## **Electromagnetic form factors of Baryons**

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with Q.H.Yang, D.Guo, M.Li, J.Haidenbauer, X.W. Kang, U.-G. Meissner, et.al.

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大学名称或校徽

#### **Outline**



## **Baryon**

- Baryon inner structure?
- EIC, EicC: 3D structure of proton?
- § Mass, spin,radius?
- § STCF: EMFF, the inner structure of baryons?
- **Threshold enhancement?** pp,  $\Lambda\Lambda$ ,  $\Sigma\Sigma$ ,  $\Lambda_c\Lambda_c$ ,  $\Xi\Xi(?)...$



#### **Strategy**

#### ■ New insights in strong interactions?



## **2. NN scattering amplitudes**

## § **SU(2) N scattering amplitude**

- elastic NN scattering: E.Epelbaum *et.al.*, EPJA51 (2015) , 53
	- pion(s) exchange: NN Chiral EFT+G-parity
	- LECs of contact term: to be fixed by data
- annihilation: unitarity, fit to the data



$$
V^{NN} = V_{1\pi} + V_{2\pi} + V_{3\pi} + ... + V_{cont}
$$
  

$$
V_{el}^{NN} = -V_{1\pi} + V_{2\pi} - V_{3\pi} + ... + V_{cont}
$$
  

$$
V_{ann}^{NN} = \sum_{X} V^{NN \to X}
$$

J.Haidenbauer, talk at Bochum

## **ChEFT**

- Up to N<sup>3</sup>LO, in time ordered ChEFT:
	- only irreducible diagrams contributes
	- Lippmann-Shwinger equation



## **ChEFT: potentials**

■ pion(s) exchange potentials:

$$
V_{1\pi}(q) = \left(\frac{g_A}{2F_\pi}\right)^2 \left(1 - \frac{p^2 + p^{\prime 2}}{2m^2}\right) \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_2 \frac{\boldsymbol{\sigma}_1 \cdot \mathbf{q} \boldsymbol{\sigma}_2 \cdot \mathbf{q}}{\mathbf{q}^2 + M_\pi^2}
$$

 $V_{2\pi} = V_C + \tau_1 \cdot \tau_2 W_C + [V_S + \tau_1 \cdot \tau_2 W_S] \sigma_1 \cdot \sigma_2 + [V_T + \tau_1 \cdot \tau_2 W_T] \sigma_1 \cdot q \sigma_2 \cdot q$ +  $[V_{LS} + \tau_1 \cdot \tau_2 W_{LS}] i(\sigma_1 + \sigma_2) \cdot (q \times k)$ ,

#### ■ Fourier transformation: change it into corordinat space to do regularization  $\frac{0.002}{0.0022}$

$$
V_C(q) = 4\pi \int_0^\infty f(r) V_C(r) j_0(qr) r^2 dr,
$$
  
\n
$$
V_S(q) = 4\pi \int_0^\infty f(r) \left( V_S(r) j_0(qr) + \tilde{V}_T(r) j_2(qr) \right) r^2 dr,
$$
  
\n
$$
V_T(q) = -\frac{12\pi}{q^2} \int_0^\infty f(r) \tilde{V}_T(r) j_2(qr) r^2 dr,
$$
  
