

# Study of gluon GPDs via vector meson production in ep scattering

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# Outline

This slide focus on the gluon GPDs to study vector meson production.  
It contains follow sections:

- Introduction to GPDs
- Theoretical frame of vector meson production using GPDs method
- Differential cross section of  $J/\psi$  in GPDs method
- Asymmetry in  $J/\psi$  production in ep scattering
- Summary

# Introduction to GPDs

Generalized Parton Distributions (GPDs) can be extracted from deep virtual Compton Scattering ( DVCS), Time-like Compton Scattering (TCS) and Hard Exclusive Meson Production (HEMP) processes.

GPDs can be employed to study

- Spin puzzle
- Energy Momentum tensor
- Mass radius, distributions and pressure

## Quark helicity conservation distributions

The quark helicity conservation distributions go with the Dirac matrix  $\gamma^+$  and  $\gamma^+ \gamma_5$ , where  $i = 1, 2$  is a transverse index, it is defined as [EPJC-19-485]

$$\begin{aligned} & \frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p', \lambda' | \bar{\psi}(-\frac{1}{2}z) \gamma^+ \psi(\frac{1}{2}z) | P, \lambda \rangle |_{z^+=0, z_T=0} \\ &= \frac{1}{2P^+} \bar{u}(p', \lambda') \left[ H^q \gamma^+ + E^q \frac{i\sigma^{+\alpha} \Delta_\alpha}{2m} \right] u(p, \lambda). \end{aligned} \quad (1)$$

$$\begin{aligned} & \frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p', \lambda' | \bar{\psi}(-\frac{1}{2}z) \gamma^+ \gamma_5 \psi(\frac{1}{2}z) | P, \lambda \rangle |_{z^+=0, z_T=0} \\ &= \frac{1}{2P^+} \bar{u}(p', \lambda') \left[ \tilde{H}^q \gamma^+ \gamma_5 + \tilde{E}^q \frac{\gamma_5 \Delta^+}{2m} \right] u(p, \lambda). \end{aligned} \quad (2)$$

$H^q$ ,  $E^q$ ,  $\tilde{H}^q$  and  $\tilde{E}^q$  are quark helicity conservation distributions.

# Gluon GPD

The gluon GPD have four parts of GPDs

$$\begin{aligned} & \langle p'v' | \sum_{a,a'} A^{a\rho}(0) A^{a'\rho'}(\bar{z}) | pV \rangle \\ = & \frac{1}{2} \sum_{\lambda=\pm 1} \varepsilon^\rho(k_g, \lambda) \varepsilon^{*\rho'}(k_g, \lambda') \\ & \times \int_0^1 \frac{dx}{(x+\xi-i\varepsilon)(x-\xi+i\varepsilon)} e^{-i(x-\xi)p\cdot\bar{z}} \\ & \times \left\{ \frac{\bar{u}(p'v') \not{n} u(pV)}{2\bar{p}\cdot n} H^g(x, \xi, t) + \frac{\bar{u}(p'v') i \sigma^{\alpha\beta} n_\alpha \Delta_\beta u(pV)}{4m \bar{p}\cdot n} E^g(x, \xi, t) \right. \\ & \left. + \lambda \frac{\bar{u}(p'v') \not{n} \gamma_5 u(pV)}{2\bar{p}\cdot n} \tilde{H}^g(x, \xi, t) + \lambda \frac{\bar{u}(p'v') n \cdot \Delta \gamma_5 u(pV)}{4m \bar{p}\cdot n} \tilde{E}^g(x, \xi, t) \right\}. \end{aligned} \quad (3)$$

# Sum rules of GPDs

GPD connects parton distribution via  $H(x, 0, 0) = xf(x)$ . Hadron Form factor can be obtain from GPDs

$$\int dx H^q(x, \xi, t) = F_1^q(t), \quad \int dx E_q(x, \xi, t) = F_2^q(t); \quad (4)$$

$$\int dx \tilde{H}^q(x, \xi, t) = G_A^q(t), \quad \int dx \tilde{E}^q(x, \xi, t) = G_P^q(t). \quad (5)$$

Ji sum rules for the proton angular memonta

$$\int x dx (H^q(x, \xi, 0) + E^q(x, \xi, 0)) = 2J^q. \quad (6)$$

$J_q = \frac{1}{2}\Delta q + L_q$ .  $L_q$  is key quantity to solve the spin puzzle.

