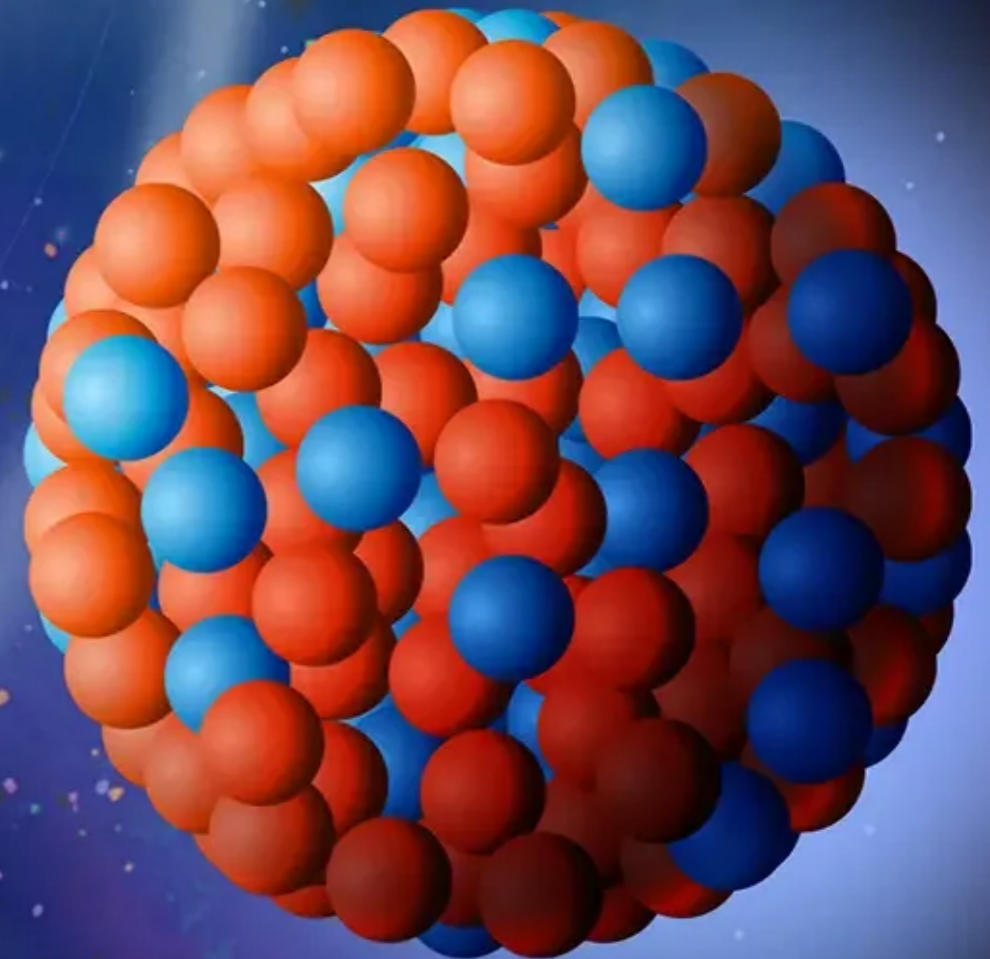


Exploring Nuclear Structure at the Ultra-Relativistic Heavy-Ion Collisions

You Zhou (周铀)
Niels Bohr Institute



UNIVERSITY OF
COPENHAGEN



Funded by
the European Union



European Research Council
Established by the European Commission

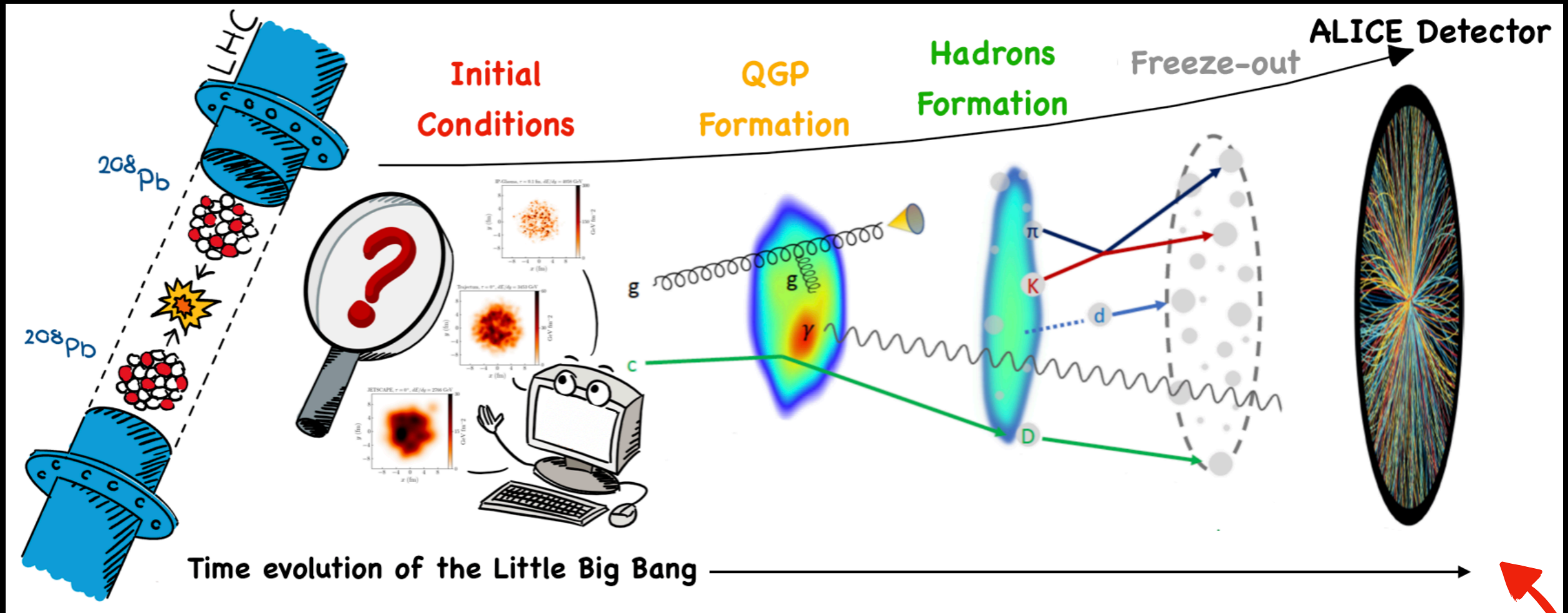
VILLUM FONDEN



INDEPENDENT
RESEARCH FUND
DENMARK

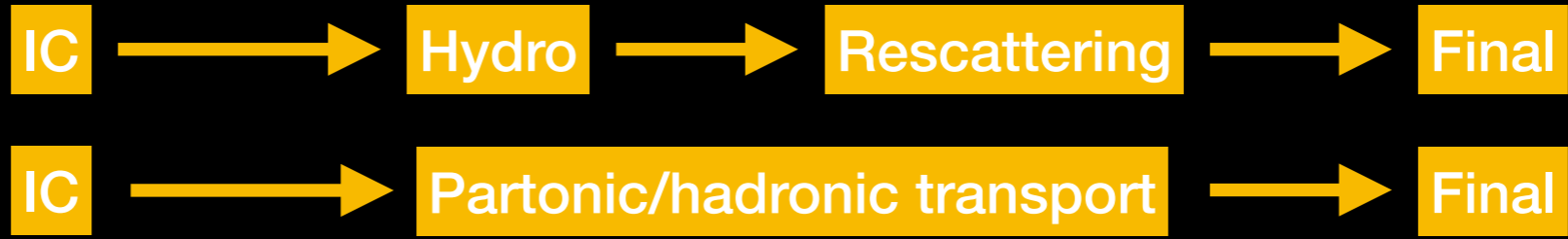
见微学术沙龙

Study of Quark-Gluon Plasma in the *Little Bang*

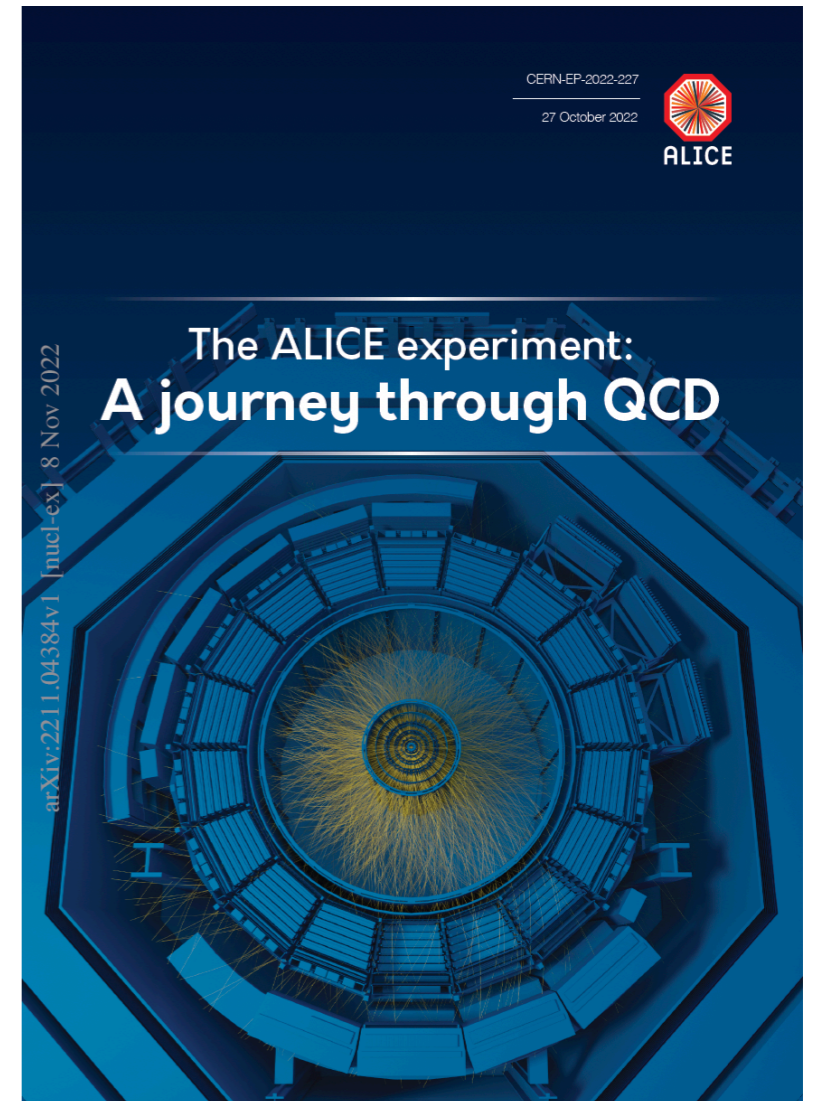


Time evolution of the Little Big Bang

TH



State-of-the-art: Viscosities of QGP

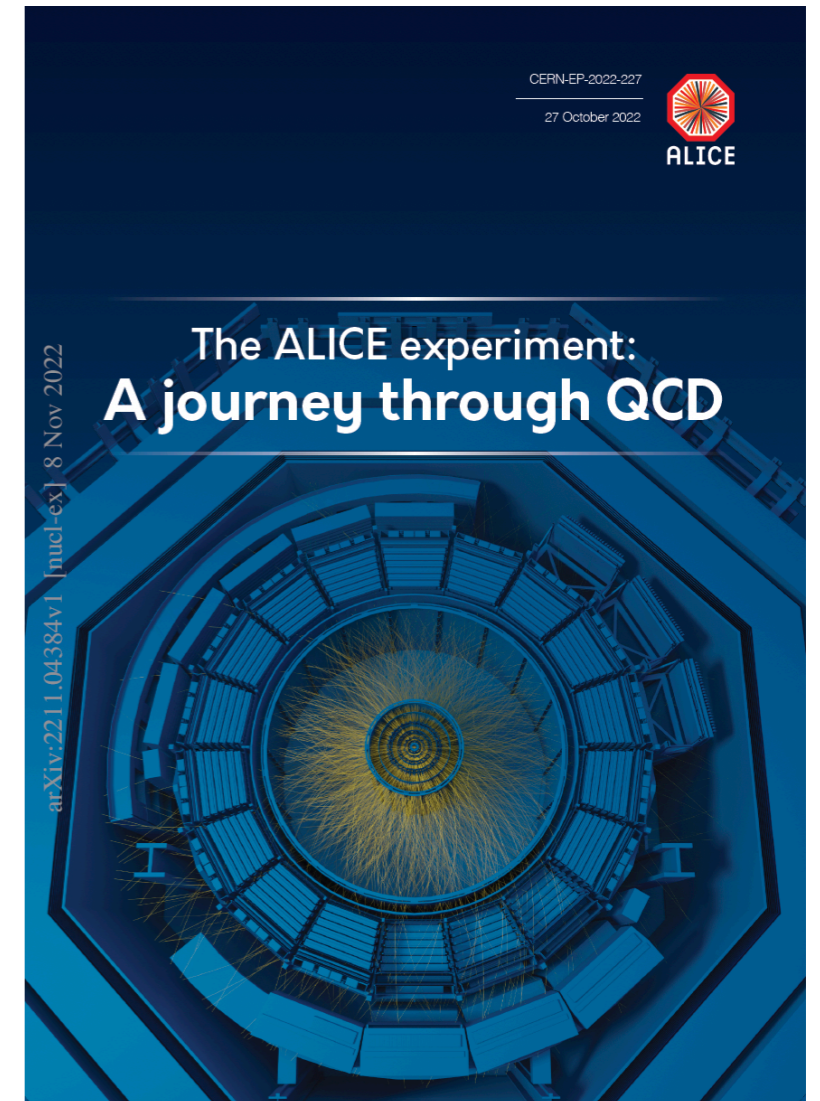
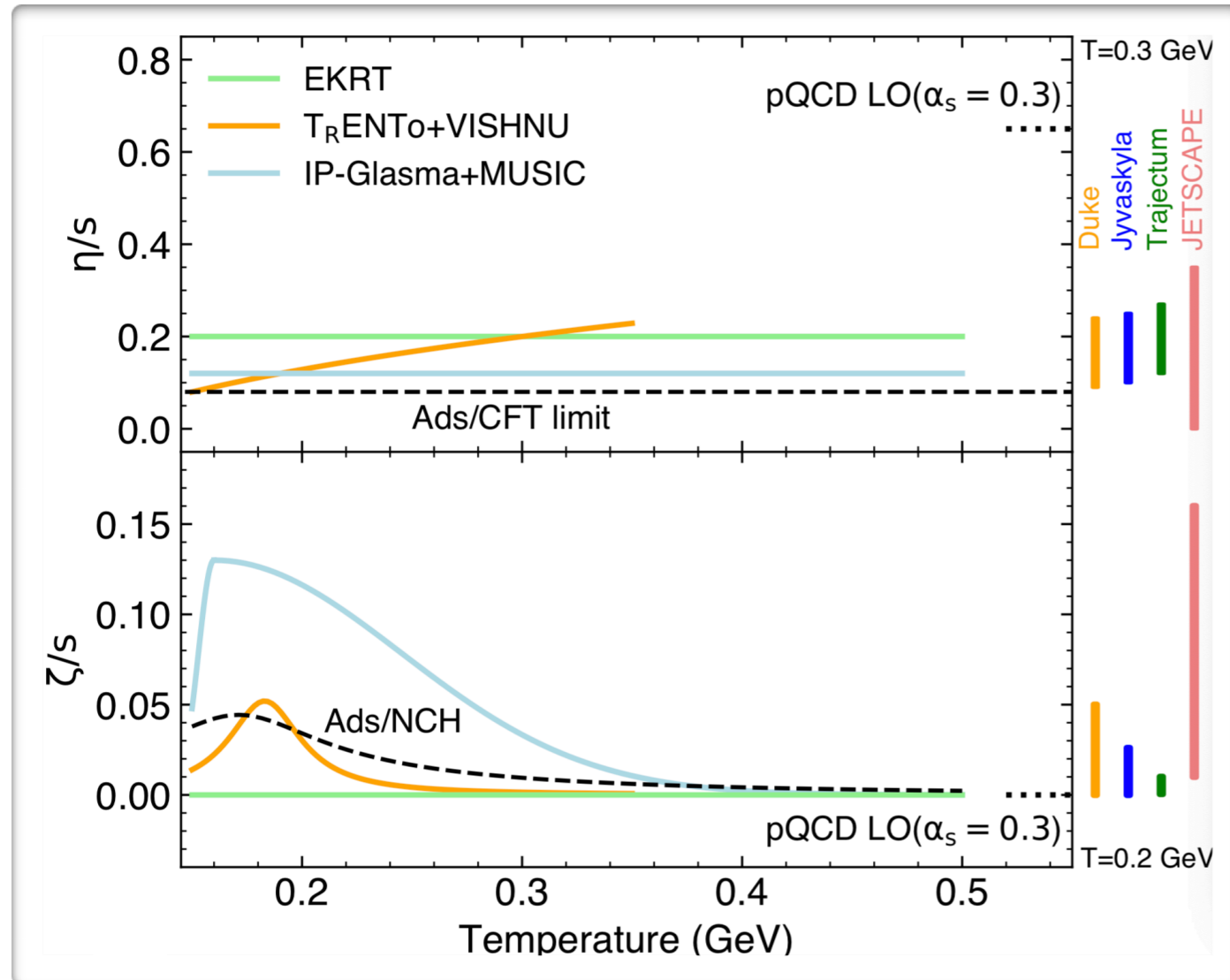


State-of-the-art: Viscosities of QGP

Extracted viscosities of QGP

- shear viscosity η/s
- bulk viscosity ζ/s

Duke: *Nature Phys.* 15 (2019) 11, 1113
Jyväskylä: *Phys. Rev. C* 104, 054904 (2021)
Trajectum: *Phys. Rev. Lett.* 126, 202301 (2021)
JETSCAPE: *Phys. Rev. Lett.* 126, 242301 (2021)
IP-Glasma: *Phys. Rev. Lett.* 128, 042301 (2022)

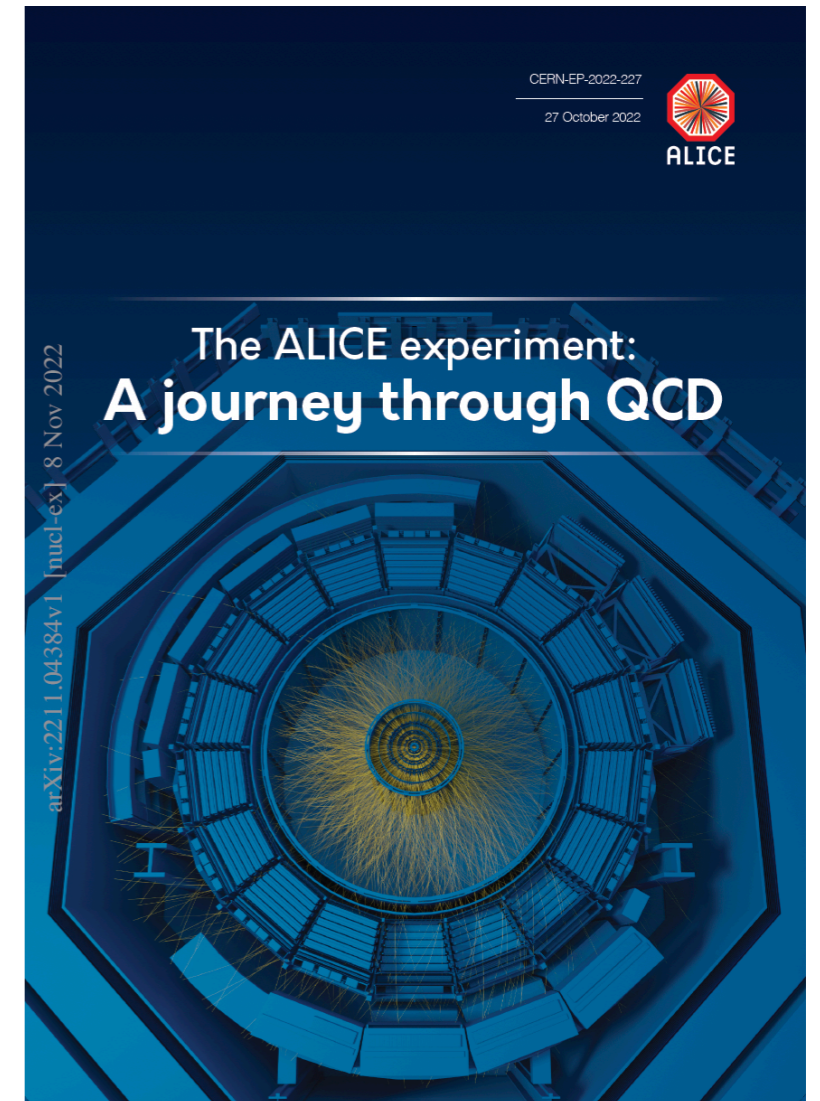
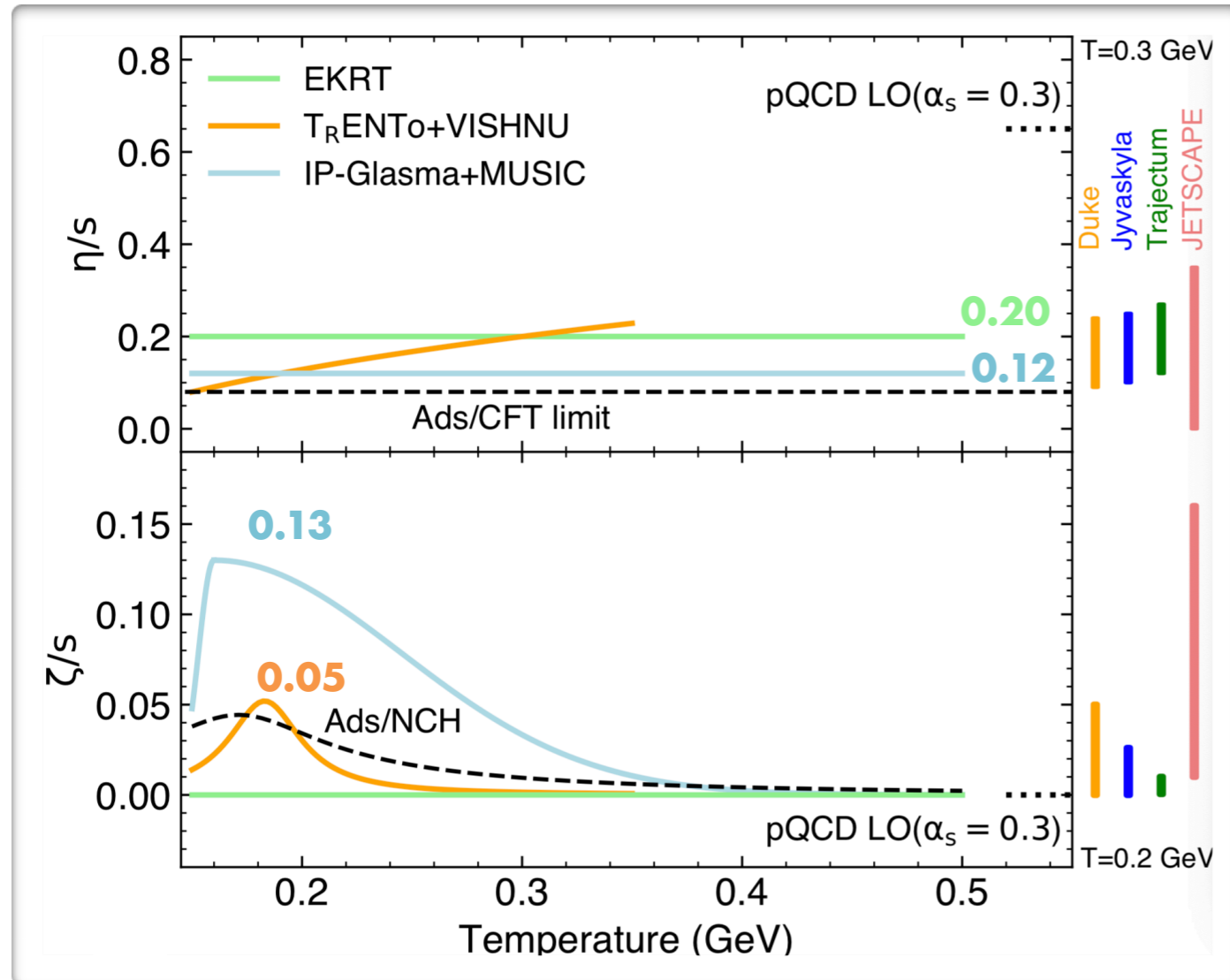


State-of-the-art: Viscosities of QGP

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IP-Glasma: *Phys. Rev. Lett.* 128, 042301 (2022)



Huge uncertainties of the extracted *QGP properties*, due to poorly known *initial conditions*

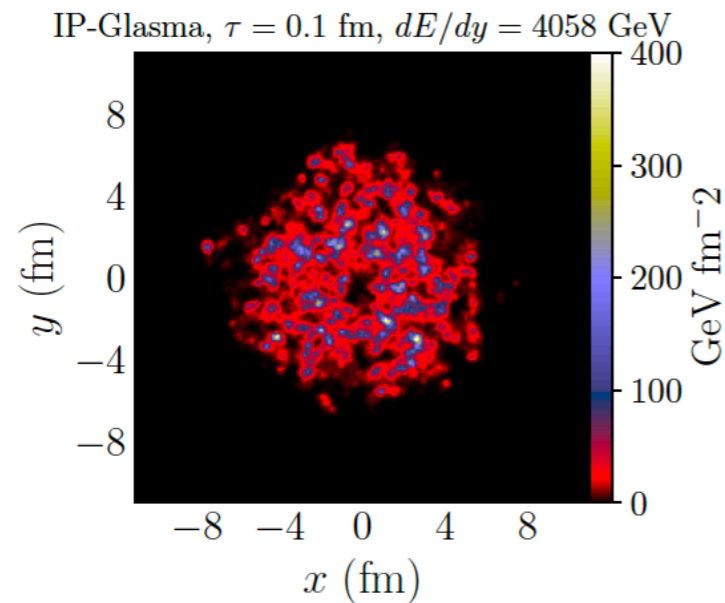


IC: What is our current understanding?

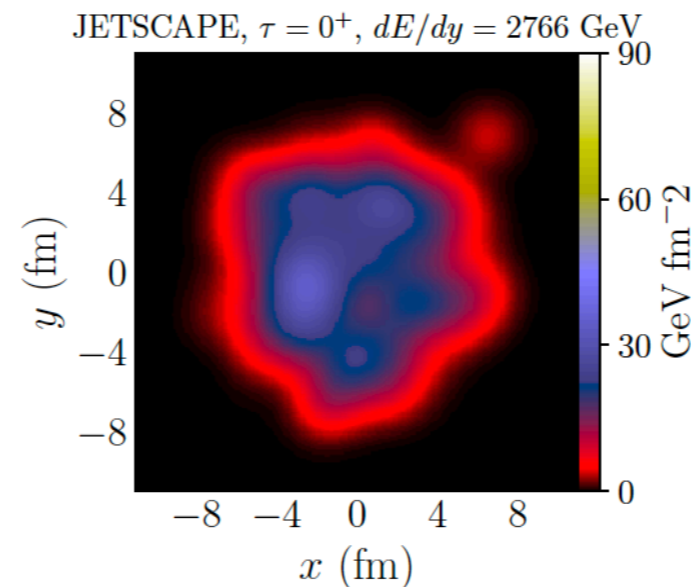


IC: What is our current understanding?

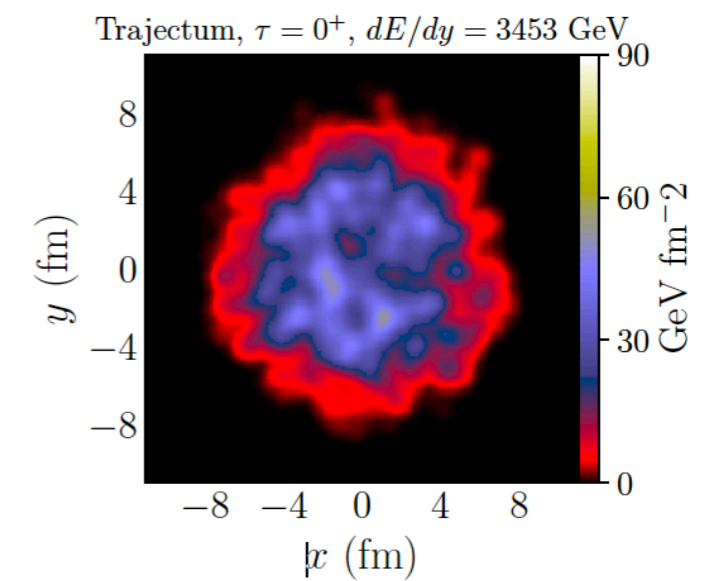
IP-Glasma



JETSCAPE

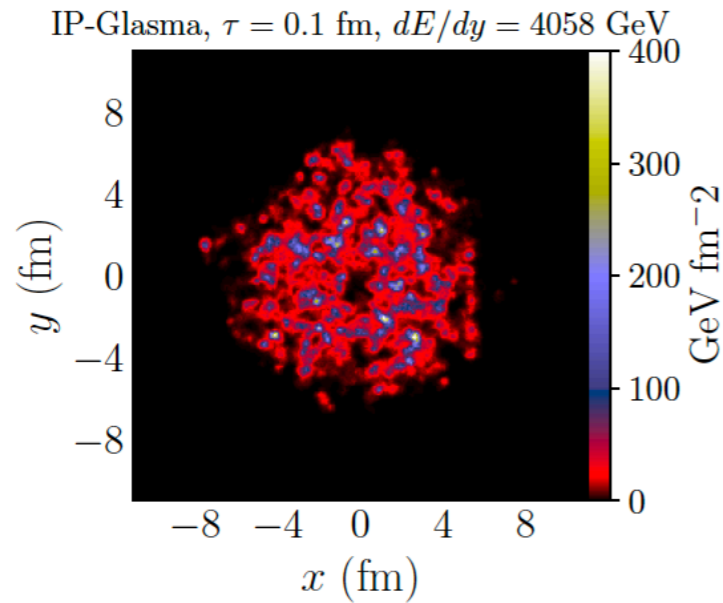


Trajectum

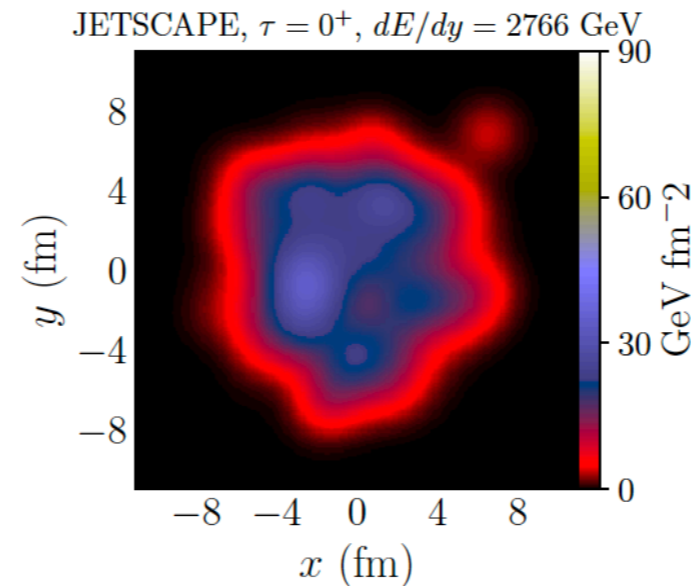


IC: What is our current understanding?

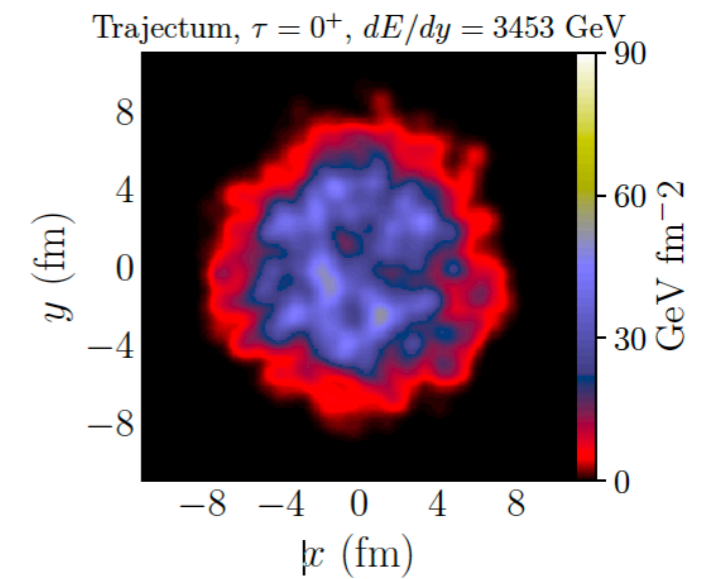
IP-Glasma



JETSCAPE

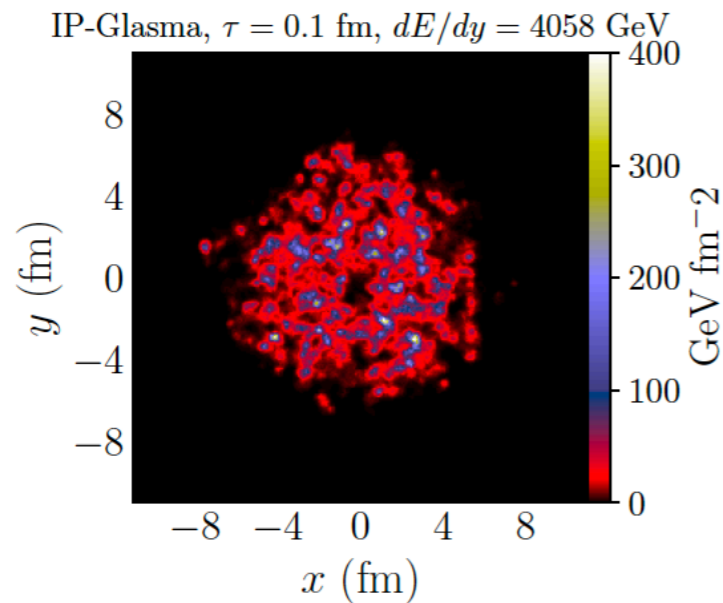


Trajectum

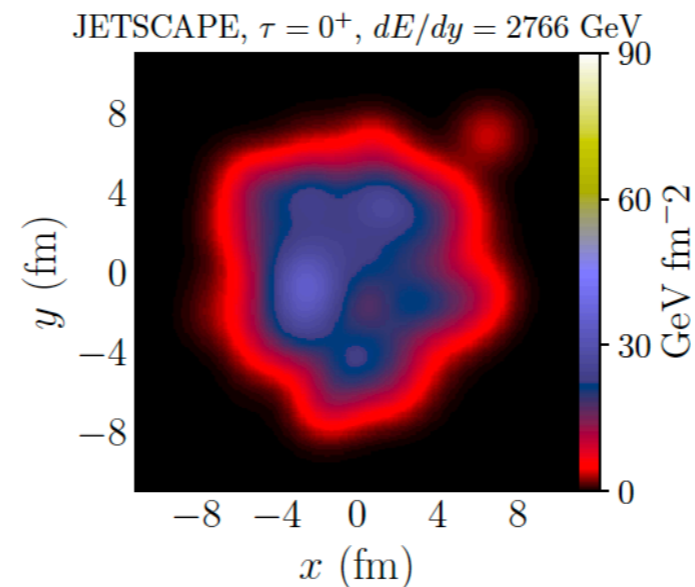


IC: What is our current understanding?

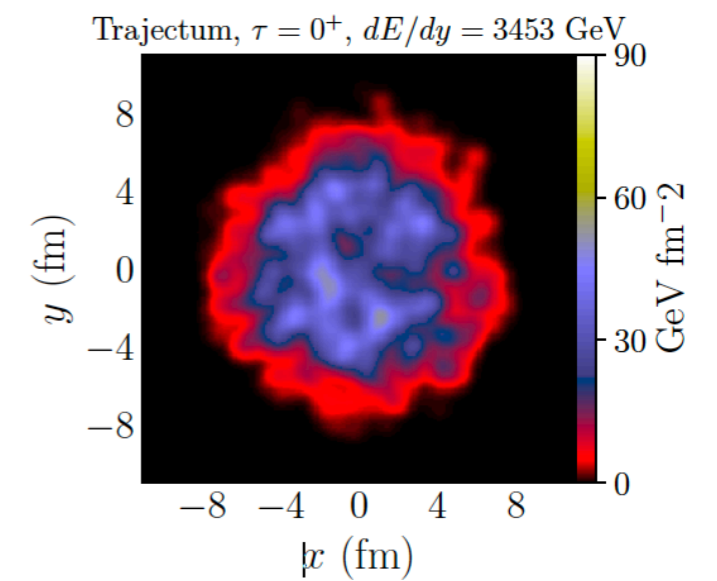
IP-Glasma



JETSCAPE



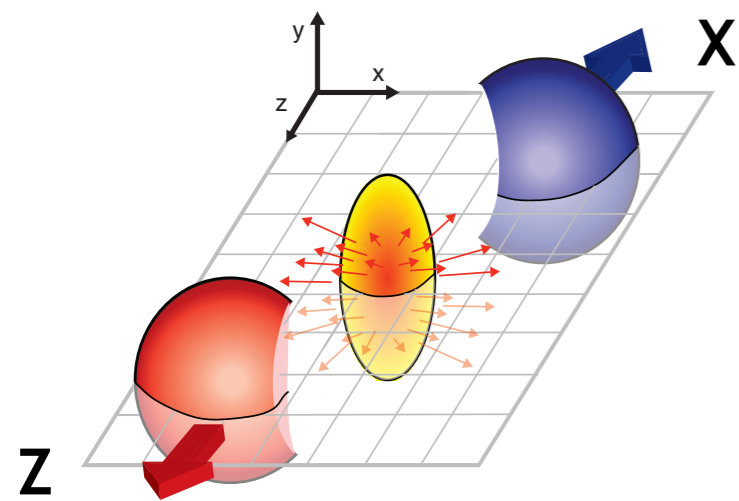
Trajectum



How can we access the initial conditions in EXP ?

From eccentricity to elliptic flow

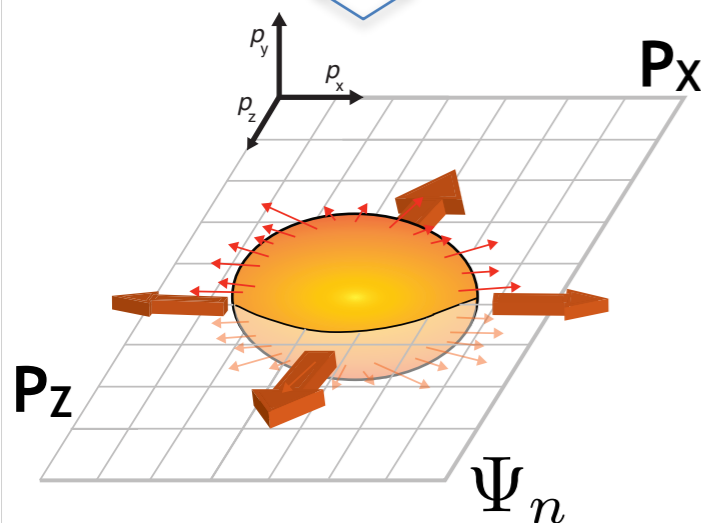
- ❖ Spatial anisotropy in the initial state converted to momentum anisotropic particle distributions
 - known as **elliptic flow**
 - reflect initial **eccentricity** and **transport properties** of QGP



$$\varepsilon_2 = \left\langle \frac{y^2 - x^2}{y^2 + x^2} \right\rangle$$

coordinate space **Eccentricity**

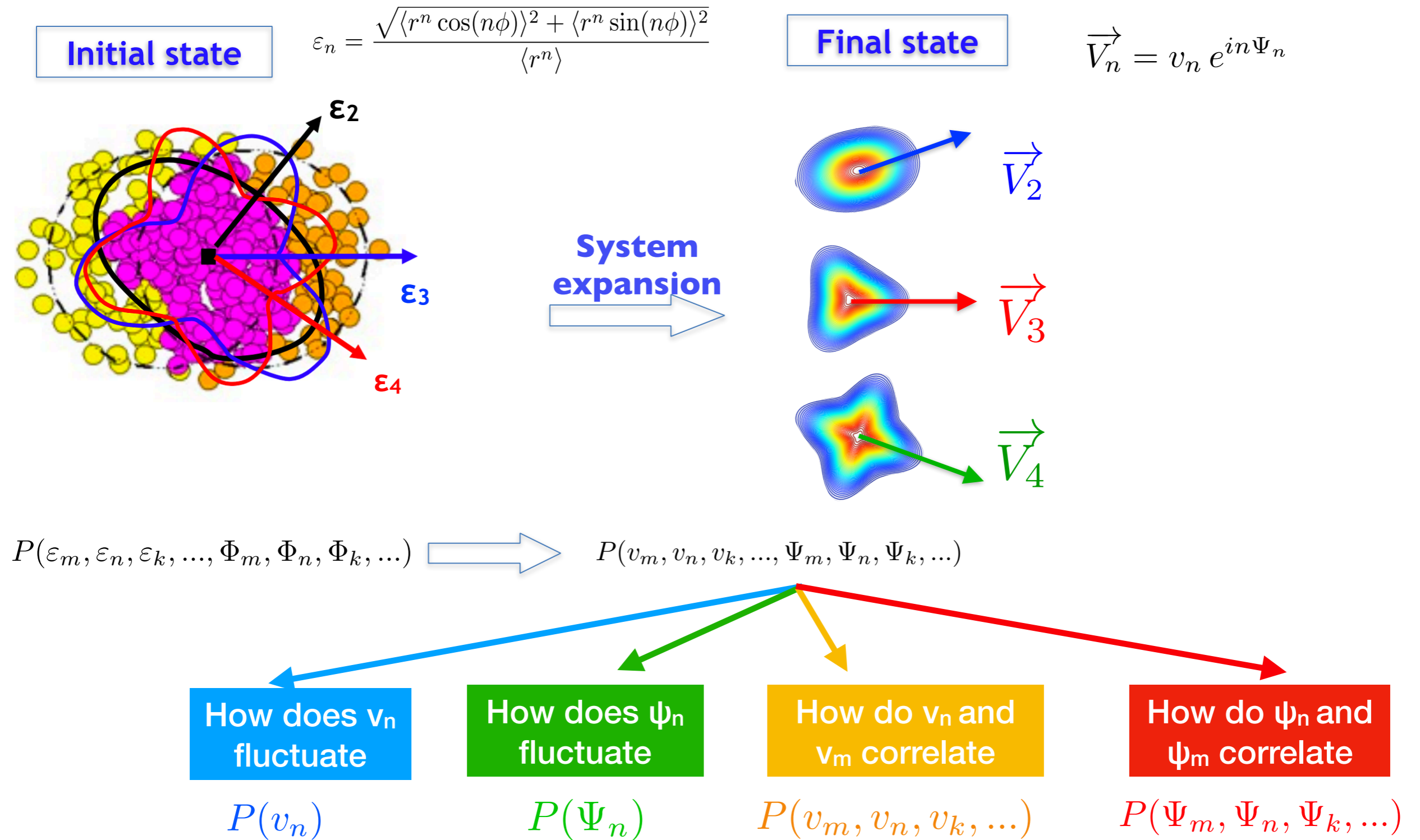
system expansion



$$v_2 = \langle \cos 2(\varphi - \Psi_{RP}) \rangle$$

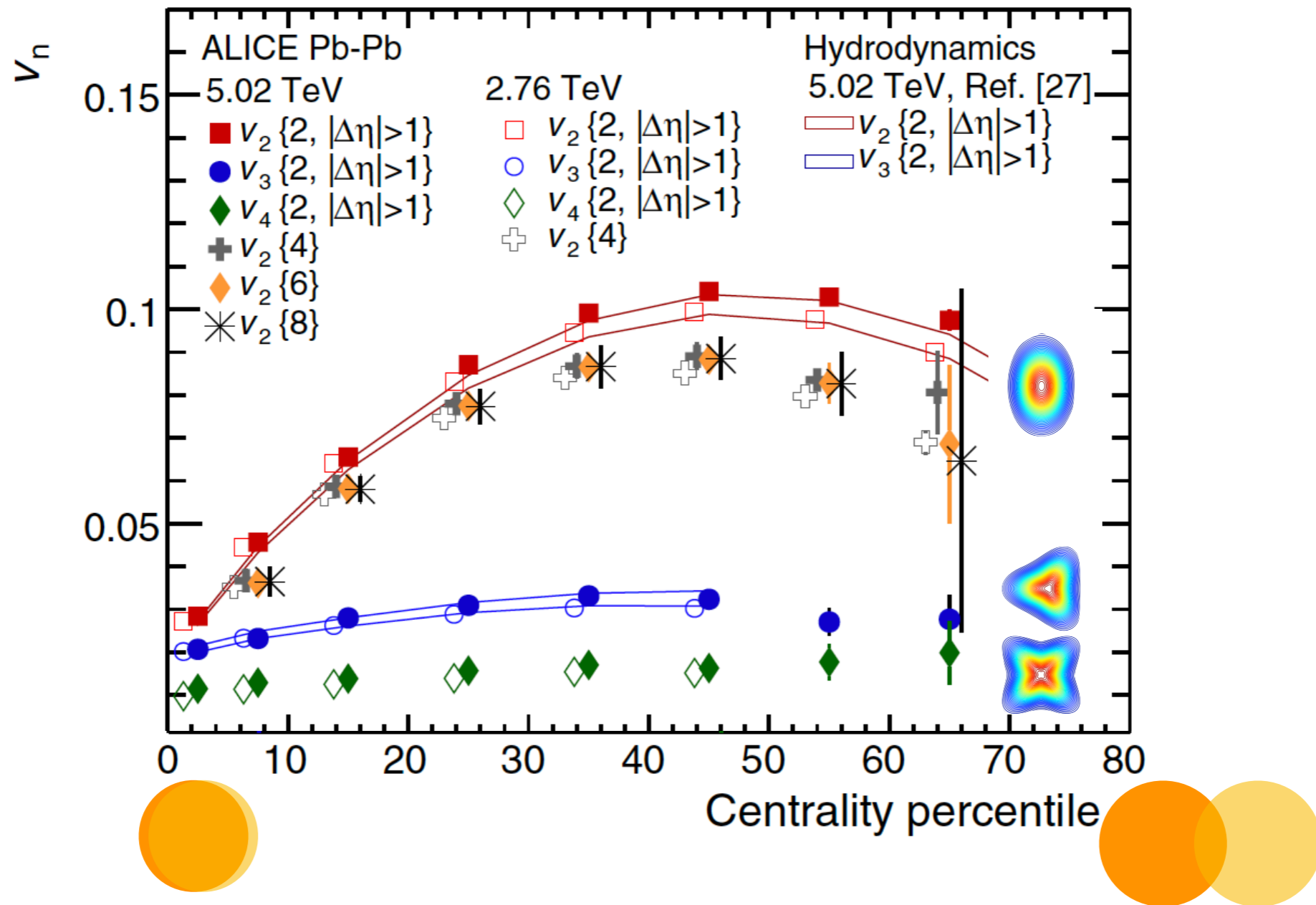
momentum space **Elliptic Flow**

From initial anisotropy to anisotropic flow



Probe QGP properties with Flow

ALICE, Physical Review Letters 116, 132302 (2016)