\n
$$
V_{SL}(q) = \frac{4\pi}{q} \int_0^\infty f(r) V_{LS}(r) j_1(qr) r^3 dr.
$$
  
\n
$$
f(r) = \left[ 1 - \exp\left( -\frac{r^2}{R^2} \right) \right]^n.
$$



#### **ChEFT: potentials**

#### ■ Contact terms: short distance<br> $V(^{1}S_{0}) = \bar{C}_{1S_{0}} + C_{1S_{0}}(p^{2} + p^{2}) + D^{1}{}_{1S_{0}}p^{2}p^{2} + D^{2}{}_{1S_{0}}(p^{4} + p^{4}),$  $V(^3S_1) = \tilde{C}_{^3S_1} + C_{^3S_1}(p^2 + p'^2) + D^1{}_{^3S_1}p^2p'^2 + D^2{}_{^3S_1}(p^4 + p'^4),$  $V(^{1}P_{1}) = C_{1p,} pp' + D_{1p,} pp'(p^{2} + p'^{2}),$  $V(^3P_1) = C_{3p_1} p p' + D_{3p_1} p p' (p^2 + p'^2),$  $V(^3P_0) = C_{^3P_0} p p' + D_{^3P_0} p p' (p^2 + p'^2),$  $V(^3P_2) = C_{3p_2} p p' + D_{3p_2} p p' (p^2 + p'^2)$ ,  $V(^3D_1 - {}^3S_1) = C_{\epsilon}, p'^2 + D^1_{\epsilon}, p^2p'^2 + D^2_{\epsilon}, p'^4$ ,  $V({}^3S_1-{}^3D_1)=C_{\epsilon_1}p^2+D^1{}_{\epsilon_1}p^2p^2+D^2{}_{\epsilon_1}p^4,$

■ Non-local regularization

 $f(p',p)=\exp\left(-\frac{p'^m+p^m}{\Lambda^m}\right)$ 

■ Annihilation terms: short distance physics, around 1 fm or less the same form as that of contact terms

$$
V_{\rm ann} = V_{\bar N N \to X} G_X V_{X \to \bar N N}
$$

Ignore the transition between annihilation channels

#### **Phase shifts of different cutoff**

#### ■ LS equation to solve amplitrudes

$$
T_{L''L'}(p'',p';E_k) = V_{L''L'}(p'',p') + \sum_{L} \int_0^\infty \frac{dpp^2}{(2\pi)^3} V_{L''L}(p'',p) \frac{1}{2E_k - 2E_p + i0^+} T_{LL'}(p,p';E_k)
$$





#### **Observables**

- Cross sections
- Angular distributions





#### **Why SU(3) ChEFT**

- SU(2): so far, so good, but
	- only pion exchanges
	- only works for nucleons
- SU(3) G-parity transformation is not OK as kaon does not have definitive G-parity
	- Direct calculation of BB scattering
	-

$$
B = \begin{pmatrix} \frac{\Sigma^0}{\sqrt{2}} + \frac{\Lambda}{\sqrt{6}} & \Sigma^+ & p \\ \Sigma^- & -\frac{\Sigma^0}{\sqrt{2}} + \frac{\Lambda}{\sqrt{6}} & n \\ -\Xi^- & \Xi^0 & -\frac{2\Lambda}{\sqrt{6}} \end{pmatrix}
$$



## **SU(3) ChEFT**

- § Fit results
- Phase shifts **being a struck of the Phase shifts**
- 
- Cross sections<br>differential cross sections differential cross sections  $\frac{1}{2}$   $\frac{1}{2}$   $\frac{1}{2}$   $\frac{1}{2}$   $\frac{1}{2}$   $\frac{1}{2}$
- ratios, etc.



Yang, Guo, Li, Dai, Haidenbauer, Meissner, JHEP08 (2024) 208



#### **SU(3) ChEFT**

§ Angular distributions also help to fix partial wave amplitudes







#### **ChEFT+OGE?**



- Consider onegluon exchange potential in the high energy region
- It can reproduce the fractional oscillations
- An efficient way to describe the strong interaction in both low energy region and high energy region

Yang, Guo, Dai\*, Haidenbauer, Kang, Meissner, Sci.Bull. 68 (2023) 2729;

#### **3. Application**:**EMFFs of nucleons**

CMD-3 has excellent measurement in low energy region § BESIII's high statistics' measurements on nucleon EMFFs









BESIII: PRL 130 (2023) 15, 151905



BESIII: PRD 99 (2019) 092002; PRL 124 (2020) 4, 042001, Nature Phys.17 (2021) 1200

#### **FSI**

- To analyze  $ee \rightarrow NN$ , we need to consider FSI
- § Distorted-wave Born approximation (DWBA):



Vector meson dominance:  ${}^{3}S_{1}$ - ${}^{3}D_{1}$ 

 $-3D_1$  Sci.Bull. 68 (2023) 2729; SU(3) ChEFT: Yang, Guo, Dai\*, Haidenbauer, Kang, Meissner,

> SU(2)ChEFT: J.Haidenbauer, X.-W. Kang, U.-G. Meißner, NPA 929 (2014) , PRD91 (2015) 074003.