# Heavy vector meson production diagram

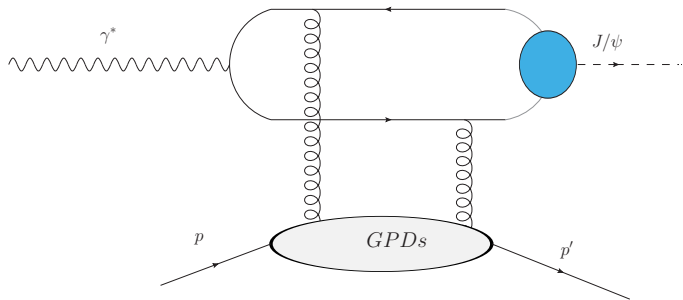


Figure 1: Typical diagram of heavy vector meson in photon-proton scattering.

# Dipole model

Dipole model is employed to calculate vector mesons production in ep scattering. There are several models of the dipole amplitudes models, for example, IIM, IPsat, BGBK model. [PRD-74-074016 et al]

- Dipole model is valid in  $x_B < 0.01$  region
- It didn't consider the the skewness of the  $\xi$  effect
- It can not calculate the asymmetries of the vector mesons production



## Differential cross sections of vector mesons

The longitudinal and transversal differential cross sections as functions of  $|t|$  and total cross sections of heavy vector meson in photon-proton scattering as function of  $W$  and  $Q^2$  are calculated as

$$\frac{d\sigma_T}{dt} = \frac{1}{16\pi W^2(W^2 + Q^2)} [|\mathcal{M}_{++,++}|^2 + |\mathcal{M}_{+-,++}|^2], \quad (7)$$

$$\frac{d\sigma_L}{dt} = \frac{Q^2}{m_V^2} \frac{d\sigma_T}{dt}; \quad (8)$$

$$\frac{d\sigma}{dt} = \frac{d\sigma_T}{dt} + \varepsilon \frac{d\sigma_L}{dt}. \quad (9)$$

## Differential cross section of vector mesons

The gluon contribution to light vector meson electroproduction within GPD approach were calculated in [EPJC-42-281]. The helicity conservation amplitude of heavy vector meson production is given as

$$\begin{aligned} \mathcal{M}_{\mu'+, \mu+} &= \frac{e}{2} C_V \int_0^1 \frac{dx}{(x+\xi)(x-\xi+i\epsilon)} \\ &\times \left\{ \mathcal{H}_{\mu', \mu}^{V+} H_g(x, \xi, t, \mu_F) + \mathcal{H}_{\mu', \mu}^{V-} \tilde{H}_g(x, \xi, t, \mu_F) \right\}. \end{aligned} \quad (10)$$

While the helicity flip amplitude can be written as

$$\begin{aligned} \mathcal{M}_{\mu'-, \mu+} &= -\frac{e}{2} C_V \frac{\sqrt{-t}}{2m} \int_0^1 \frac{dx}{(x+\xi)(x-\xi+i\epsilon)} \\ &\times \left\{ \mathcal{H}_{\mu', \mu}^{V+} E_g(x, \xi, t, \mu_F) + \mathcal{H}_{\mu', \mu}^{V-} \tilde{E}_g(x, \xi, t, \mu_F) \right\}. \end{aligned} \quad (11)$$

Here the amplitudes  $\mathcal{H}_{\mu', \mu}^{V\pm}$  are determined as a sum and differences of amplitudes with different gluon helicities.

$$\mathcal{H}_{\mu', \mu}^{V\pm} = \left[ \mathcal{H}_{\mu'+, \mu+}^V \pm \mathcal{H}_{\mu'-, \mu-}^V \right], \quad (12)$$

# Scattering amplitudes

There are 6 feynman diagrams of  $\gamma + p \rightarrow V + p$ . We must calculate the sum of feynman amplitudes of them

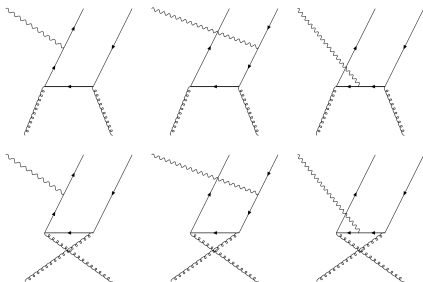


Figure 2: 6 feynman diagrams of  $\gamma + g \rightarrow V + g$

# Scattering amplitudes

To calculate hard scattering amplitude we consider six gluon Feynman diagrams. After a length calculations, the hard amplitude can be cast into

$$\mathcal{H}_{\mu',\mu}^{V\pm}(x,\xi) = 64\pi^2\alpha_s(\mu_R) \int_0^1 d\tau \int \frac{d^2\mathbf{k}_\perp}{16\pi^3} \psi(\tau, \mathbf{k}_\perp) \mathcal{F}_{\mu',\mu}^{\pm}(\tau, x, \xi, \mathbf{k}_\perp^2). \quad (13)$$

