ pairs
- Provide a new way to explore hyper-nuclei properties



Summary & Outlook

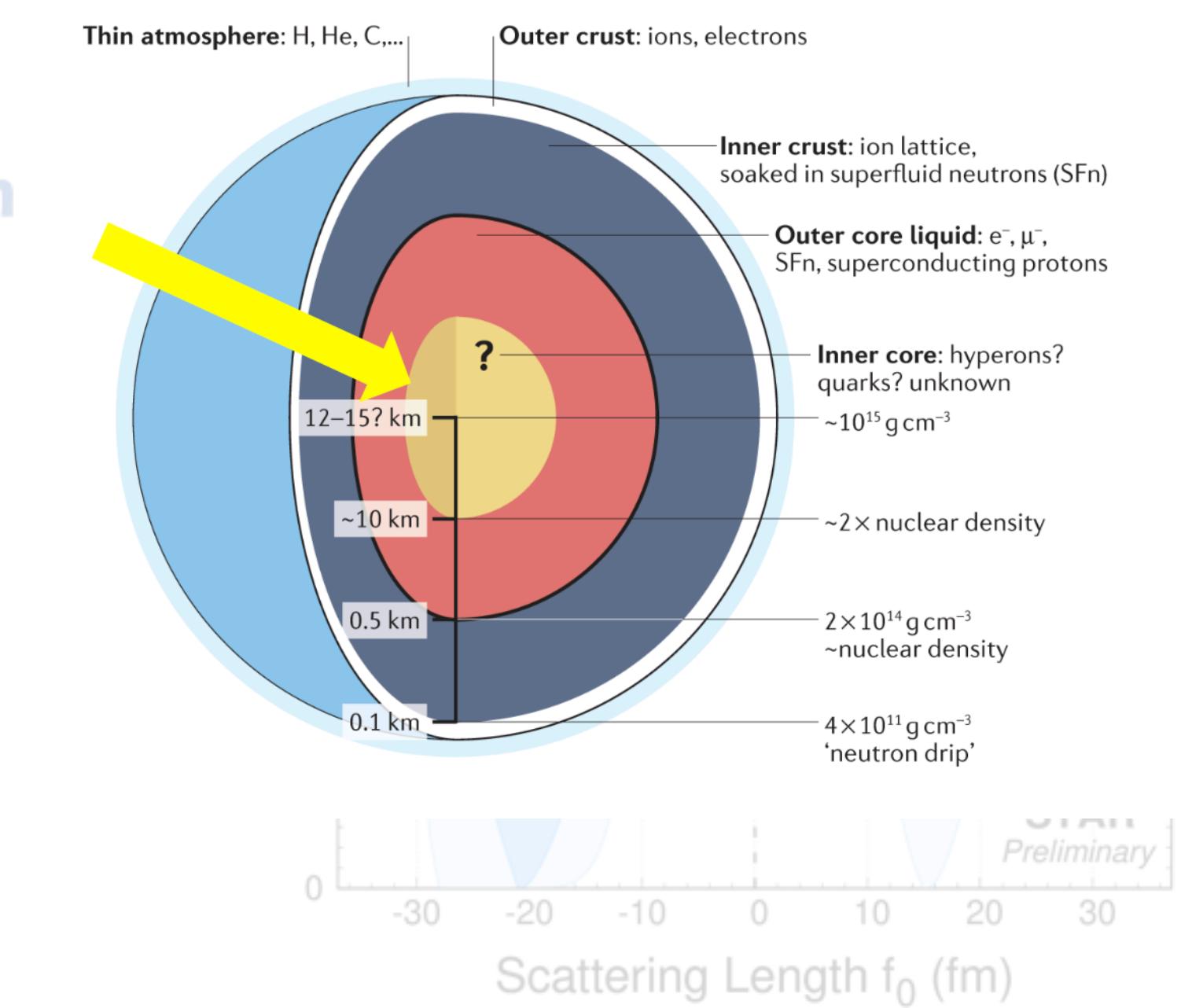