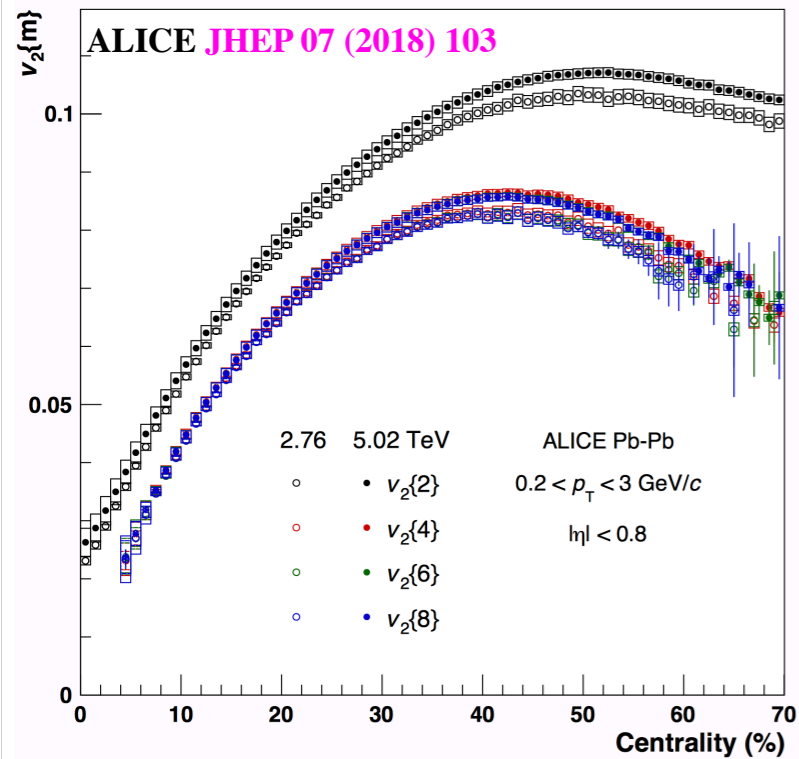
- ❖ Flow measurements at the top LHC energies agree with hydrodynamic predictions
 - The Quark-Gluon Plasma behaves like a perfect fluid
 - Constrain initial state models
 - EKRT ✓, TRENTo ✓, IP-Glasma ✓, MC-KLN ✗, MC-Glauber ✗



Initial geometry fluctuations

How does v_n fluctuate

$v_n\{m\}$



$$v_n\{2\} = \sqrt{\langle v_n^2 \rangle},$$

$$v_n\{4\} = \sqrt[4]{2\langle v_n^2 \rangle^2 - \langle v_n^4 \rangle},$$

$$v_n\{6\} = \sqrt[6]{\langle v_n^6 \rangle - 9\langle v_n^2 \rangle \langle v_n^4 \rangle + 12\langle v_n^2 \rangle^3},$$

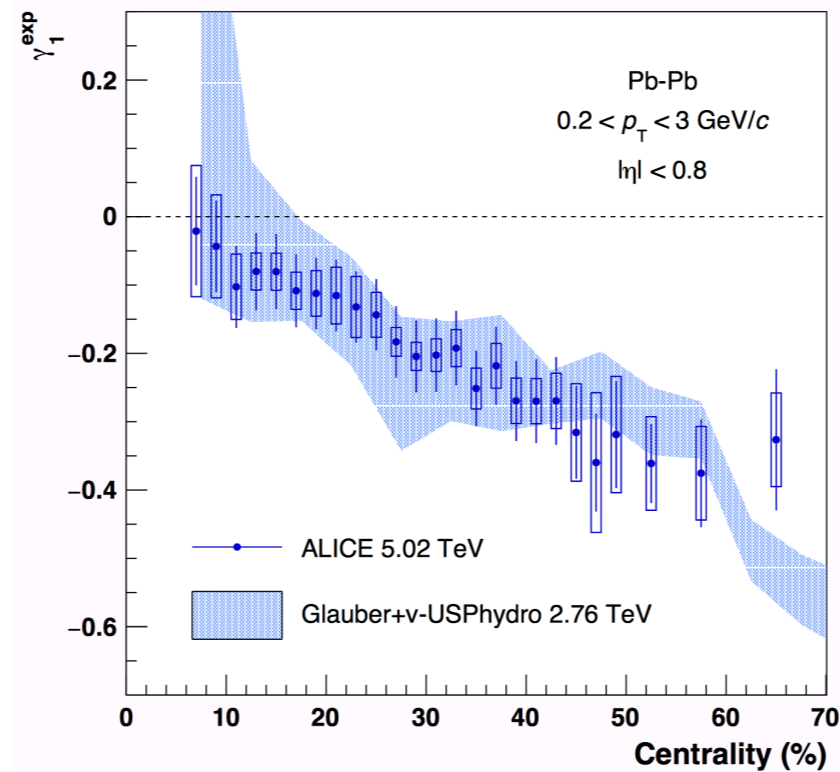
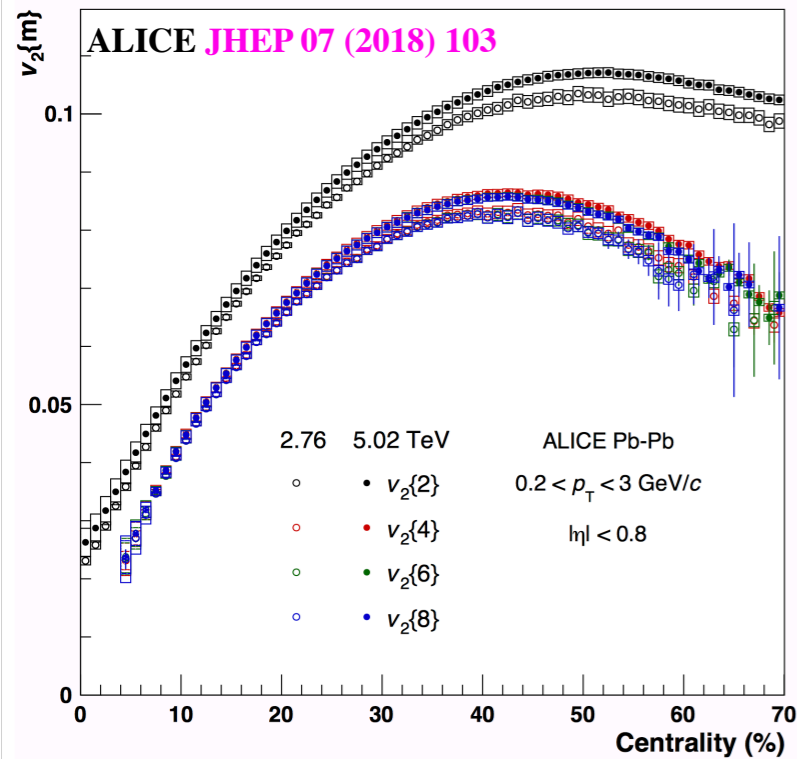
$$v_n\{8\} = \sqrt[8]{\langle v_n^8 \rangle - 16\langle v_n^2 \rangle \langle v_n^6 \rangle - 18\langle v_n^4 \rangle^2 + 144\langle v_n^2 \rangle^2 \langle v_n^4 \rangle - 144\langle v_n^2 \rangle^4}.$$



Initial geometry fluctuations

How does v_n fluctuate

$v_n\{m\}$ → Moments



$$v_n\{2\} = \sqrt{\langle v_n^2 \rangle},$$

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$$\gamma_1^{\text{exp}} = -6\sqrt{2}v_2\{4\}^2 \frac{v_2\{4\} - v_2\{6\}}{(v_2\{2\}^2 - v_2\{4\}^2)^{3/2}}$$

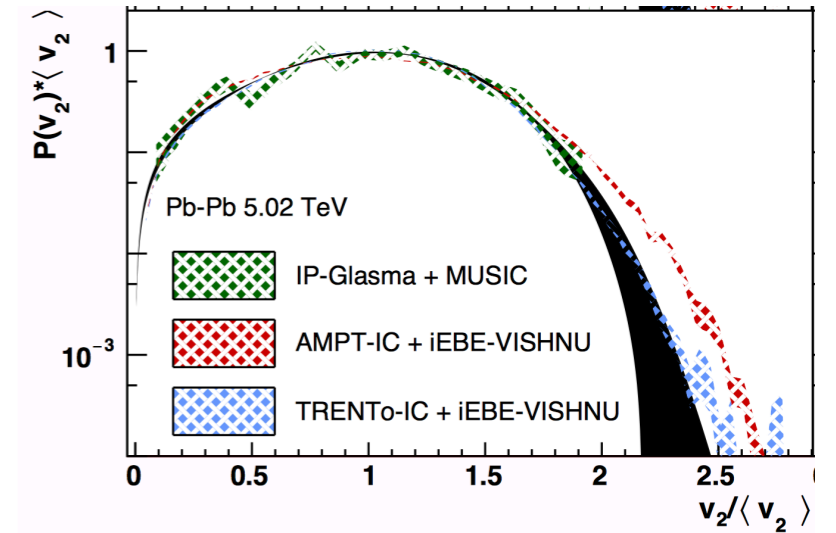
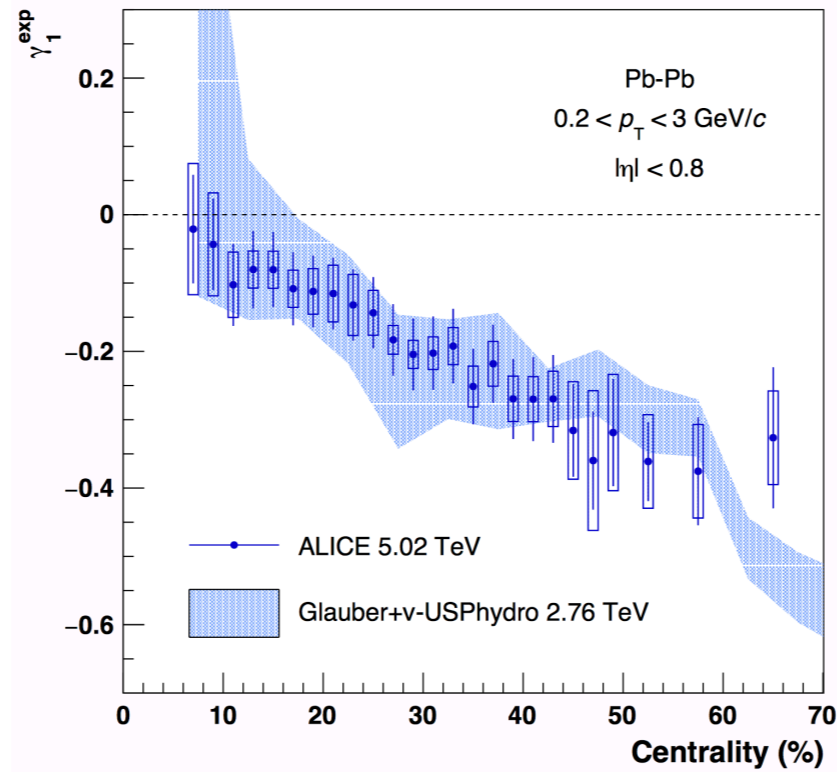
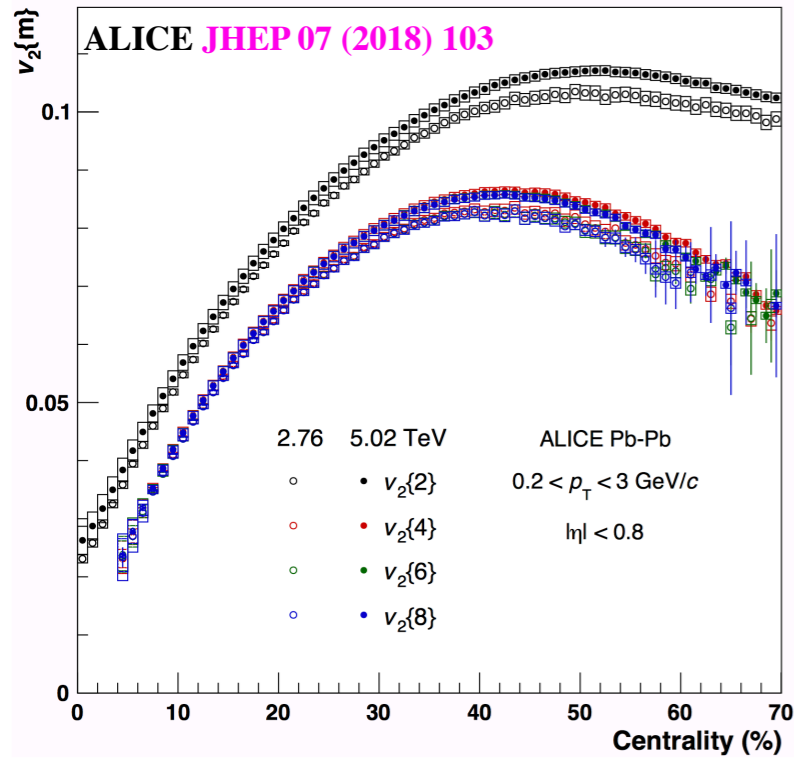
$$\gamma_2 \simeq \gamma_2^{\text{expt}} \equiv -\frac{3v_2\{4\}^4 - 12v_2\{6\}^4 + 11v_2\{8\}^4}{2(v_2\{2\}^2 - v_2\{4\}^2)^2}$$



Initial geometry fluctuations

How does v_n fluctuate

$v_n\{m\}$ → Moments → $p(v_n)$



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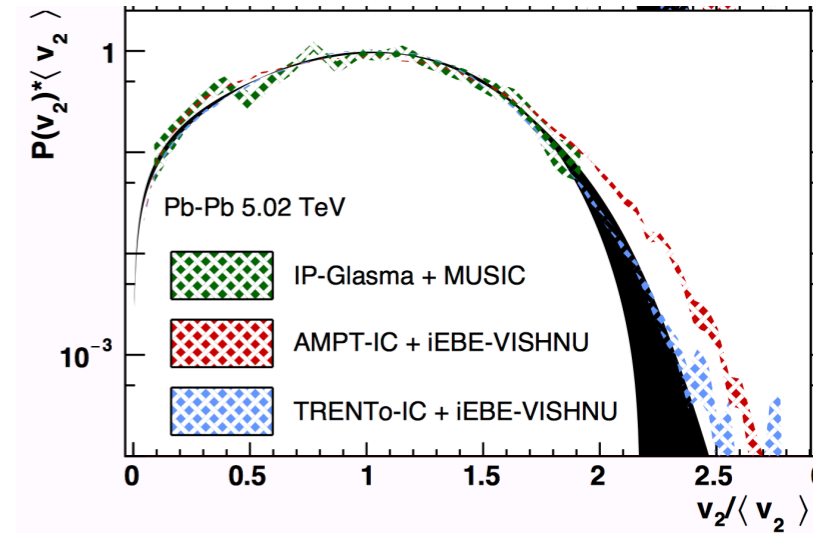
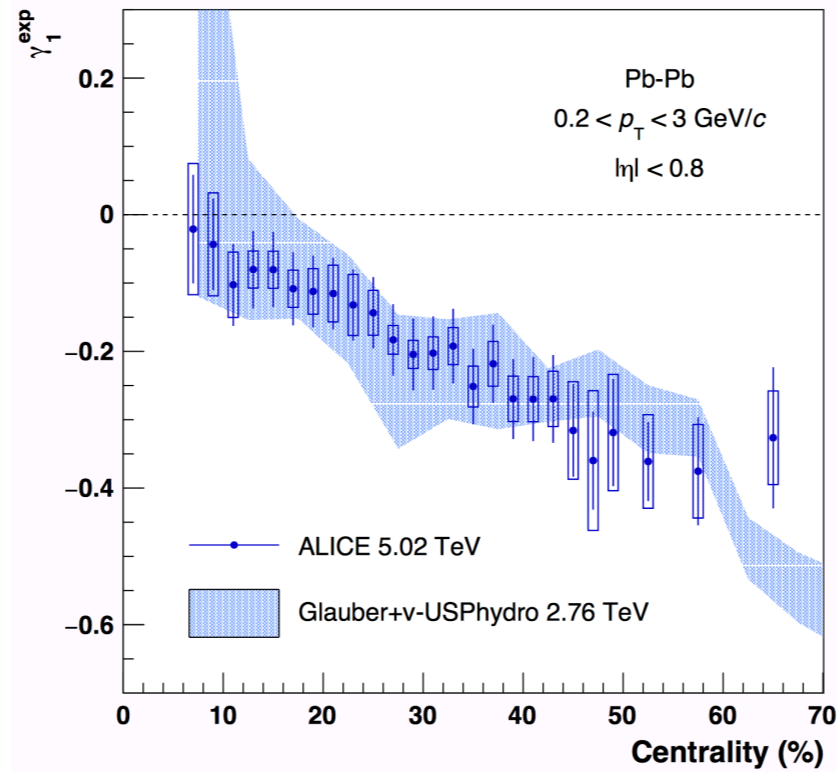
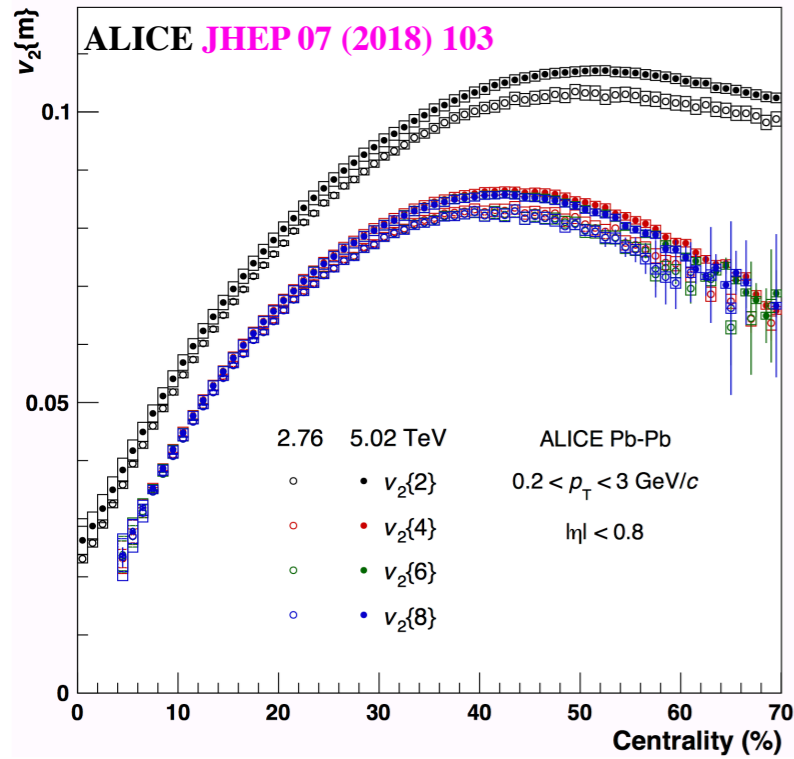
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Initial geometry fluctuations

How does v_n fluctuate

$v_n\{m\}$ → Moments → $p(v_n)$ → $p(\epsilon_n)$



$$v_n \propto \epsilon_n$$

$$P(v_n / \langle v_n \rangle) \approx P(\epsilon_n / \langle \epsilon_n \rangle)$$

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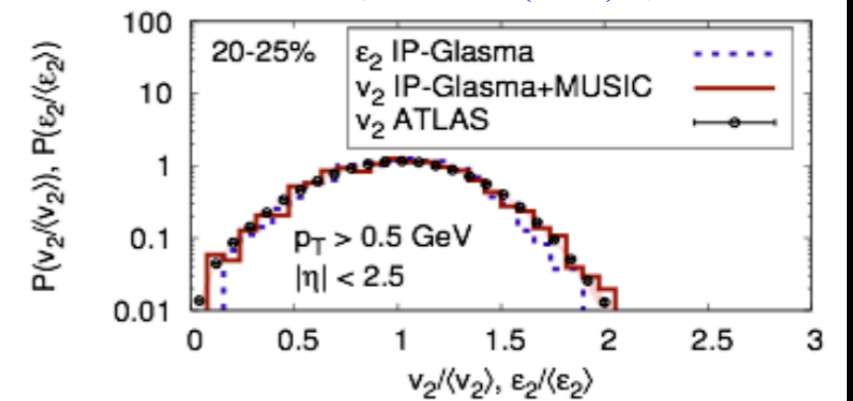
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C. Gale etc, PRL110 (2013) 1, 012302



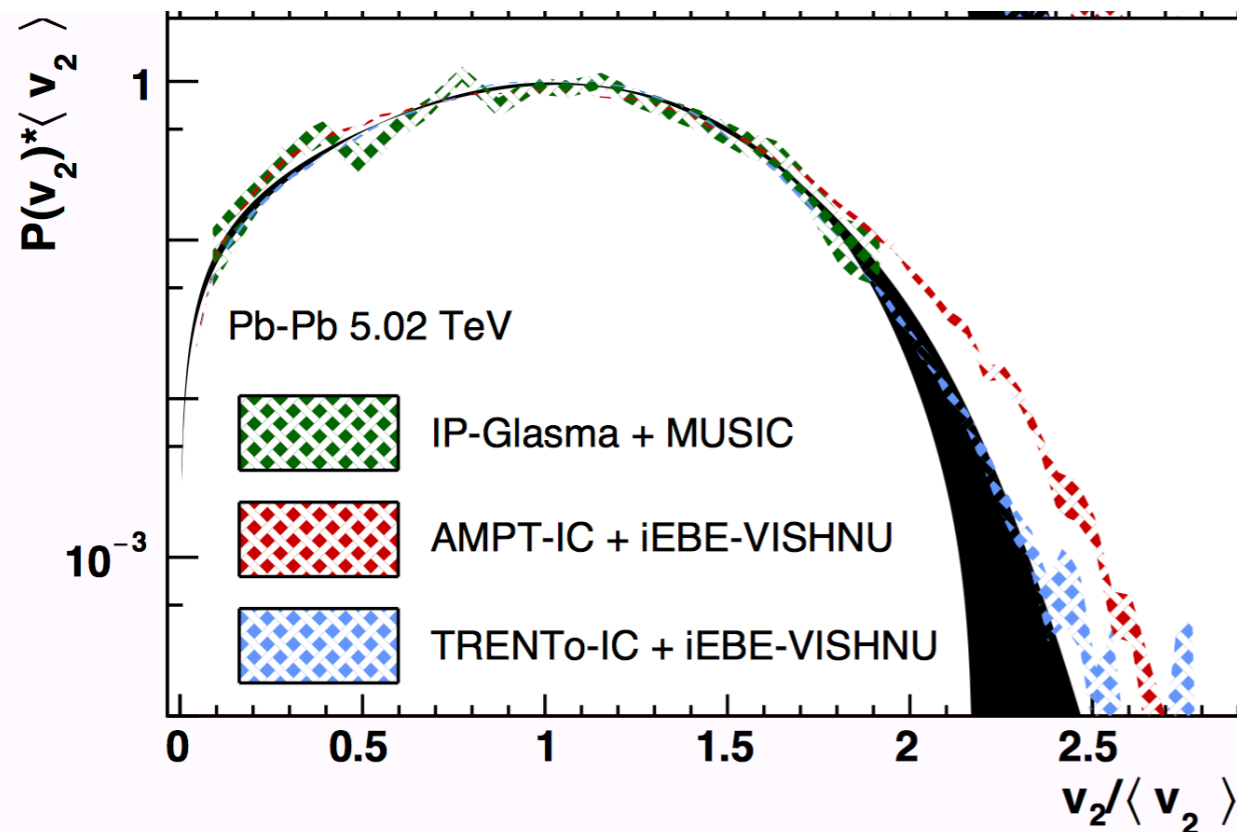
$P(v_n) \rightarrow P(\epsilon_n)$

How does v_n fluctuate

$$v_n \propto \epsilon_n$$

$$P(v_n / \langle v_n \rangle) \approx P(\epsilon_n / \langle \epsilon_n \rangle)$$

Final state $P(v_2 / \langle v_2 \rangle)$



- ❖ Despite the precision of experimental data (ALICE, ATLAS, CMS), the differences of $P(\epsilon_n)$ from various initial state models are minor

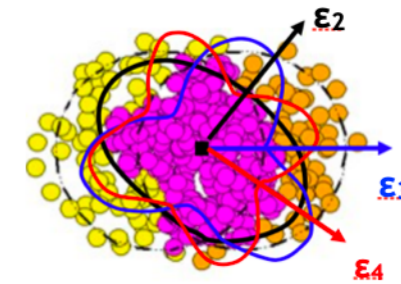


$P(v_n) \rightarrow P(\epsilon_n)$

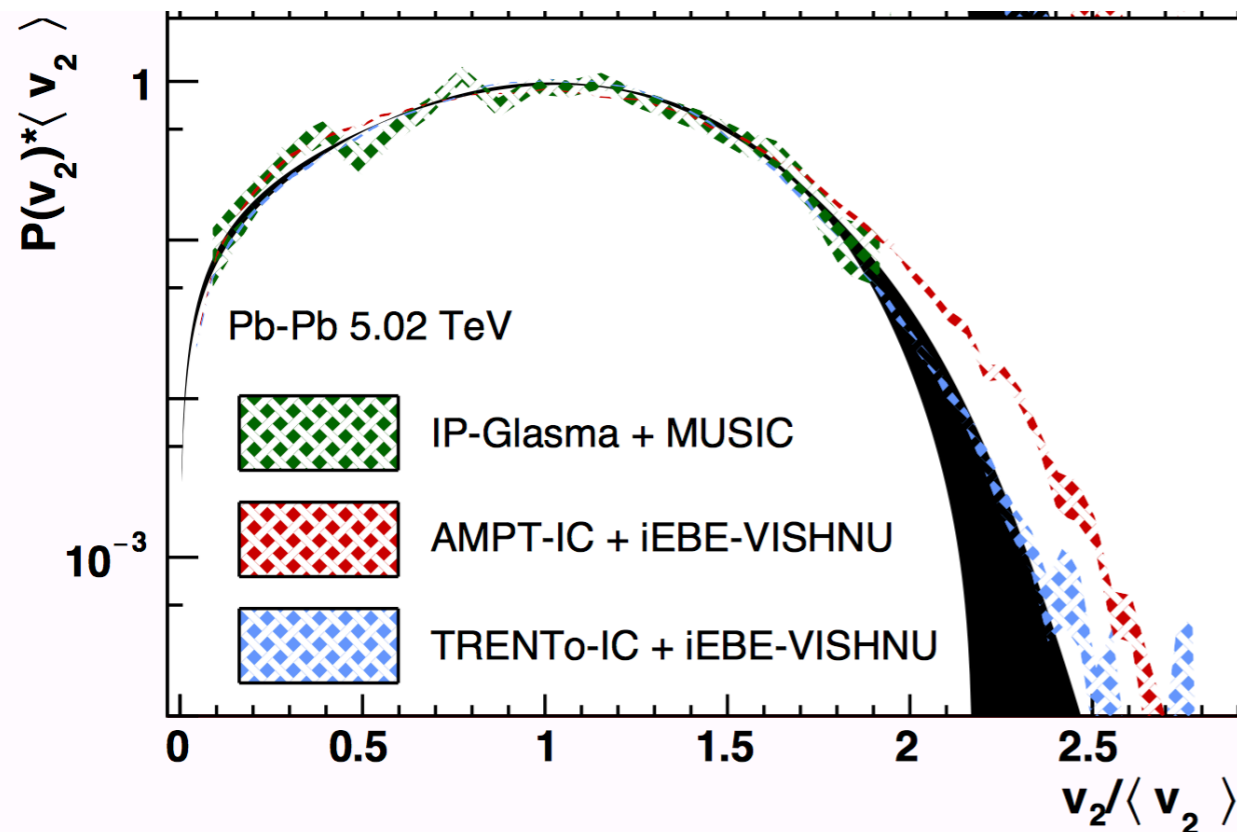
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$$v_n \propto \epsilon_n$$

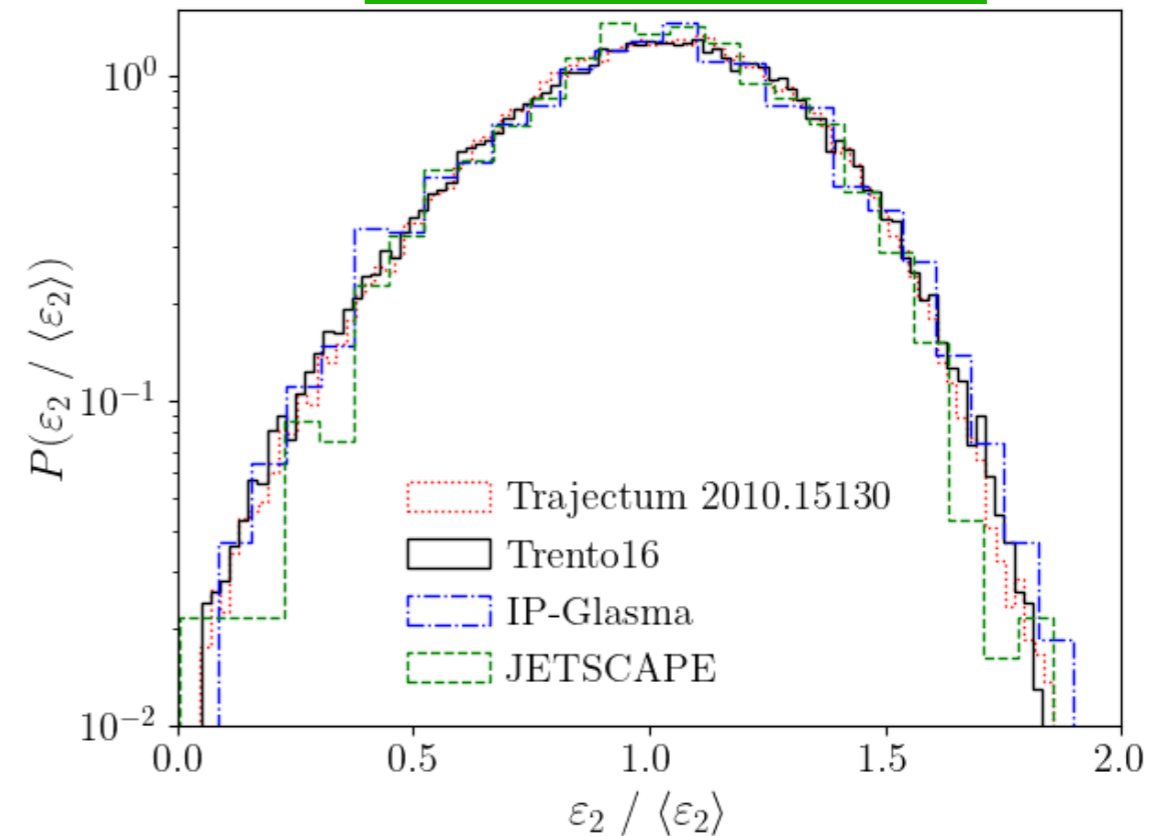
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Final state $P(v_2 / \langle v_2 \rangle)$

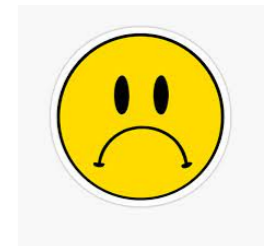


Initial state $P(\epsilon_2 / \langle \epsilon_2 \rangle)$



Minor difference from IC

❖ Despite the precision of experimental data (ALICE, ATLAS, CMS), the differences of $P(\epsilon_n)$ from various initial state models are minor

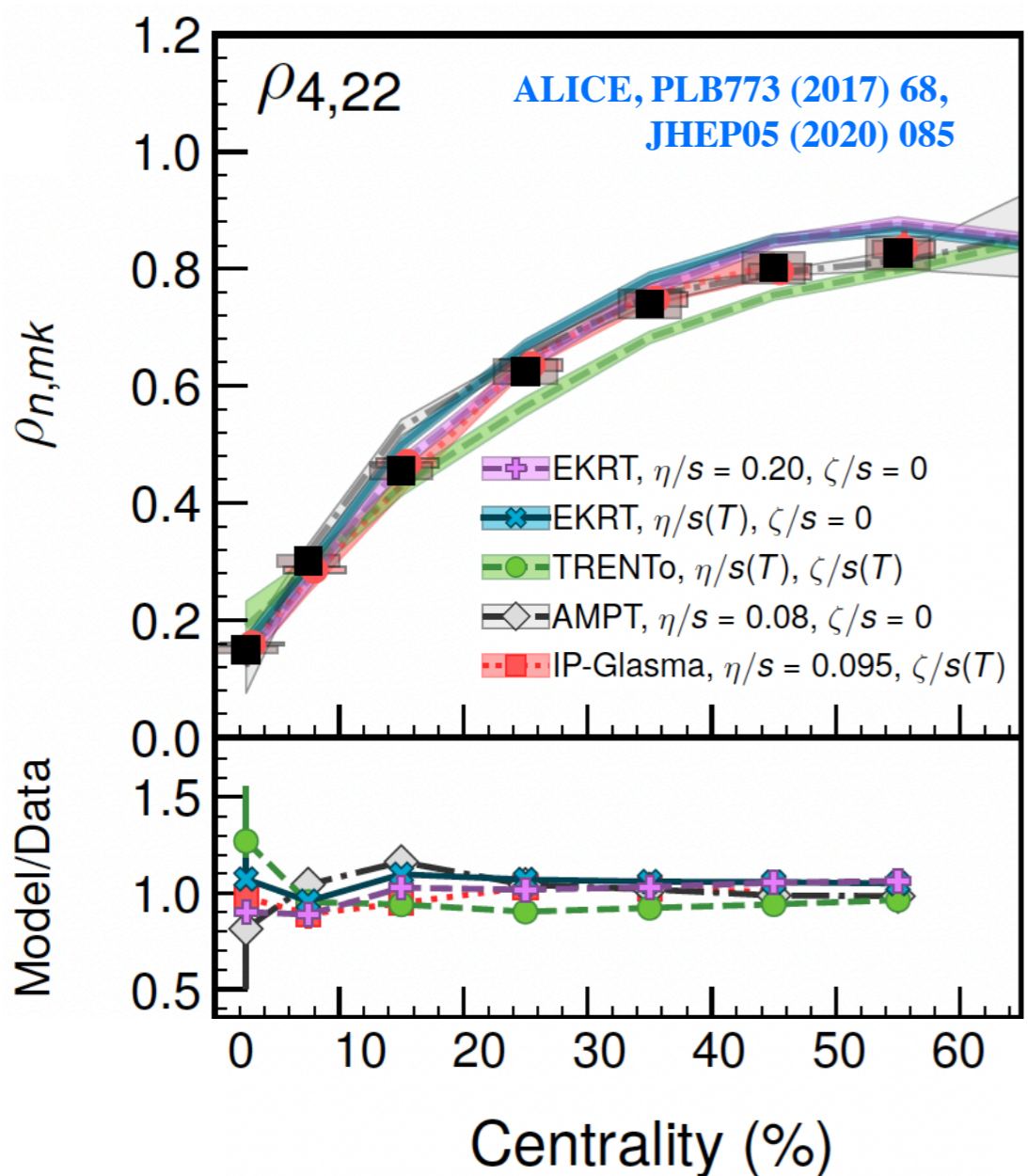
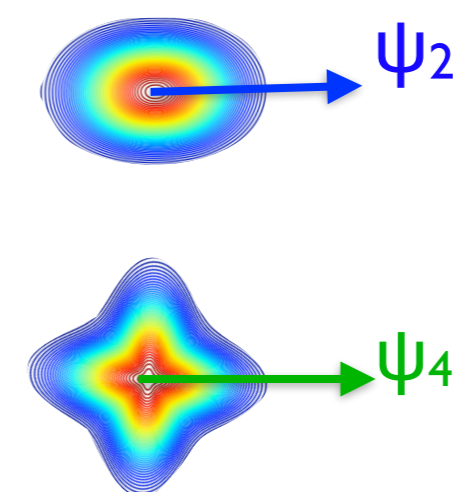


$\Psi_n - \Psi_m$ correlations

How do ψ_n and ψ_m correlate



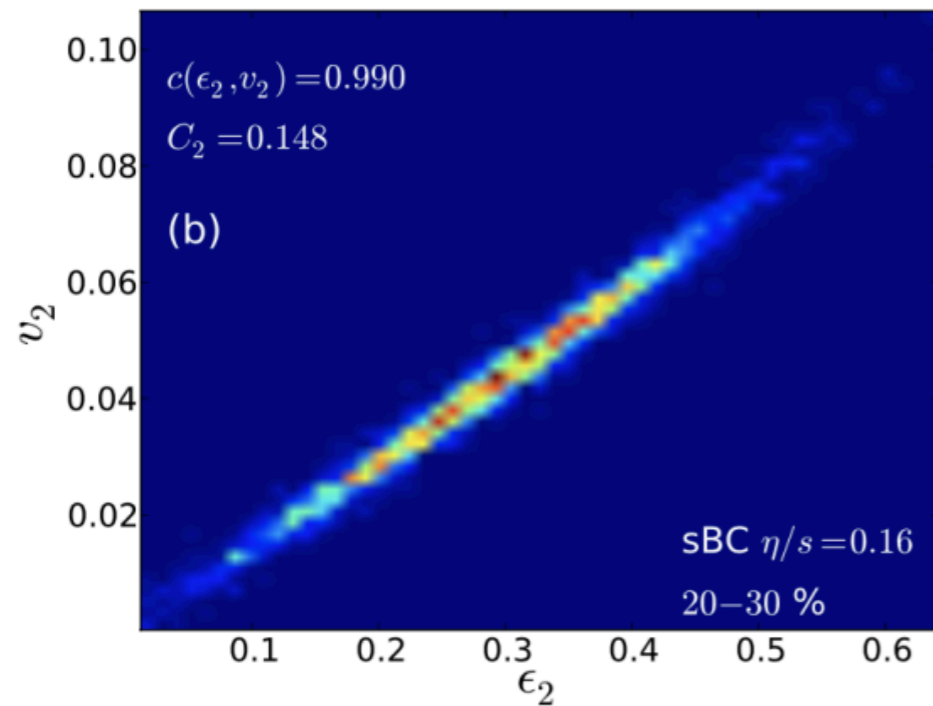
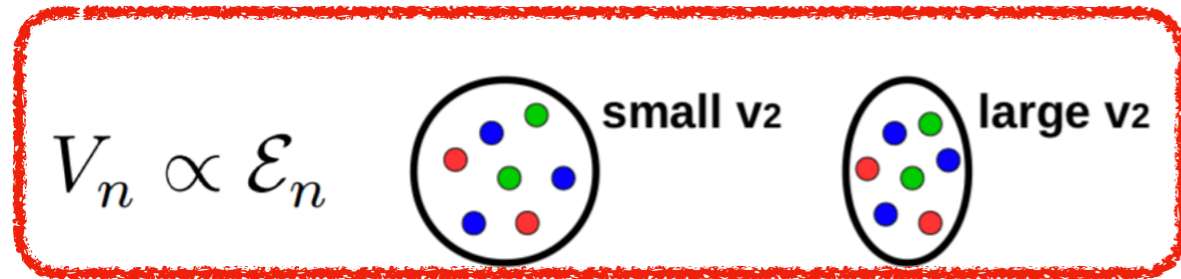
$$\rho_{422} \approx \langle \cos(4\Psi_4 - 4\Psi_2) \rangle$$



- **Central collision:**
 - Initial ϕ_2, ϕ_4 randomly fluctuate, weak correlations
 - $\langle \cos 4(\psi_2 - \psi_4) \rangle$ is small
- **Peripheral collisions:**
 - Initial ϕ_2, ϕ_4 tend to align, strong correlations
 - $\langle \cos 4(\psi_2 - \psi_4) \rangle$ is large

Initial conditions (size) through $[\rho\tau]$

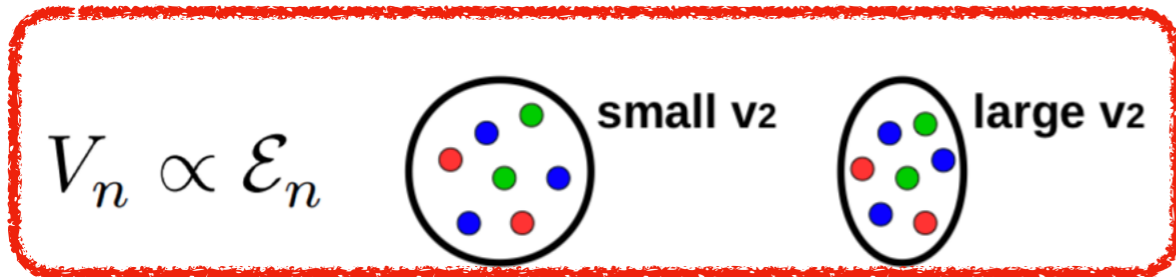
❖ Shape of the fireball: **Anisotropic flow**



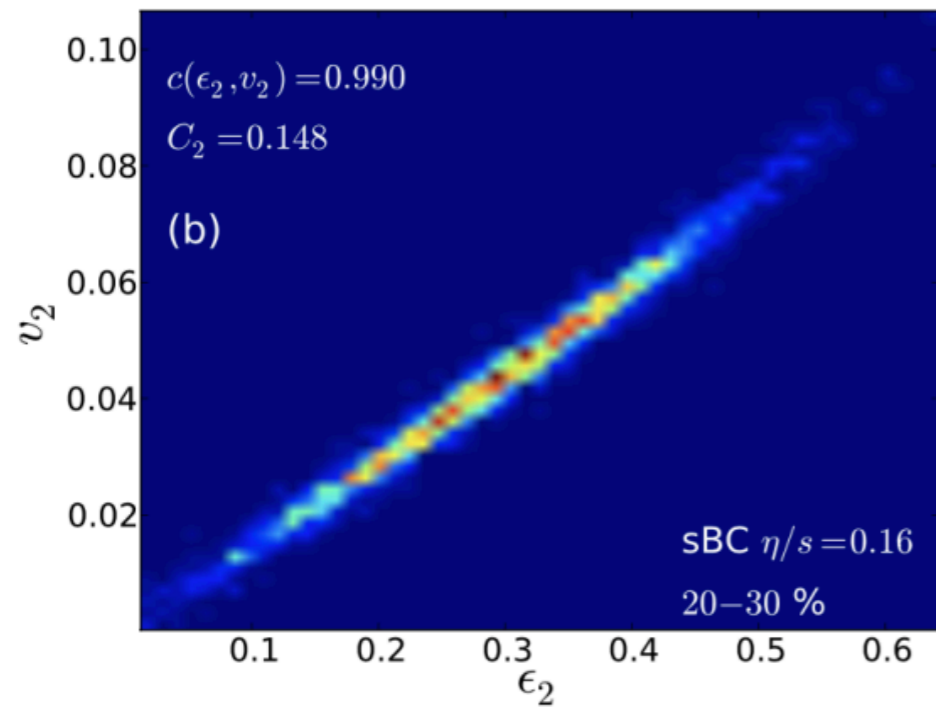
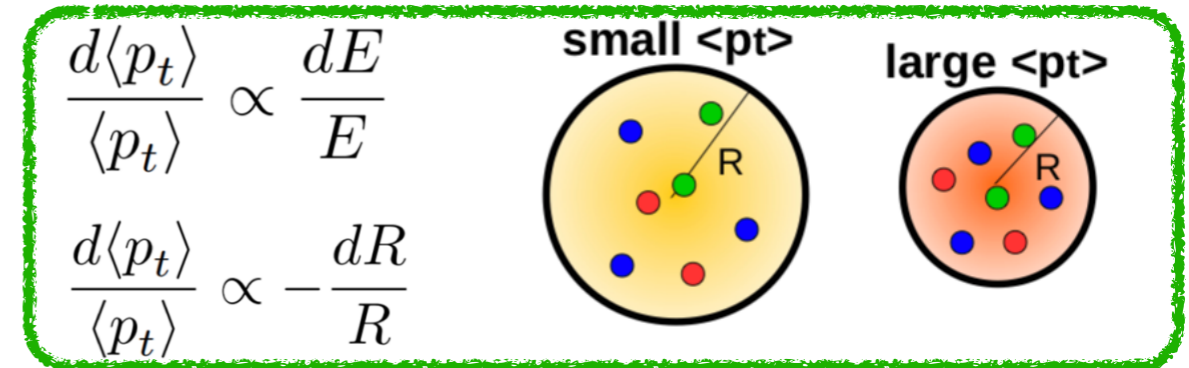
[H. Niemi et al., PRC 87 (2013) 5, 054901]