Here  $\tau$  and  $1 - \tau$  are the fraction of longitudinal part of quark (antiquark) momenta incoming to the meson wave function,  $\mathbf{k}_\perp$  is there transverse part. The  $k$ -dependent wave function of the vector meson is written as

$$\psi(\tau, \mathbf{k}_\perp) = a_v^2 f_v \exp\left(-a_v^2 \frac{\mathbf{k}_\perp^2}{\tau(1-\tau)}\right). \quad (14)$$

Here  $f_v$  is a  $J/\psi$  decay constant, the parameter  $a_v$  is fixed from the best fit  $J/\psi$  cross section and determine the average value of  $\langle \mathbf{k} \rangle_\perp^2$ .

# Hard part of scattering amplitude in $J/\psi$ production

For  $\tau = 1/2$ , the hard part of the amplitude can be written as

$$\mathcal{F}_{\mu',\mu}^{\pm} = \frac{f_{\mu',\mu}^{\pm}}{\text{denominator}} \quad (15)$$

$$\begin{aligned} \text{denominator} &= (2\mathbf{k}_{\perp}^2 + m_V^2 + Q^2)(4\xi\mathbf{k}_{\perp}^2 + (m_V^2 + Q^2)) \\ &(\xi - x) + i\epsilon)(4\xi\mathbf{k}_{\perp}^2 + (m_V^2 + Q^2)(\xi + x)) \end{aligned} \quad (16)$$

For longitudinal and transverse helicity conservation amplitudes  $f_{\mu,\mu}^+$  have a form

$$f_{00}^+ = -64\sqrt{Q^2}(m_V^2 + Q^2)^2(x^2 - \xi^2), \quad (17)$$

$$f_{11}^+ = 64m_V(m_V^2 + Q^2)^2(x^2 - \xi^2). \quad (18)$$

Here we omit  $k$  dependent terms. For the  $f_{\mu,\mu}^-$  which contains  $\tilde{H}$  contribution, we find that

$$f_{11}^- = -256(m_V^2 + Q^2)\mathbf{k}_{\perp}^2 m_V x \xi, \quad f_{00}^- = 0. \quad (19)$$

## GPDs function definitions

The GPDs are constructed adopting the double distribution representation

$$F(x, \xi, t) = \int_{-1}^1 d\beta \int_{-1+|\beta|}^{1-|\beta|} d\alpha \delta(\beta + \xi \alpha - x) f_g(\beta, \alpha, t), \quad (20)$$

$F$  with PDFs  $h$  via the double distribution functions  $f_i(\beta, \alpha, t)$ . For gluon double distribution functions, it is

$$f_g(\beta, \alpha, t) = e^{-bvt} h_i(\beta, \mu_F) \frac{15 [(1 - |\beta|)^2 - \alpha^2]^2}{16 (1 - |\beta|)^5}. \quad (21)$$

The  $t$ -dependence in PDFs  $h(\beta, \mu_F)$  is the fitted from conlinear PDF (CT18NLO, NNPDF, ABMP)

# Ratio of the Re and Im of the amplitude

We can show the ratio of the Re and Im of the amplitudes.

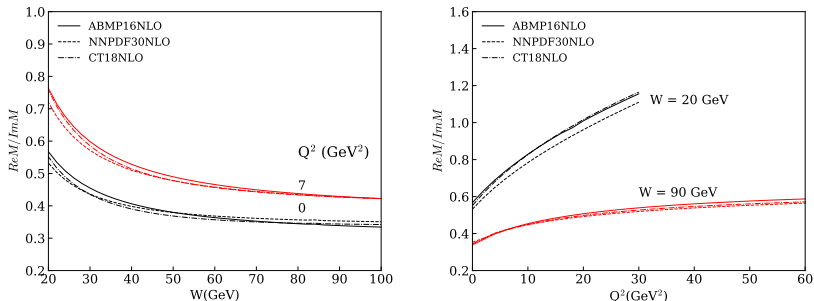


Figure 3: Ratio of  $ReM/ImM$  parts of  $J/\psi$  amplitudes at fixed  $W$  vs  $Q^2$ .