#### **Individual EMFFs of nucleons**

- Modulus:  $|G_E|=|G_M|$ at threshold, and will  $\sum_{0.0}^{\frac{0.1}{1.9} \text{ proton}}$   $\sum_{2.0}^{\frac{0.1}{1.9} \text{ neutron}}$
- § Phases:
	- An overall phase is  $\frac{35}{9}$ unobservable  $\overbrace{a_1 \atop a_0 \tbinom{0.2}{1.9} \tbinom{0.2}{2.0} \tbinom{0.2}{2.1} \tbinom{0.2}{2.0} \tbinom{0.2}{2.1} \tbinom{0.2}{2.0} \tbinom{0.2}{2.1} \tbinom{0.2}{2.1} \tbinom{0.2}{2.1} \tbinom{0.2}{2.1} \tbinom{0.2}{2.1} \tbinom{0.2}{2.1} \tbinom{0.2}{2.1} \tbinom{0.2}{2.1} \tbinom{0.2}{2.1$
	- rapidly near threshold  $\frac{3}{26}$  -40



#### **Oscillation**

■ Effective EMFFs

$$
G_{\text{eff}}(s)| = \sqrt{\frac{\sigma_{e^+e^- \to \bar{N}N}(s)}{\frac{4\pi\alpha^2\beta}{3s}C(s)[1 + \frac{2M_N^2}{s}]}}
$$

■ Subtracted form factors: oscillation a metal of the space A. Bianconi & E. Tomasi-Gustafsson, PRL114 (2015) 232301; PRC103 (2021) 035203

$$
G_{\rm osc}(s) = |G_{\rm eff}| - G_D(s), \quad G_D^p(s) = \frac{\mathcal{A}_p}{(1 + s/m_a^2)[1 - s/q_0^2]^2}, \quad G_D^n(s) = \frac{\mathcal{A}_n}{[1 - s/q_0^2]^2}
$$



#### **Oscillation**

■ We propose a fractional oscillation model

$$
G_{\rm osc}^{N}(\tilde{p}) = G_{\rm osc,1}^{N}(\tilde{p}) + G_{\rm osc,2}^{N}(\tilde{p}),
$$
  
\n
$$
G_{\rm osc,j}^{N}(\tilde{p}) = G_{\rm osc,j}^{0,N} - \frac{\omega_{j}^{2}}{\Gamma(\alpha_{j}^{N})} \int_{0}^{\tilde{p}+p_{0}^{N}} (\tilde{p}+p_{0}^{N}-t)^{\alpha_{j}^{N}-1} G_{\rm osc,j}^{N}(t)dt
$$

#### ■ Oscillation behavior of SFFs



#### **Oscillation**



- The 'overdamped' oscillator dominates near the threshold. It reveals the enhancement near threshold.
- The 'underdamped' oscillator dominates in the high energy region. The proton's and neutron's has a 'phase delay'.
- 

§ Other dynamics? Lin, Hammer, Meißner, PRL128 (2022) 052002 Cao, J.P. Dai, Lenske, PRD 105 (2022) 7, L071503, etc Qian, Liu, Cao, Liu, PRD 107 (2023) 9, L091502; Yan, Chen, Xie, PRD 107 (2023) 7, 076008

#### **Underlying physics?**



- § Two limits of fractional oscillators:1 for diffusion and 2 for wave equations of motions.
- Distributions of higher order polarized charges.

#### **Underlying physics?**



- § Proton: valence quarks of uud; Neutron: udd
- negative polarization electric charges for the proton, when not very faraway from the nucleon.
- § positive polarization for the neutron
- **It explains the phase** difference!

#### **EMFFs of other baryons**

§ NN-YY potentials given by Juelich model



- **FSI described by LS equation**
- parameters fixed by fitting to the pp-->YY data





#### **SU(3) ChEFT**

- SU(3) gives more information in pp,  $\Sigma\Sigma$ ,  $\Lambda\Lambda$  coupled channel scattering Juelich model: Haidenbauer et.al.,
	- NPA562 (1993) 317; Haidenbauer, Meissner, Dai, PRD103 (2021) 014028.
- More data in BB scattering:  $p p \rightarrow \Sigma \Sigma$ ,  $\Lambda \Lambda$ , etc.