Initial conditions (size) through $[p_T]$

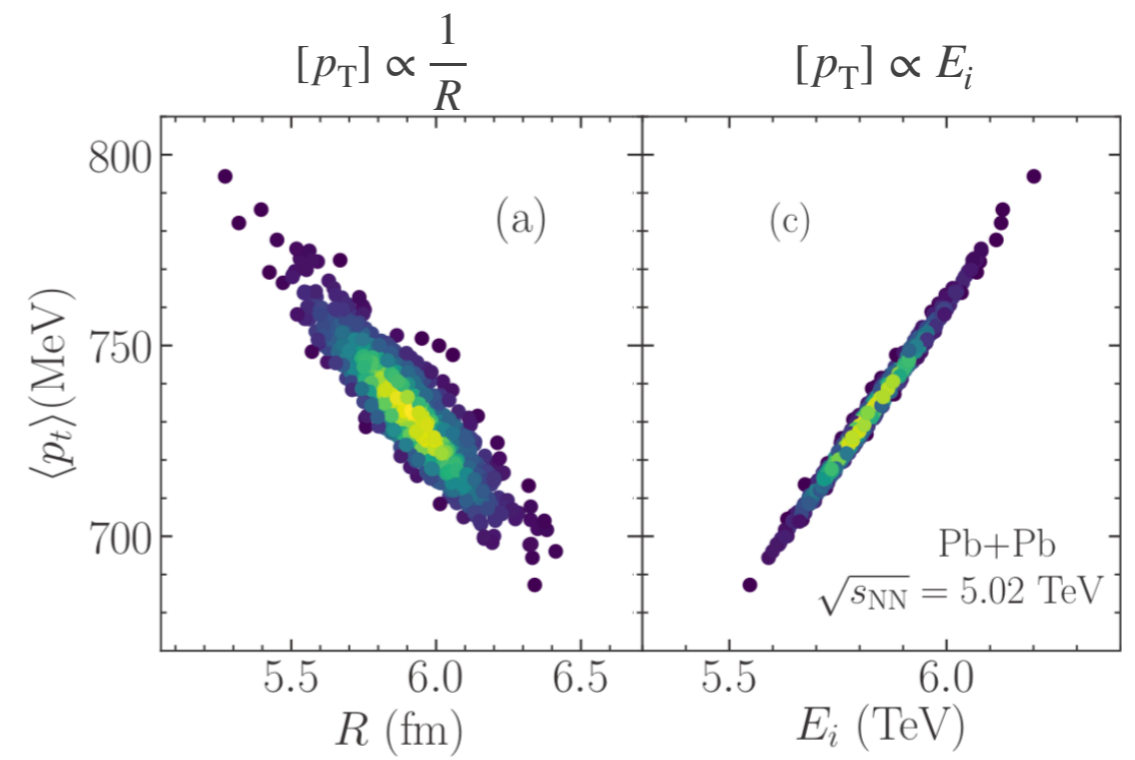
❖ Shape of the fireball: **Anisotropic flow**



❖ Size of the fireball: radial flow, $[p_T]$



[H. Niemi et al., PRC 87 (2013) 5, 054901]

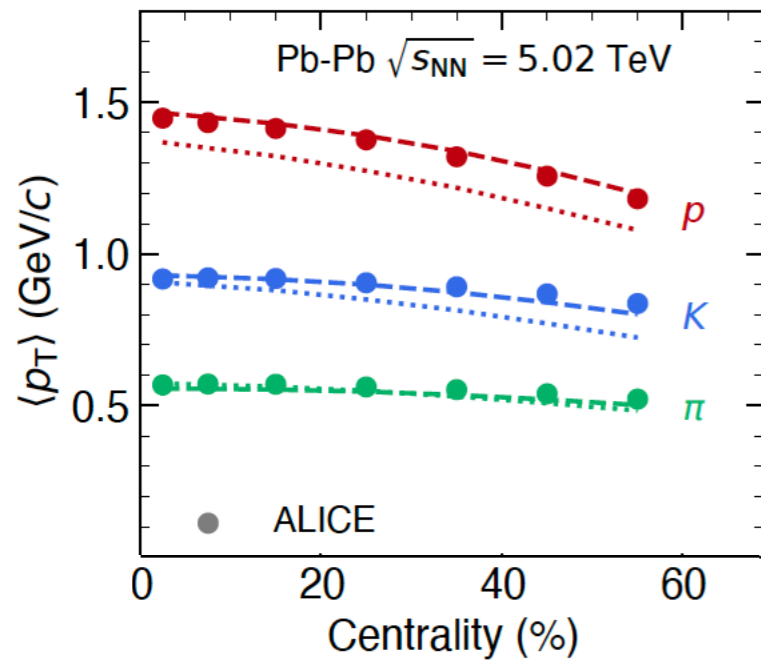


[G. Giacalone et al., PRC103 (2021) 2, 024909]



Initial conditions (size) through $[p_T]$

ALICE, PRC88 (2013) 044910, PRL111 (2013) 222301



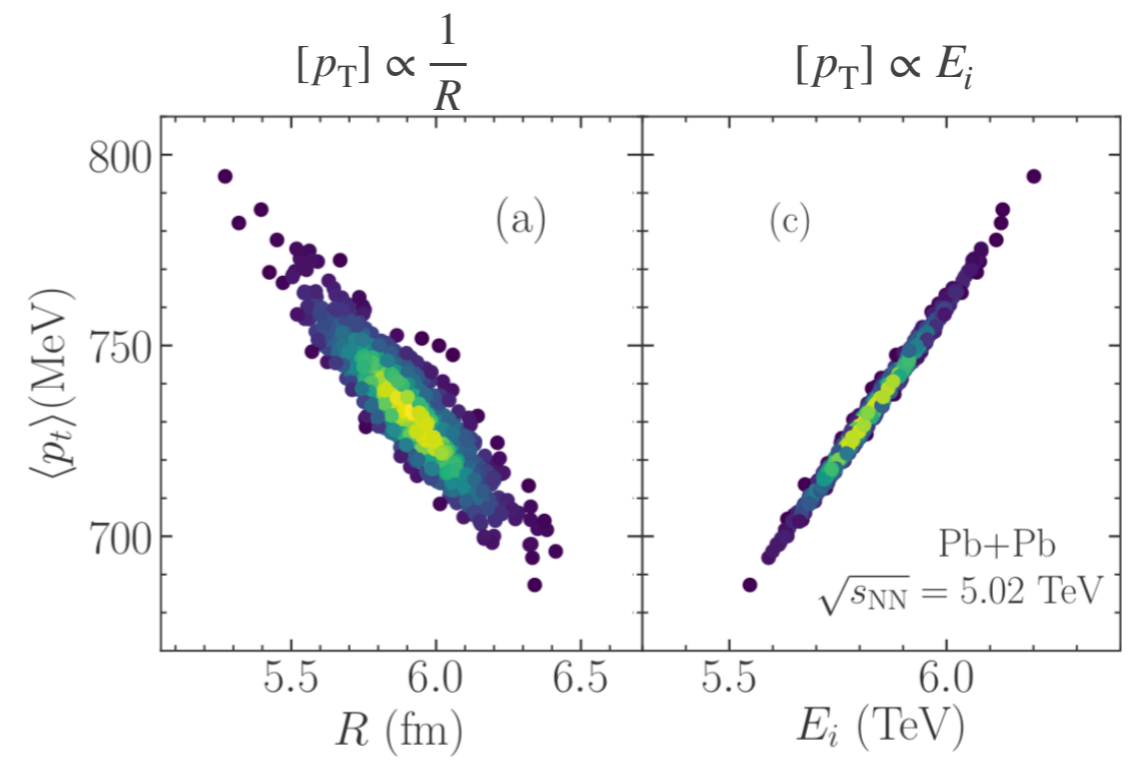
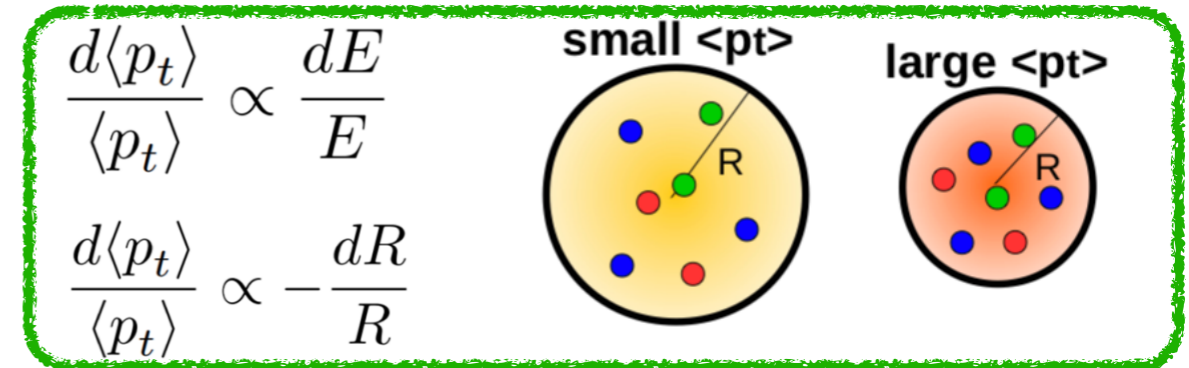
❖ Multi-particle $[p_T]$ correlations:

$$\langle p_T \rangle = \frac{\sum_{i=1}^{N_{ch}} p_{T,i}}{N_{ch}}$$

$$\langle \Delta p_{T,i} \Delta p_{T,j} \rangle = \left\langle \frac{\sum_{i \neq j}^{N_{ch}} (p_{T,i} - \langle p_T \rangle)(p_{T,j} - \langle p_T \rangle)}{N_{ch}(N_{ch} - 1)} \right\rangle_{ev}$$

$$\langle \Delta p_{T,i} \Delta p_{T,j} \Delta p_{T,k} \rangle = \left\langle \frac{\sum_{i \neq j \neq k}^{N_{ch}} (p_{T,i} - \langle p_T \rangle)(p_{T,j} - \langle p_T \rangle)(p_{T,k} - \langle p_T \rangle)}{N_{ch}(N_{ch} - 1)(N_{ch} - 2)} \right\rangle_{ev}$$

❖ Size of the fireball: radial flow, $[p_T]$

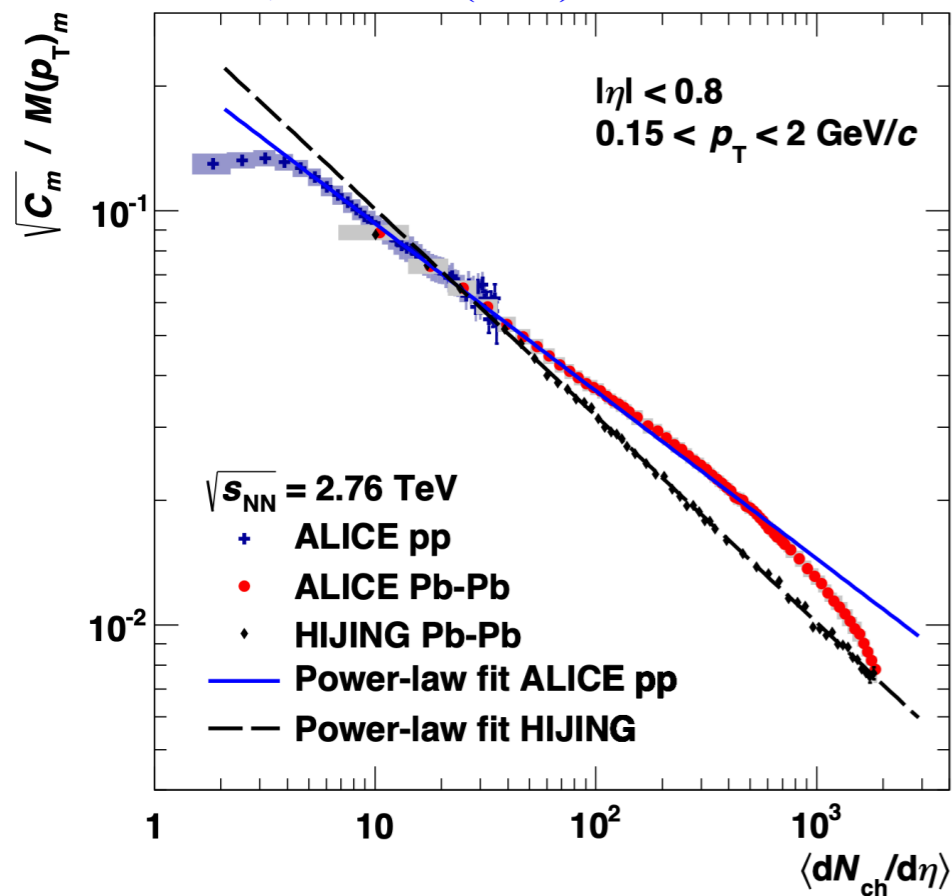


[G. Giacalone et al., PRC103 (2021) 2, 024909]



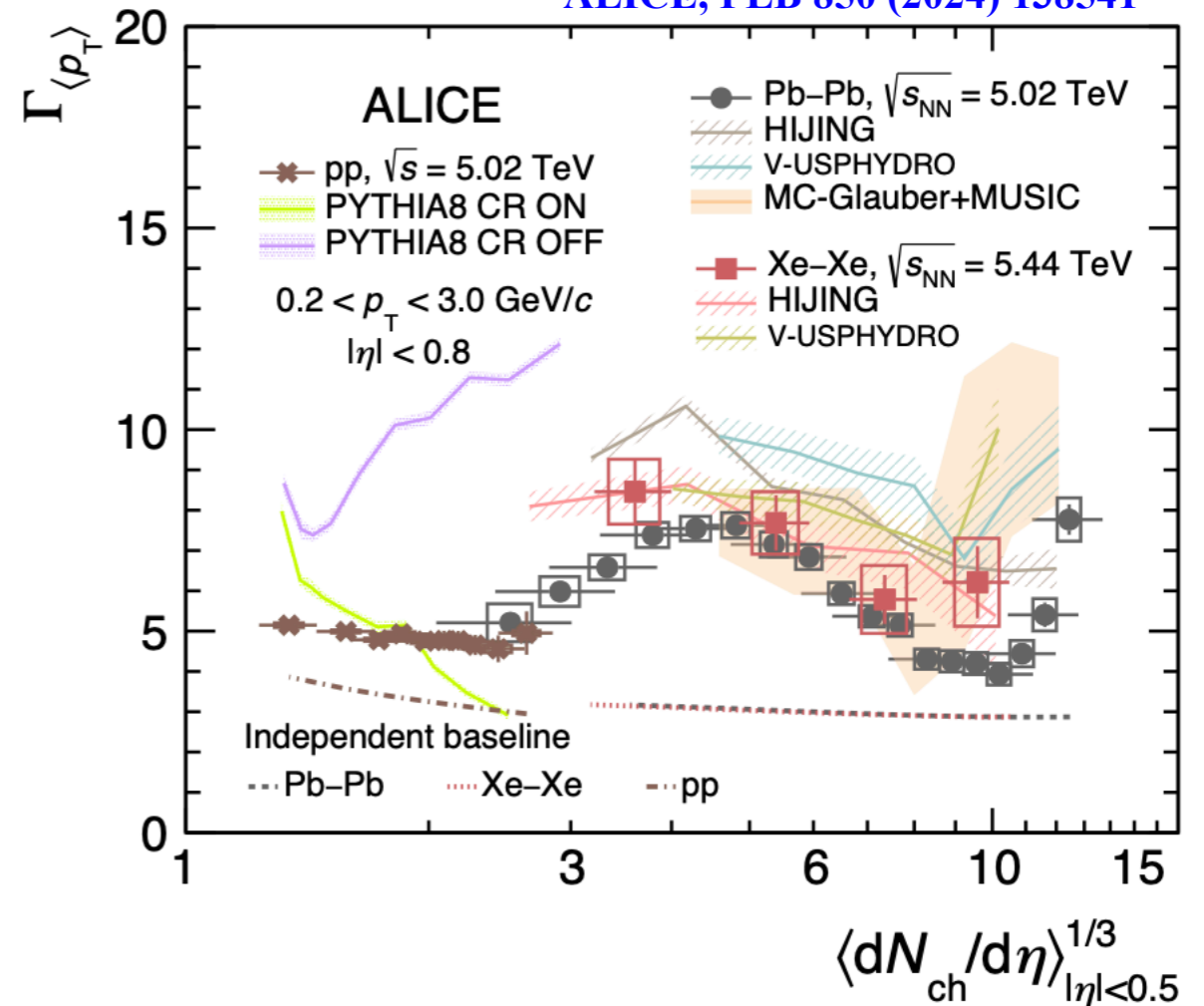
[p_T] fluctuations

ALICE, EPJC 74 (2014) 3077



2nd-moment / 1st-moment

ALICE, PLB 850 (2024) 138541



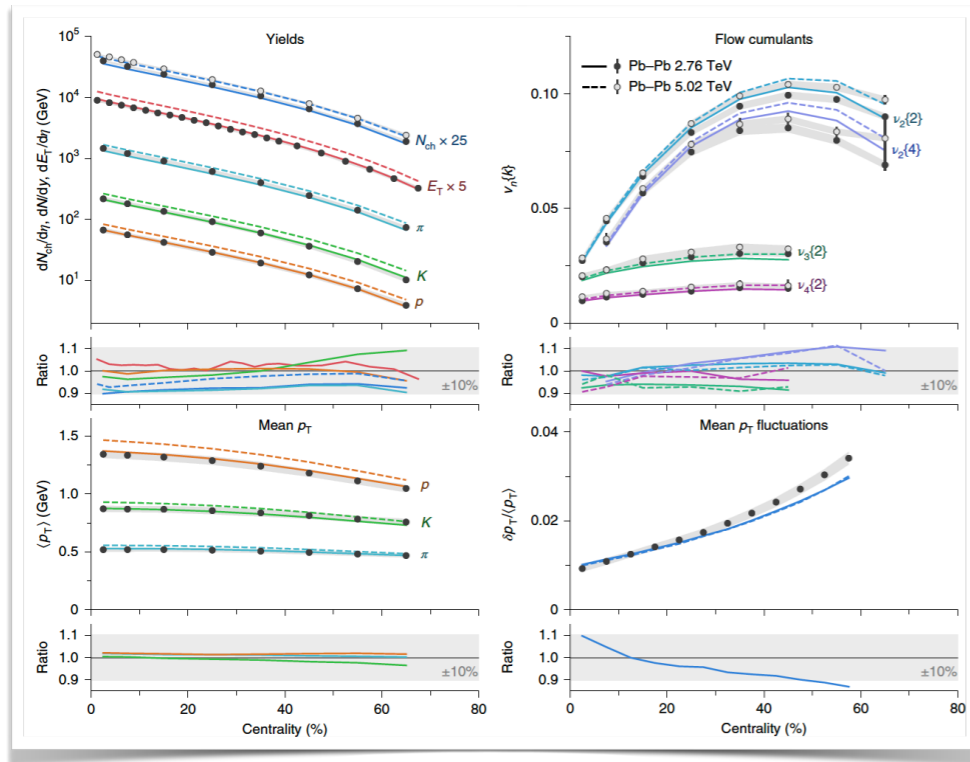
3rd-moment / 2nd-moment

- [P_T] and its event-by-event fluctuations measured in heavy-ion collisions at the LHC -> probe initial **size** and **size fluctuations**



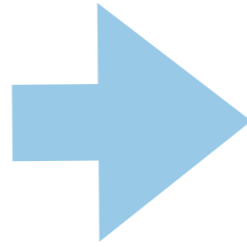
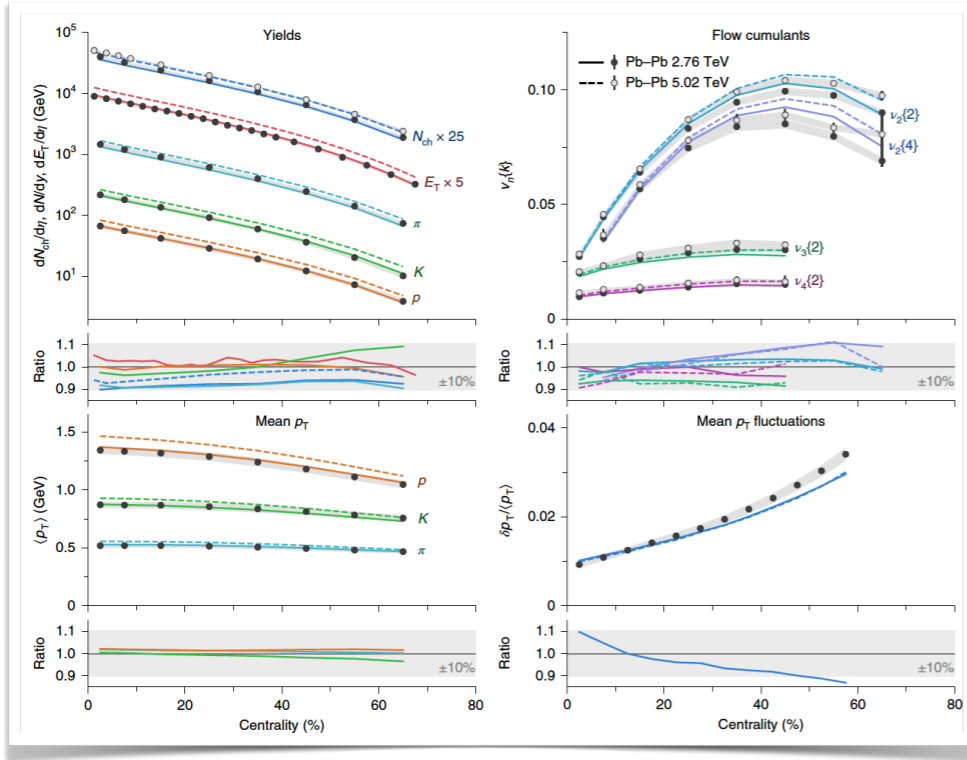
Bayesian analyses: status before 2022

J.E. Bernhard etc, Nature Physics,15, 1113 (2019)

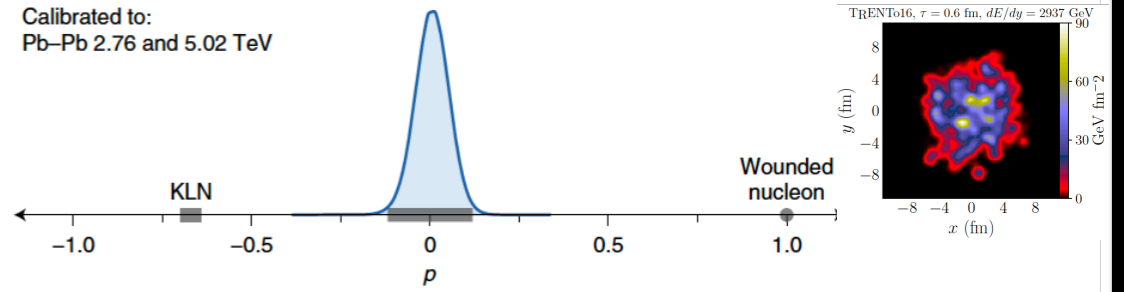


Bayesian analyses: status before 2022

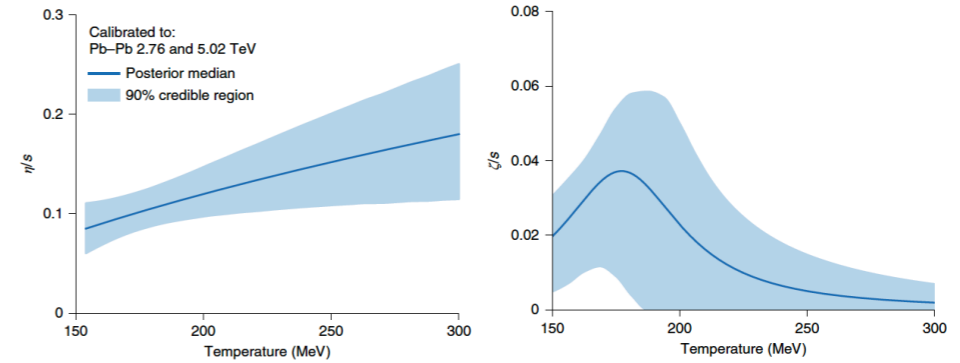
J.E. Bernhard etc, Nature Physics, 15, 1113 (2019)



Calibrated to:
Pb-Pb 2.76 and 5.02 TeV

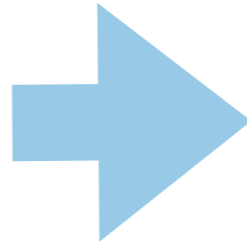
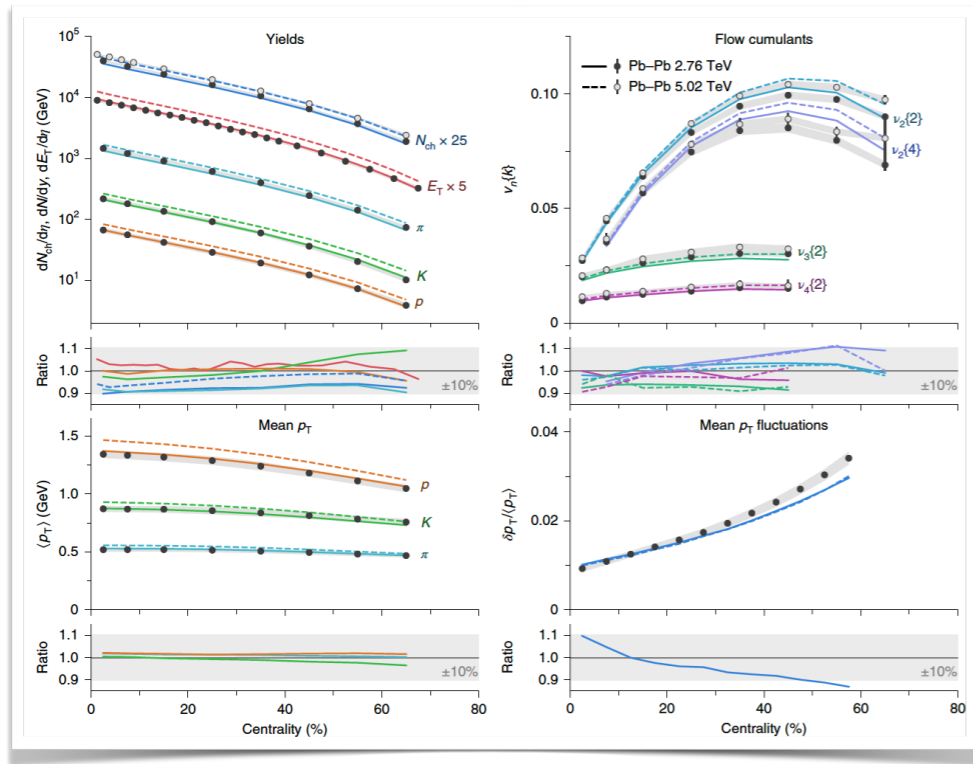


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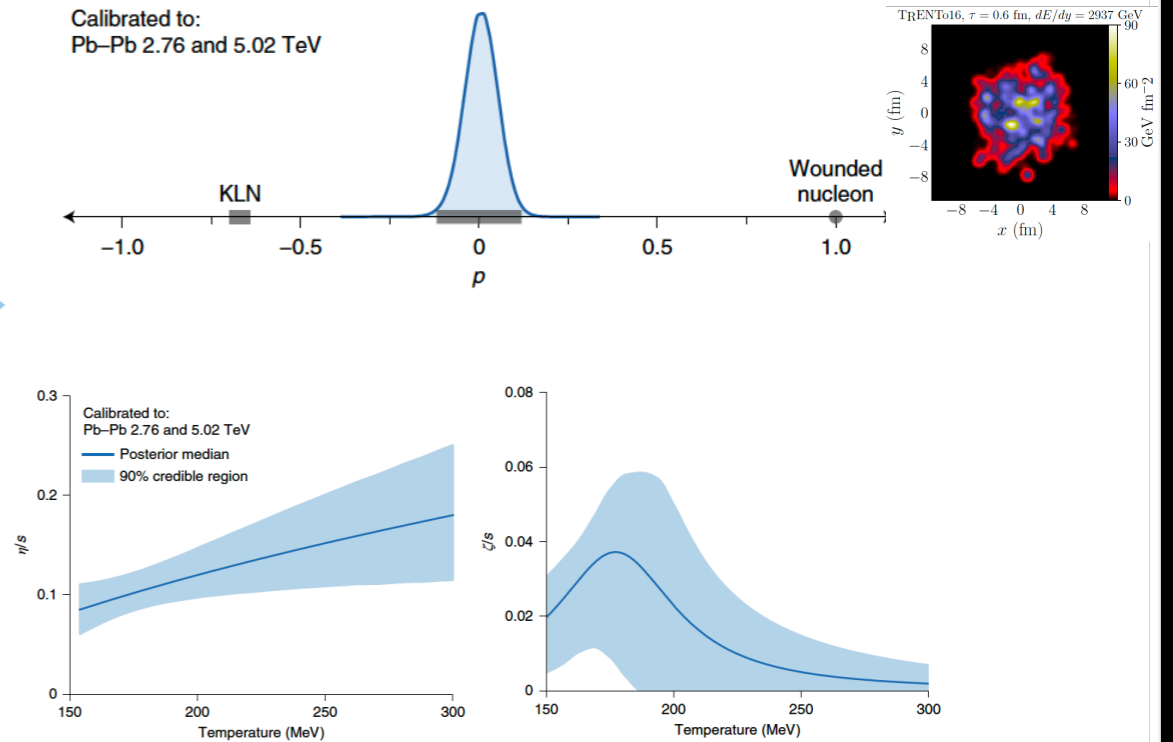


Bayesian analyses: status before 2022

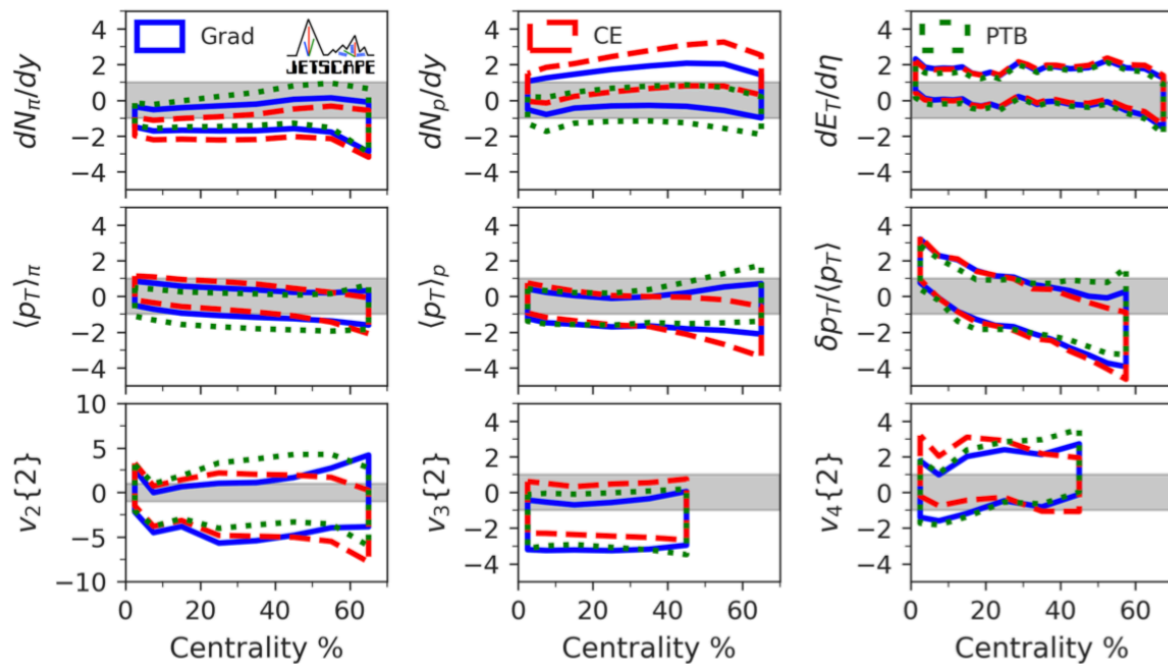
J.E. Bernhard etc, Nature Physics,15, 1113 (2019)



Calibrated to:
Pb-Pb 2.76 and 5.02 TeV

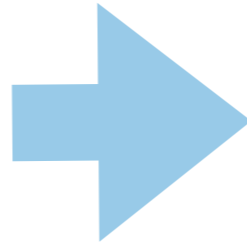
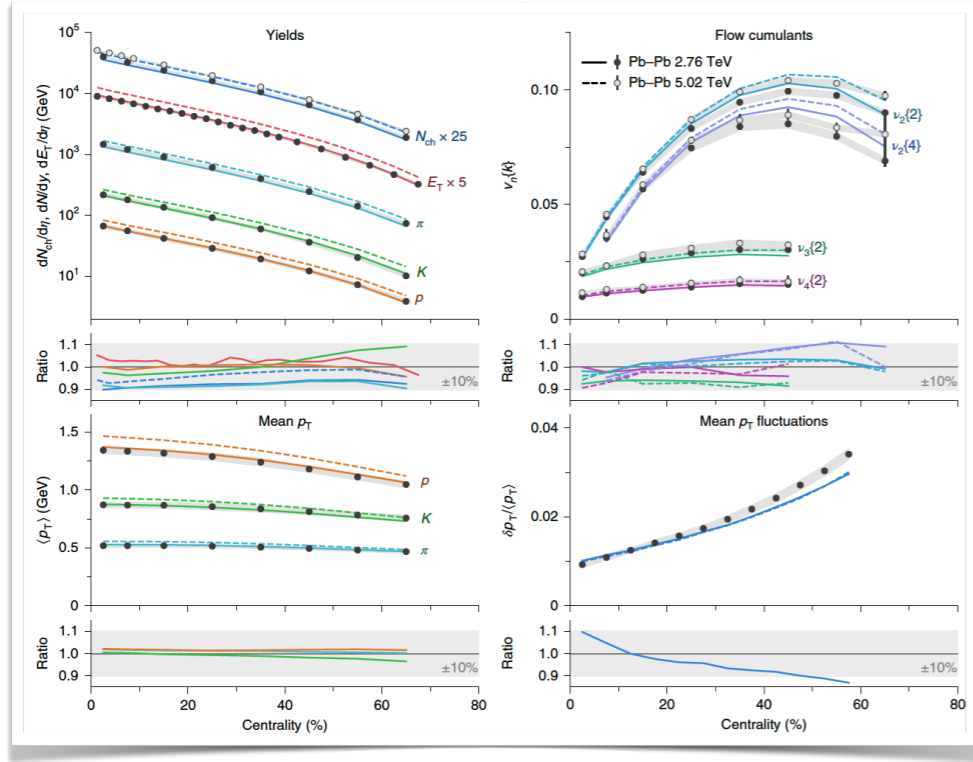


JETSCAPE, Phys. Rev. Lett. 126, 242301 (2021)

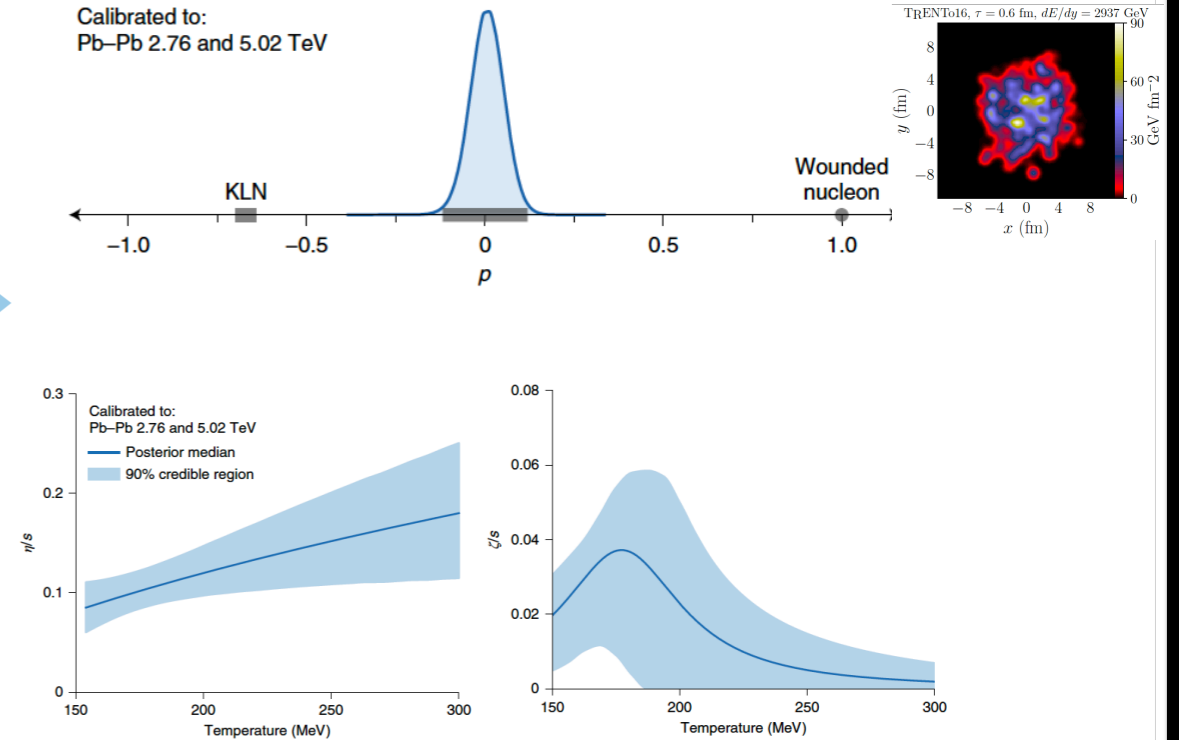


Bayesian analyses: status before 2022

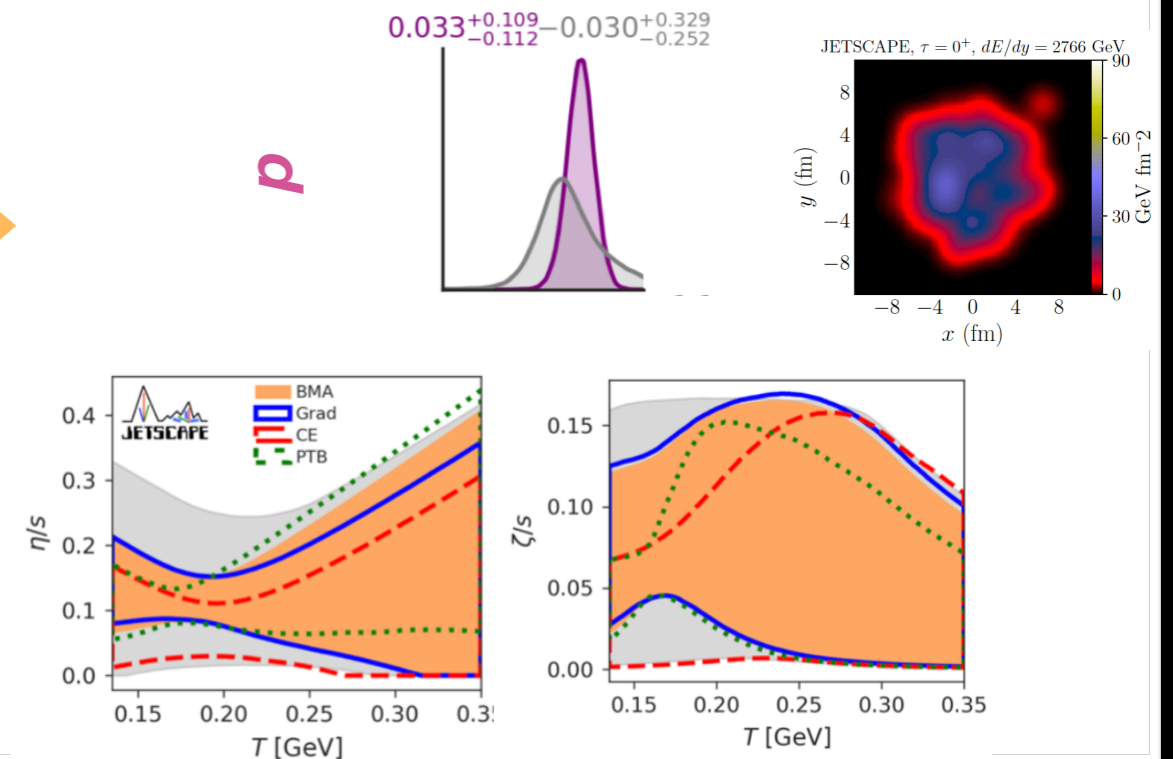
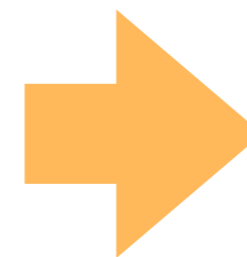
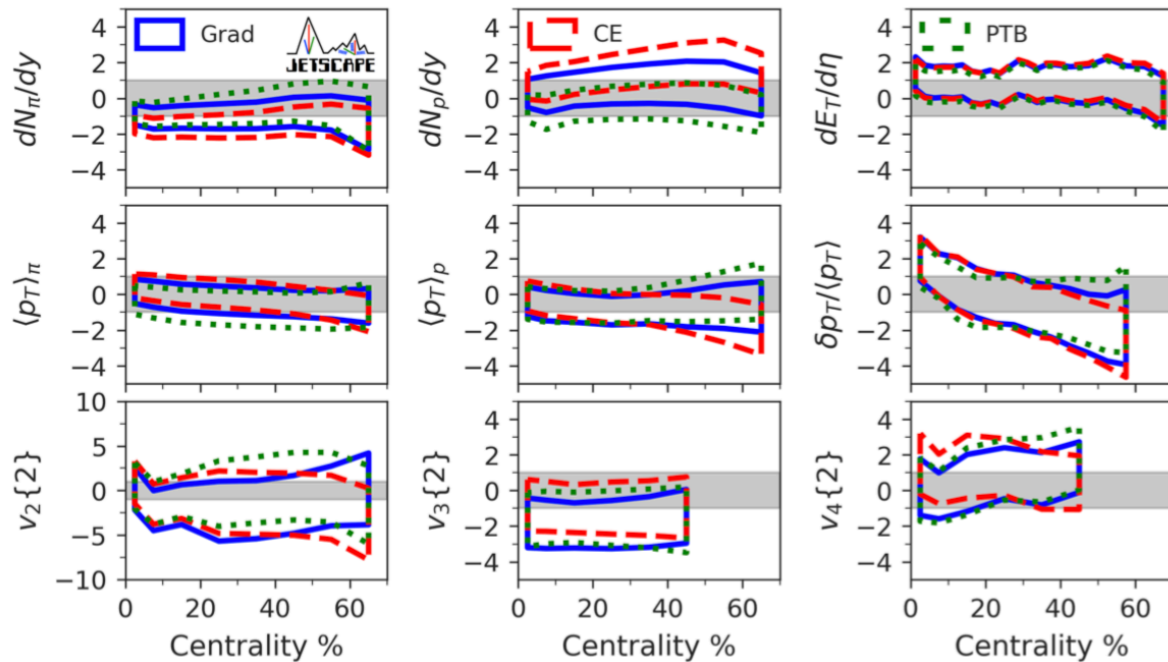
J.E. Bernhard etc, Nature Physics,15, 1113 (2019)



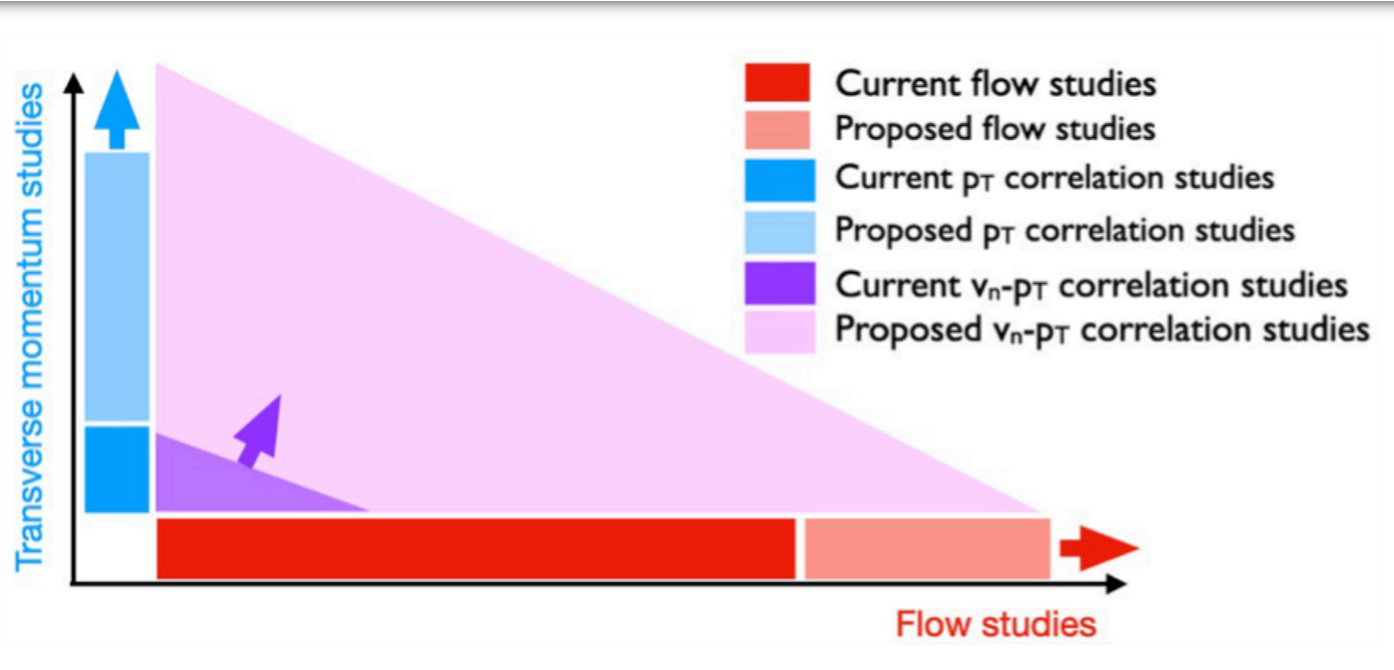
Calibrated to:
Pb-Pb 2.76 and 5.02 TeV



JETSCAPE, Phys. Rev. Lett. 126, 242301 (2021)



v_n - $[p_T]$ correlations



❖ **Shape** of the fireball: **Anisotropic flow**

❖ **Size** of the fireball: radial flow, $[p_T]$

❖ Final state: correlation between v_n and p_T

$$\rho(v_n^2, [p_T]) = \frac{\text{cov}(v_n^2, [p_T])}{\sqrt{\text{var}(v_n^2)}\sqrt{\text{var}([p_T])}}$$