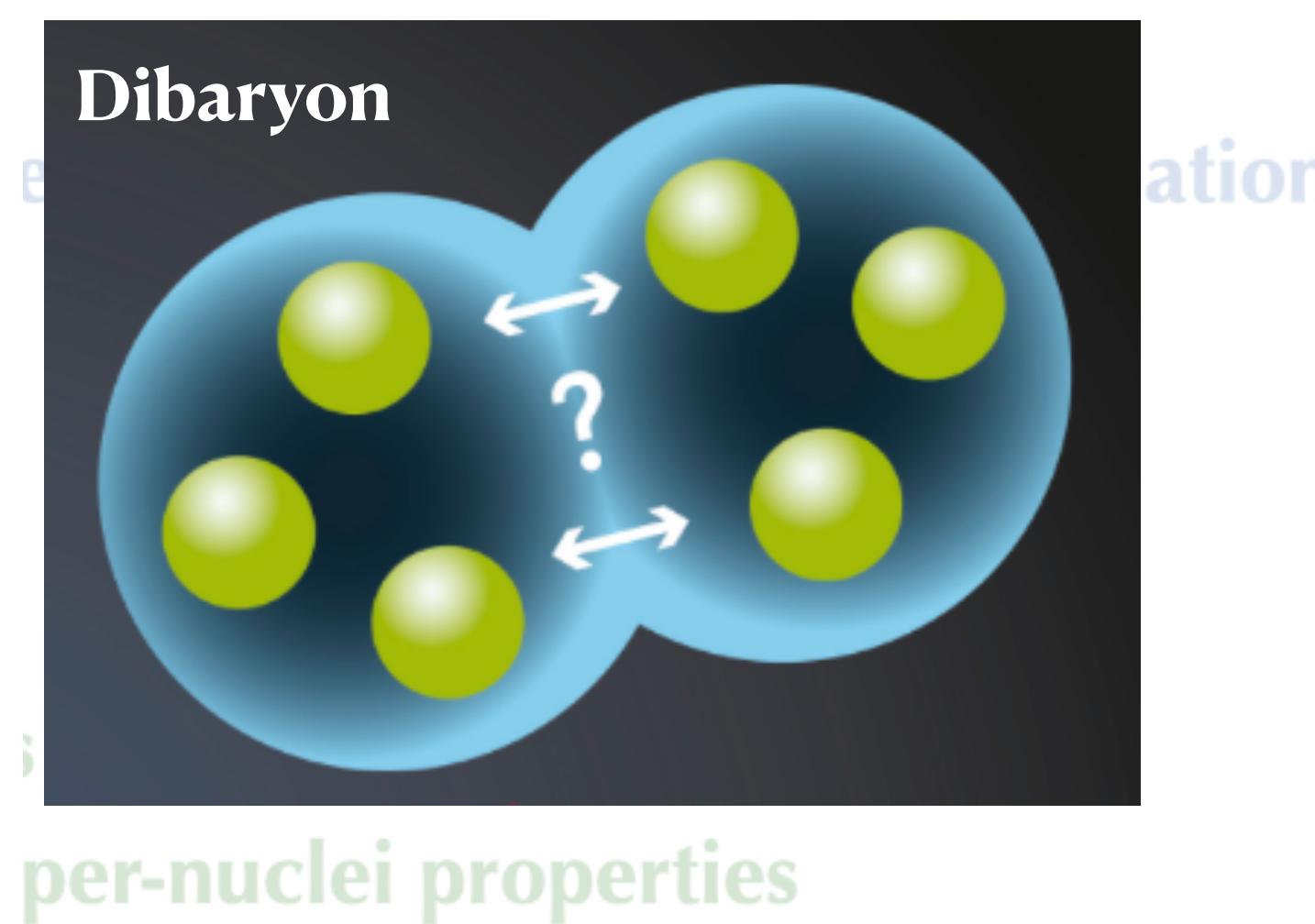
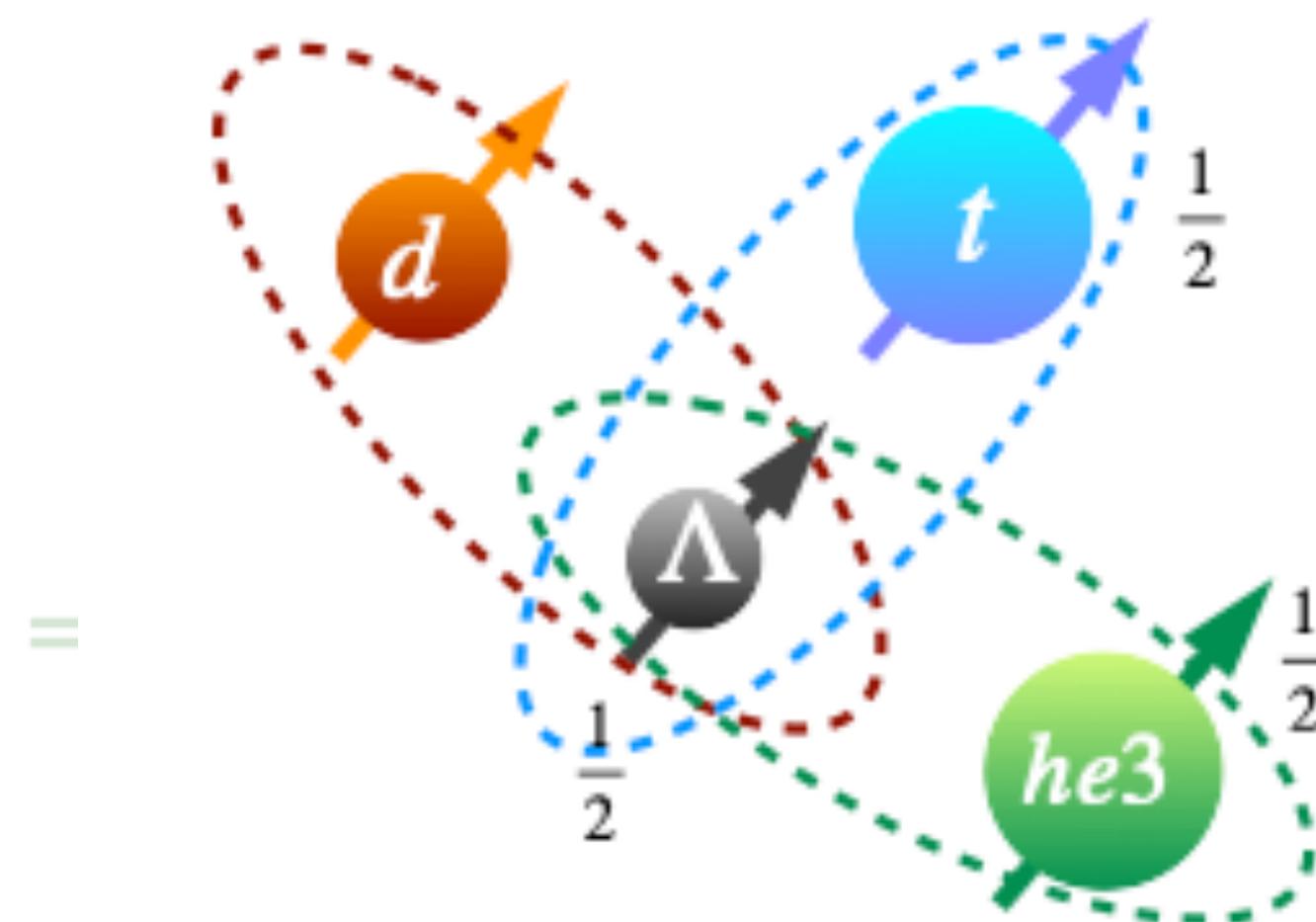