# $J/\psi$ production at different $|t|$

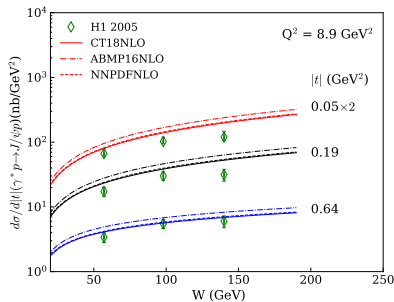
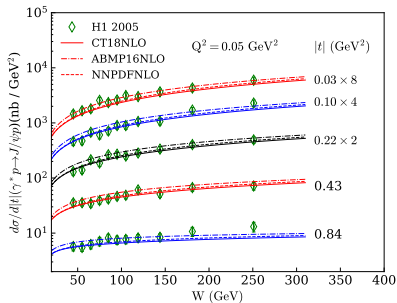
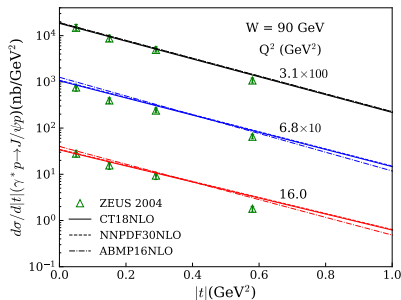
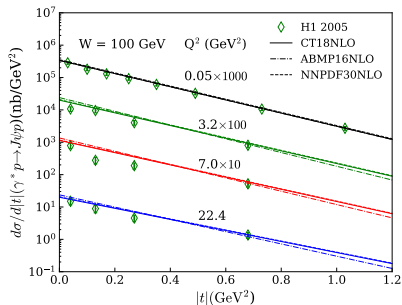


Figure 4:  $J/\psi$  differential cross section as a function of  $W$  at different  $|t|$ . The H1 experimental data are from EPJC-46-585.



# $J/\psi$ production at different $|t|$



**Figure 5:**  $J/\psi$  differential cross section vs  $|t|$  at fixed  $W$  and different  $Q^2$ . The HERA experimental data are from from NPB-695-3 and EPJC-46-585. Cross sections are scaled by the factor shown in the graph.

# $J/\psi$ production at different $Q^2$

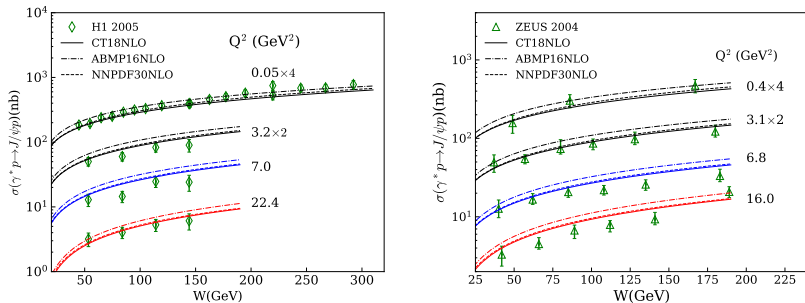
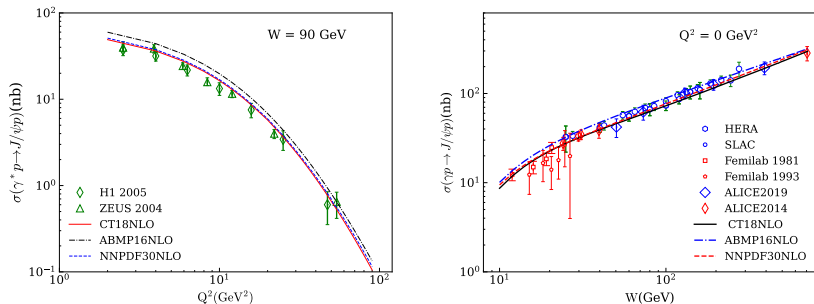


Figure 6:  $J/\psi$  total cross section vs  $W$  at different  $Q^2$  comparing with the HERA experimental data are taken from NPB-695-3 and EPJC-46-585.