P. Bozek etc, PRC96 (2017) 014904

❖ Considering $v_n \propto \varepsilon_n$, $[p_T] \propto E_0$

$$\rho(v_n^2, [p_T]) = \rho(\varepsilon_n^2, [E_0])$$

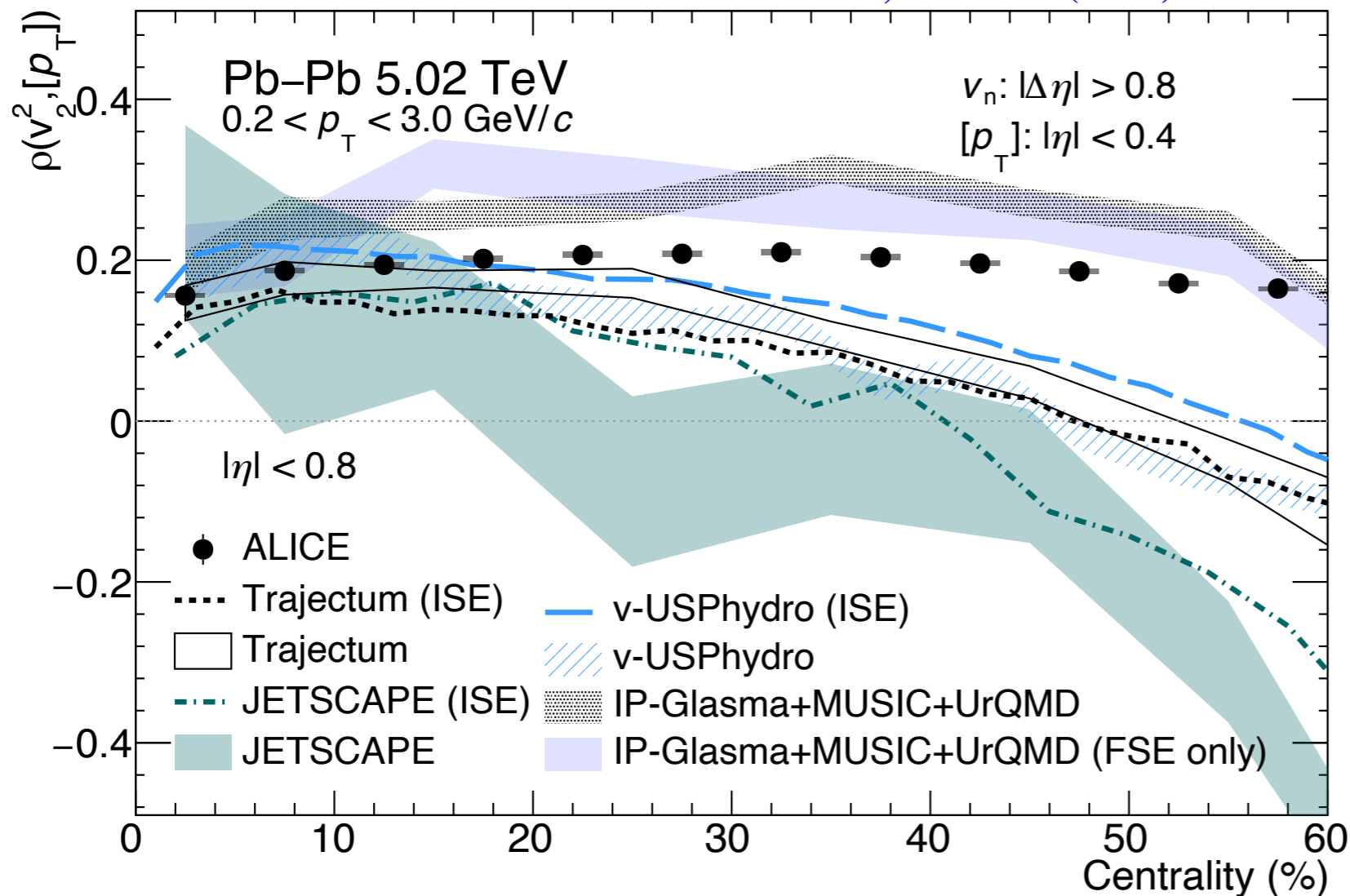
final-state model
calculation

Initial-state model
estimation

❖ One can compare $\rho(v_n^2, [p_T])$ measurements to $\rho(\varepsilon_n^2, [E_0])$ calculations, to constrain the initial state model

$\rho(v_n^2, [p_T])$ in Pb-Pb

ALICE, PLB 834 (2022) 137393



$$\rho(v_n^2, [p_T]) = \frac{\text{cov}(v_n^2, [p_T])}{\sqrt{\text{var}(v_n^2)}\sqrt{\text{var}([p_T])}}$$

v-USPhydro, PRC103 (2021) 2, 024909
 IP-Glasma, PRC102, 034905 (2020)
 JETSCAPE, PRL126, 242301 (2021)
 Privation communication
 Trajectum, PRL126, 202301 (2021)
 Privation communication

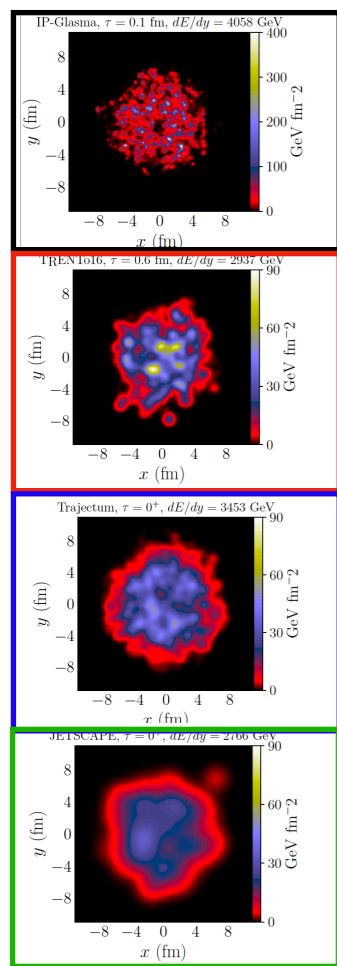
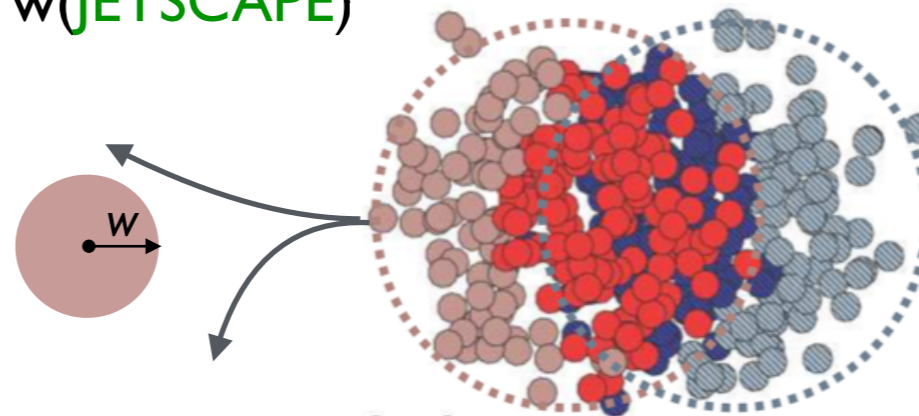
- ❖ IP-Glasma+MUSIC+UrQMD shows a weak centrality dependence and describe the data fairly well
- ❖ State-of-the-art Bayesian results (Trajectum, JETSCAPE) with TRENTo initial conditions all show strong centrality dependence, negative values for centrality >40%



Constraining nucleon width

❖ Sensitive to the nucleon width parameter (size of nucleon)

- IP-Glasma ~ 0.4 fm; v-USPhydro ~ 0.5 fm; Trajectum ~ 0.7 fm; JETSCAPE (T_RENTo) ~ 1.1 fm
- $w(\text{IP-Glasma}) < w(\text{v-USPhydro}) < w(\text{Trajectum}) < w(\text{JETSCAPE})$
- New constraints on the **nucleon size**

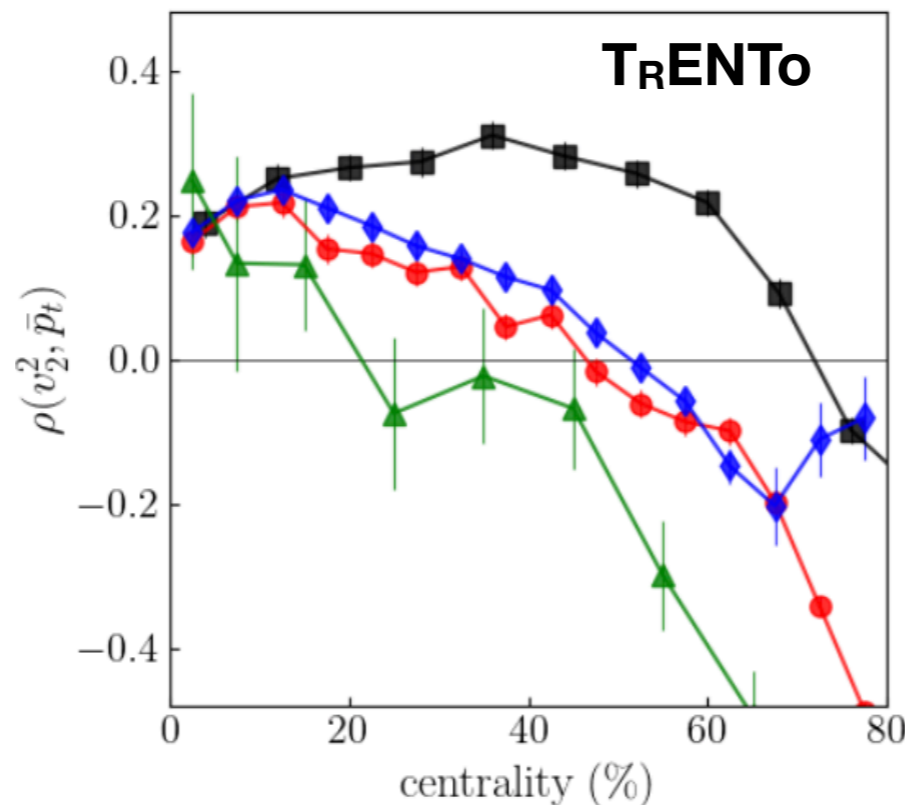


$w \sim 0.4$

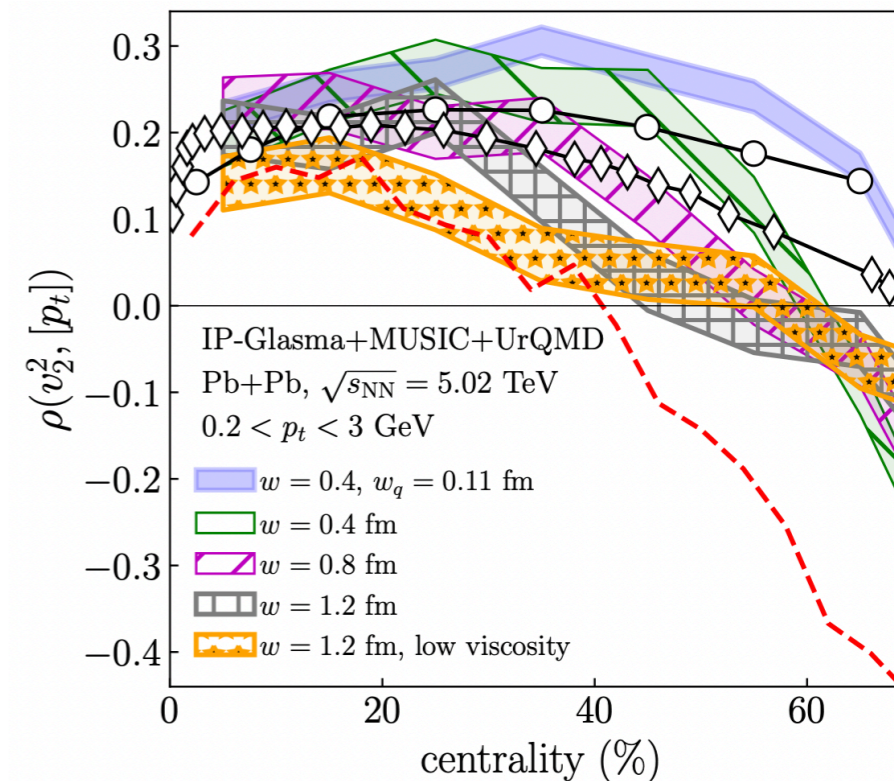
$w \sim 0.5$

$w \sim 0.7$

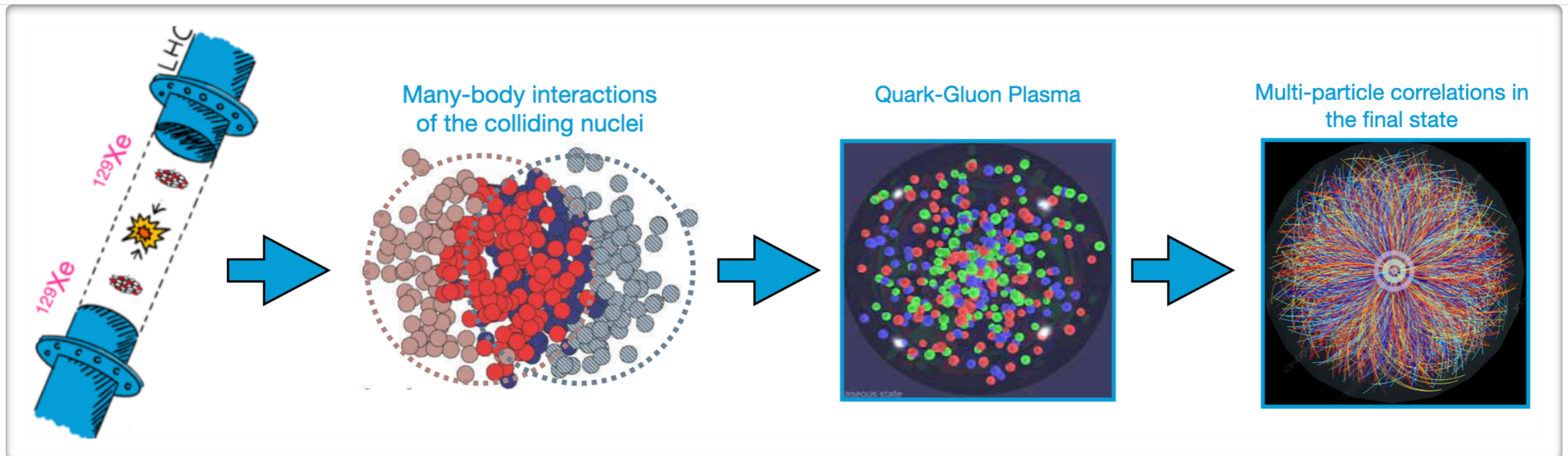
$w \sim 1.1$



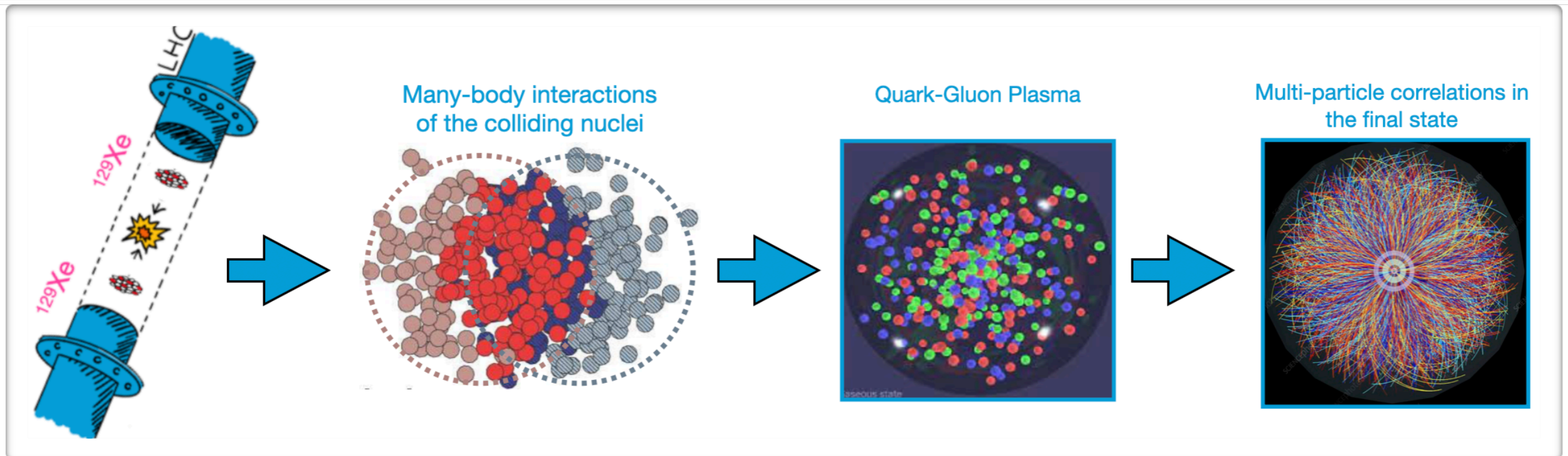
G. Giacalone etc., PRL128, 042301 (2022)



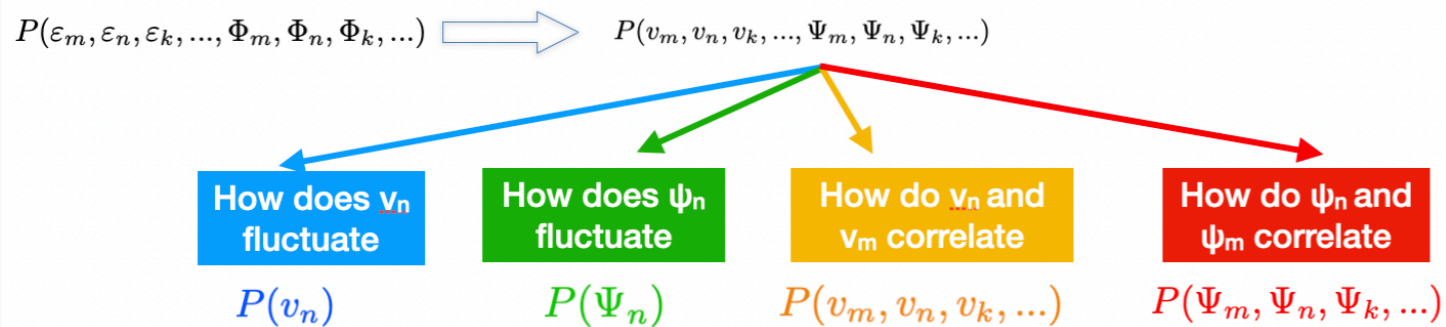
Nuclear structure at high energies



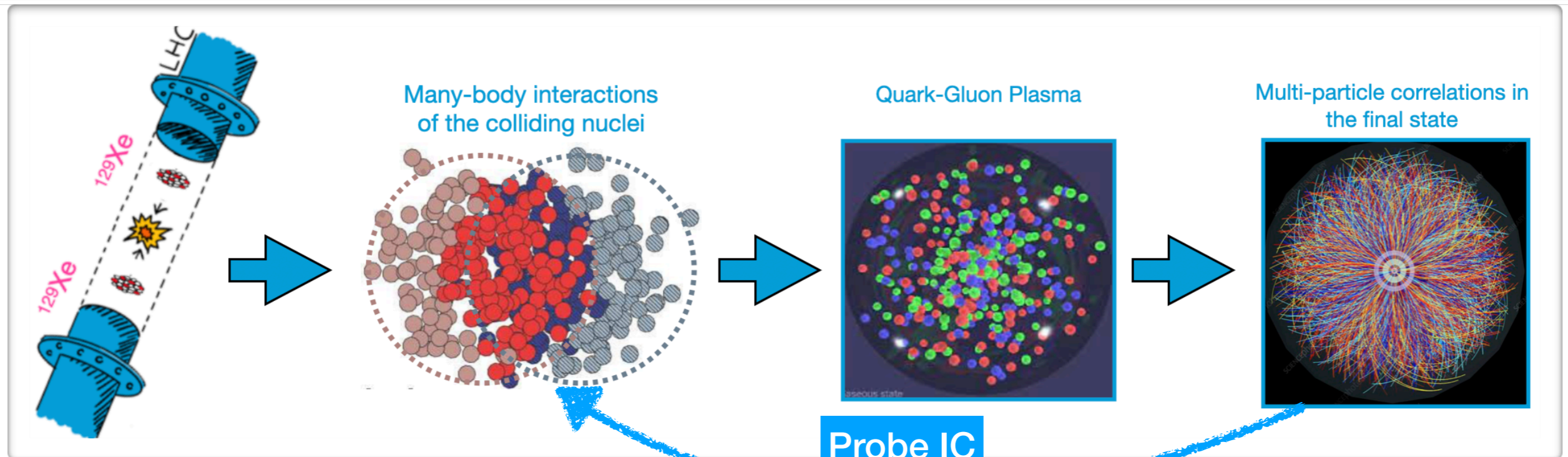
Nuclear structure at high energies



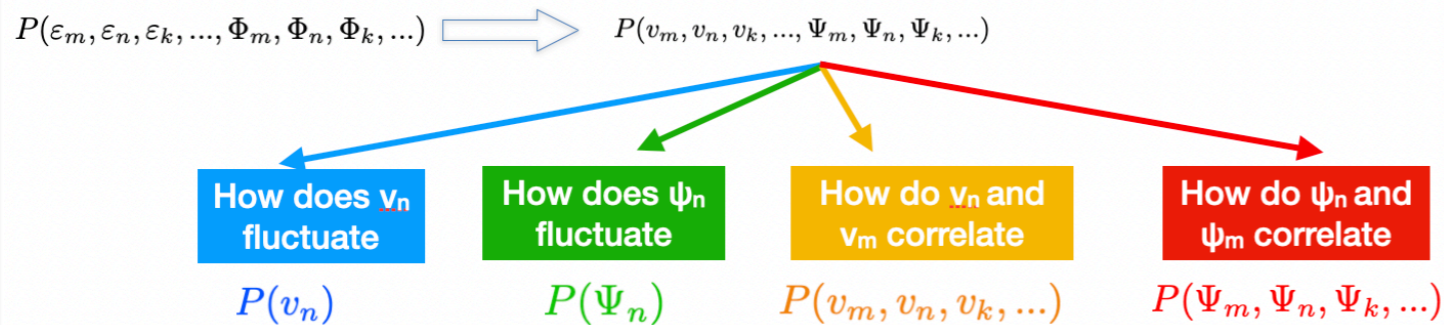
ALICE, Physics Letters B 850, 138477 (2024)
 ALICE, JHEP 05 (2023) 243
 ALICE, Phys. Rev. C Letters, 107 (2023) 051901
 ALICE, Physics Letters B 834, 137393 (2022)
 ALICE, Physics Letters B 818, 136354 (2021)
 ALICE, Phys. Rev. C 104, 024903 (2021)
 ALICE, Phys. Rev. C 103, 024913 (2021)
 ALICE, ALICE-PUBLIC-2021-004 (2021)
 ALICE, JHEP 06, 147 (2020)
 ALICE, JHEP 05, 085 (2020)
 ALICE, Eur. Phys. J. C 80, 846 (2020)
 ALICE, Physics Letters B784 (2018) 82
 ALICE, Phys. Rev. C 97, 024906 (2018)
 ALICE, JHEP07 (2018) 103



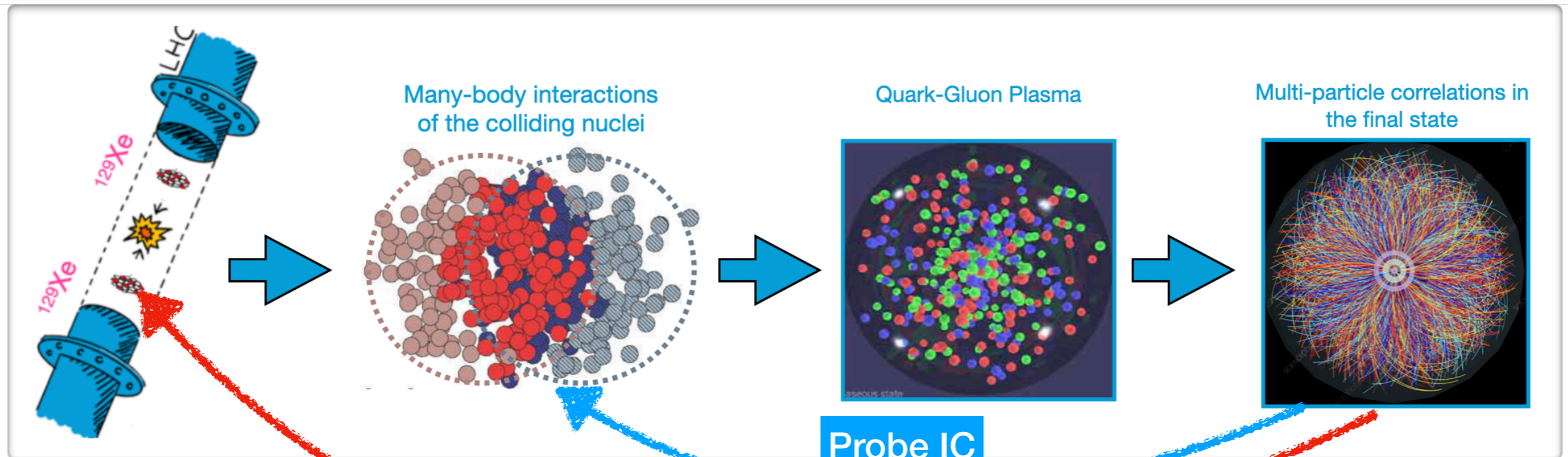
Nuclear structure at high energies



ALICE, Physics Letters B 850, 138477 (2024)
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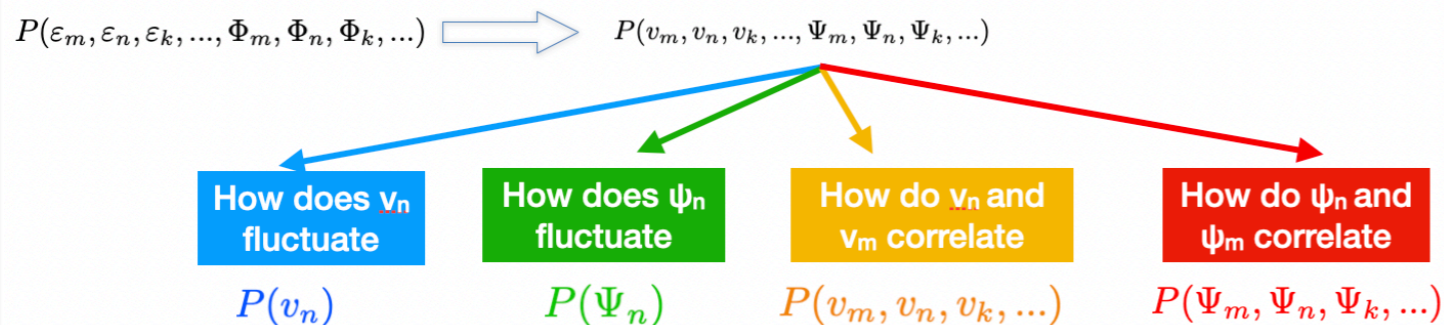


Nuclear structure at high energies



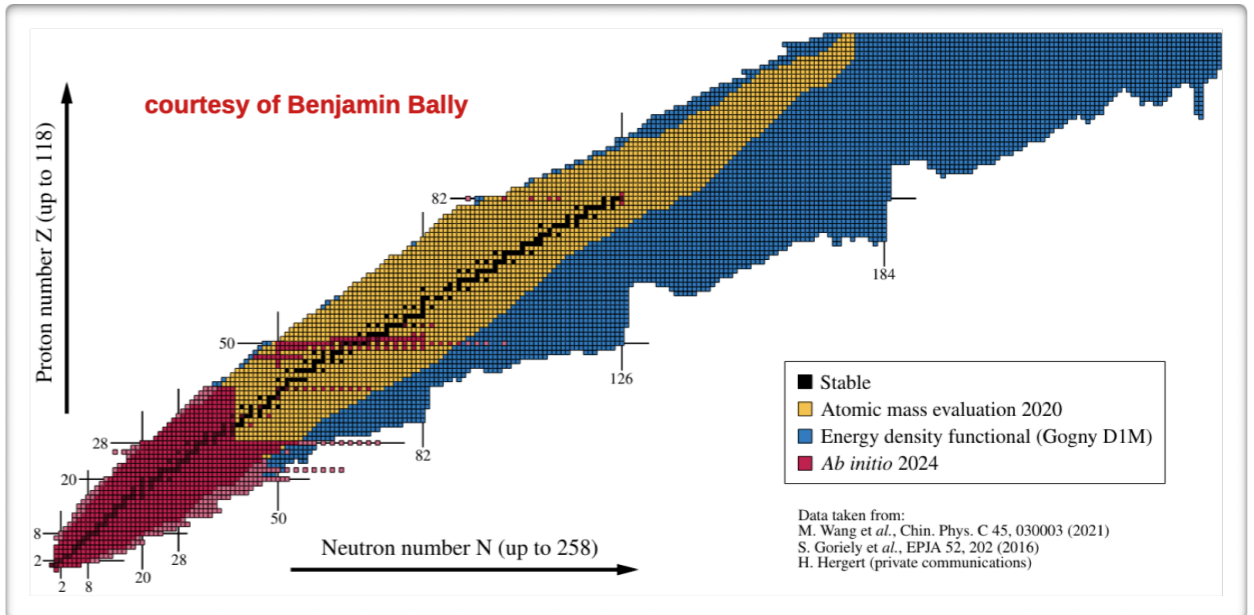
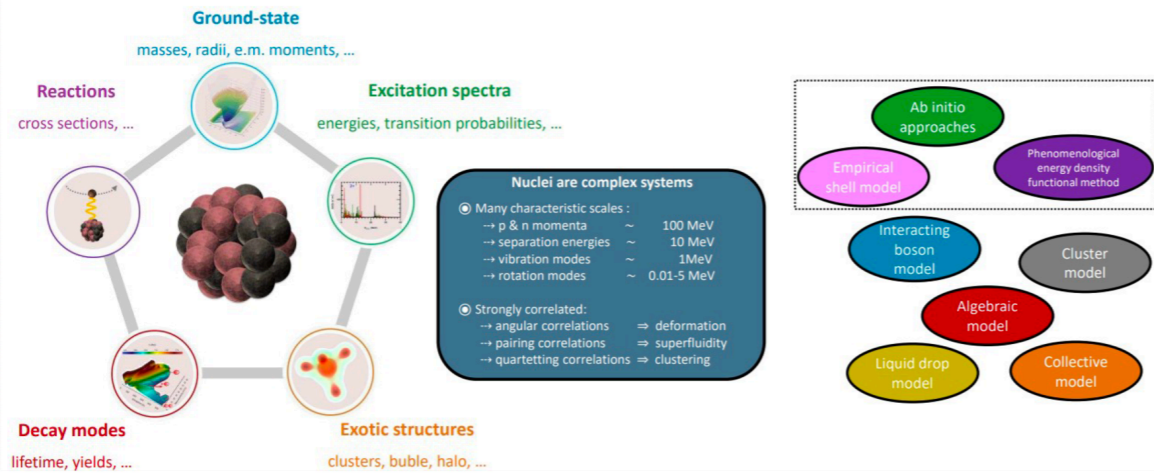
Imagine technique

ALICE, Physics Letters B 850, 138477 (2024)
 ALICE, JHEP 05 (2023) 243
 ALICE, Phys. Rev. C Letters, 107 (2023) 051901
 ALICE, Physics Letters B 834, 137393 (2022)
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 ALICE, Phys. Rev. C 104, 024903 (2021)
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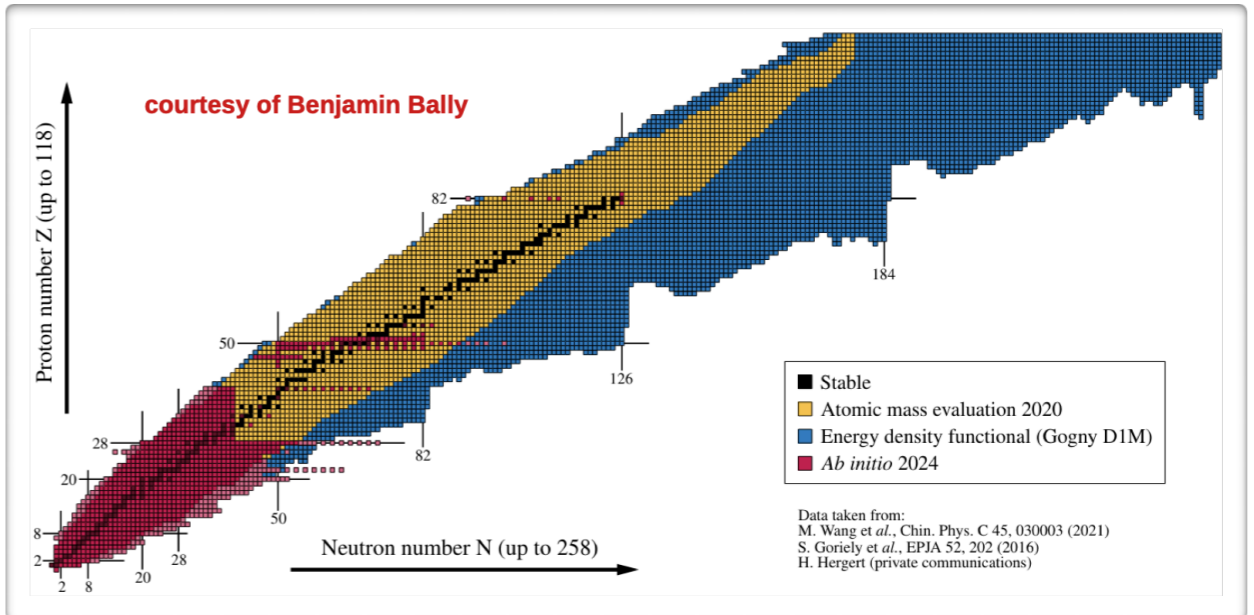
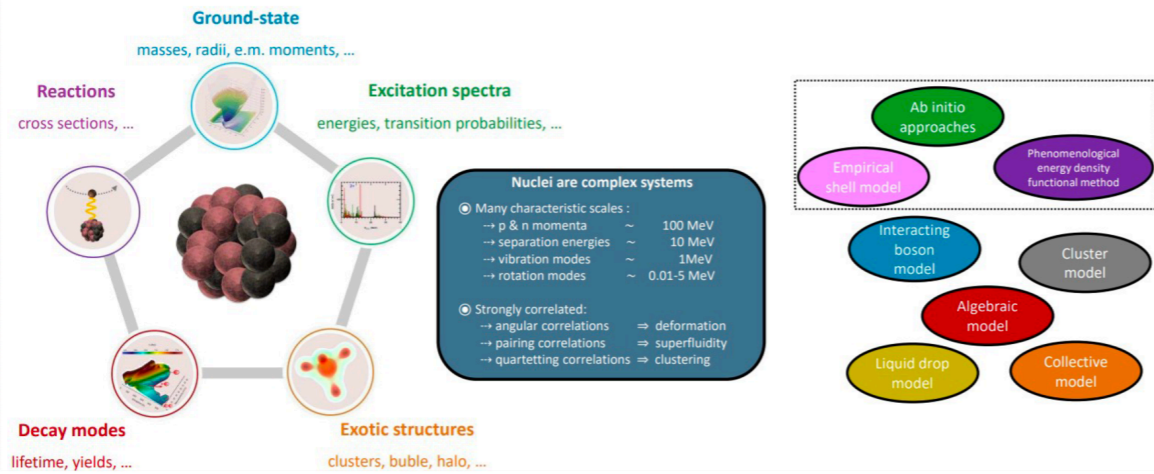
Nuclear structure at low energies

Atomic nuclei have rich phenomenology. Rooted in the strong nuclear force.
Nuclear structure is a very old field. Many different approaches.

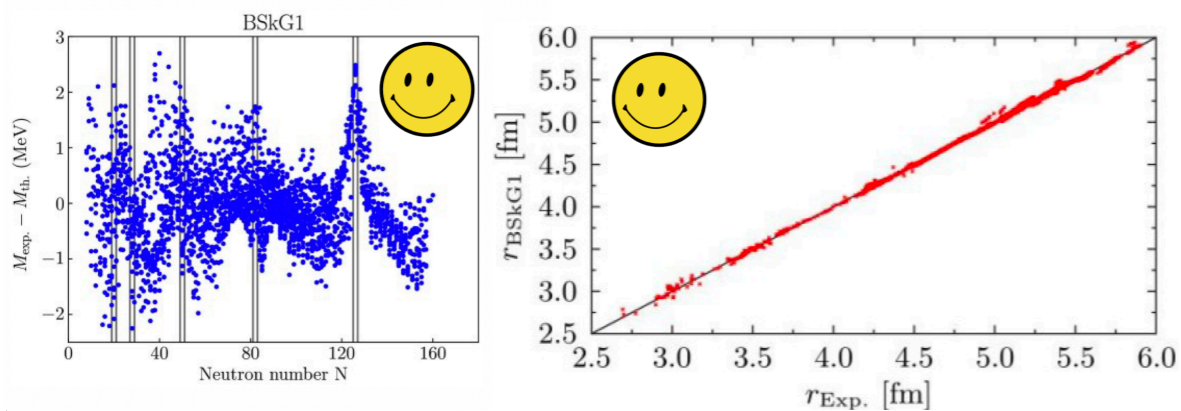


Nuclear structure at low energies

Atomic nuclei have rich phenomenology. Rooted in the strong nuclear force. Nuclear structure is a very old field. Many different approaches.

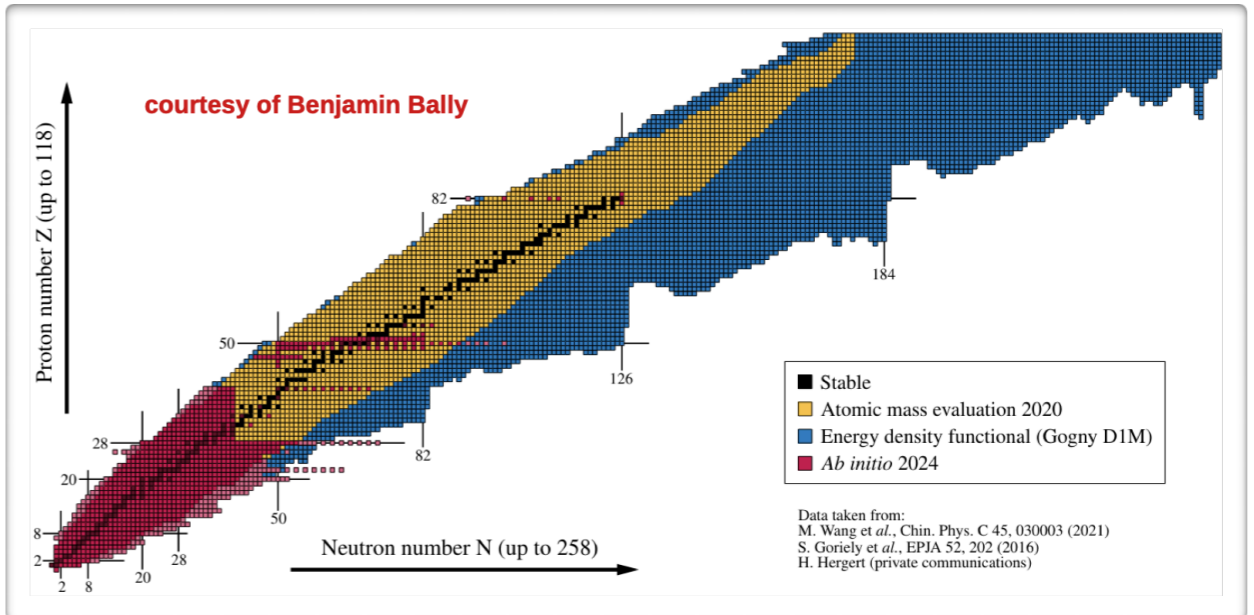
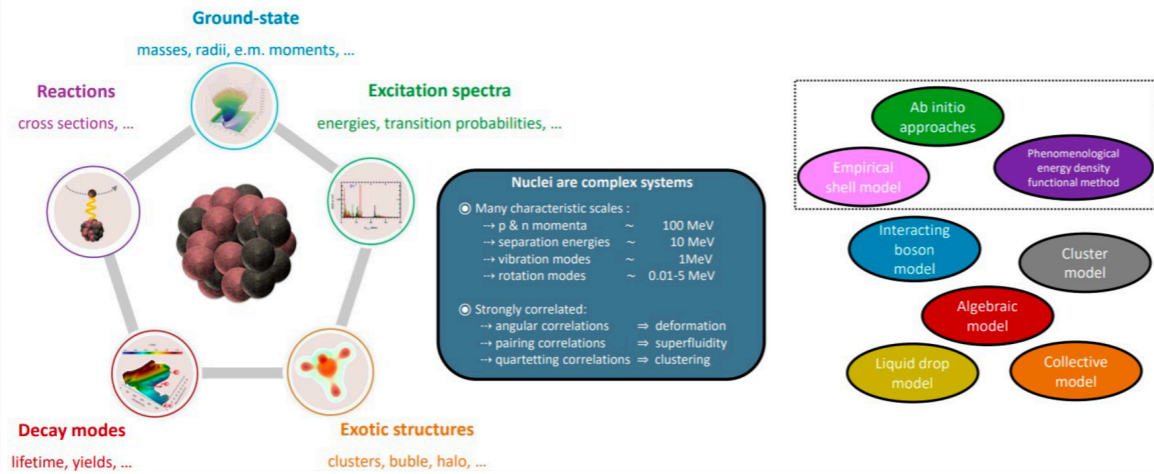


Energy density function method : accurate description of masses and radii

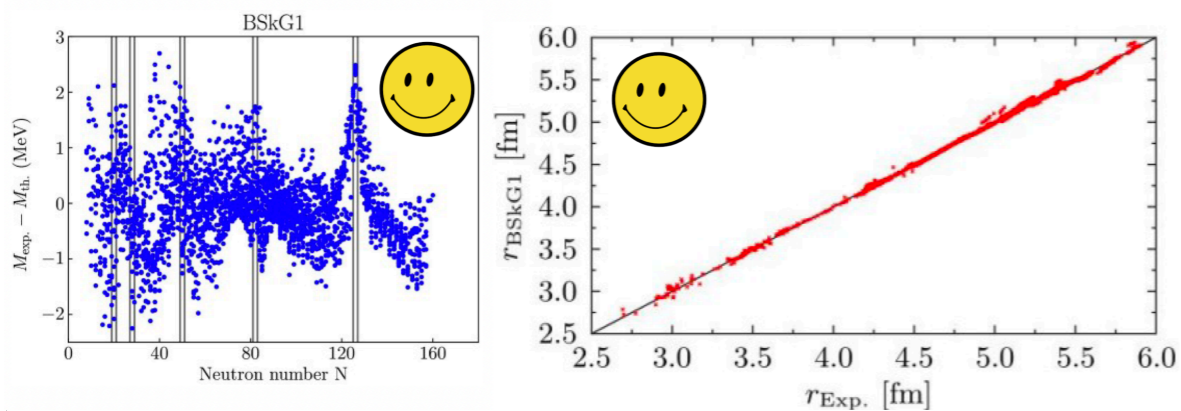


Nuclear structure at low energies

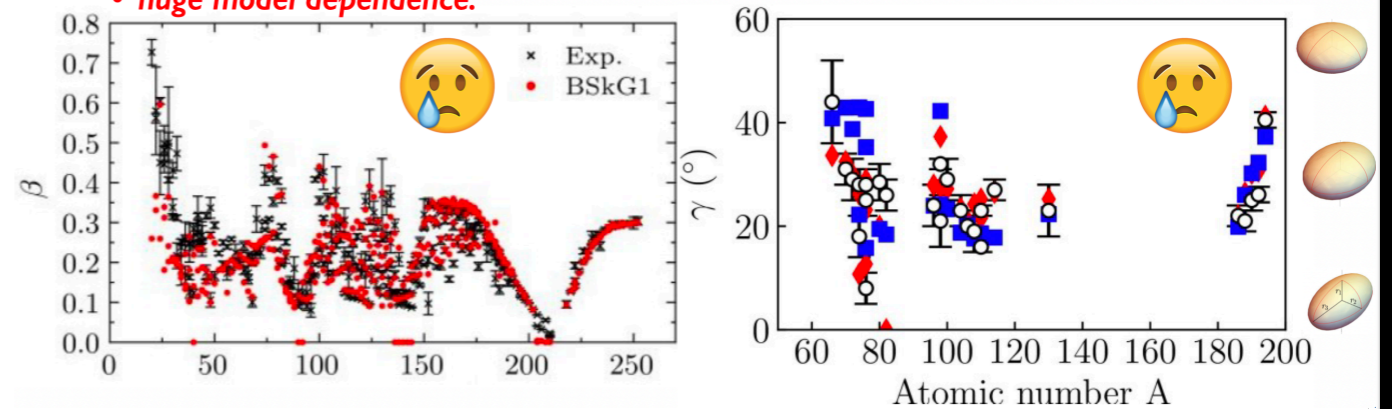
Atomic nuclei have rich phenomenology. Rooted in the strong nuclear force. Nuclear structure is a very old field. Many different approaches.