⇒ Femtoscopy measurements from heavy-ion collisions provides
a unique tool to explore strong interactions and evolution dynamics

More precise femtoscopy results with large statistics is coming soon!
(hypernuclei, many body, exotica ...)

First measurements of p-U and d-d correlation functions in STAR

cess for deuteron formation in the

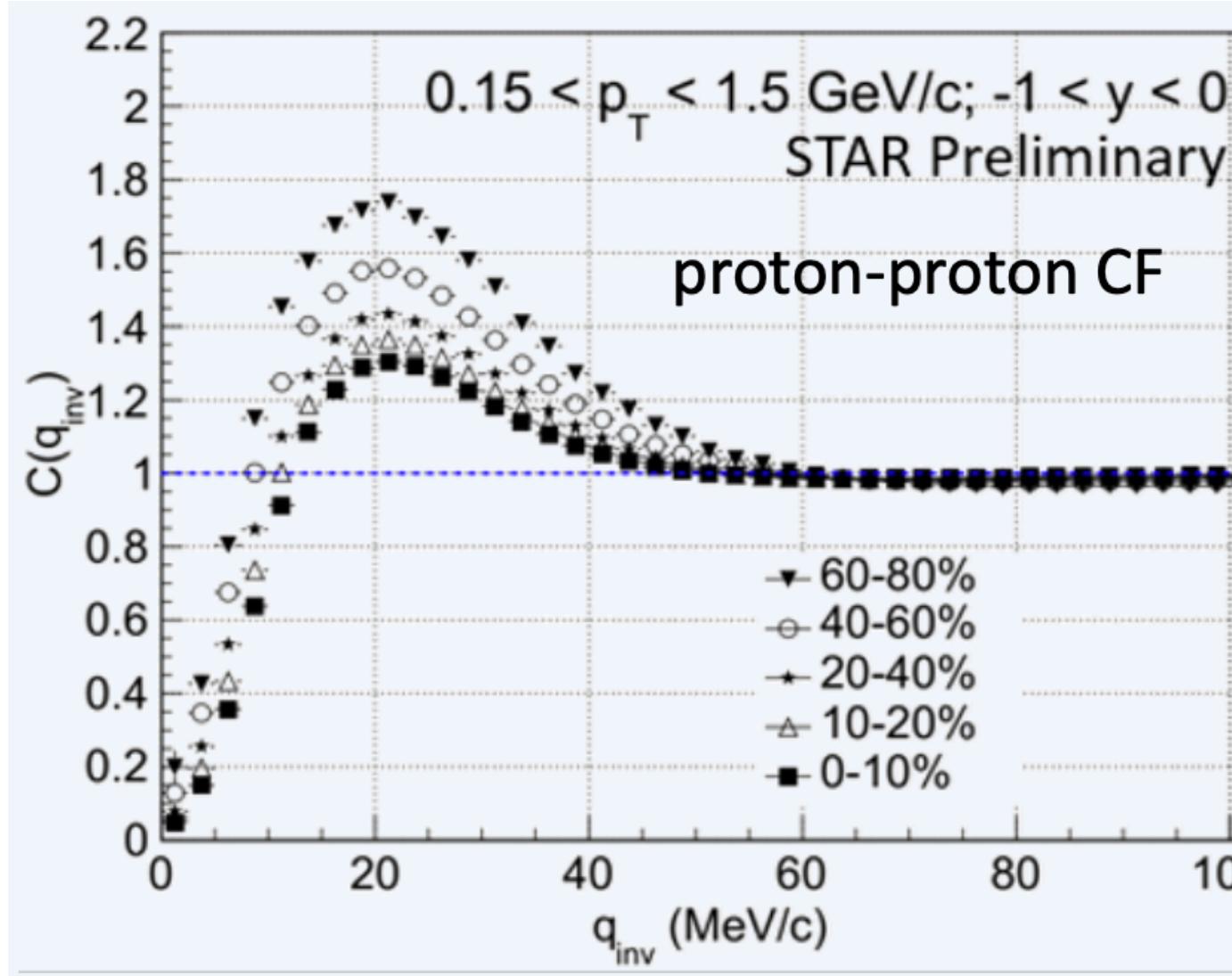


Thank you for your attention!