BESIII, PRD107 (2023) 7, 072005

For BESIII's YN scattering data, See Jielei Zhang's Talk

- An overall description of the EMFFs of the Octet? STCF?
- **BB** scattering from SU(3) is partly done

#### **Individal EMFFs of Λ<sup>c</sup>**

- Effective form factors for LO, NLO from ChEFT
- Cutoff independent. 6.6

$$
B_{\bar{3}} = \begin{pmatrix} 0 & \Lambda_c & \Xi_c^+ \\ -\Lambda_c & 0 & \Xi_c^0 \\ -\Xi_c^+ & -\Xi_c^0 & 0 \end{pmatrix} \quad B_6 = \begin{pmatrix} \Sigma_c^{++} & \frac{1}{\sqrt{2}} \Sigma_c^+ & \frac{1}{\sqrt{2}} \Xi_c^{\prime +} \\ \frac{1}{\sqrt{2}} \Sigma_c^+ & \Sigma_c^0 & \frac{1}{\sqrt{2}} \Xi_c^{\prime 0} \\ \frac{1}{\sqrt{2}} \Xi_c^{\prime +} & \frac{1}{\sqrt{2}} \Xi_c^{\prime 0} & \Omega_c \end{pmatrix}.
$$

 $\frac{\sum_{3}^{2} - \left(-\frac{1}{2c} + \frac{1}{c^{2}}\right)}{\sum_{1}^{2} - \left(-\frac{1}{2c} + \frac{1}{c^{2}}\right)}$  (1992) 1148 6<br>
Yan, Cheng, et.al., PRD46 (1992) 1148 6 Zou, Liu, Liu, Jiang,PRD108 (2023) 014027



Guo, Yang, Dai, PRD109 (2024) 104005  $\frac{3.8}{10}$  4.60  $\frac{4.65}{\sqrt{5}}$  (GeV)



#### **Separated contributions**

- § Modulus
	- LO: Flat  $G_E^{\Lambda_c}/G_M^{\Lambda_c} \simeq \sqrt{s}/2M_{\Lambda_c} \simeq 1$
	- § NLO: Fluctuations in the high energy  $\frac{1}{10}$   $\frac{1}{10}$   $\frac{1}{10}$   $\frac{1}{10}$   $\frac{1}{10}$ region  $\frac{1}{\sum_{0.8}^{0.8}}$ <br>small cut-off
	- § small cut-off
- Phases  $\frac{e^{0.8}}{\frac{\sqrt{2}}{9}0.6}$ 
	- an overall phase is  $\frac{1}{\sqrt{2}}$  and  $\frac{1}{\sqrt{2}}$  a unknown, we set it  $\left[\begin{array}{cc} 0.2 \\ 0.0 \end{array}\right]_{4.60}$   $\left[\begin{array}{cc} 0.2 \\ 4.60 \end{array}\right]_{4.70}$   $\left[\begin{array}{cc} 0.2 \\ 0.0 \end{array}\right]_{4.60}$
	- threshold<br>more fluctuations in  $\frac{1}{\sum_{\omega=0.8}^{\infty}1.2}$ more fluctuations in  $\frac{8}{3}$   $\frac{1}{3}$   $\frac{1}{3}$   $\frac{1}{3}$   $\frac{1}{3}$   $\frac{1}{3}$   $\frac{1}{3}$   $\frac{1}{3}$ the phase of  $G_F$



#### **Separated contributions**

- Contact term: essential for threshold enhancement
	- S-wave contribution is significant!
- Annihilation term: crucial for fluctuation



#### **4. Summary**

**NN Amplitude** 

SU(2) ChEFT works well at  $P_{Lab}$ <300 MeV up to N<sup>3</sup>LO. For SU(3) one, we calculate NN scattering with other Baryons included. Need more measurements on hyperons.

**EMFFs of N** 

We study the EMFFs of nucleons within SU(3) ChEFT. A fractional oscillation model is proposed, polarized charge density distributions.

EMFFs of Y EMFFs are predicted. SU(3) ChEFT is necessary to improve YY amplitude are calculated based on Juelich model. The the analysis. Individual EMFFs of  $\mathsf{\Lambda_c}$  , oscillation from  $\blacksquare$ interference.

Prospects?

BESIII's new data for SU(3) ChEFT? ChEFT + OGE to study NN scatterings? Hyperons?----**STCF can give more measurements for SU(3) ChEFT and EMFFs.**



# Thank You For your patience!