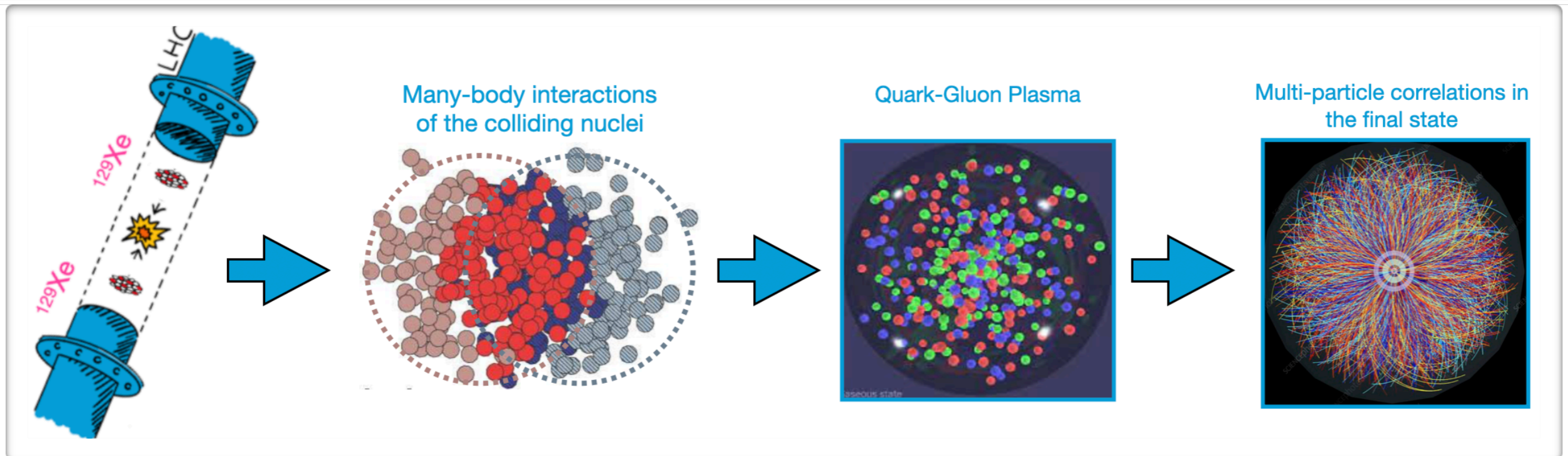
Energy density function method : accurate description of masses and radii



- there are no real probes of multi-nucleon correlations
- huge model dependence.



Nuclear Structure of ^{129}Xe



Aage Niels Bohr (NBI)

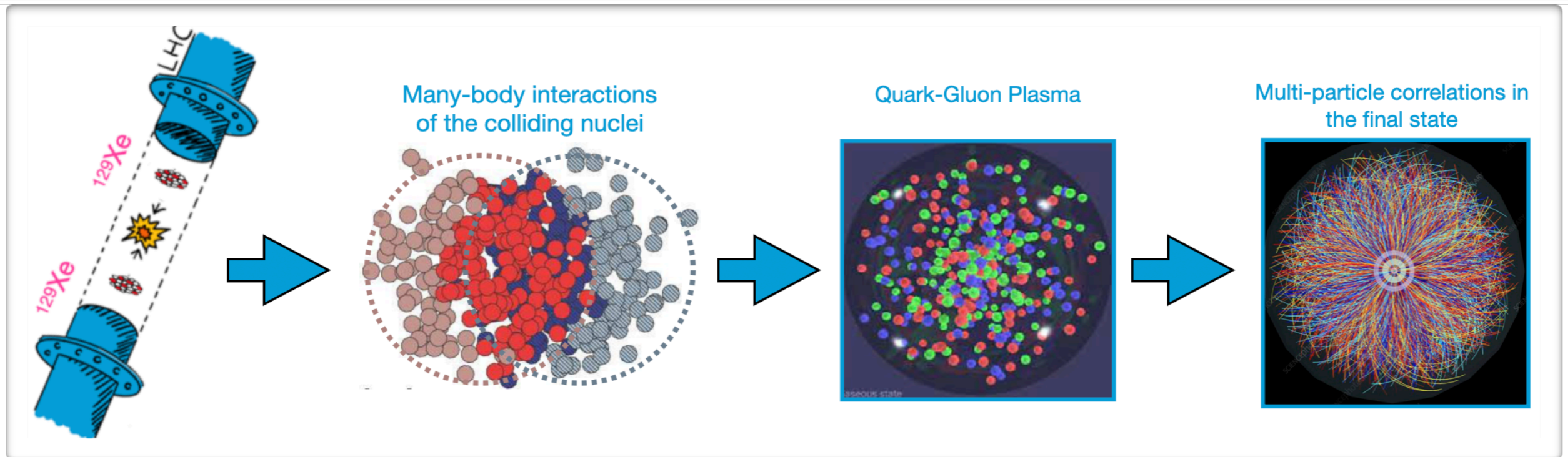
Ben Mottelson (NBI)



Nobelprisen i fysik
1975

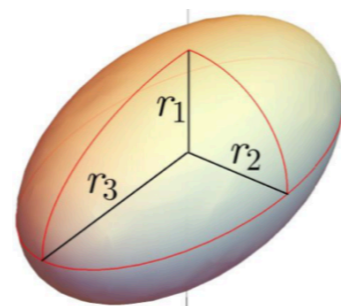
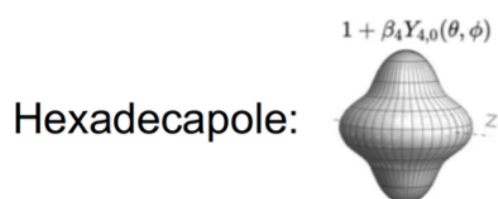
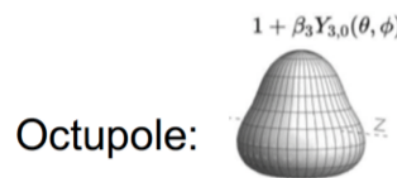
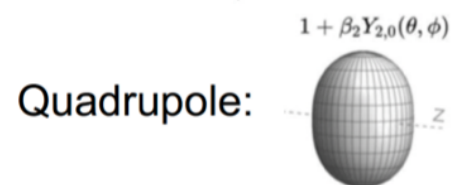


Nuclear structure at high energies

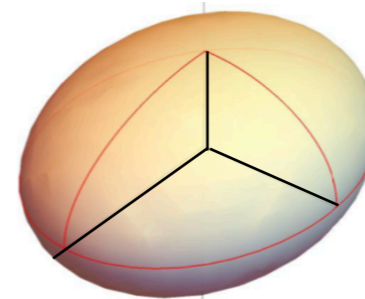


$$\rho(r, \theta, \phi) = \frac{\rho_0}{1 + e^{(r-R(\theta, \phi))/a_0}}$$

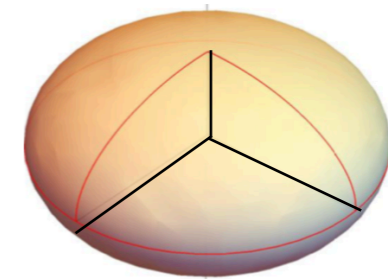
$$R(\theta, \phi) = R_0 \left(1 + \beta_2 [\cos \gamma Y_{2,0} + \sin \gamma Y_{2,2}] + \beta_3 \sum_{m=-3}^3 \alpha_{3,m} Y_{3,m} + \beta_4 \sum_{m=-4}^4 \alpha_{4,m} Y_{4,m} \right)$$



$\gamma = 0$
 $r_1 = r_2 < r_3$
 prolate



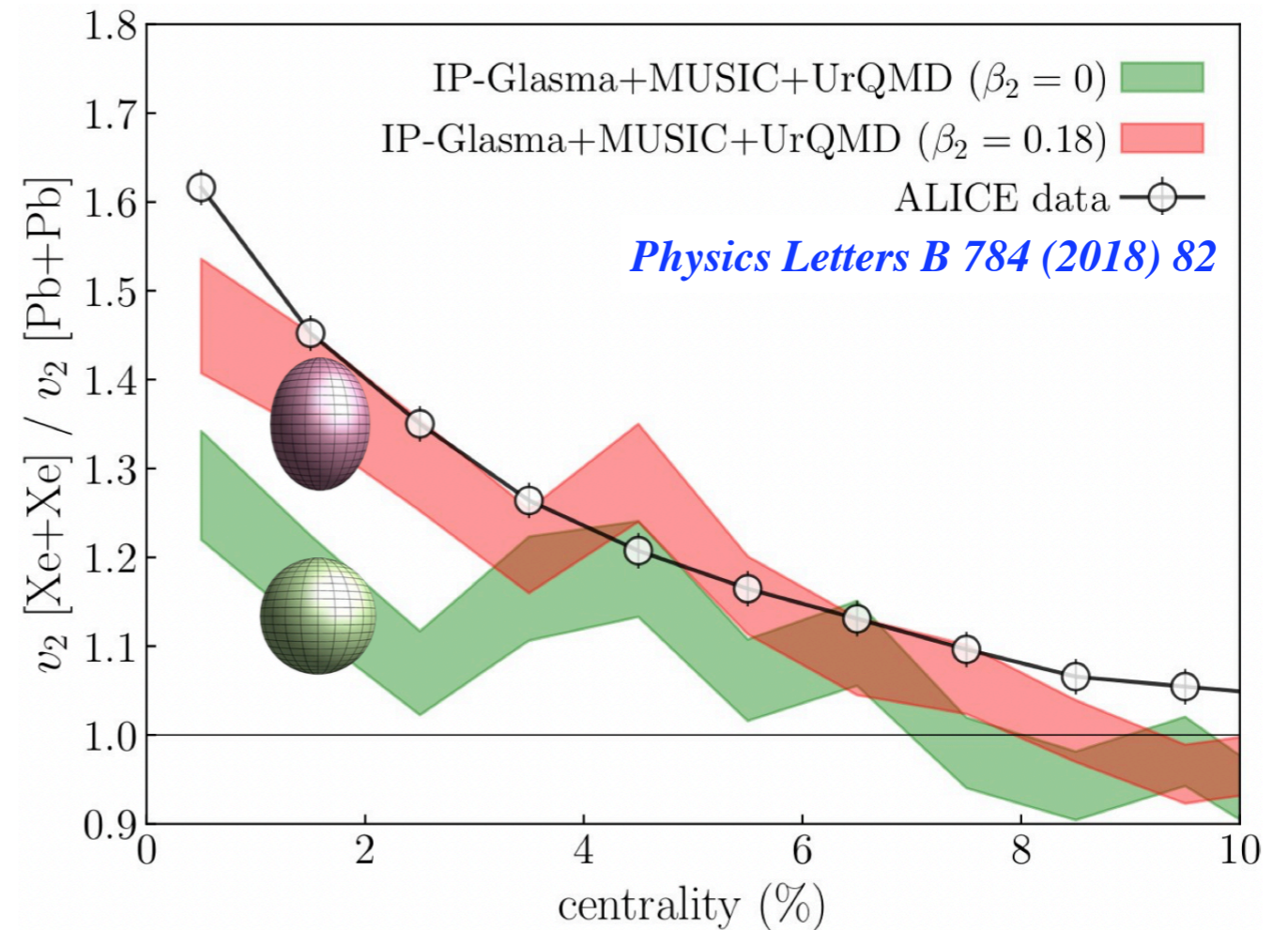
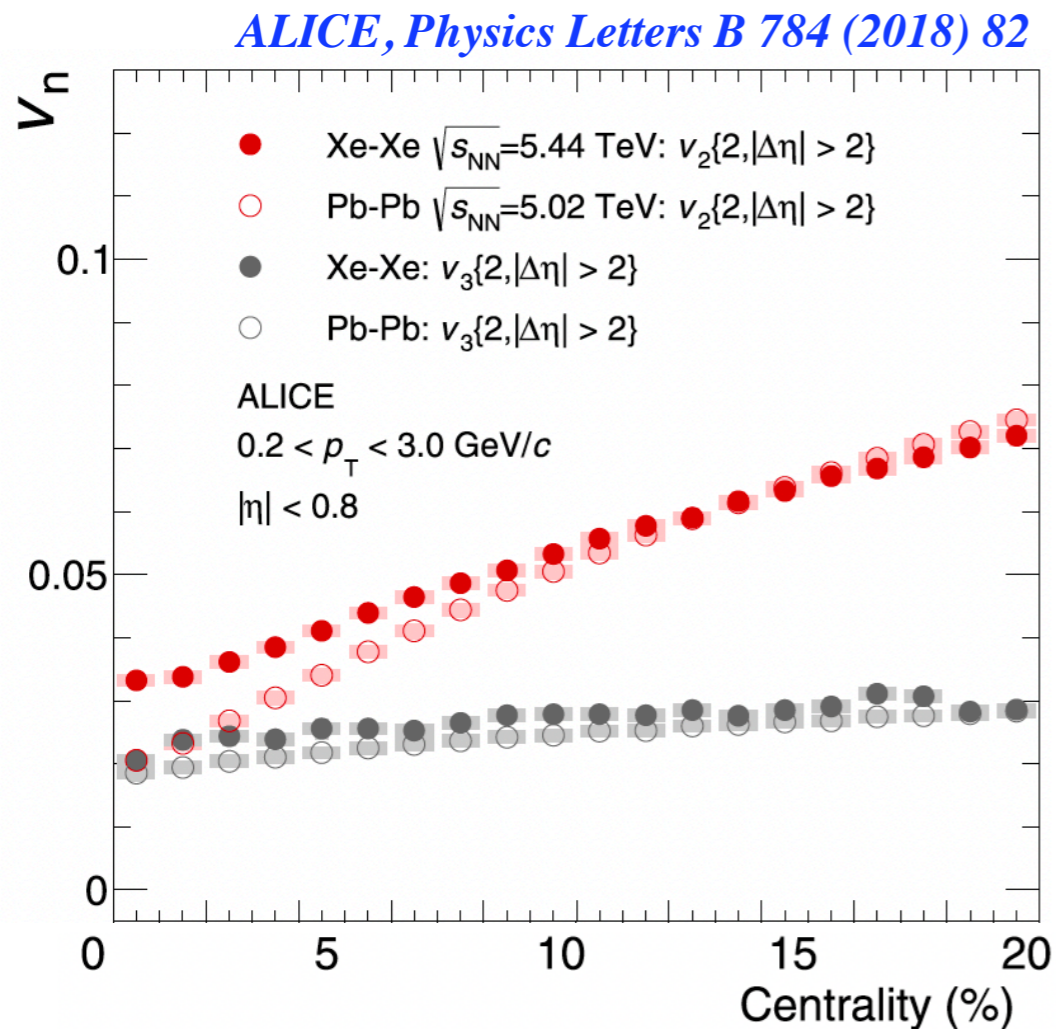
$\gamma = 30^\circ$
 $r_1 \neq r_2 \neq r_3$
 triaxial



$\gamma = 60^\circ$
 $r_1 < r_2 = r_3$
 oblate

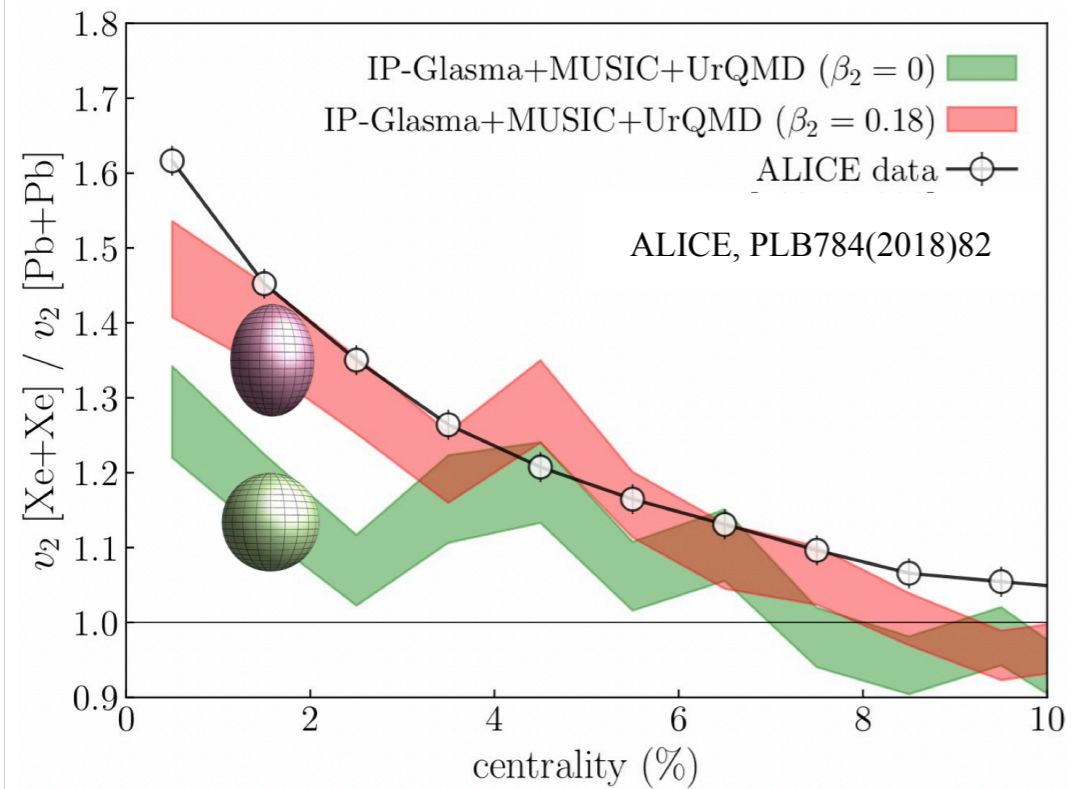
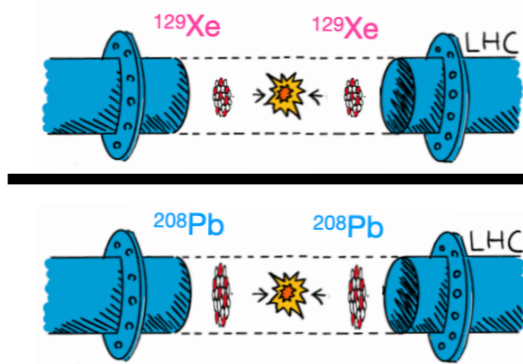


Probe nuclear structure of ^{129}Xe with v_n

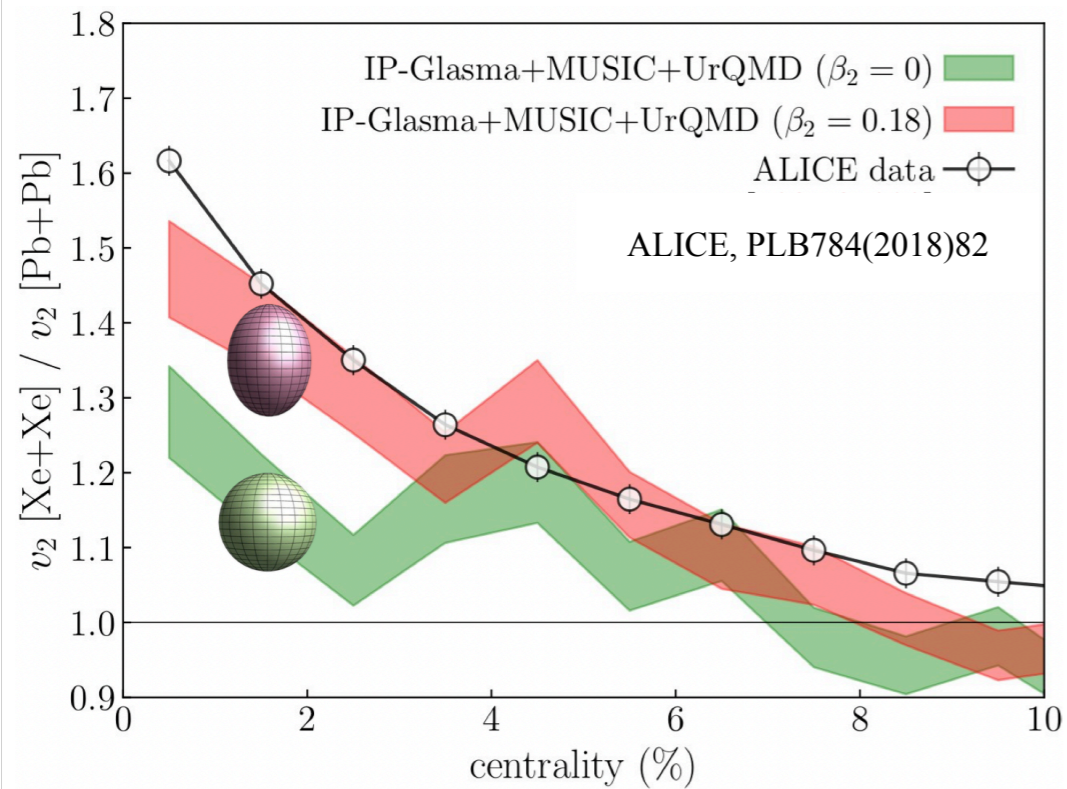
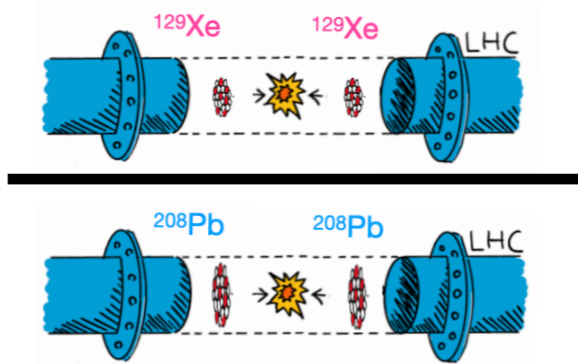


- ❖ Significant v_2 enhancements in central Xe-Xe collisions
- ❖ LHC data clearly suggests a non-zero β_2 (deformation of ^{129}Xe)

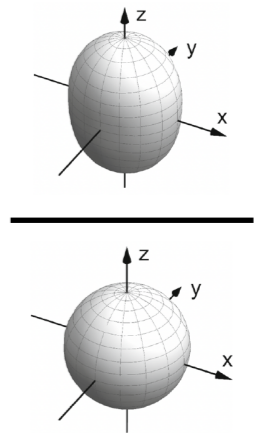
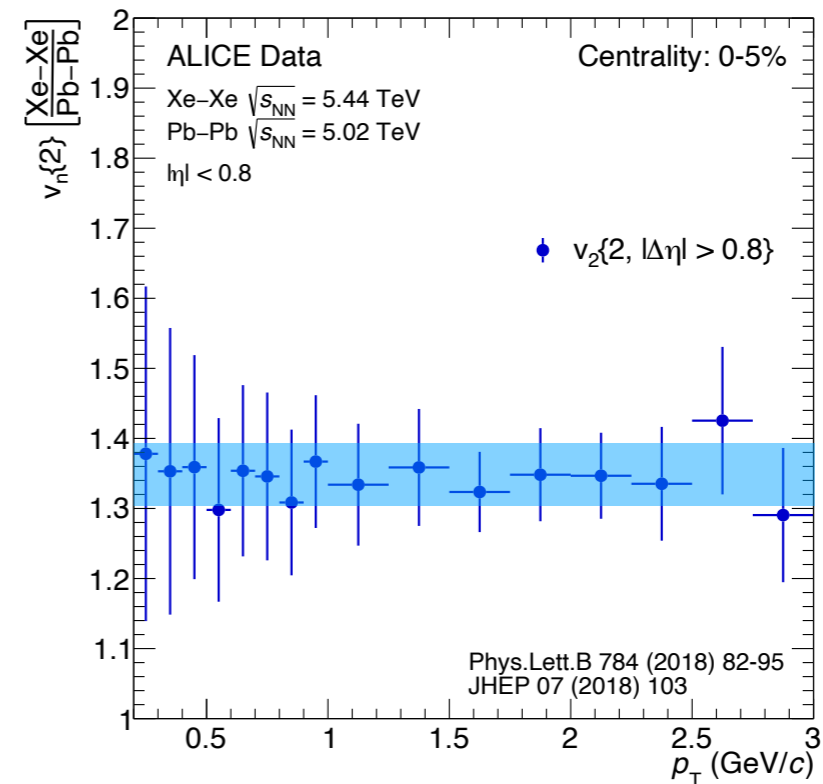
Differential flow vs p_T and η



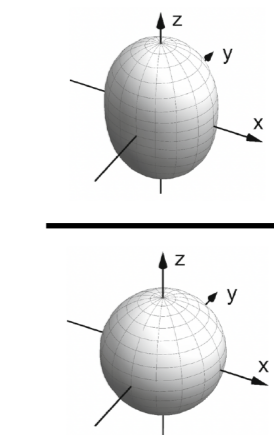
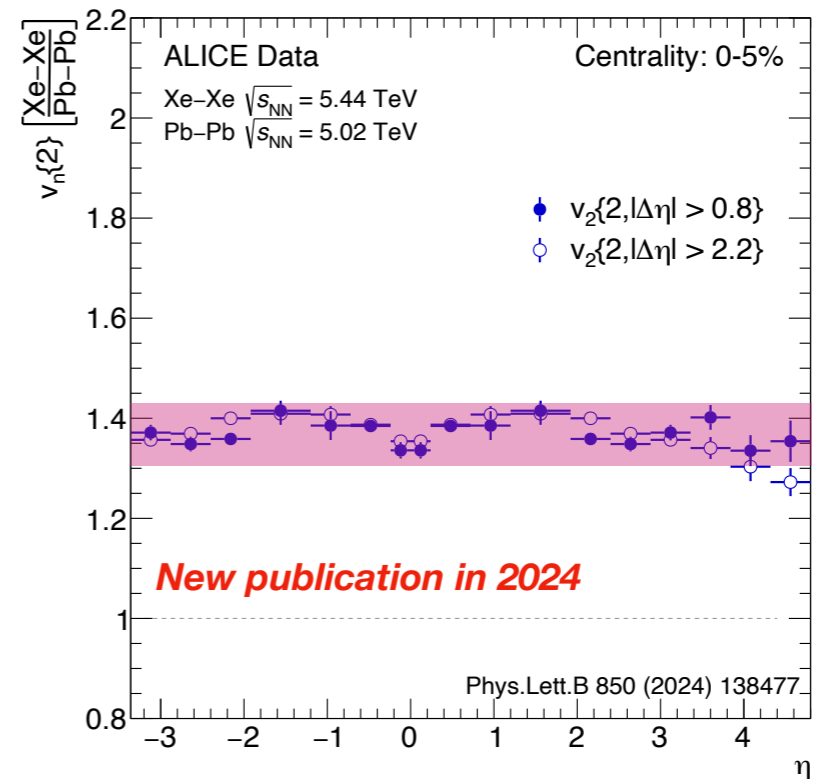
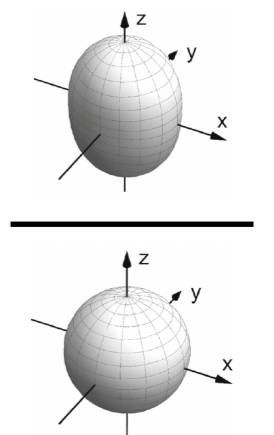
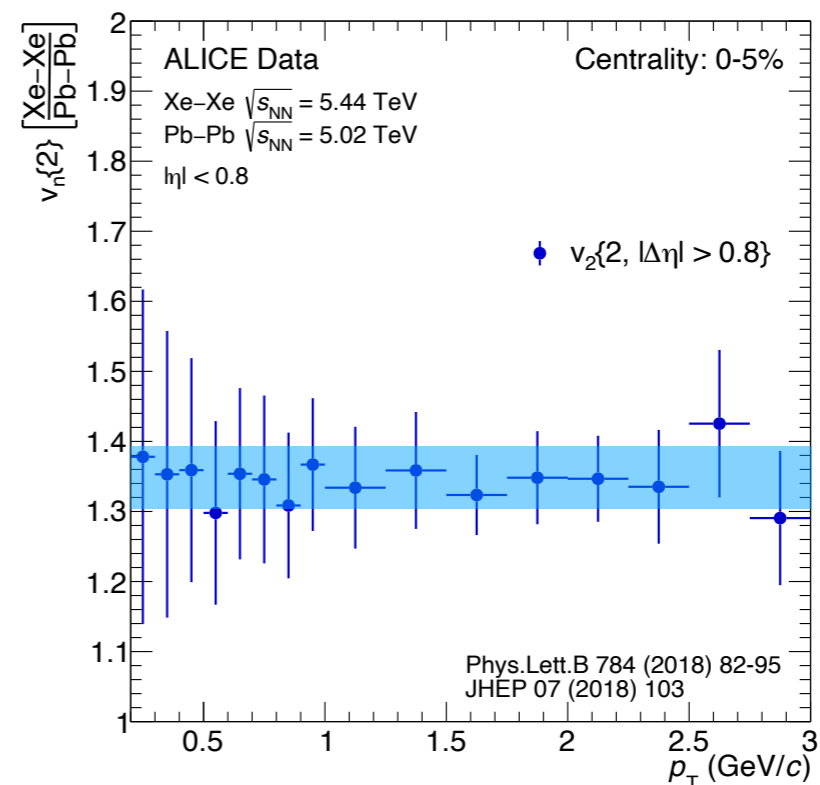
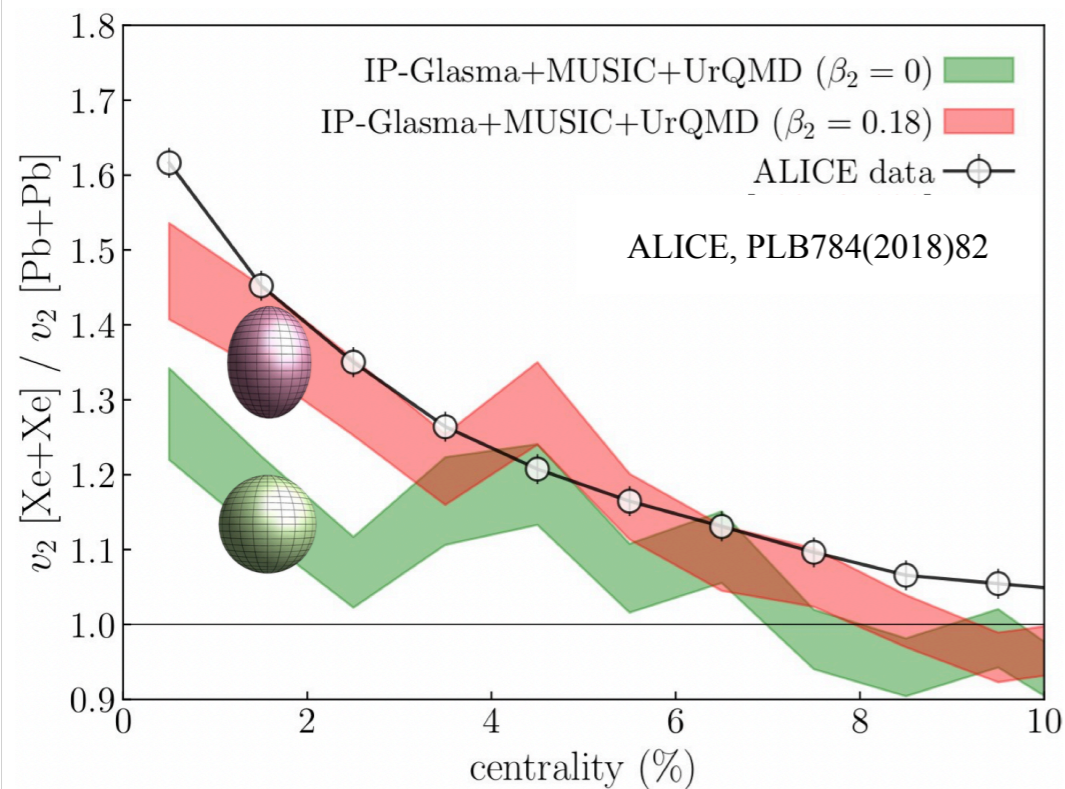
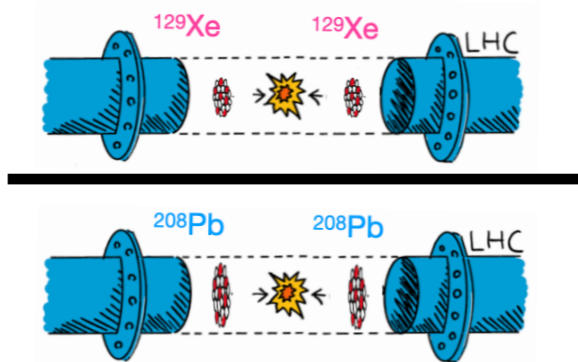
Differential flow vs p_T and η



p_T -differential



Differential flow vs p_T and η

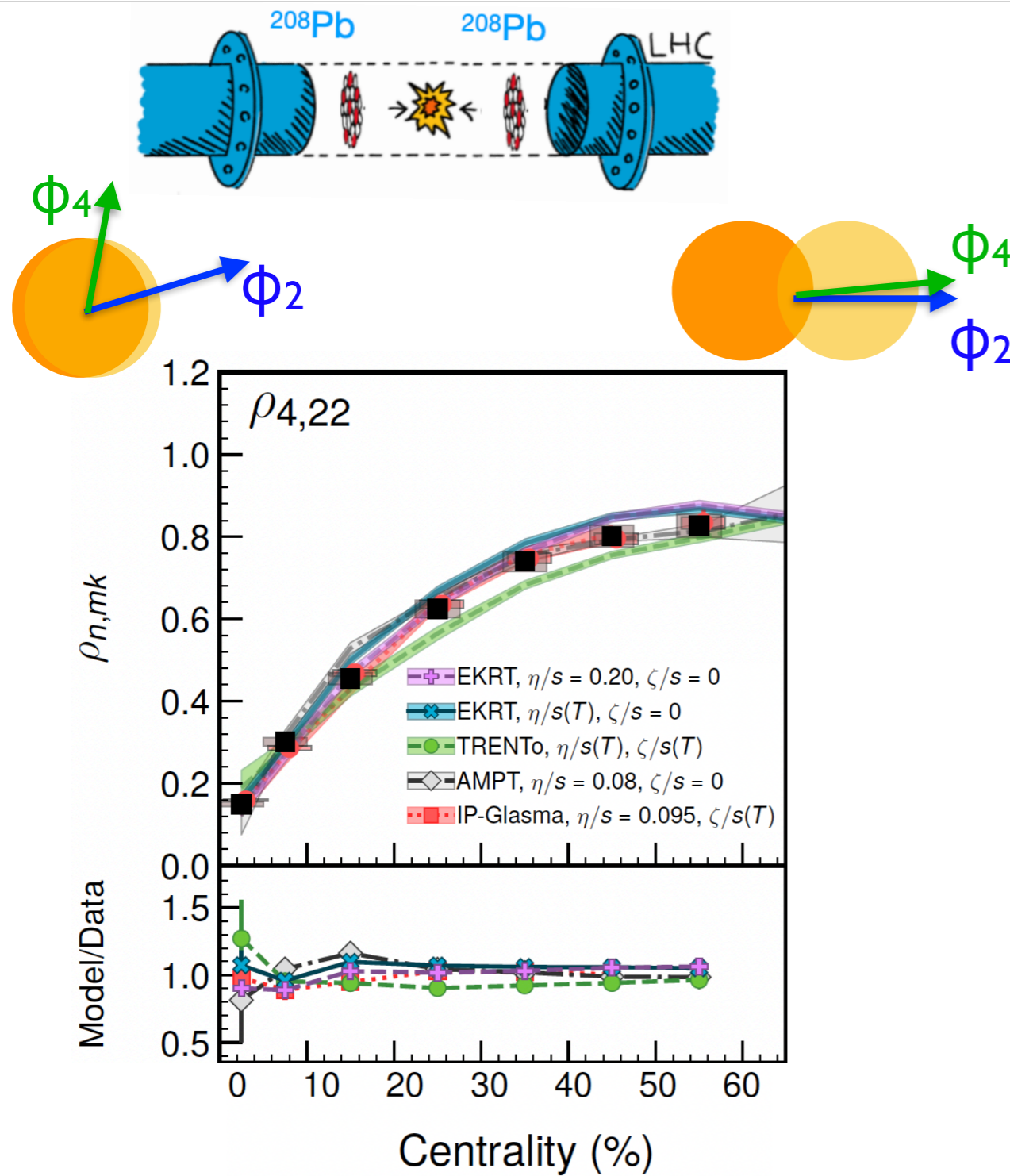


- ❖ For the first time observe the impact of NS over a very wide pseudorapidity range ($-3.5 < \eta < 5.0$)
 - New input for the low-x physics



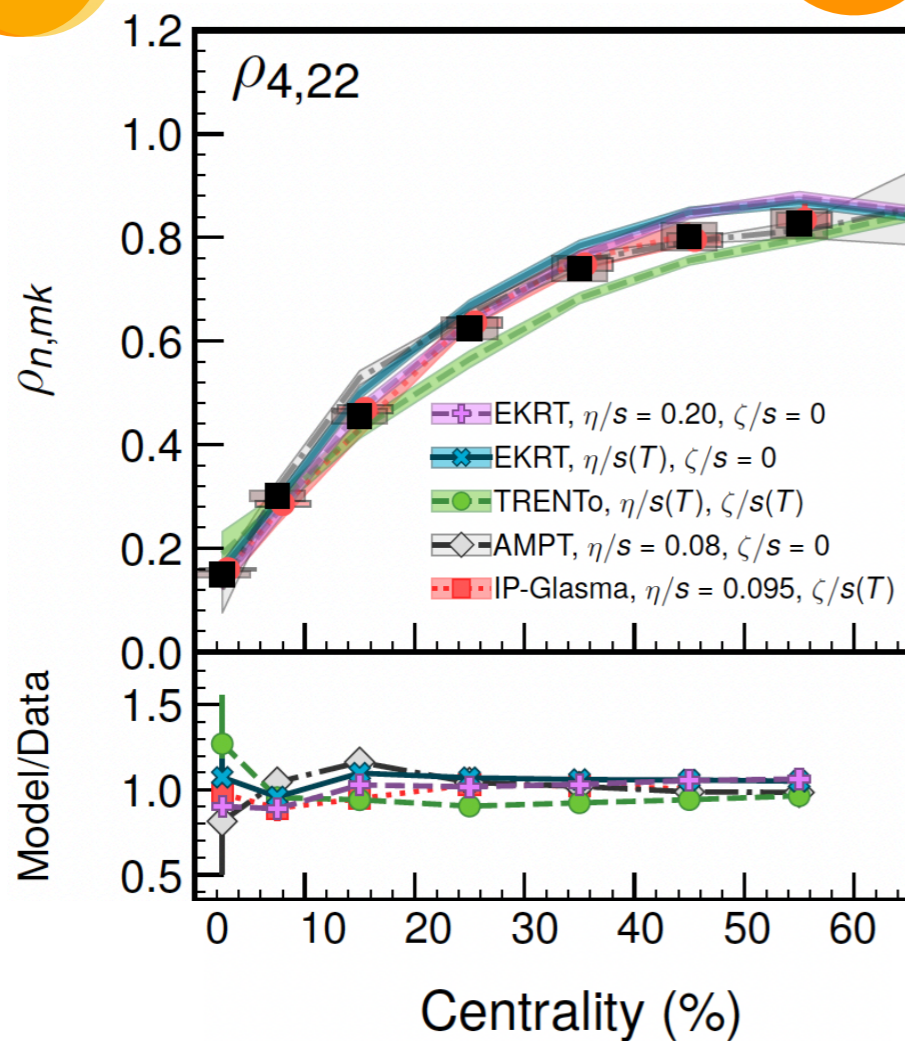
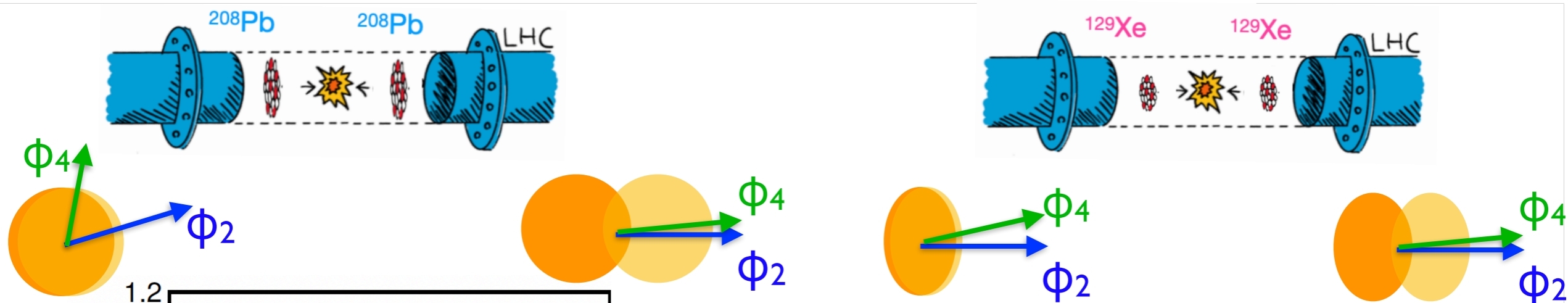
$\Psi_n - \Psi_m$ correlations

How do ψ_n and ψ_m correlate



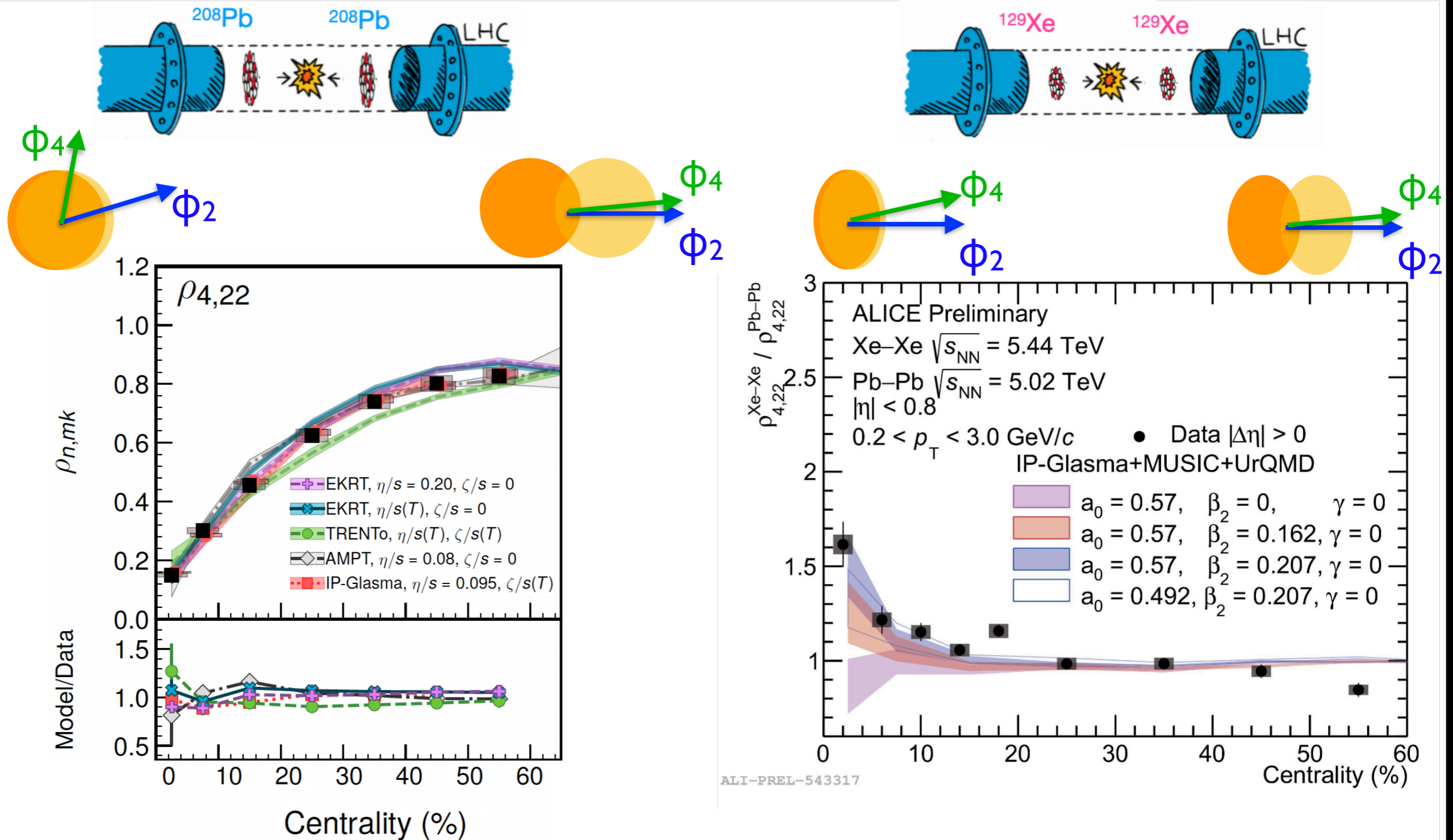
$\Psi_n - \Psi_m$ correlations

How do ψ_n and ψ_m correlate



$\psi_n - \psi_m$ correlations

How do ψ_n and ψ_m correlate



❖ A **stronger** correlation is observed in the Xe-Xe collisions.