# $J/\psi$ production at different $Q^2$



**Figure 7:**  $J/\psi$  total cross section vs  $Q^2$  at HERA energy  $W = 90 \text{ GeV}$  (left graph) and at  $Q^2 = 0 \text{ GeV}^2$  vs  $W$  from low to very high energies (right graph). The experimental data are taken from EPJC-24-345 et al

## $A_{LL}$ asymmetry in VM production

In heavy vector meson production, some asymmetries can be adopted to constrain the GPD functions. Initial state helicity correlations  $A_{LL}$  can be measured with longitudinally polarized beam and target. It can be expressed in terms of helicity amplitudes as Ref.[EPJC-42-281].

$$\begin{aligned} A_{LL}(ep \rightarrow epV) &= \frac{\sqrt{1-\varepsilon^2}}{32\pi W^2(W^2-Q^2)} \frac{|\mathcal{M}_{++,++}|^2 - |\mathcal{M}_{-,-,-}|^2}{\varepsilon d\sigma_L/dt + d\sigma_T/dt} \\ &= 2\sqrt{1-\varepsilon^2} \frac{\text{Re}[\mathcal{M}_{++,++}^H \mathcal{M}_{++,++}^{\tilde{H}*}]}{\varepsilon |\mathcal{M}_{0+,0+}^H|^2 + |\mathcal{M}_{++,++}^H|^2}. \end{aligned} \quad (22)$$

It can be seen that  $A_{LL}$  can be used to study property of polarized GPDs  $\tilde{H}$  of gluon.

## $A_N$ and $A_{LS}$

On the other hand, the single spin asymmetry  $A_N$  can be also measured at heavy vector meson production. For the photoproduction case when the longitudinal amplitude can be omitted the  $A_N$  asymmetry can be written as [PRD-85-051502].

$$A_N(ep \rightarrow epV) = -\frac{2\text{Im}[\mathcal{M}_{++,+}^H \mathcal{M}_{+-,+}^{E*}]}{|\mathcal{M}_{++,+}^H|^2 + |\mathcal{M}_{+-,+}^E|^2}. \quad (23)$$

The double spin asymmetry  $A_{LS}$  the proton beam is longitudinally polarized, and the outgoing nucleon is transversely polarized (in the reaction plane, “sideways”) can be obtained via amplitudes [PRD-85-051502].

$$A_{LS}(ep \rightarrow epV) = \frac{2\text{Re}[\mathcal{M}_{++,+}^H \mathcal{M}_{+-,+}^{E*}]}{|\mathcal{M}_{++,+}^H|^2 + |\mathcal{M}_{+-,+}^E|^2}. \quad (24)$$

# Asymmetries of $J/\psi$ in ep scattering

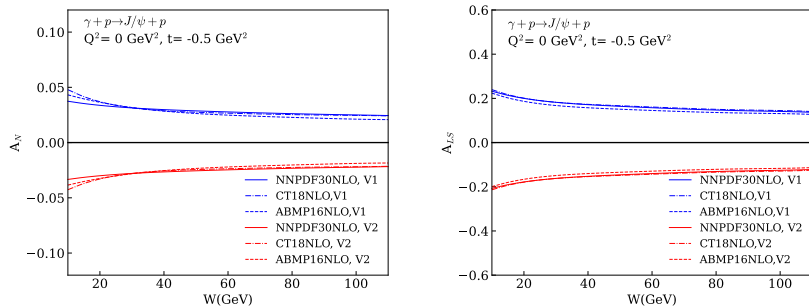


Figure 8:  $J/\psi$  single spin asymmetry  $A_N$  and double spin asymmetry  $A_{LS}$  versus  $W$  at  $Q^2 = 0 \text{ GeV}^2$ .

# Asymmetries of $J/\psi$ in ep scattering

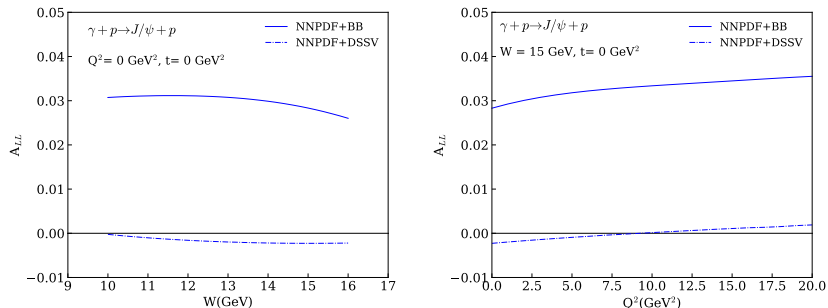


Figure 9: Helicity correlation  $A_{LL}$  of  $J/\psi$  at different  $Q^2$  and  $W$ .

# Summary

We can conclude following conclusions:

- GPDs method can be employed to perform heavy vector mesons production in ep scattering.
- Asymmetries can be obtained via GPDs methods in ep scattering.
- Results of this work can be applied in future EicC experiments to give additional essential constraints on transversity GPDs at EicC energies range.
- EicC will be good perform to study gluon GPDs adopting vector mesons at the future.



The End

*Thanks for your attentions !*