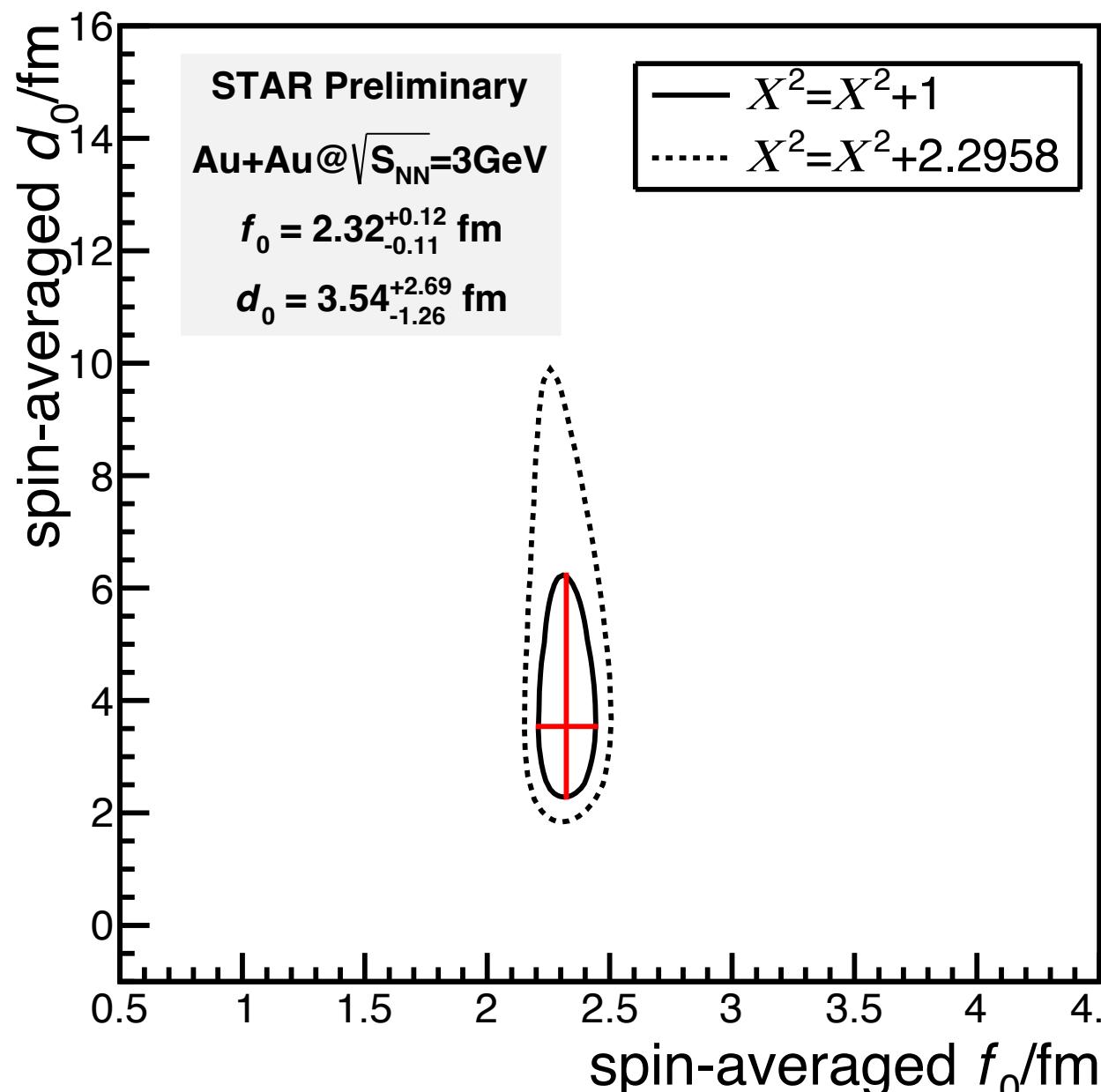


Backup

p-p, p- Λ correlation functions @ 3 GeV



X^2 contour of spin-averaged d_0 and f_0 for $p\Lambda$ ($-1 < y < 0$)



QM2022/ QM2023

$p\Lambda$ Correlation Function with Lednicky-Lyuboshit Fitting

STAR Preliminary
Au+Au@ $\sqrt{S_{NN}}=3\text{GeV}$