Probe NS with **two**-particle $[\rho\tau]$ correlations

Eur. Phys. J. A (2024) 60:38
<https://doi.org/10.1140/epja/s10050-024-01266-x>

THE EUROPEAN
 PHYSICAL JOURNAL A



Regular Article - Theoretical Physics

Generic multi-particle transverse momentum correlations as a new tool for studying nuclear structure at the energy frontier

Emil Gorm Dahlbæk Nielsen, Frederik K. Rømer, Kristjan Gulbrandsen, You Zhou^a

Niels Bohr Institute, University of Copenhagen, 2200 Copenhagen, Denmark

Table 2 The cumulants of d_{\perp} up to eighth order in a liquid-drop model potential averaged over random orientations. The first three entries are given in [29]

Final state Cumulant	Initial state Cumulant	Liquid-drop Model
κ_2	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle$	$\frac{1}{32\pi} \langle \beta_2^2 \rangle$
κ_3	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle$	$\frac{\sqrt{5}}{896\pi^{3/2}} \langle \cos(3\gamma) \beta_2^3 \rangle$
κ_4	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^4 \right\rangle - 3 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle^2$	$-\frac{3}{14336\pi^2} (7 \langle \beta_2^2 \rangle^2 - 5 \langle \beta_2^4 \rangle)$
κ_5	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^5 \right\rangle - 10 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle$	$-\frac{5\sqrt{5}}{315392\pi^{5/2}} (11 \langle \cos(3\gamma) \beta_2^3 \rangle \langle \beta_2^2 \rangle - 5 \langle \beta_2^5 \rangle)$
κ_6	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^6 \right\rangle - 15 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^4 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle$ $+ 30 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle^3 - 10 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle^2$	$\frac{5}{918412504\pi^3} (42042 \langle \beta_2^2 \rangle^3 - 5720 \langle \cos(3\gamma) \beta_2^3 \rangle^2)$ $-45045 \langle \beta_2^2 \rangle \langle \beta_2^4 \rangle + 8575 \langle \beta_2^6 \rangle + 700 \langle \cos(6\gamma) \beta_2^6 \rangle$
κ_7	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^7 \right\rangle - 21 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^5 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle$ $+ 210 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle^2$ $- 35 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^4 \right\rangle$	$-\frac{15\sqrt{5}}{524812288} (2002 \langle \beta_2^2 \rangle^2 \langle \cos(3\gamma) \beta_2^3 \rangle)$ $+715 \langle \cos(3\gamma) \beta_2^3 \rangle \langle \beta_2^4 \rangle$ $+910 \langle \cos(3\gamma) \beta_2^5 \rangle \langle \beta_2^2 \rangle - 175 \langle \cos(3\gamma) \beta_2^7 \rangle$
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Regular Article - Theoretical Physics

Generic multi-particle transverse momentum correlations as a new tool for studying nuclear structure at the energy frontier

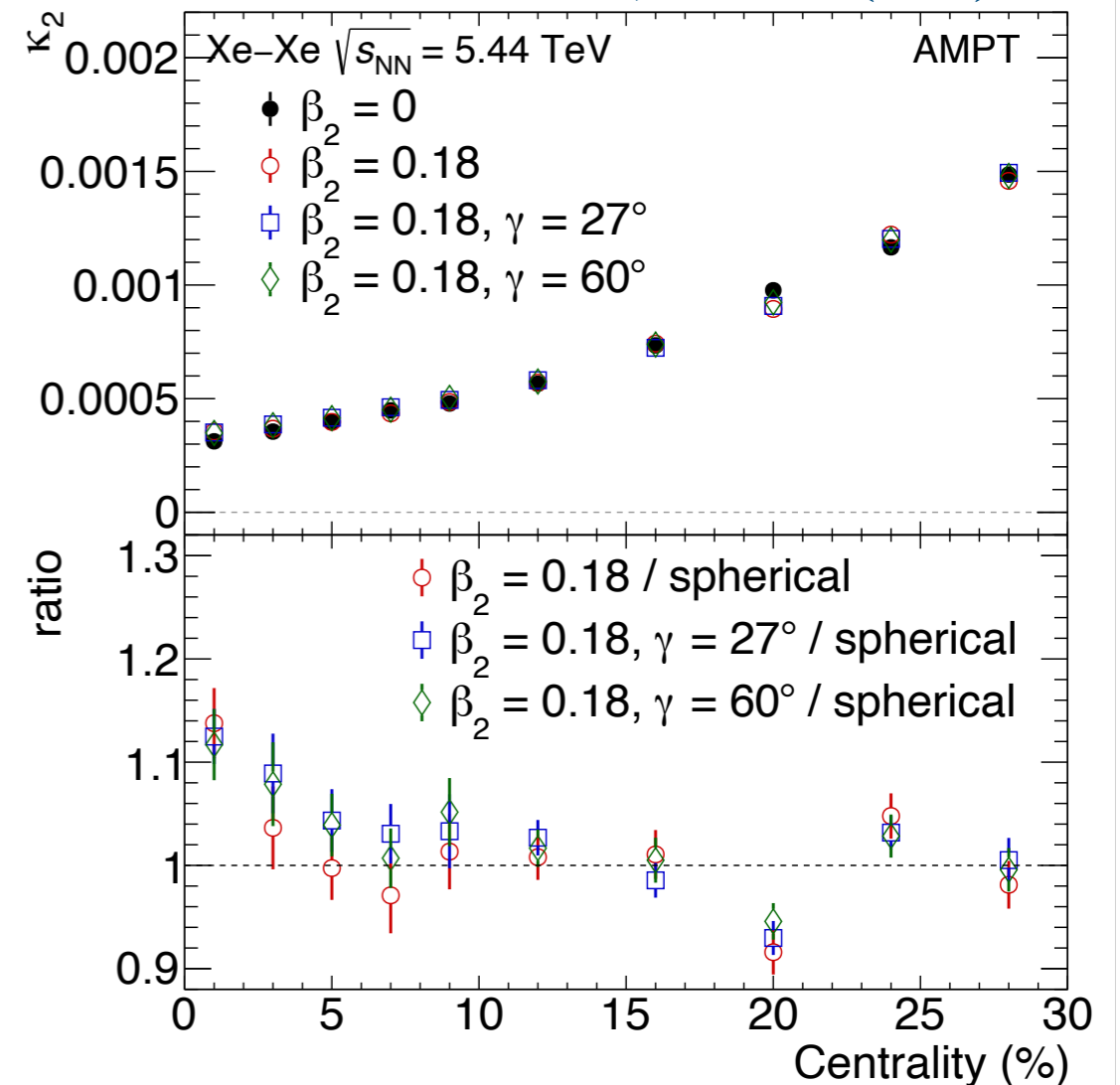
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κ_4	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^4 \right\rangle - 3 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle^2$	$-\frac{3}{14336\pi^2} (7 \langle \beta_2^2 \rangle^2 - 5 \langle \beta_2^4 \rangle)$
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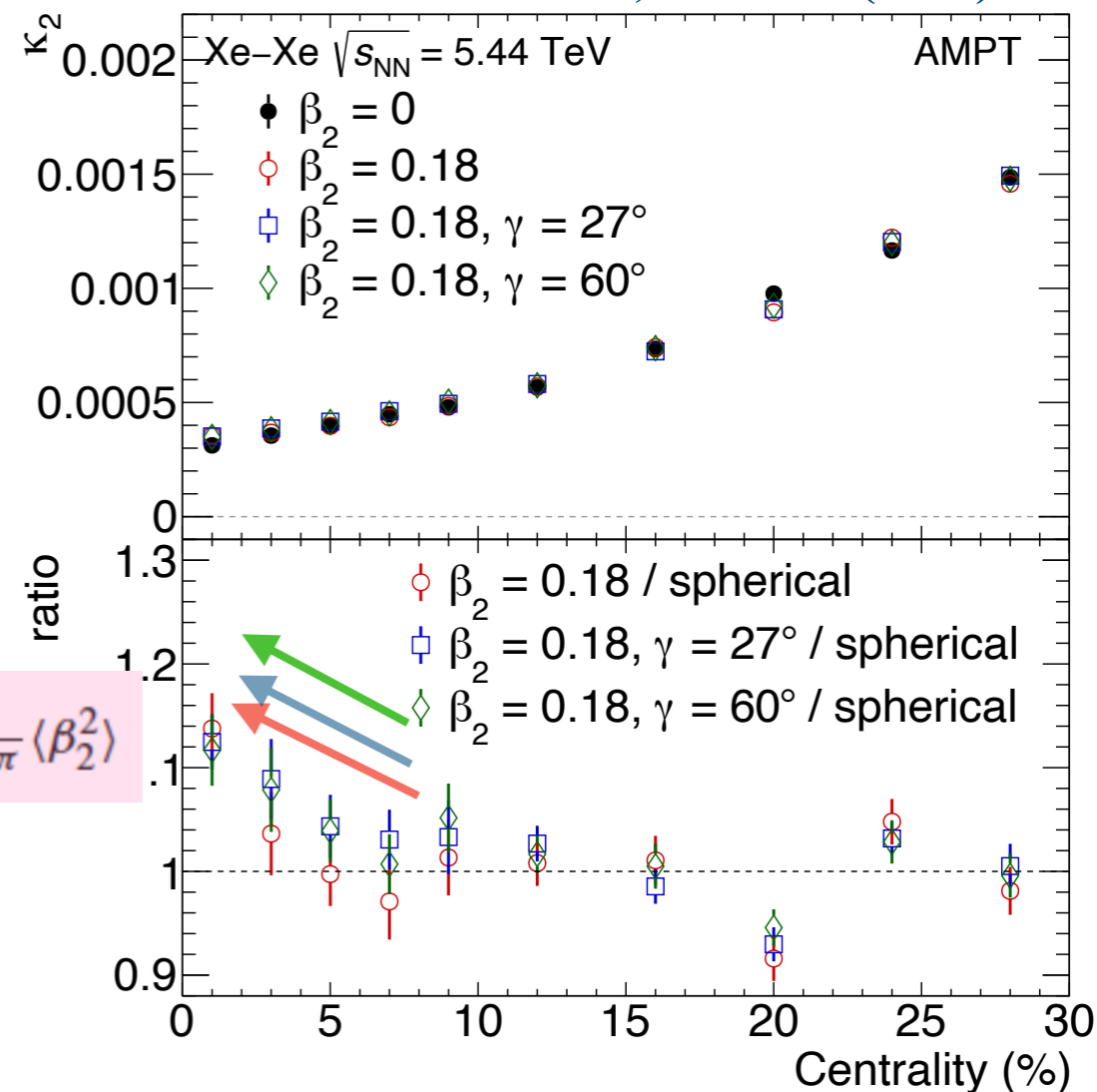
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Regular Article - Theoretical Physics

Generic multi-particle transverse momentum correlations as a new tool for studying nuclear structure at the energy frontier

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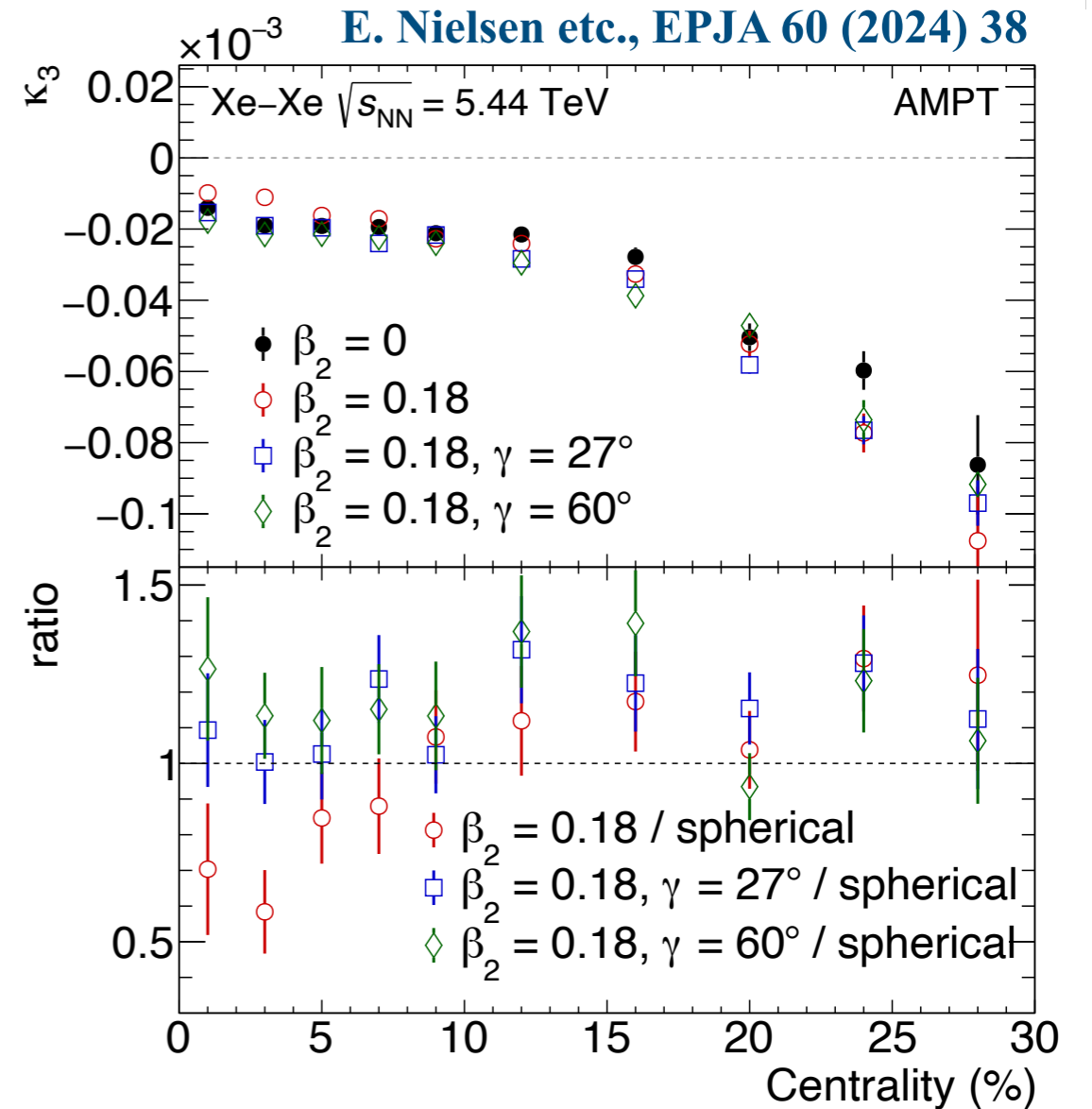
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κ_6	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^6 \right\rangle - 15 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^4 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle$ $+ 30 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle^3 - 10 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle^2$	$\frac{5}{918412504\pi^3} (42042 \langle \beta_2^2 \rangle^3 - 5720 \langle \cos(3\gamma) \beta_2^3 \rangle^2)$ $-45045 \langle \beta_2^2 \rangle \langle \beta_2^4 \rangle + 8575 \langle \beta_2^6 \rangle + 700 \langle \cos(6\gamma) \beta_2^6 \rangle$
κ_7	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^7 \right\rangle - 21 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^5 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle$ $+ 210 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle^2$ $- 35 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^4 \right\rangle$	$-\frac{15\sqrt{5}}{524812288} (2002 \langle \beta_2^2 \rangle^2 \langle \cos(3\gamma) \beta_2^3 \rangle)$ $+715 \langle \cos(3\gamma) \beta_2^3 \rangle \langle \beta_2^4 \rangle$ $+910 \langle \cos(3\gamma) \beta_2^5 \rangle \langle \beta_2^2 \rangle - 175 \langle \cos(3\gamma) \beta_2^7 \rangle$
κ_8	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^8 \right\rangle - 28 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^6 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle$ $+ 420 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^4 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle^2$ $- 35 \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^4 \right\rangle^2 - 630 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle^4$ $+ 560 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle^2 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle$ $- 56 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^5 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle$	$\frac{5}{142748942336\pi^4} (2144142 \langle \beta_2^2 \rangle^4 - 3063060 \langle \beta_2^2 \rangle^2 \langle \beta_2^4 \rangle)$ $-340 \langle \beta_2^2 \rangle (2288 \langle \cos(3\gamma) \beta_2^3 \rangle^2 - 35 (49 \langle \beta_2^6 \rangle$ $+ 4 \langle \cos(6\gamma) \beta_2^6 \rangle)) + 25 (21879 \langle \beta_2^4 \rangle^2$ $+ 14144 \langle \cos(3\gamma) \beta_2^3 \rangle \langle \cos(3\gamma) \beta_2^5 \rangle$ $- 35 (79 \langle \beta_2^8 \rangle + 16 \langle \cos(6\gamma) \beta_2^8 \rangle))$



Probe NS with **multi**-particle $[p_T]$ correlations

Eur. Phys. J. A (2024) 60:38
<https://doi.org/10.1140/epja/s10050-024-01266-x>

THE EUROPEAN
 PHYSICAL JOURNAL A



Regular Article - Theoretical Physics

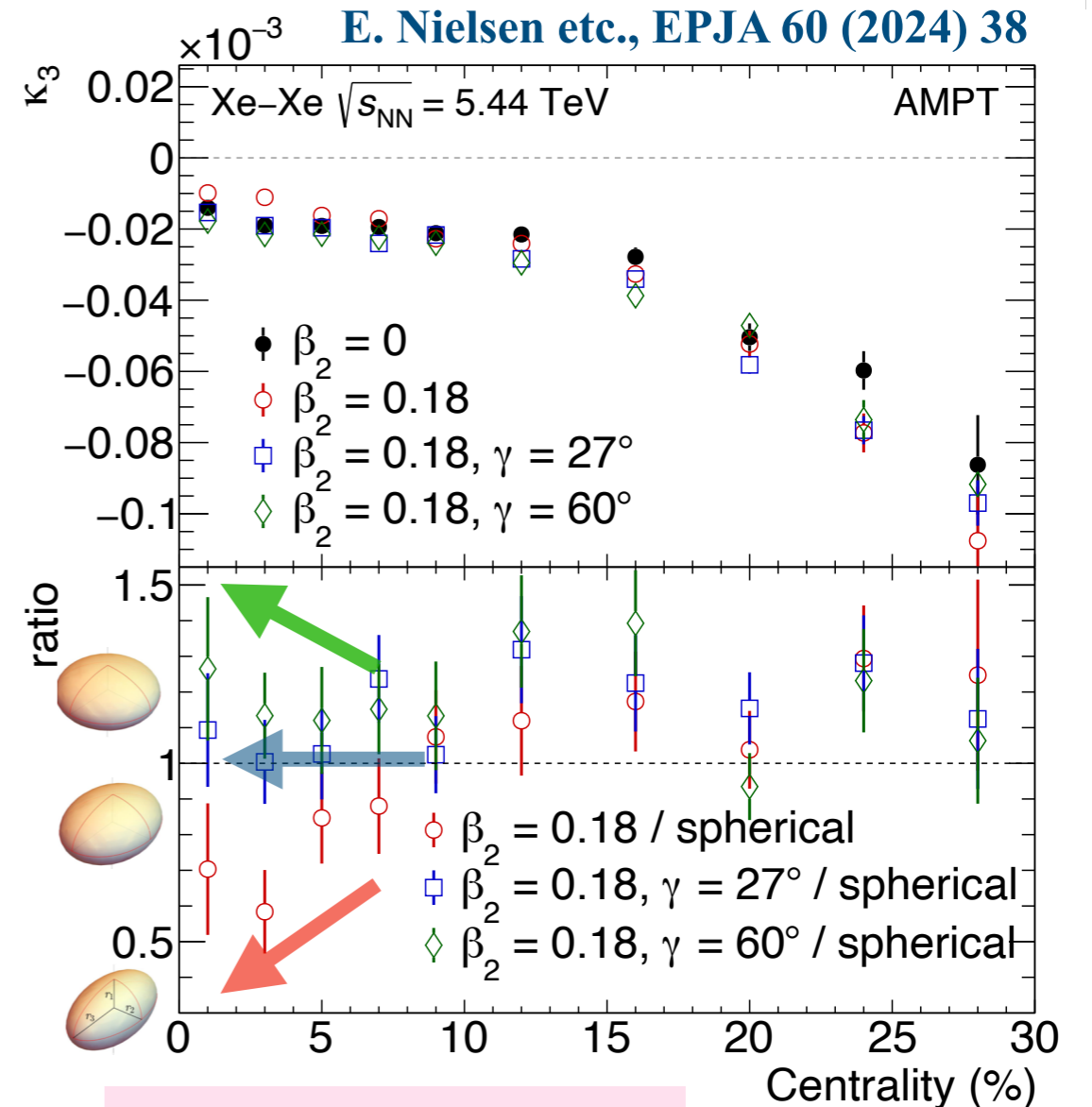
Generic multi-particle transverse momentum correlations as a new tool for studying nuclear structure at the energy frontier

Emil Gorm Dahlbæk Nielsen, Frederik K. Rømer, Kristjan Gulbrandsen, You Zhou^a

Niels Bohr Institute, University of Copenhagen, 2200 Copenhagen, Denmark

Table 2 The cumulants of d_{\perp} up to eighth order in a liquid-drop model potential averaged over random orientations. The first three entries are given in [29]

Final state Cumulant	Initial state Cumulant	Liquid-drop Model
κ_2	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle$	$\frac{1}{32\pi} \langle \beta_2^2 \rangle$
κ_3	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle$	$\frac{\sqrt{5}}{896\pi^{3/2}} \langle \cos(3\gamma) \beta_2^3 \rangle$
κ_4	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^4 \right\rangle - 3 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle^2$	$-\frac{3}{14336\pi^2} (7 \langle \beta_2^2 \rangle^2 - 5 \langle \beta_2^4 \rangle)$
κ_5	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^5 \right\rangle - 10 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle$	$-\frac{5\sqrt{5}}{315392\pi^{5/2}} (11 \langle \cos(3\gamma) \beta_2^3 \rangle \langle \beta_2^2 \rangle - 5 \langle \beta_2^5 \rangle)$
κ_6	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^6 \right\rangle - 15 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^4 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle$ $+ 30 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle^3 - 10 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle^2$	$\frac{5}{918412504\pi^3} (42042 \langle \beta_2^2 \rangle^3 - 5720 \langle \cos(3\gamma) \beta_2^3 \rangle^2)$ $-45045 \langle \beta_2^2 \rangle \langle \beta_2^4 \rangle + 8575 \langle \beta_2^6 \rangle + 700 \langle \cos(6\gamma) \beta_2^6 \rangle$
κ_7	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^7 \right\rangle - 21 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^5 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle$ $+ 210 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle^2$ $- 35 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^4 \right\rangle$	$-\frac{15\sqrt{5}}{524812288} (2002 \langle \beta_2^2 \rangle^2 \langle \cos(3\gamma) \beta_2^3 \rangle)$ $+715 \langle \cos(3\gamma) \beta_2^3 \rangle \langle \beta_2^4 \rangle$ $+910 \langle \cos(3\gamma) \beta_2^5 \rangle \langle \beta_2^2 \rangle - 175 \langle \cos(3\gamma) \beta_2^7 \rangle$
κ_8	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^8 \right\rangle - 28 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^6 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle$ $+ 420 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^4 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle^2$ $- 35 \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^4 \right\rangle^2 - 630 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle^4$ $+ 560 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle^2 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle$ $- 56 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^5 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle$	$\frac{5}{142748942336\pi^4} (2144142 \langle \beta_2^2 \rangle^4 - 3063060 \langle \beta_2^2 \rangle^2 \langle \beta_2^4 \rangle)$ $-340 \langle \beta_2^2 \rangle (2288 \langle \cos(3\gamma) \beta_2^3 \rangle^2 - 35 (49 \langle \beta_2^6 \rangle$ $+ 4 \langle \cos(6\gamma) \beta_2^6 \rangle)) + 25 (21879 \langle \beta_2^4 \rangle^2$ $+ 14144 \langle \cos(3\gamma) \beta_2^3 \rangle \langle \cos(3\gamma) \beta_2^5 \rangle$ $- 35 (79 \langle \beta_2^8 \rangle + 16 \langle \cos(6\gamma) \beta_2^8 \rangle))$

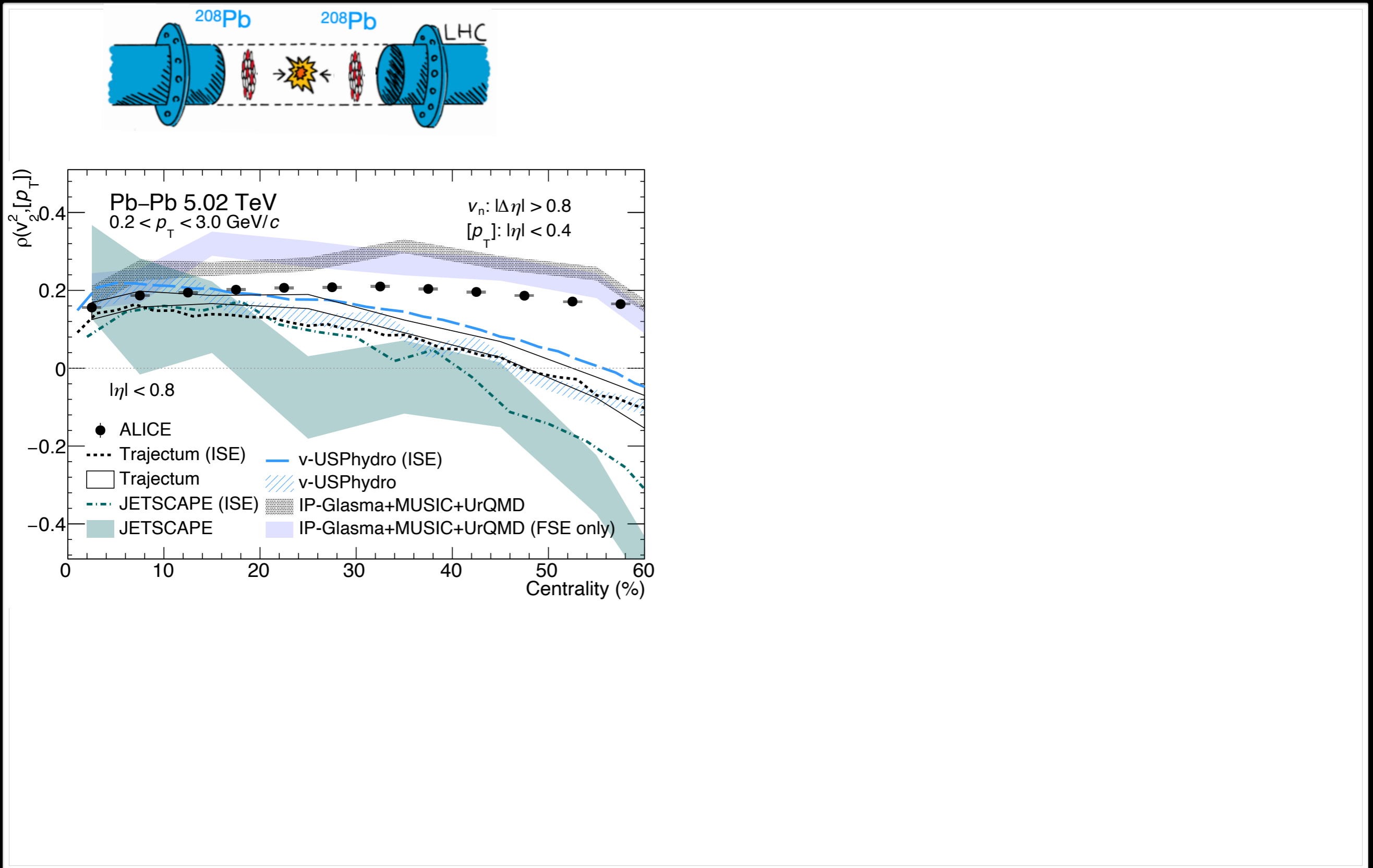


$$\frac{\sqrt{5}}{896\pi^{3/2}} \langle \cos(3\gamma) \beta_2^3 \rangle$$

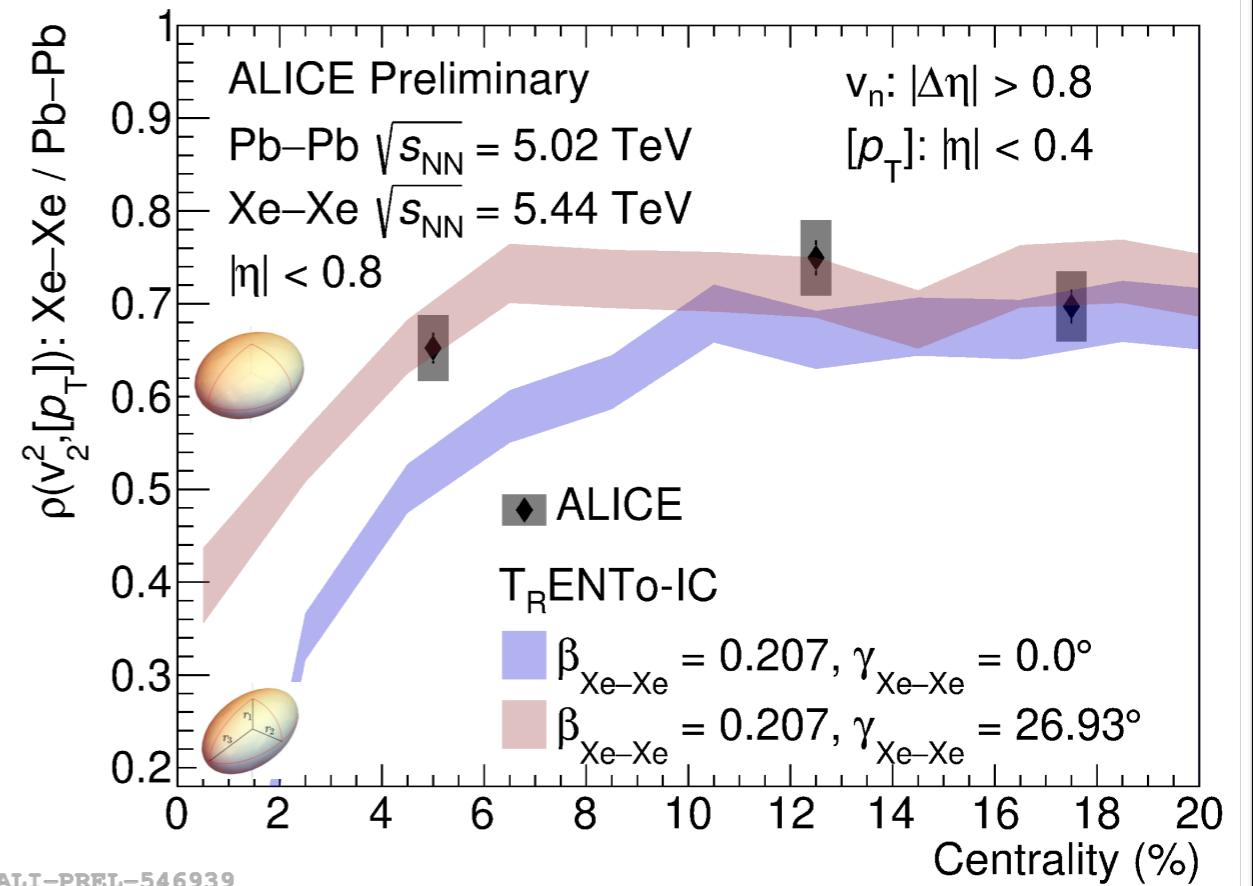
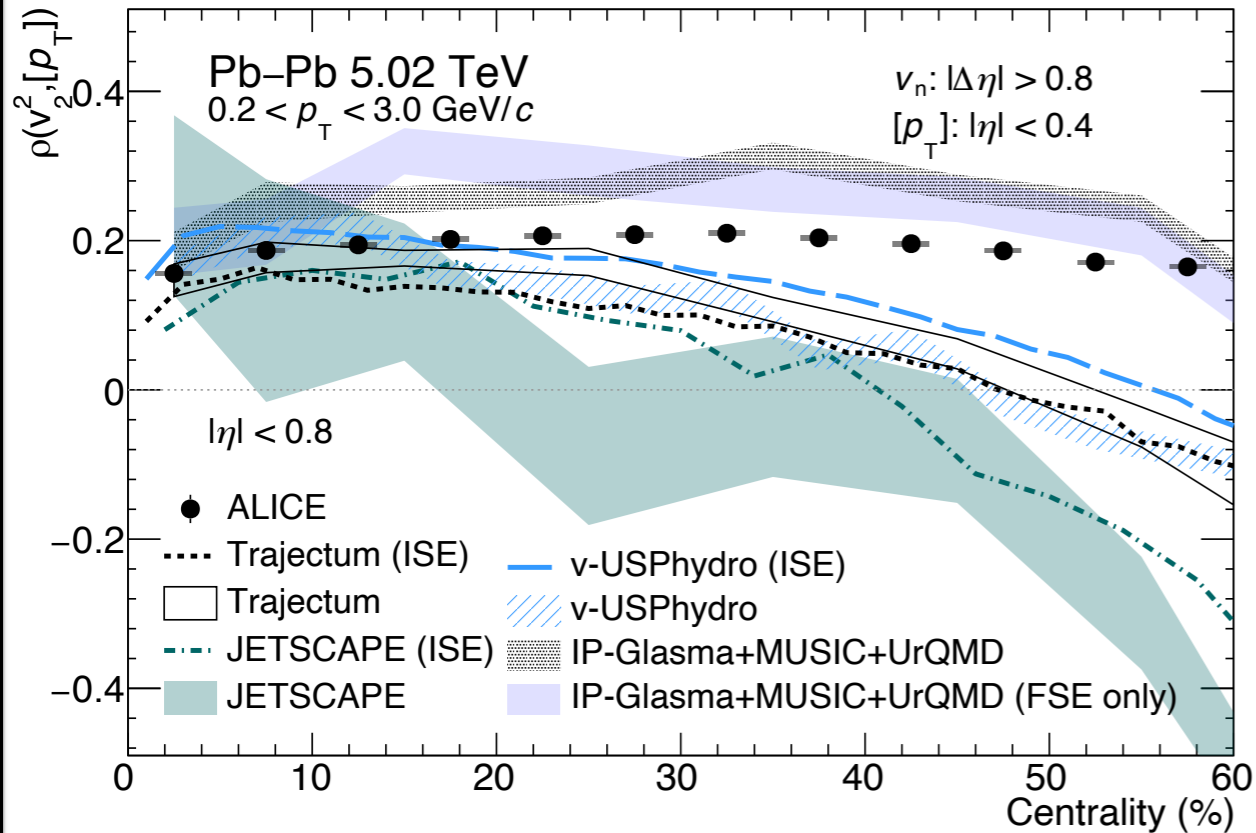
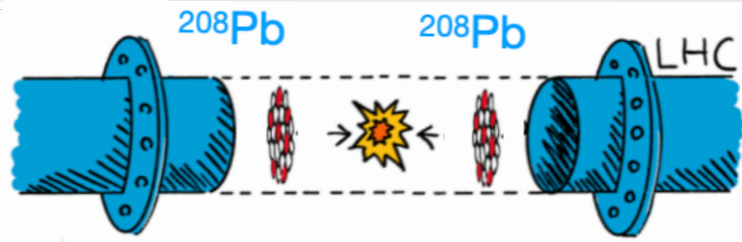
- Multi-particle $[p_T]$ correlation reflects the initial size fluctuations, also bring new information on the **triaxial** structure.



Probe triaxial structure of ^{129}Xe



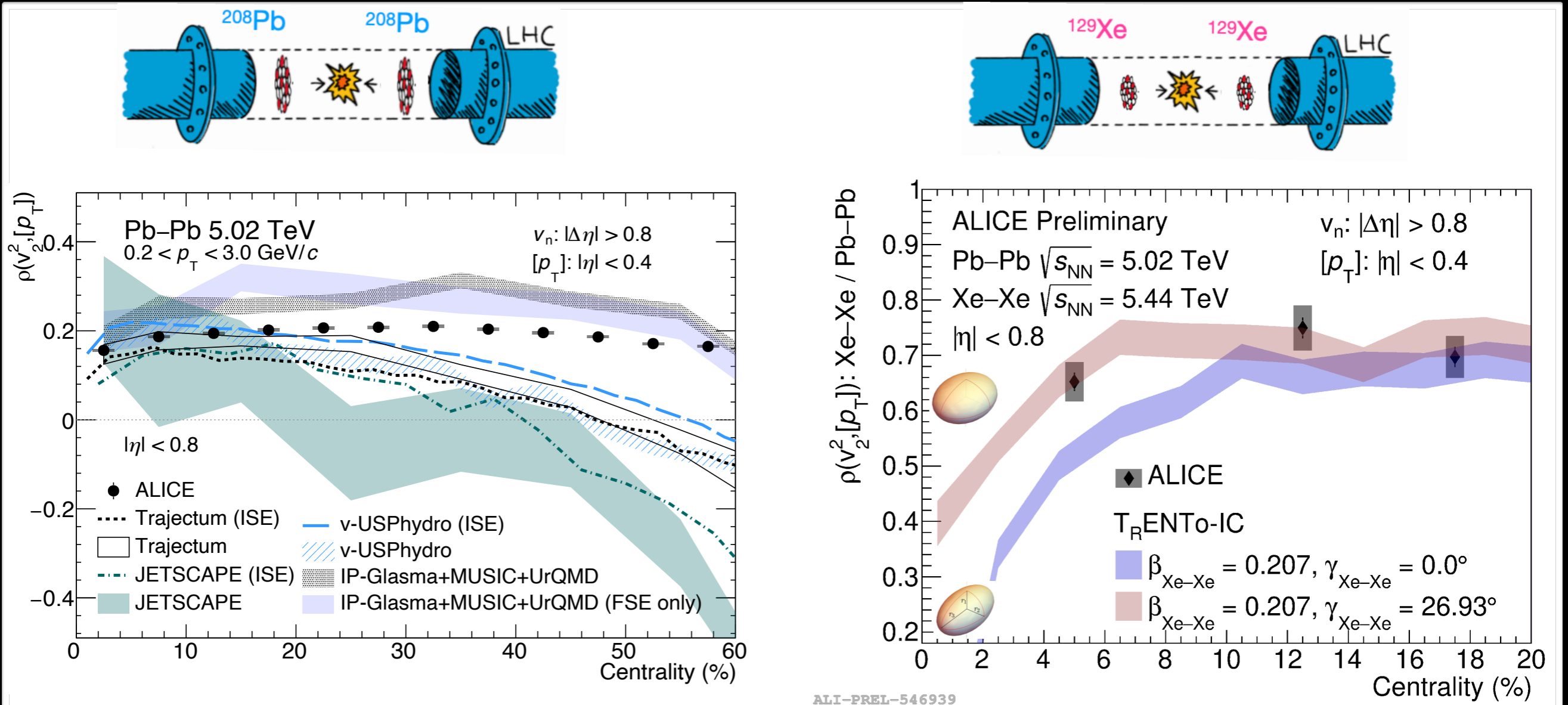
Probe triaxial structure of ^{129}Xe



ALI-PREL-546939



Probe triaxial structure of ^{129}Xe



❖ Better agreement between LHC data and calculations with $\gamma = 26.93^\circ$

- First study of triaxial structure of ^{129}Xe at high energy collisions at the LHC
- Similar results confirmed by ATLAS

▪ **Evidence of triaxial structure of ^{129}Xe ?** B. Bally etc, PRL128 (2022) 8, 082301



Probe γ -soft structure of ^{129}Xe

arXiv:2403.07441, submitted to PRL

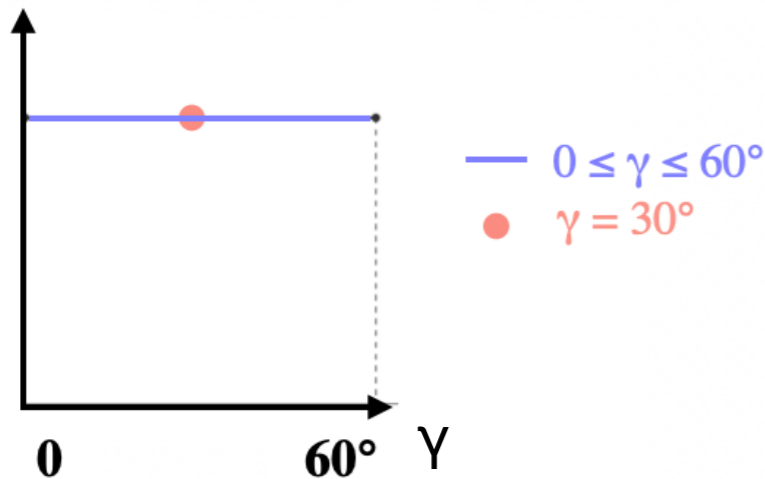
Nuclear Theory

[Submitted on 12 Mar 2024]

Exploring the Nuclear Shape Phase Transition in Ultra-Relativistic $^{129}\text{Xe}+^{129}\text{Xe}$ Collisions at the LHC

Shujun Zhao, Hao-jie Xu, You Zhou, Yu-Xin Liu, Huichao Song

The shape phase transition for certain isotope or isotone chains, associated with the quantum phase transition of finite nuclei, is an intriguing phenomenon in nuclear physics. A notable case is the Xe isotope chain, where the structure transits from a γ -soft rotor to a spherical vibrator, with the second-order shape phase transition occurring in the vicinity of $^{128-130}\text{Xe}$. In this letter, we focus on investigating the γ -soft deformation of ^{129}Xe associated with the second-order shape phase transition by constructing novel correlators for ultra-relativistic $^{129}\text{Xe}+^{129}\text{Xe}$ collisions. In particular, our iEBE-VISHNU model calculations show that the $v_2^2 - [p_T]$ correlation ρ_2 and the mean transverse momentum fluctuation Γ_{p_T} , which were previously interpreted as the evidence for the rigid triaxial deformation of ^{129}Xe , can also be well explained by the γ -soft deformation of ^{129}Xe . We also propose two novel correlators $\rho_{4,2}$ and $\rho_{2,4}$, which carry non-trivial higher-order correlations and show unique capabilities to distinguish between the γ -soft and the rigid triaxial deformation of ^{129}Xe in $^{129}\text{Xe}+^{129}\text{Xe}$ collisions at the LHC. The present study also provides a novel way to explore the second-order shape phase transition of finite nuclei with ultra-relativistic heavy ion collisions.

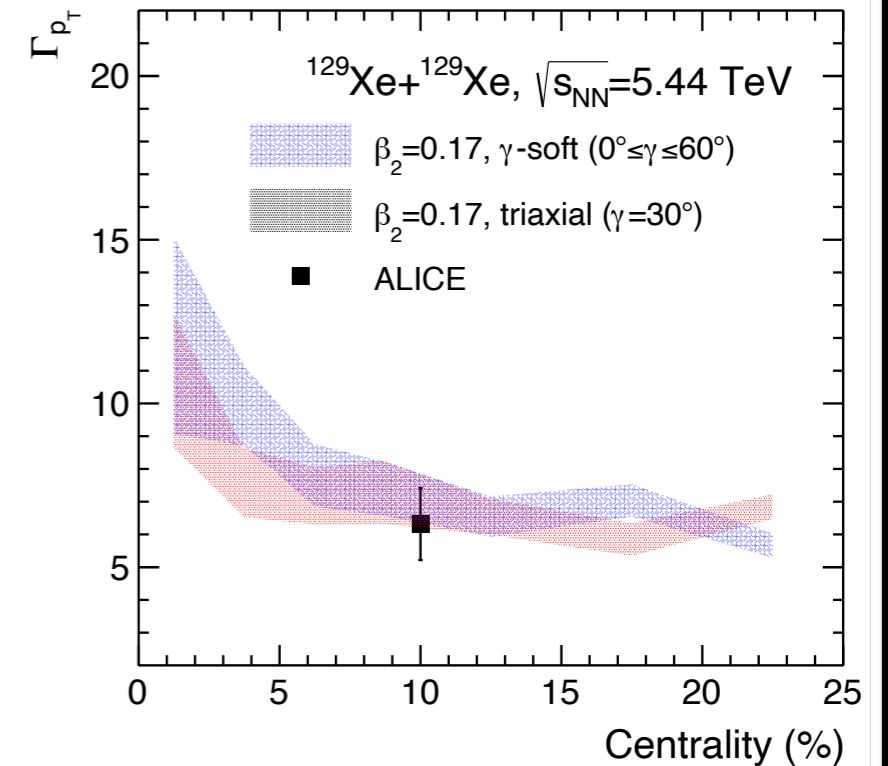


❖ As soon as the $\langle \cos(3\gamma) \rangle$ is the same, the ρ_2 and Γ_{p_T} are identical

- One can **NOT** distinguish triaxial (fixed $\gamma = 30^\circ$) and γ -soft (fluctuating γ) structures with existing 3-particle correlations

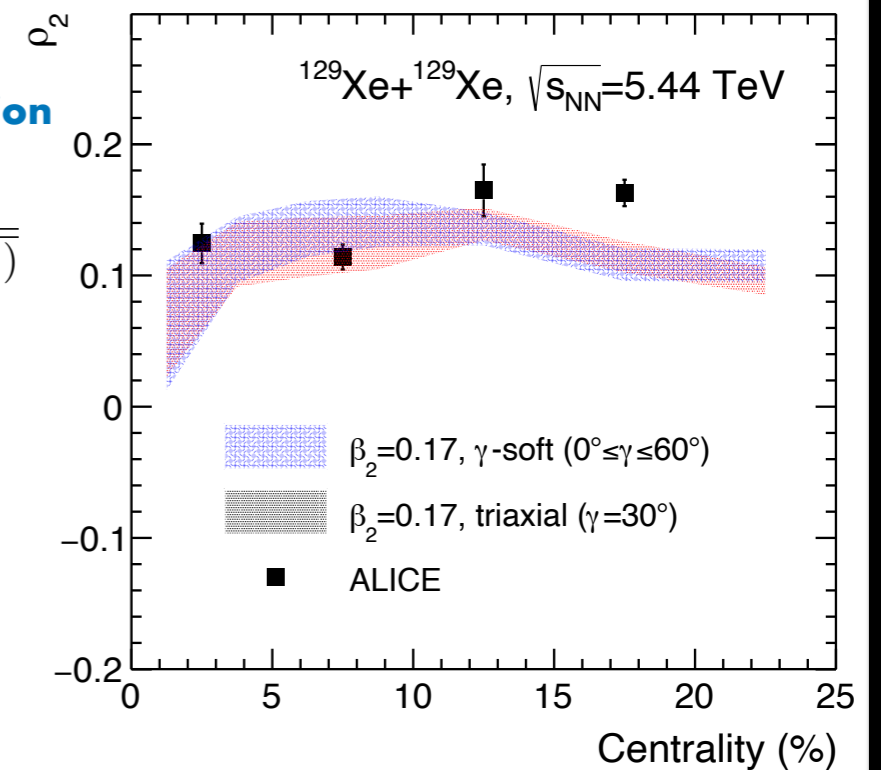
3-particle $[p_T]$ correlator

$$\Gamma_{p_T} = \frac{\langle \delta p_{T,i} \delta p_{T,j} \delta p_{T,k} \rangle \langle [x] \rangle}{\langle \delta p_{T,i} \delta p_{T,j} \rangle^2}$$

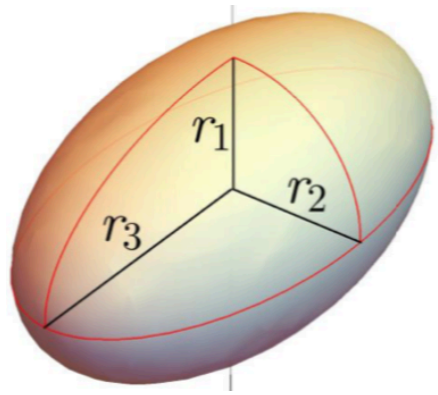


3-particle $v_2^2 - [p_T]$ correlation

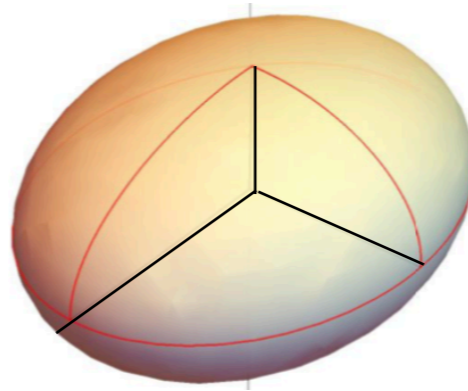
$$\rho_2 \equiv \frac{\text{cov}(v_2\{2\}^2, [p_T])}{\sqrt{\text{var}(v_2\{2\}^2)} \sqrt{\text{var}([p_T])}}$$



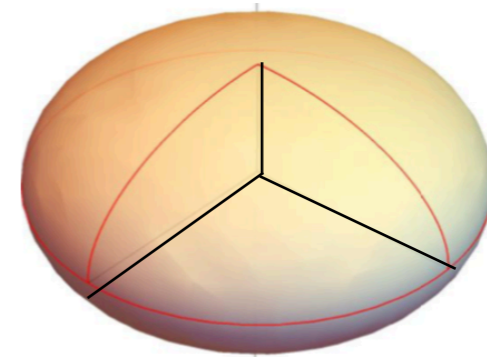
Simple logic



$\gamma = 0$
 $r_1 = r_2 < r_3$
prolate

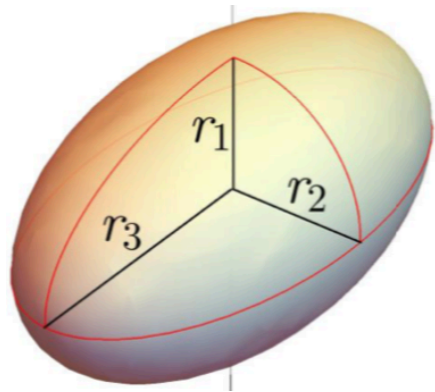


$\gamma = 30^\circ$
 $r_1 \neq r_2 \neq r_3$
triaxial

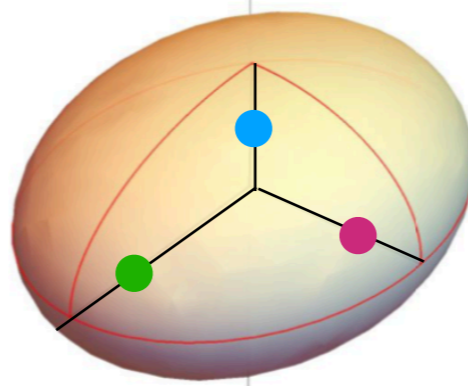


$\gamma = 60^\circ$
 $r_1 < r_2 = r_3$
oblate

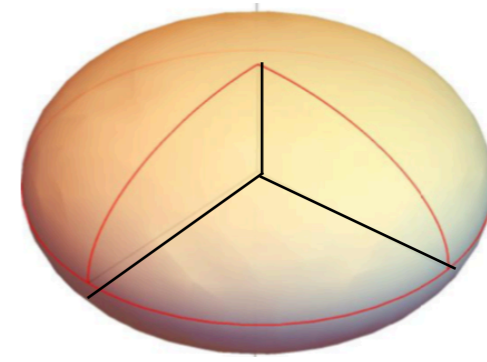
Simple logic



$\gamma = 0$
 $r_1 = r_2 < r_3$
prolate



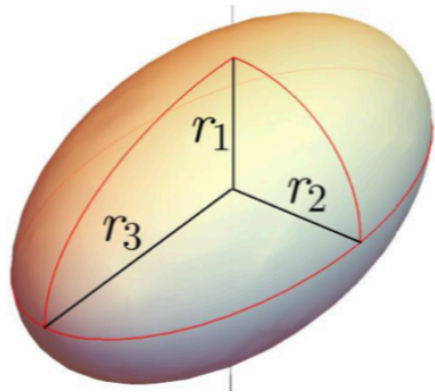
$\gamma = 30^\circ$
 $r_1 \neq r_2 \neq r_3$
triaxial



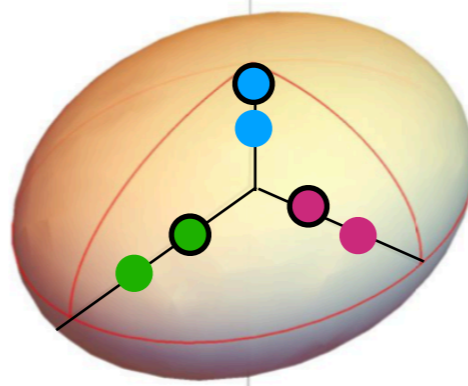
$\gamma = 60^\circ$
 $r_1 < r_2 = r_3$
oblate

❖ To probe the relation of r_1 , r_2 and r_3 , we need 3-particle correlations

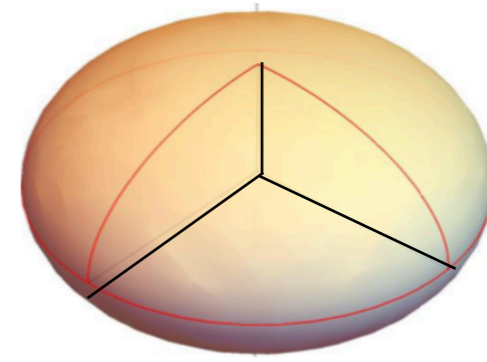
Simple logic



$\gamma = 0$
 $r_1 = r_2 < r_3$
prolate



$\gamma = 30^\circ$
 $r_1 \neq r_2 \neq r_3$
triaxial



$\gamma = 60^\circ$
 $r_1 < r_2 = r_3$
oblate

- ❖ To probe the relation of r_1 , r_2 and r_3 , we need 3-particle correlations
- ❖ To probe the γ fluctuations, we need 6-particle correlations

New probe for the γ -soft structure

New proposals:

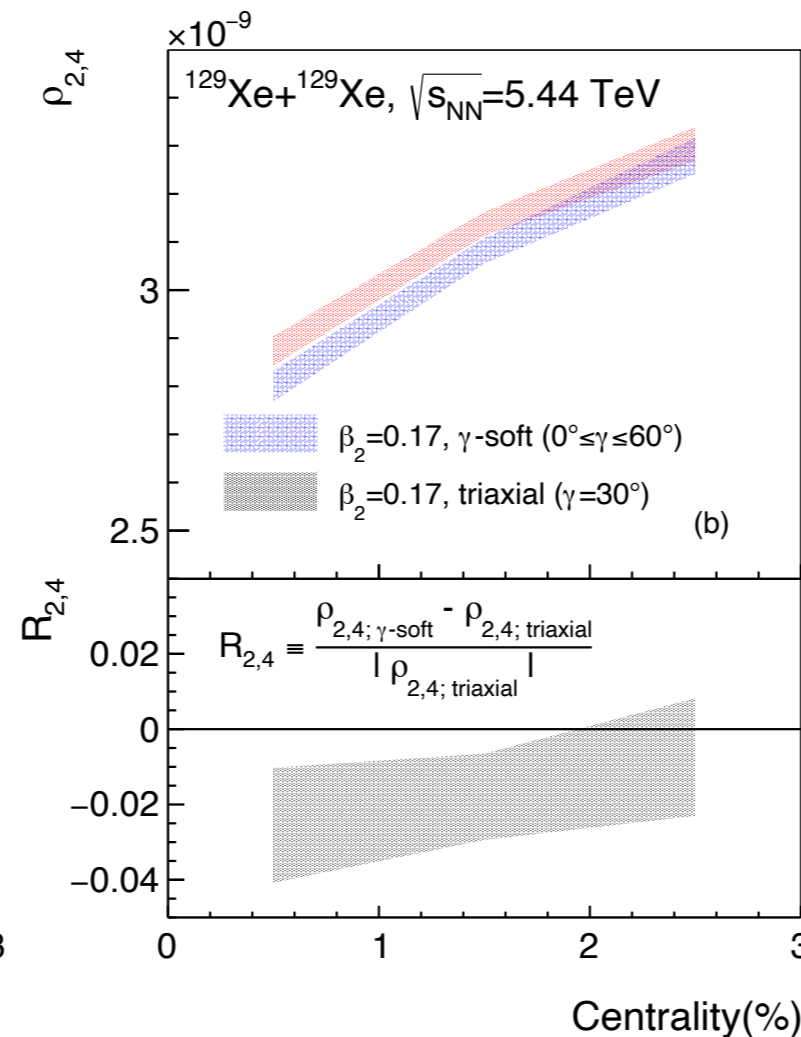
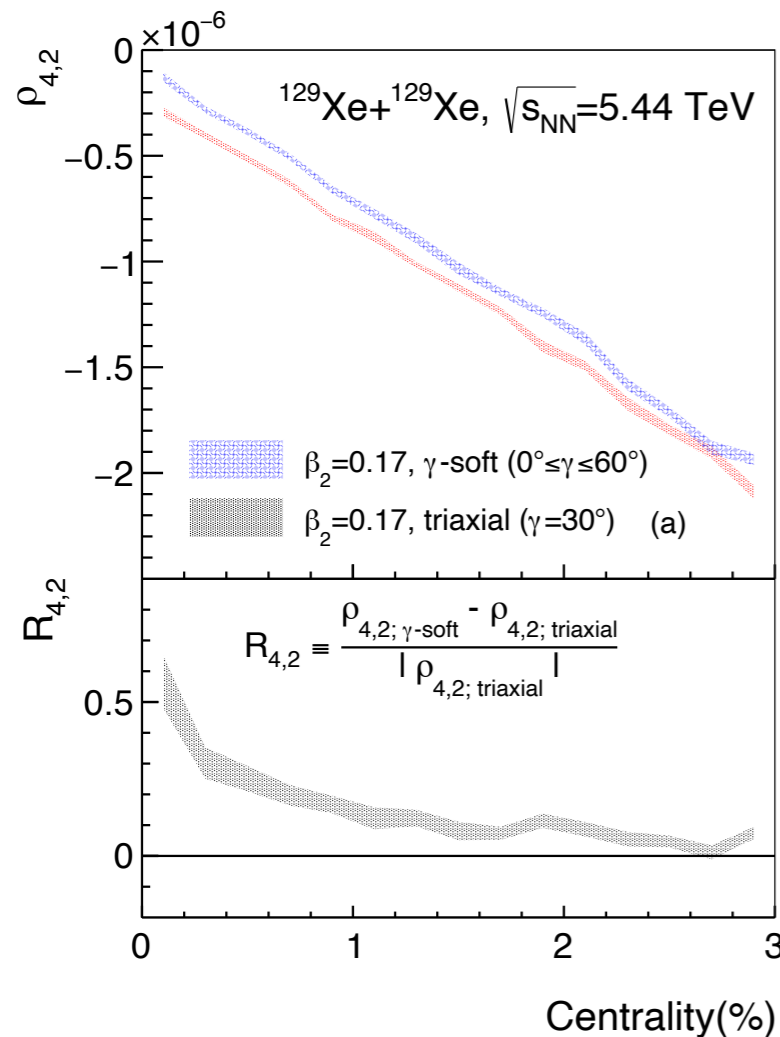
$$\rho_{4,2} \equiv \left(\frac{\langle \varepsilon_2^4 \delta d_\perp^2 \rangle}{\langle \varepsilon_2^4 \rangle \langle d_\perp \rangle^2} \right)_c \equiv \frac{1}{\langle \varepsilon_2^4 \rangle \langle d_\perp \rangle^2} [\langle \varepsilon_2^4 \delta d_\perp^2 \rangle + 4 \langle \varepsilon_2^2 \rangle^2 \langle \delta d_\perp^2 \rangle - \langle \varepsilon_2^4 \rangle \langle \delta d_\perp^2 \rangle - 4 \langle \varepsilon_2^2 \rangle \langle \varepsilon_2^2 \delta d_\perp^2 \rangle - 4 \langle \varepsilon_2^2 \delta d_\perp \rangle^2]$$

$$\rho_{2,4} \equiv \left(\frac{\langle \varepsilon_2^2 \delta d_\perp^4 \rangle}{\langle \varepsilon_2^2 \rangle \langle d_\perp \rangle^4} \right)_c \equiv \frac{1}{\langle \varepsilon_2^2 \rangle \langle d_\perp \rangle^4} [\langle \varepsilon_2^2 \delta d_\perp^4 \rangle - 6 \langle \varepsilon_2^2 \delta d_\perp^2 \rangle \langle \delta d_\perp^2 \rangle - 4 \langle \varepsilon_2^2 \delta d_\perp \rangle \langle \delta d_\perp^3 \rangle - \langle \varepsilon_2^2 \rangle \langle \delta d_\perp^4 \rangle + 6 \langle \varepsilon_2^2 \rangle (\langle \delta d_\perp^2 \rangle)]$$

Expectations:

$$\langle \varepsilon_2^4 \rangle \rho_{4,2} = A \beta_2^6 (53 + 16 \langle \cos(6\gamma) \rangle) + f_{4,2}(\beta_2^6, \langle \cos(3\gamma) \rangle)$$

$$\langle \varepsilon_2^2 \rangle \rho_{2,4} = \frac{A}{16} \beta_2^6 (43 - 14 \langle \cos(6\gamma) \rangle) + f_{2,4}(\beta_2^6, \langle \cos(3\gamma) \rangle)$$



❖ The six-particle correlations allow to differentiate triaxial (fixed $\gamma = 30^\circ$) and γ -soft (fluctuating γ) structures.

❖ Difference in $\rho_{4,2}$ can reach 50% in the ultra-central collisions.

❖ **Opening a new pathway to probe nuclear shape phase transition at the ultra-relativistic energies.**

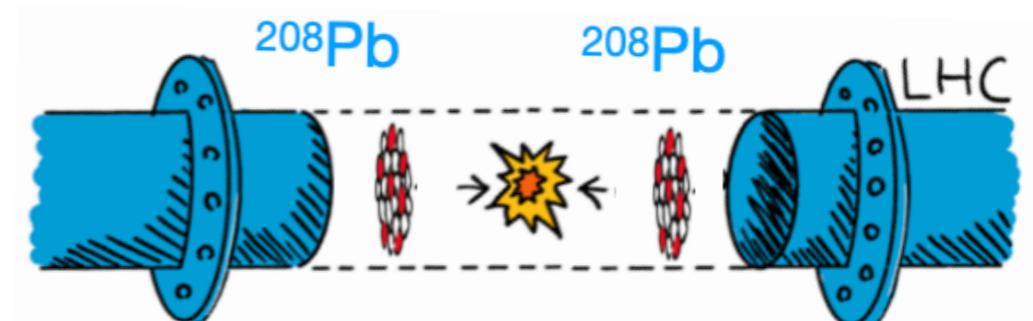
Massive Pb-Pb data



Run 2 2017 (pilot)

8 hours data taken

Massive Pb-Pb data



Run 2 2017 (pilot)

8 hours data taken

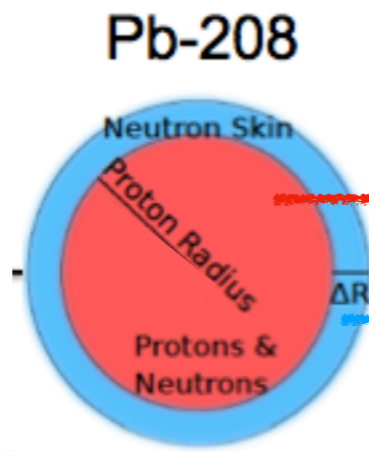
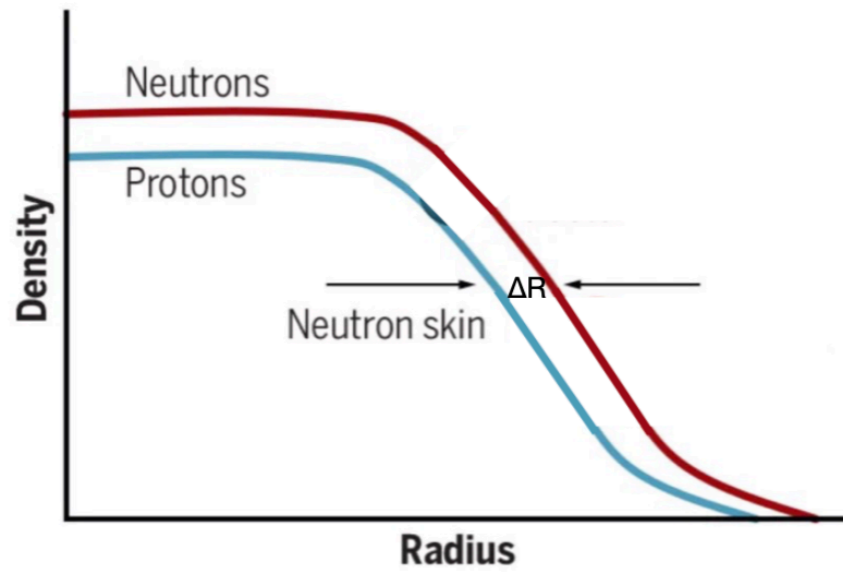
Run 1 2010, 2011

Run 2 2015, 2018

Run 3 2022 (pilot), 2023, 2024

4-6 weeks each period

Neutron skin study at High Energy

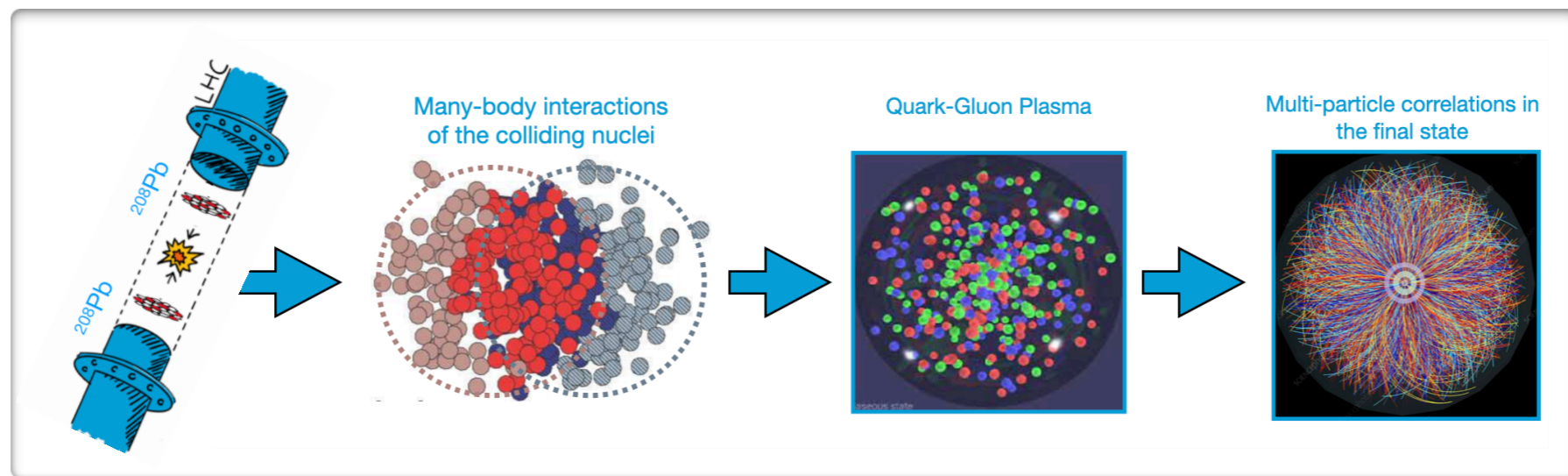


$$\rho(r, \Theta, \Phi) \propto \frac{1}{1 + \exp([r - R(\Theta, \Phi)] / a)}$$

$$\rho_p(r, \Theta, \Phi) \propto \frac{1}{1 + \exp([r_p - R_p(\Theta, \Phi)] / a_p)}$$

$$\rho_n(r, \Theta, \Phi) \propto \frac{1}{1 + \exp([r_n - R_n(\Theta, \Phi)] / a_n)}$$

$a_p = 0.448$ fm,
 $R_p = 6.680$ fm,
 $r_p = 5.436$ fm,
 $R_n = 6.690$ fm



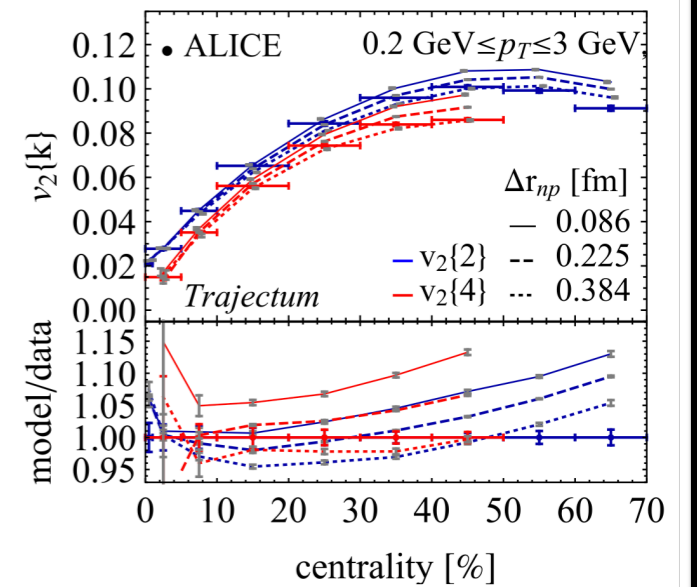
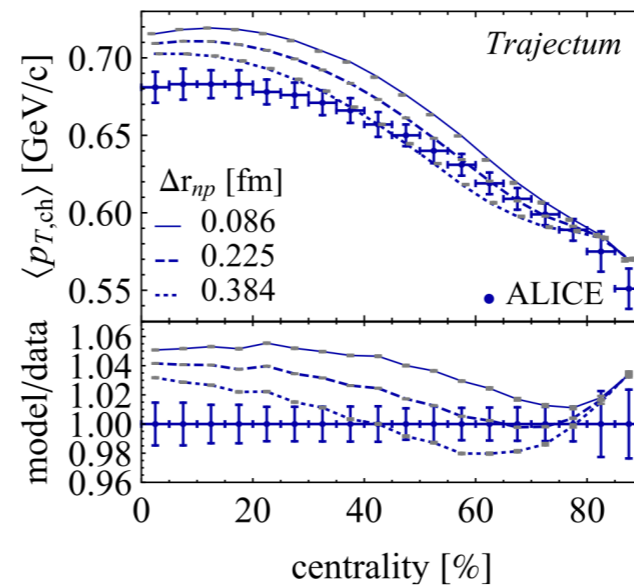
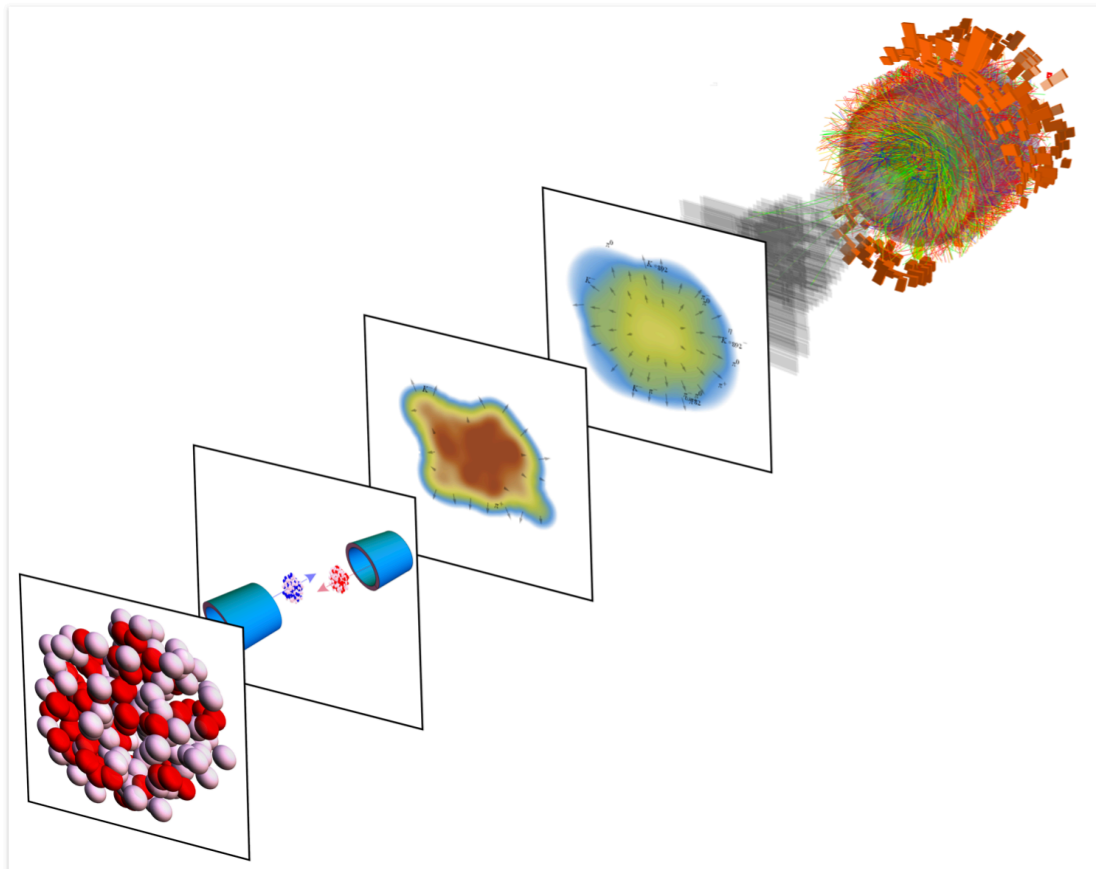
Extracting neutron skin of ^{208}Pb



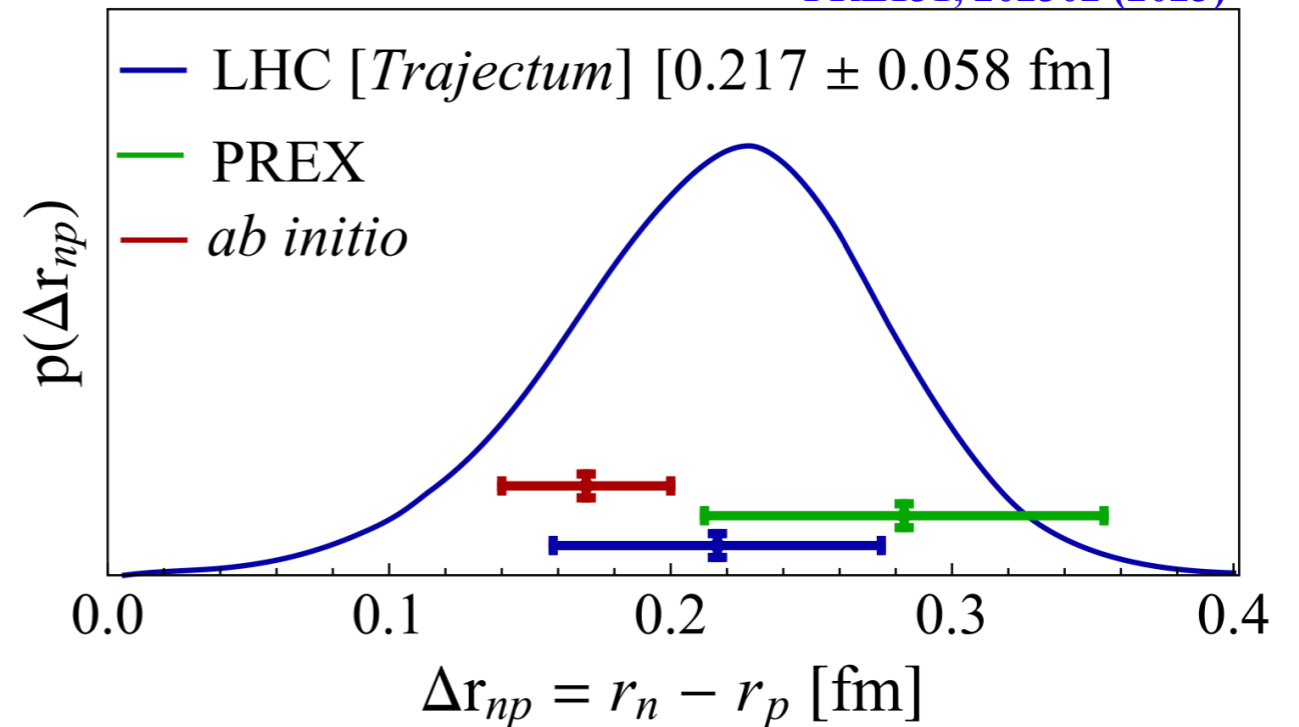
Thick-skinned: Using heavy-ion collisions at the LHC, scientists determine the thickness of neutron "skin" in lead-208 nuclei

This is the first measurement of the neutron skin of lead-208 using exchanges predominantly involving gluons and it can provide insight into the structure of nuclei and neutron stars

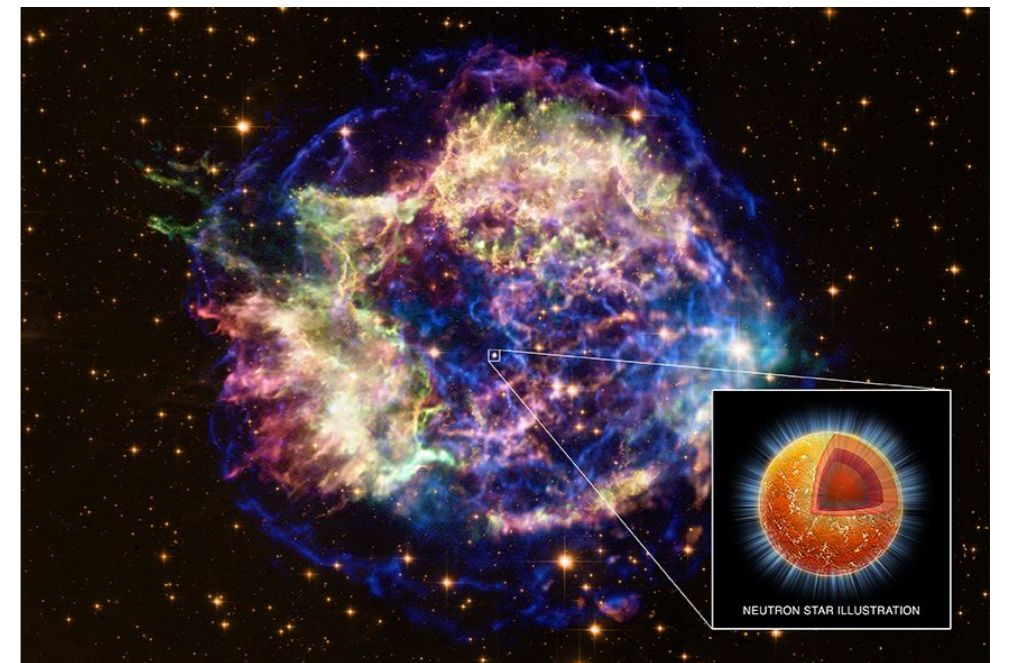
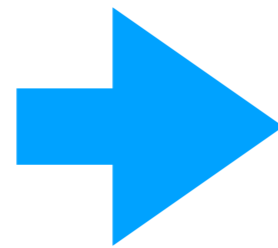
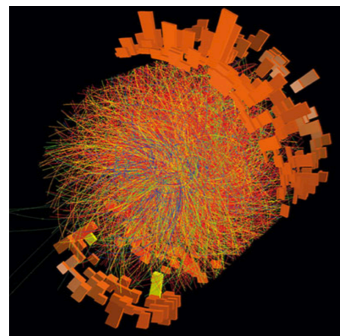
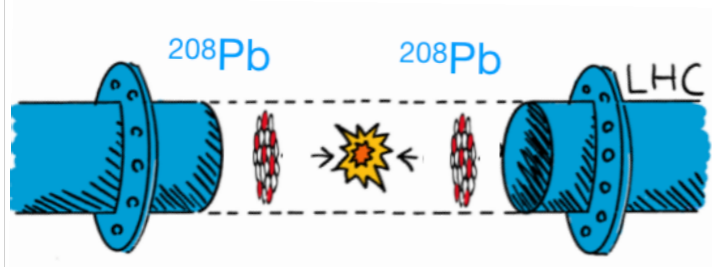
15 NOVEMBER, 2023 | By Naomi Dinmore



PRL131, 202302 (2023)



Connecting to astrophysics



Heavy-ion collisions

Neutron stars

And more

❖ More than just flow and $[p_T]$

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covering nuclear physics

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Effect of initial nuclear deformation on dielectron photoproduction in hadronic heavy-ion collisions

Jiaxuan Luo, Xinbai Li, Zebo Tang, Xin Wu, and Wangmei Zha
Phys. Rev. C **108**, 054906 – Published 27 November 2023



arXiv > hep-ph > arXiv:2405.16491


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High Energy Physics – Phenomenology

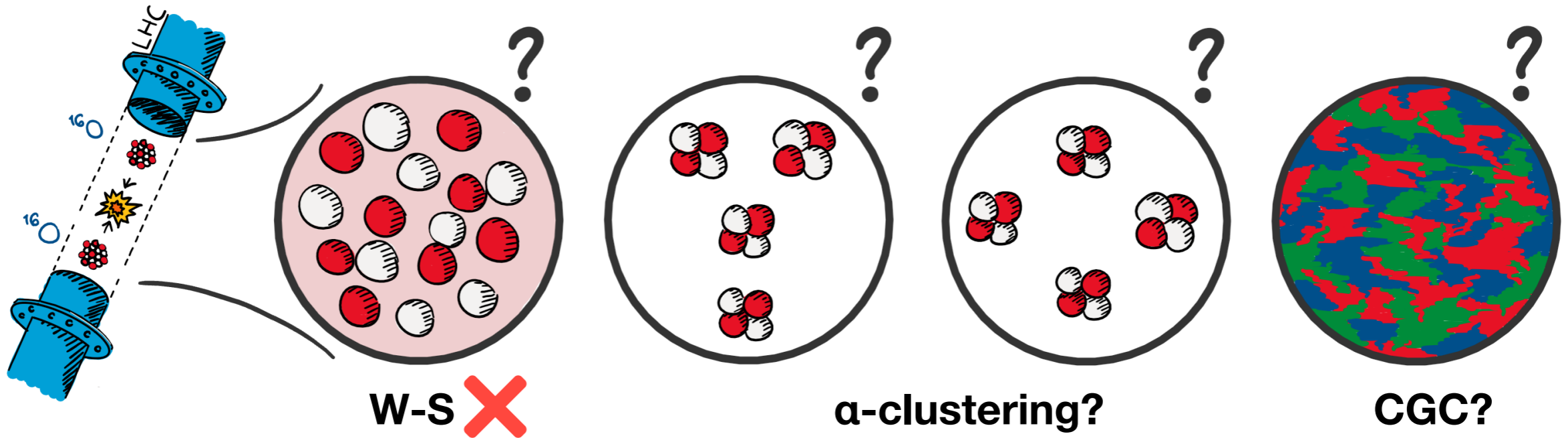
[Submitted on 26 May 2024]

Nuclear deformation effects in photoproduction of ρ mesons in ultraperipheral isobaric collisions

Shuo Lin, Jin-Yu Hu, Hao-Jie Xu, Shi Pu, Qun Wang



O-O collisions at the LHC in 2025



arXiv: 2402.05995

The unexpected uses of a bowling pin: exploiting ^{20}Ne isotopes for precision characterizations of collectivity in small systems

Giuliano Giacalone,^{1,*} Benjamin Bally,² Govert Nijs,³ Shihang Shen,⁴ Thomas Duguet,^{5,6} Jean-Paul Ebran,^{7,8} Serdar Elhatisari,^{9,10} Mikael Frosini,¹¹ Timo A. Lähde,^{12,13} Dean Lee,¹⁴ Bing-Nan Lu,¹⁵ Yuan-Zhuo Ma,¹⁴ Ulf-G. Meißner,^{10,16,17} Jacquelyn Noronha-Hostler,¹⁸ Christopher Plumberg,¹⁹ Tomás R. Rodríguez,²⁰ Robert Roth,^{21,22} Wilke van der Schee,^{3,23,24} and Vittorio Somà⁵

arXiv: 2404.08385

Ab-initio nucleon-nucleon correlations and their impact on high energy $^{16}\text{O}+^{16}\text{O}$ collisions

Chunjian Zhang,^{1,2,3,*} Jinhui Chen,^{1,2,†} Giuliano Giacalone,^{4,‡} Shengli Huang,^{3,§} Jianguyong Jia,^{3,5,¶} and Yu-Gang Ma^{1,2,**}

¹Key Laboratory of Nuclear Physics and Ion-beam Application (MOE), and Institute of Modern Physics, Fudan University, Shanghai 200433, China
²Shanghai Research Center for Theoretical Nuclear Physics, NSFC and Fudan University, Shanghai 200438, China
³Department of Chemistry, Stony Brook University, Stony Brook, NY 11794, USA
⁴Institut für Theoretische Physik, Universität Heidelberg, Philosophenweg 16, 69120 Heidelberg, Germany
⁵Physics Department, Brookhaven National Laboratory, Upton, NY 11976, USA

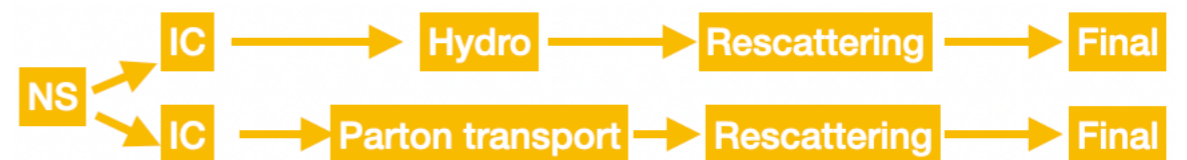
Investigating nucleon-nucleon correlations inherent to the strong nuclear force is one of the core goals in nuclear physics research. We showcase the unique opportunities offered by collisions of ^{16}O nuclei at high-energy facilities to reveal detailed many-body properties of the nuclear ground state. We interface existing knowledge about the geometry of ^{16}O coming from *ab-initio* calculations of nuclear structure with transport simulations of high-energy $^{16}\text{O}+^{16}\text{O}$ collisions. Bulk observables in these processes, such as the elliptic flow or the fluctuations of the mean transverse momentum, are found to depend significantly on the input nuclear model and to be sensitive to realistic clustering and short-range repulsive correlations, effectively opening a new avenue to probe these features experimentally. This finding demonstrates collisions of oxygen nuclei as a tool to elucidate initial conditions of small collision systems while fostering connections with effective field theories of nuclei rooted in quantum chromodynamics (QCD).

arXiv:2404.09780

Nuclear cluster structure effect in $^{16}\text{O}+^{16}\text{O}$ collisions at the top RHIC energy

Xin-Li Zhao,^{1,2,3} Guo-Liang Ma,^{2,3,*} You Zhou,^{4,†} Zi-Wei Lin,⁵ and Chao Zhang⁶
¹College of Science, University of Shanghai for Science and Technology, Shanghai 200093, China
²Key Laboratory of Nuclear Physics and Ion-beam Application (MOE), Institute of Modern Physics, Fudan University, Shanghai 200433, China
³Shanghai Research Center for Theoretical Nuclear Physics, NSFC and Fudan University, Shanghai 200438, China
⁴Niels Bohr Institute, Jagtvej 155A, 2200 Copenhagen, Denmark
⁵Department of Physics, East Carolina University, Greenville, NC 27858, USA
⁶School of Science, Wuhan University of Technology, Wuhan, 430070, China

The impact of nuclear structure has garnered considerable attention in the high-energy nuclear physics community in recent years. This work focuses on studying the potential nuclear cluster structure in ^{16}O nuclei using anisotropic flow observables in O+O collisions at 200 GeV. Employing an improved AMPT model with various cluster structure configurations, we find that an extended effective parton formation time is necessary to align with the recent STAR experimental data. In addition, we reveal that the presented flow observables serve as sensitive probes for differentiating configurations of α -clustering of ^{16}O nuclei. The systematic AMPT calculations presented in this paper, along with comprehensive comparisons to forthcoming experimental measurements at RHIC and the LHC, pave the way for a novel approach to investigate the α -clustering structure of ^{16}O nuclei using O+O collisions at the ultra-relativistic energies.



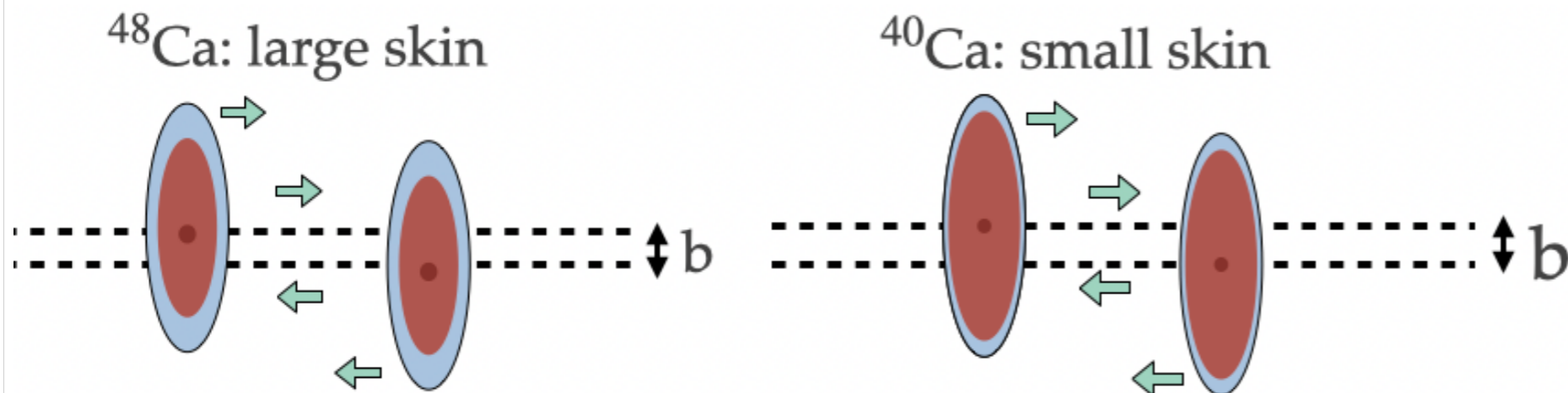
Future possibilities

CERN (11.2024)



TH Institute Light Ions at the LHC

- ☆ organised by CERN-TH, YZ (NBI), Qipeng Hu (USTC) etc.
- ☆ a dedicated workshop to discuss the new colliding light ions
- ❖ Neutron skin ^{40}Ca and ^{48}Ca



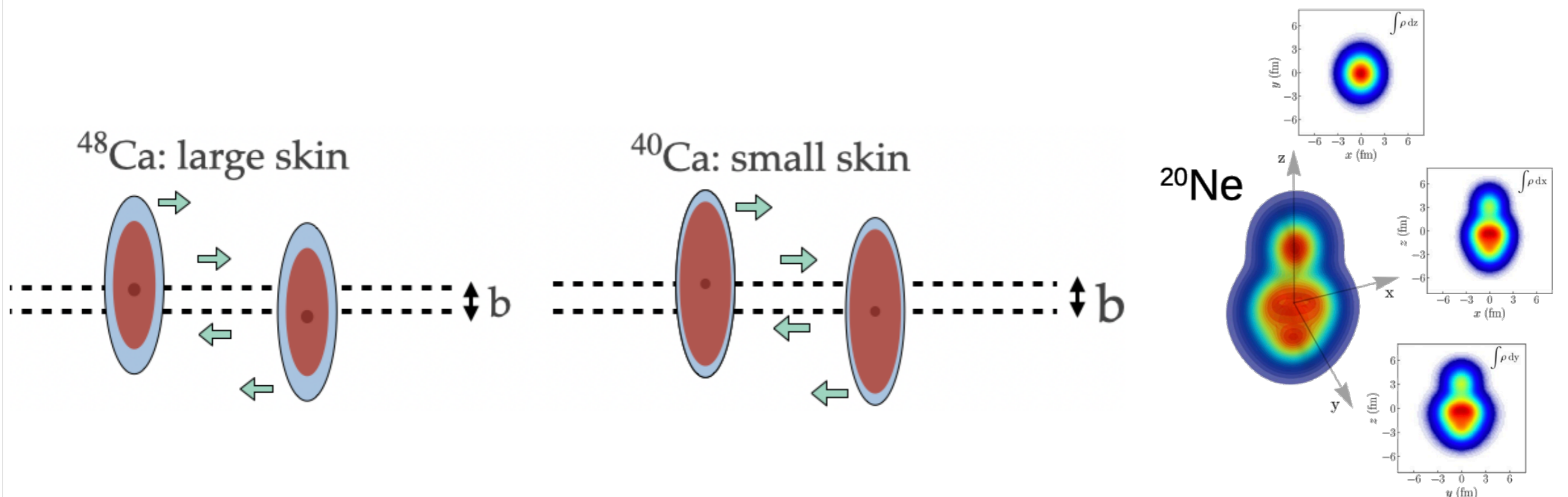
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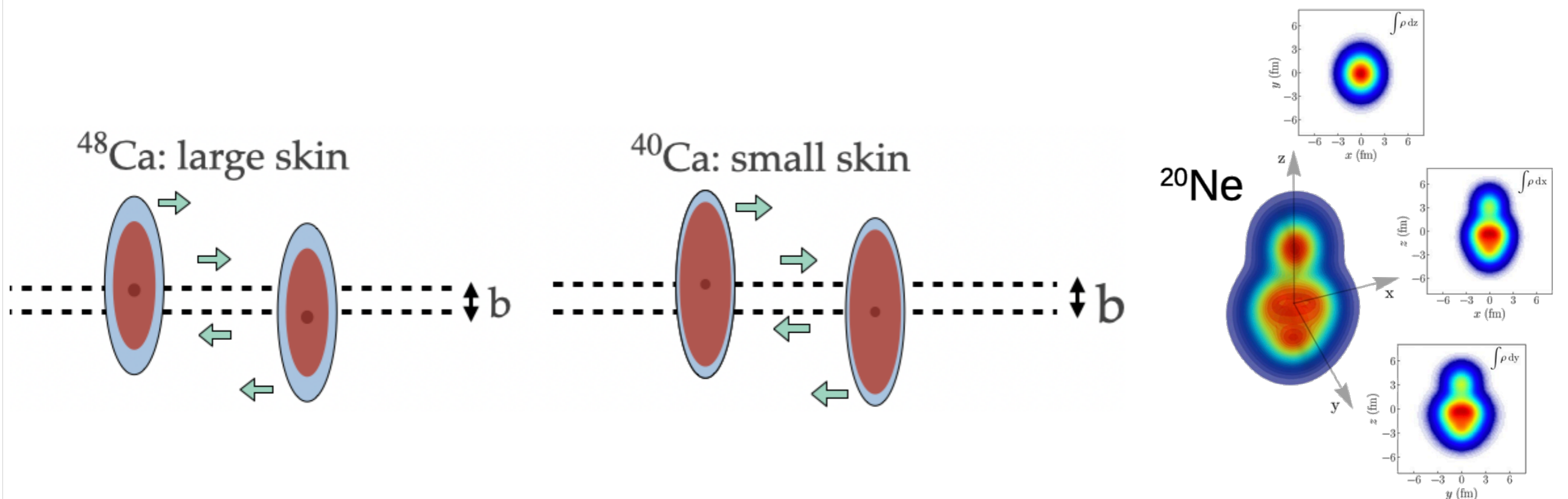
Future possibilities

CERN (11.2024)



TH Institute Light Ions at the LHC

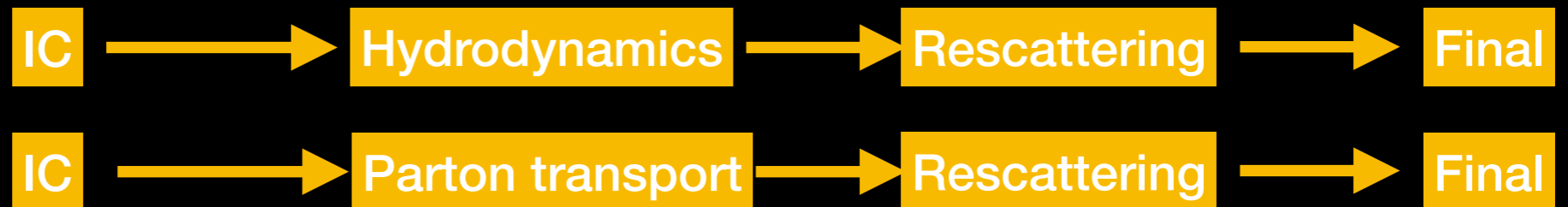
- ☆ organised by CERN-TH, YZ (NBI), Qipeng Hu (USTC) etc.
- ☆ a dedicated workshop to discuss the new colliding light ions
- ❖ Neutron skin ^{40}Ca and ^{48}Ca
- ❖ Further understanding on the α -clustering structure with ^{20}Ne
- ❖ New isobar runs ^{40}Ca vs ^{40}Ar (well within the capability of nuclear EFT calculations)



Possible open questions

Are the existing NS study at high energies model independent?

TH

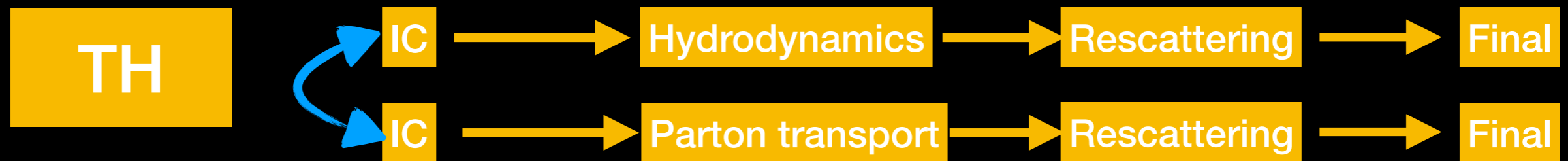


Possible open questions

Are the existing NS study at high energies model independent?

Q: Will the same NS input gives the same Initial Conditions?

- Will TRENTo gives the same $\varepsilon_2\{4\}/\varepsilon_2\{2\}$ as IP-Glasma or AMPT?



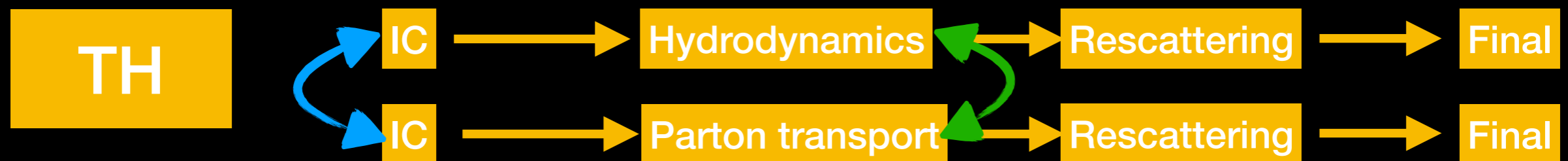
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Q: Any difference by using hydrodynamics and parton transport (AMPT)?



Possible open questions

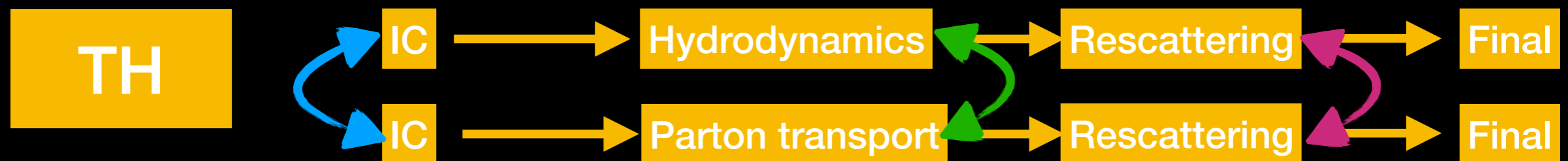
Are the existing NS study at high energies model independent?

Q: Will the same NS input gives the same Initial Conditions?

- Will TRENTo gives the same $\varepsilon_2\{4\}/\varepsilon_2\{2\}$ as IP-Glasma or AMPT?

Q: Any difference by using hydrodynamics and parton transport (AMPT)?

Q: Will the choices of hadronic rescattering models (SMASH, UrQMD, ART) matter for the NS study?

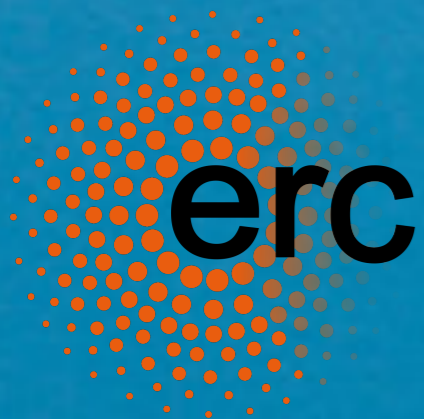


Conclusion **Remarks**

- ★ **The nuclear structure studies at the high energies (i.e., RHIC & LHC) can not replace the efforts of NS at low energies, OBVIOUSLY.**
- ★ **They complement each other**
 - ★ *NS@LE covers much wider range in the nuclide chart*
 - ★ *NS@HE enables novel opportunity to resolve some challenging questions (many-body, shape etc) with a few selected nuclei*
- ★ **The interactions between two communities are crucial**
 - ★ *Can we have a unified description of nuclear structure through the entire energy scale from MeV to TeV*

Thanks !





INDEPENDENT
RESEARCH FUND
DENMARK

★ **2 Postdoc (1 Flow, 1 FoCal)**

- starting Early 2025
- 600,000 RMB/year

★ **1 PhD (Flow)**

- Open call in spring 2025
- 450,000 RMB/year

★ **Contact You Zhou: You.Zhou AT cern.ch**



Bakcup




Recent Activities @ High Energies

BNL (01.2022)

RIKEN BNL Research Center
Physics Opportunities from the RHIC Isobar Run
This workshop will be held virtually.
January 25-28, 2022


[link](#)

GSI (05.2022)

 **EMMI Rapid Reaction Task Force: "Nuclear physics confronts relativistic collisions of isobars" (part 1/2)**
30 May 2022 to 3 June 2022
Heidelberg University

[link](#)

GSI (10.2022)

 **EMMI Rapid Reaction Task Force: "Nuclear physics confronts relativistic collisions of isobars" (part 2/2)**
12-14 October 2022
Heidelberg University

[link](#)

CEA, Saclay
(09.2022)

DE LA RECHERCHE À L'INDUSTRIE
cea
ESNT
Espace de Structure Nucléaire Théorique
DSM - DAM

Deciphering nuclear phenomenology across energy scales

[Back to the ESNT page](#)

20-23 September 2022

PROGRAM  [ESNTprogram19Sept2022DefVf.pdf](#)

[link](#)

INT (02.2023)

 **INSTITUTE for NUCLEAR THEORY**
INT PROGRAM INT-23-1A

Intersection of nuclear structure and high-energy nuclear collisions

[link](#)

NBI (06.2023)

 The VII-th International Conference on the
Initial Stages of High-Energy Nuclear
Collisions (IS2023), Copenhagen.



[link](#)



Activities in 2024 and beyond

PKU (04.2024)
Beijing

(Program + workshop
for two communities)

RHIC (0.2 TeV):

- U-U vs Au-Au
- Zr-Zr vs Ru-Ru
- O-O

LHC (~ 5 TeV):

- Xe-Xe vs Pb-Pb
- O-O

Exploring nuclear physics across energy scales 2024: intersection between nuclear structure and high energy nuclear collisions

15–26 Apr 2024
Asia/Shanghai timezone

Enter your search term



Overview

Participant List

Committees

Meeting and Hotel
Information

About Beijing

Visa to China

Transportation

Contact

✉ huichaosong@pku.edu.cn

Introduction: Recently, it has been realized that relativistic heavy ion collisions could provide new approaches to study some fundamental properties of atomic nuclei. It is therefore timely to gather scientists from both the low-energy and high-energy nuclear physics communities to discuss the recent progress and future perspective in this research direction. The two-week program+workshop on "Exploring Nuclear Physics across Energy Scales" emphasizes the intersection between nuclear structure and high-energy nuclear collisions, with a focus on the following questions: How does the low-energy structure of nuclei manifest in high-energy collisions? How do the observations made at colliders complement our knowledge of nuclear structure? During the program days ([April 15-18](#), [April 23-26](#)) the two invited speakers each day are expected to give a one-hour seminar with sufficient time for discussions. The embedded workshop ([20-22 April](#)) will be 3 days with 25-30 invited talks and 3 short discussion sections.

The scientific program includes the following topics, which emphasises the intersections between nuclear structure and high-energy collisions.

- Manifestation of nuclear deformations across energy scales
- Neutron skin determinations and applications
- Many-body correlations and clustering in light nuclei
- Bayesian analysis for high-energy collisions and nuclear structure
- Role of nuclear structure in low- and intermediate-energy collisions
- Connection to Ultra-peripheral Collisions (UPCs) and the future Electron-Ion Collider (EIC)
- Opportunities with colliding new species at future high-energy experiments

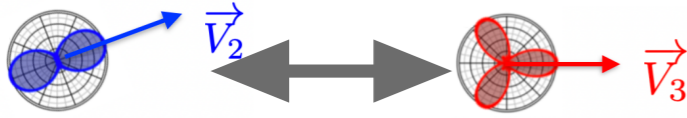


(Normalized) Symmetric Cumulant

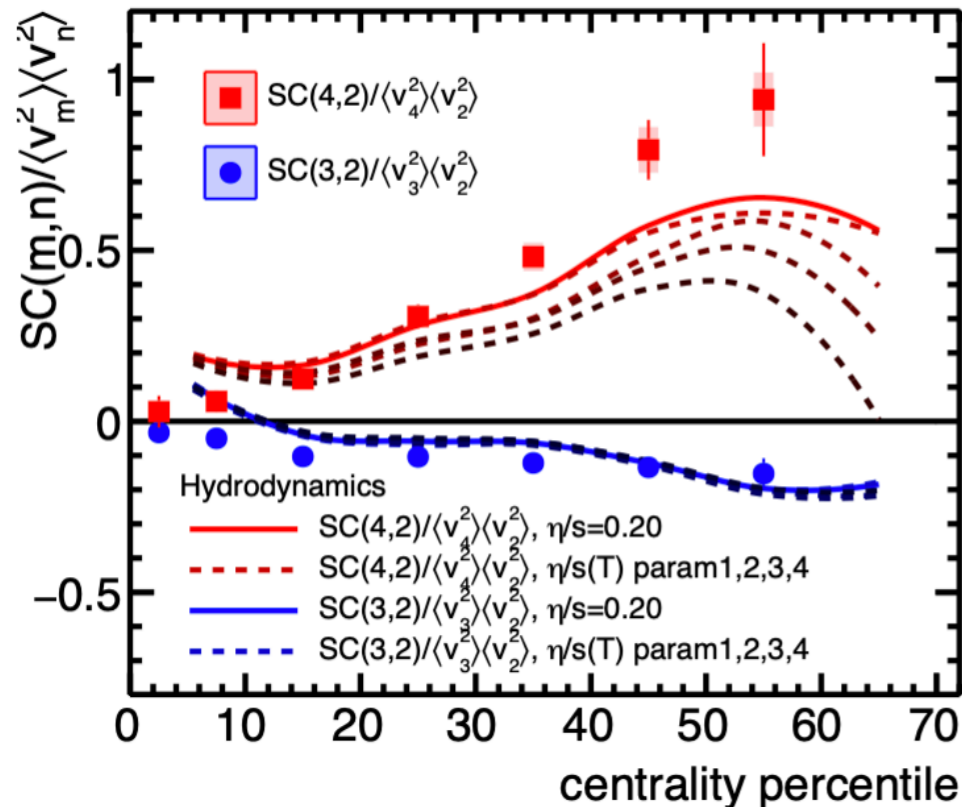
How do v_n and v_m correlate

Symmetric cumulants:

$$SC(m, n) = \langle v_m^2 v_n^2 \rangle - \langle v_m^2 \rangle \langle v_n^2 \rangle$$



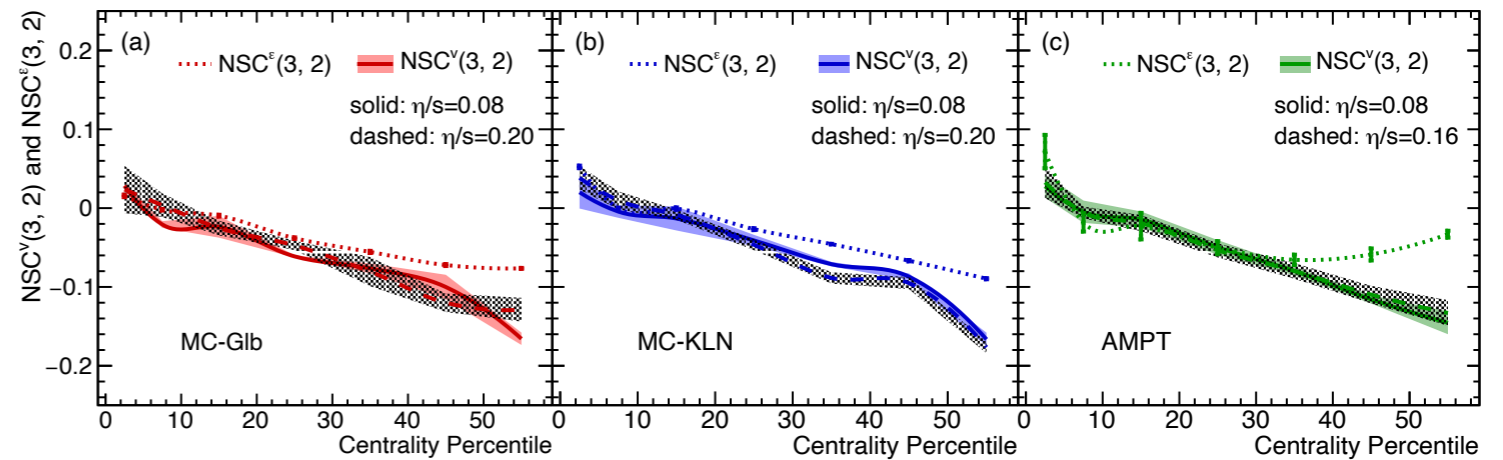
ALICE, PRL117, 182301 (2016)



Generic framework for anisotropic flow analyses with multiparticle azimuthal correlations

Ante Bilandzic,¹ Christian Holm Christensen,¹ Kristjan Gulbrandsen,¹ Alexander Hansen,¹ and You Zhou^{2,3}
¹Niels Bohr Institute, Blegdamsvej 17, 2100 Copenhagen, Denmark
²Nikhef, Science Park 105, 1098 XG Amsterdam, The Netherlands
³Utrecht University, P.O. Box 80000, 3508 TA Utrecht, The Netherlands

Xiangrong Zhu, YZ, Haojie Xu, and Huichao Song, PRC95, 044902 (2017)



$$\begin{aligned} v_2 &\propto \varepsilon_2 \\ v_3 &\propto \varepsilon_3 \end{aligned}$$



$$\frac{\langle v_2^2 v_3^2 \rangle - \langle v_2^2 \rangle \langle v_3^2 \rangle}{\langle v_2^2 \rangle \langle v_3^2 \rangle} = \frac{\langle \varepsilon_2^2 \varepsilon_3^2 \rangle - \langle \varepsilon_2^2 \rangle \langle \varepsilon_3^2 \rangle}{\langle \varepsilon_2^2 \rangle \langle \varepsilon_3^2 \rangle}$$

Or: $NSC^v(3,2) = NSC^e(3,2)$

❖ The very first direct measurement of correlations between v_n and v_m

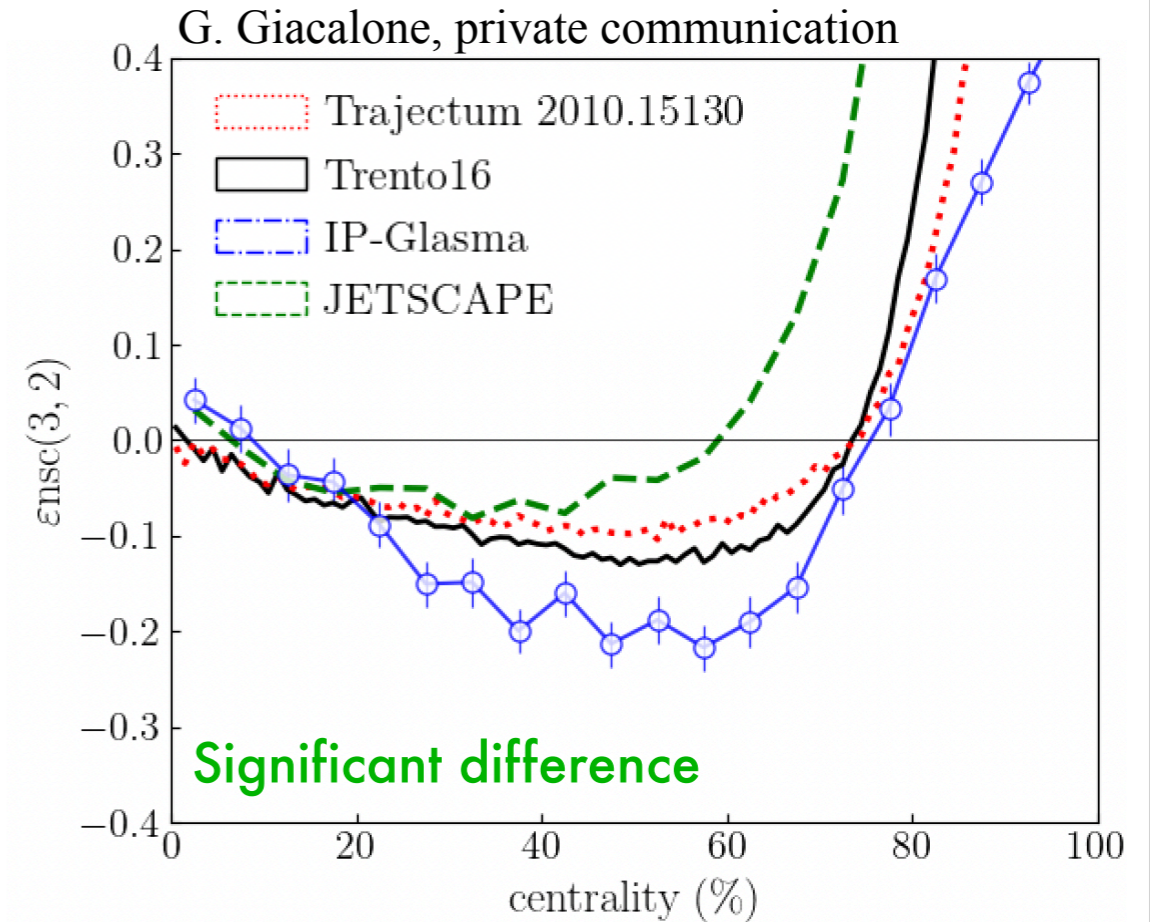
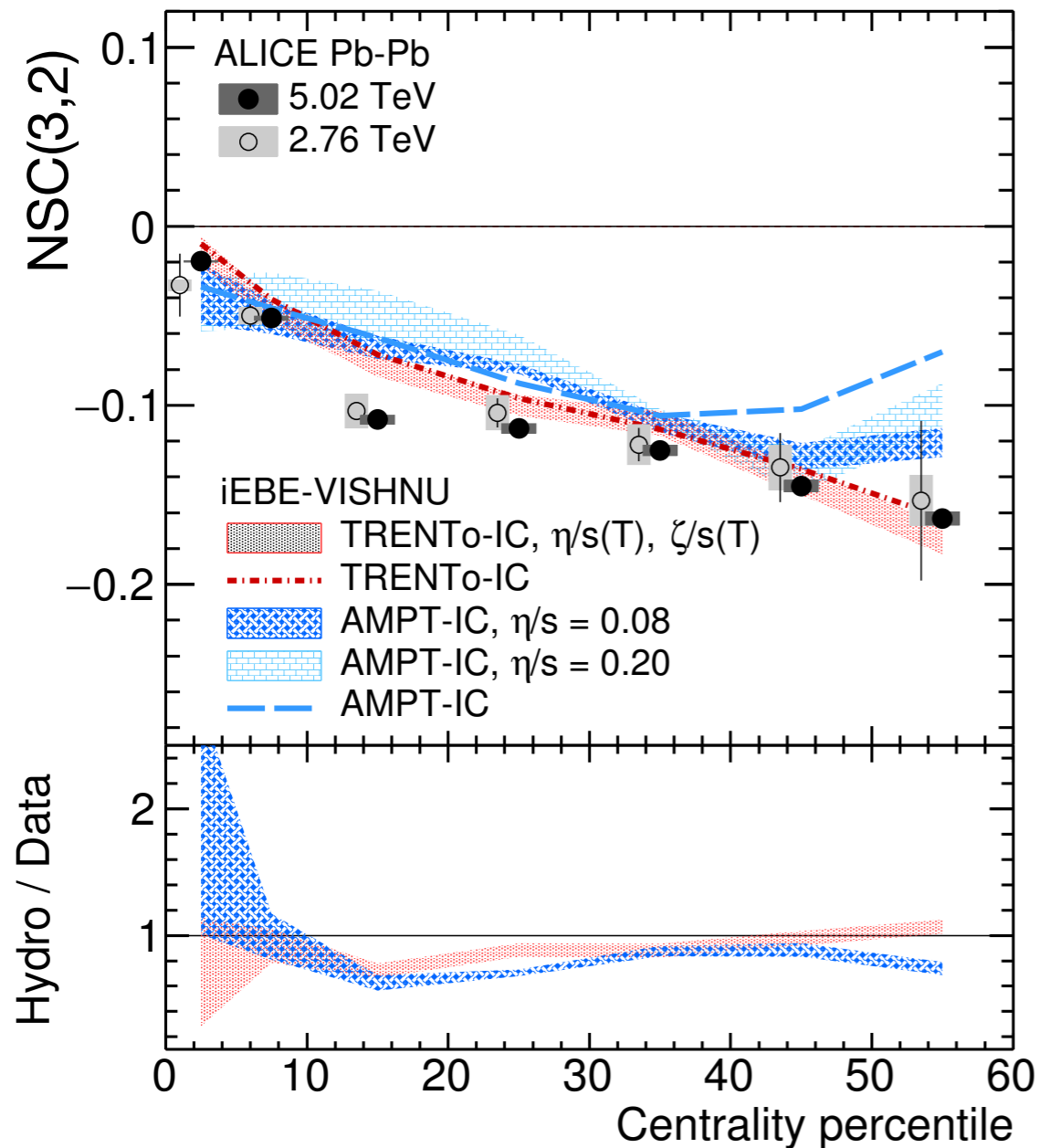
- NSC(3,2) is insensitive to η/s
- NSC(3,2) measurements provide a direct access into the initial conditions (despite details of systems evolution)
- Can we use NSC to explore the nuclear structure?



Probe IC with NSC(3,2)

How do v_n and v_m correlate

$$NSC^v(3,2) = NSC^\epsilon(3,2)$$



- ❖ Precision NSC(3,2) data provides tight constraints on the initial state models
- ❖ what is the general correlation between any order of v_n^k and v_m^p and the correlations among multiple flow coefficients

ALICE, PLB818 (2021) 136354

iEBE-VISHNU, M. Li, YZ etc, PRC104, 024903 (2021)



A reminder




J. Jia, JPG41 (2014) 124003

	pdfs	cumulants
Flow-amplitudes	$p(v_n)$	$v_n\{2k\}, k = 1,2,\dots$
	$p(v_n, v_m)$	$\langle v_n^2 v_m^2 \rangle - \langle v_n^2 \rangle \langle v_m^2 \rangle, n \neq m$...
	$p(v_n, v_m, v_l)$	$\langle v_n^2 v_m^2 v_l^2 \rangle + 2\langle v_n^2 \rangle \langle v_m^2 \rangle \langle v_l^2 \rangle -$ $\langle v_n^2 v_m^2 \rangle \langle v_l^2 \rangle - \langle v_m^2 v_l^2 \rangle \langle v_n^2 \rangle - \langle v_l^2 v_n^2 \rangle \langle v_m^2 \rangle$ $n \neq m \neq l$...
	...	Obtained recursively as above
EP-correlation	$p(\Phi_n, \Phi_m, \dots)$	$\langle v_n^{ c_n } v_m^{ c_m } \dots \cos(c_n n \Phi_n + c_m m \Phi_m + \dots) \rangle$ $\sum_k k c_k = 0$
Mixed-correlation	$p(v_l, \Phi_n, \Phi_m, \dots)$	$\langle v_l^2 v_n^{ c_n } v_m^{ c_m } \dots \cos(c_n n \Phi_n + c_m m \Phi_m + \dots) \rangle -$ $\langle v_l^2 \rangle \langle v_n^{ c_n } v_m^{ c_m } \dots \cos(c_n n \Phi_n + c_m m \Phi_m + \dots) \rangle$ $\sum_k k c_k = 0, n \neq m \neq l \dots$

- ❖ One algorithm for any particle cumulant
 - Multi-particle mixed harmonic cumulants
 - correlation between v_m^k, v_n^l and v_p^q
 - correlation between v_m^k and v_n^l
 - No need of any package !

PHYSICAL REVIEW C 103, 024913 (2021)

Generic algorithm for multiparticle cumulants of azimuthal correlations in high energy nucleus collisions

Zuzana Moravcova , Kristjan Gulbrandsen ,* and You Zhou [†]
Niels Bohr Institute, Blegdamsvej 17, 2100 Copenhagen, Denmark

m-particle cumulant

```

complex Cumulant(int* harmonic, int n, bool remove_zeros=true, int negsplit=-1,
int mult = 1, int skip = 0)
{
    bool remove_term = false;
    if (remove_zeros)
    {
        int har_sum = 0;
        for (int i = 0; i<mult; ++i) har_sum += harmonic[n-1+i];
        if (har_sum != 0) remove_term = true;
    }
    complex c = 0;
    if (!remove_term)
    {
        c = Corr(harmonic+(n-1), mult);
        if (n == 1) return c;
        c *= negsplit*Cumulant(harmonic, n-1, remove_zeros, negsplit-1);
    }

    int h_hold = harmonic[n-2];
    for (int counter = 0; counter <= n-2-skip; ++counter)
    {
        harmonic[n-2] = harmonic[counter];
        harmonic[counter] = h_hold;
        c += Cumulant(harmonic, n-1, remove_zeros, negsplit, mult+1, n-2-counter);
        harmonic[counter] = harmonic[n-2];
    }
    harmonic[n-2] = h_hold;
    return c;
}
    
```

m-particle correlation

```

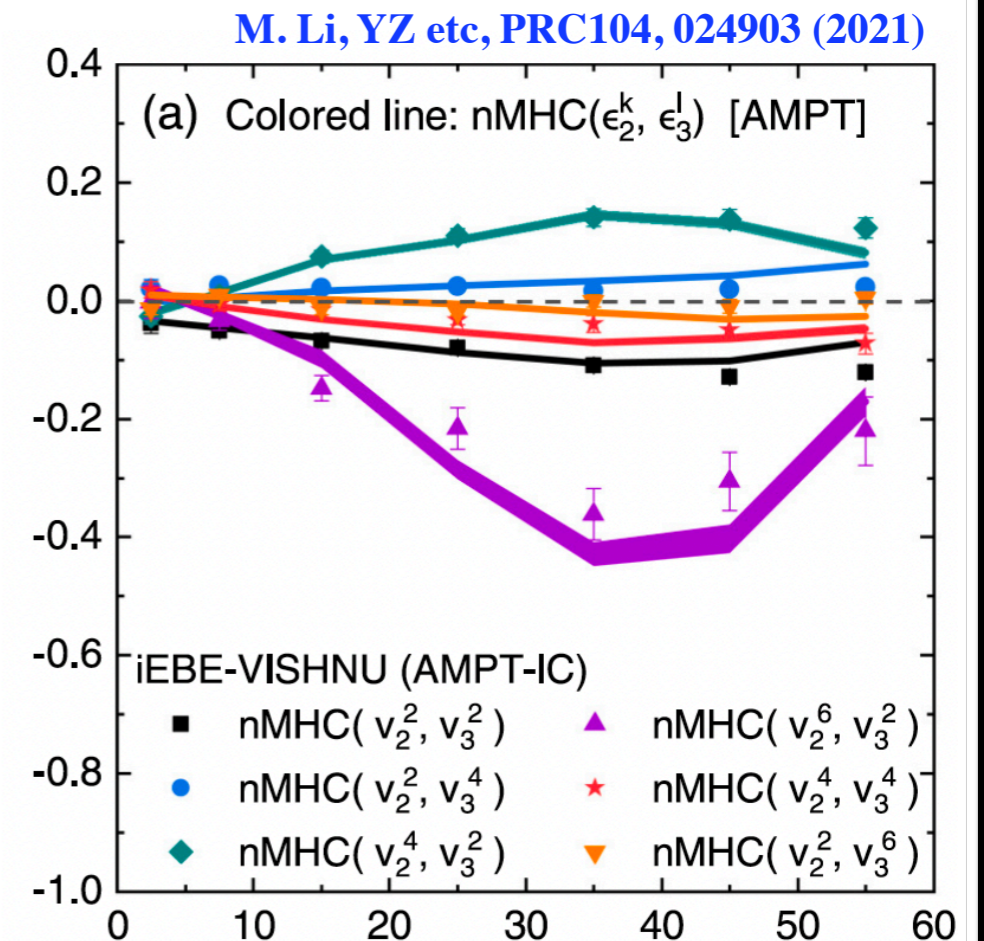
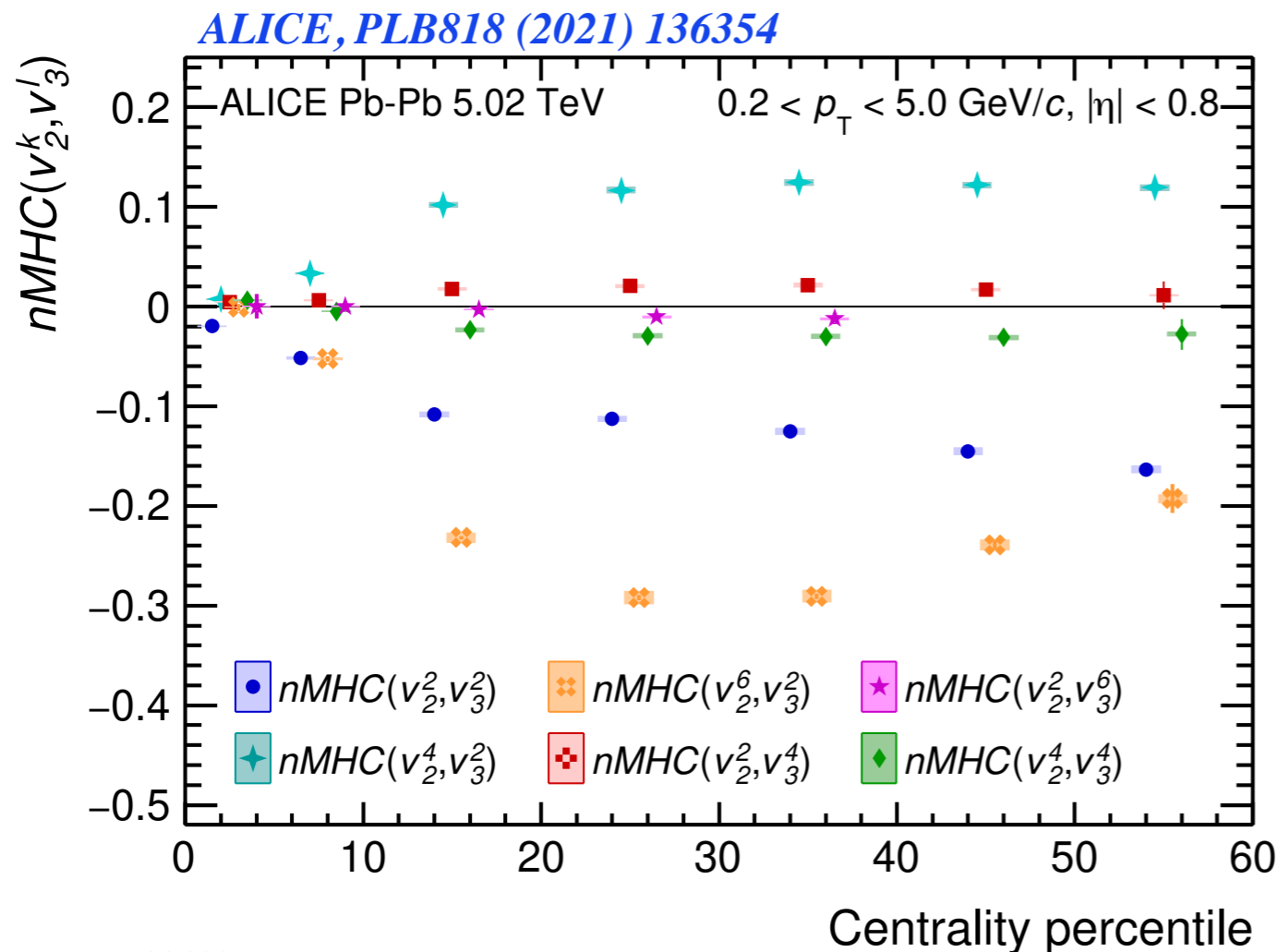
complex Correlator(int* harmonic, int n, int mult = 1, int skip = 0)
{
    int har_sum = 0;
    for (int i = 0; i<mult; ++i) har_sum += harmonic[n-1+i];
    complex c(Q(har_sum, mult));
    if (n == 1) return c;
    c *= Correlator(harmonic, n-1);
    if (n == 1+skip) return c;

    complex c2 = 0;
    int h_hold = harmonic[n-2];
    for (int counter = 0; counter <= n-2-skip; ++counter)
    {
        harmonic[n-2] = harmonic[counter];
        harmonic[counter] = h_hold;
        c2 += Correlator(harmonic, n-1, mult+1, n-2-counter);
        harmonic[counter] = harmonic[n-2];
    }
    harmonic[n-2] = h_hold;
    return c-mult*c2;
}
    
```



Mixed harmonic cumulants

How do v_n and v_m correlate



ALI-PUB-482633

- ❖ First measurement of correlations between higher order moments of v_2 and v_3
 - Final state results quantitatively reproduced by the initial state correlations
 - Experimental data provides direct constraints on the correlations of higher order moments of eccentricity coefficients from initial state models



TRENTo IC

- ❖ Fully parametrised initial conditions

$$P_{\text{wounded}} = 1 - \exp\left(-\sigma_{gg} \int d\mathbf{x} \rho_A(\mathbf{x}) \rho_B(\mathbf{x})\right), \quad \rho_{A/B} \propto \exp\left(\frac{-|\mathbf{x} - \mathbf{x}_{A/B}|^2}{2w^2}\right)$$

- ❖ Deposit energy into each nucleus' thickness function

$$T_{A/B} = \sum_{i \in \text{wounded } A/B} \gamma \exp(-|\mathbf{x} - \mathbf{x}_i|^2 / 2w^2)$$

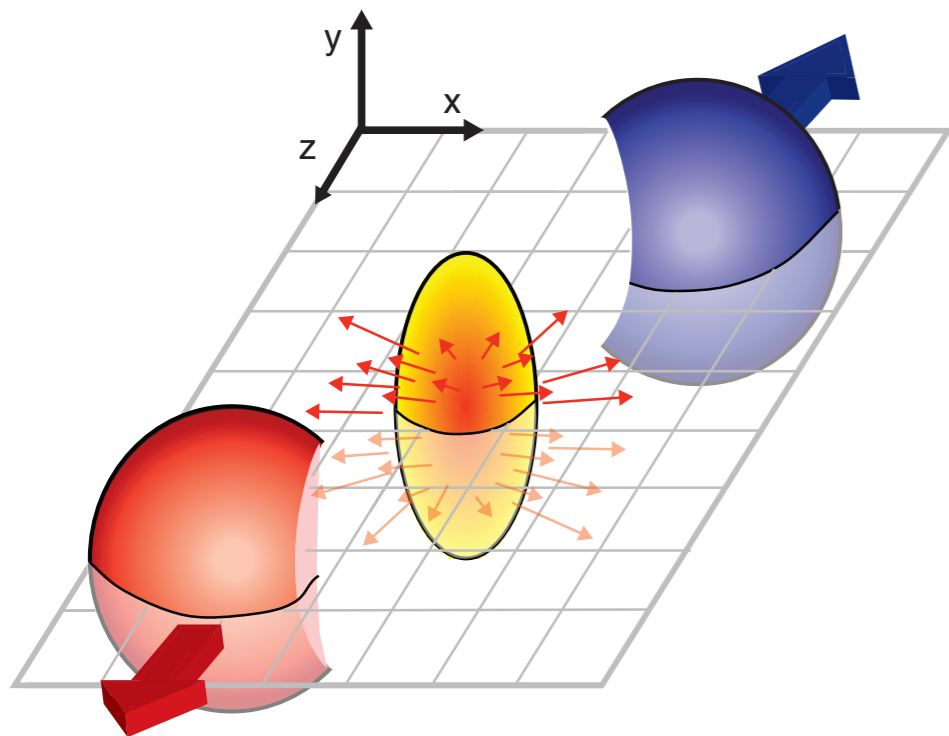
- ❖ Modify to include quark constituents $\rho_A = \frac{1}{n_c} \sum_{i=1}^{n_c} \rho_c(\mathbf{x} - \mathbf{x}_i)$

- ❖ Generalised mean of thickness functions

$$\left. \frac{dS}{d^2x_{\perp} d\eta} \right|_{\eta=0} \propto \left(\frac{(T_A + T_B)^p}{2} \right)^{1/p} \longrightarrow \left. \frac{dS}{d\eta} \right|_{\eta=0} \propto \begin{cases} \max(T_A, T_B) & p \rightarrow +\infty \\ (T_A + T_B)/2 & p = +1 \text{ (arithmetic)} \\ \sqrt{T_A T_B} & p = 0 \text{ (geometric)} \\ 2T_A T_B / (T_A + T_B) & p = -1 \text{ (harmonic)} \\ \min(T_A, T_B) & p \rightarrow -\infty \end{cases}$$

Pictures at low energy and high energy

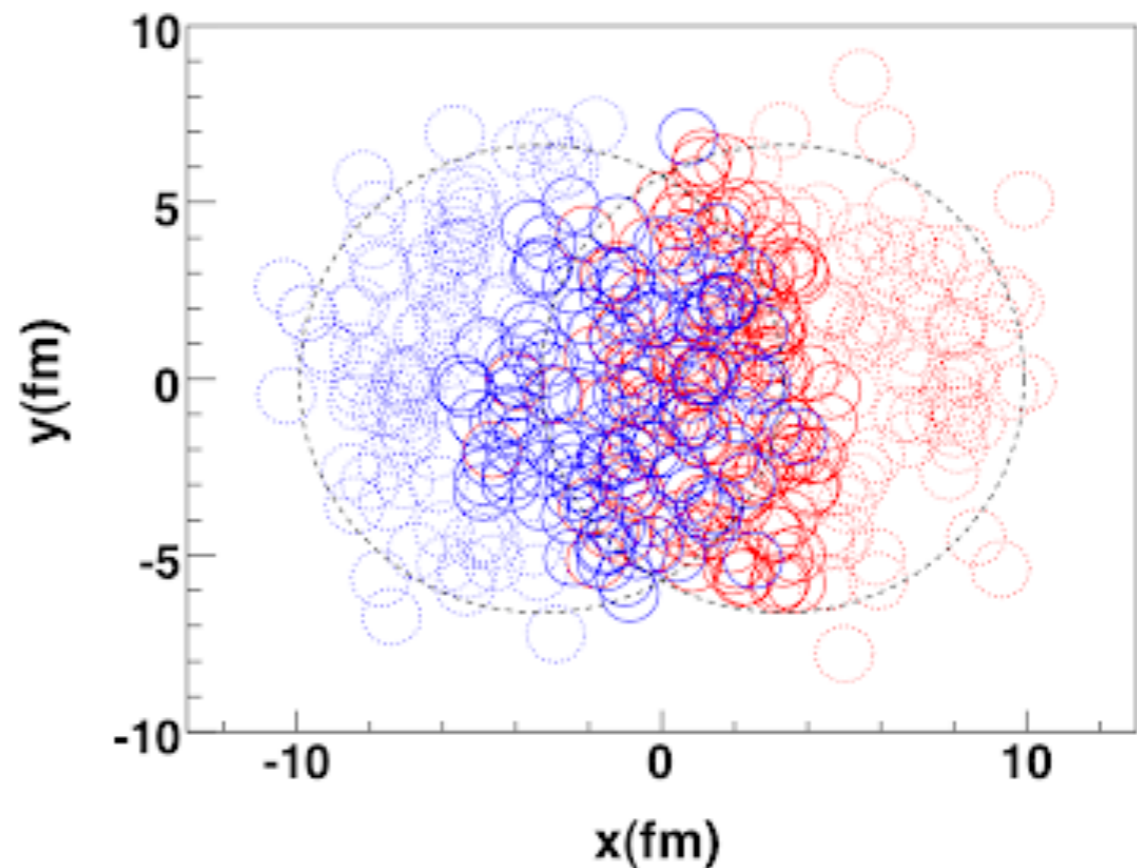
Low energy



High energy

$$\rho(r, \theta, \phi) = \frac{\rho_0}{1 + e^{(r-R(\theta, \phi))/a_0}}$$

$$R(\theta, \phi) = R_0 \left(1 + \beta_2 [\cos \gamma Y_{2,0} + \sin \gamma Y_{2,2}] + \beta_3 \sum_{m=-3}^3 \alpha_{3,m} Y_{3,m} + \beta_4 \sum_{m=-4}^4 \alpha_{4,m} Y_{4,m} \right)$$



- ❖ Even with the fixed parameters (nuclear structure), the nucleon distributions are not fixed (not identical but vary from one event to the other)

Initial geometry correlations

PHYSICAL REVIEW C **89**, 064904 (2014)

309 citations

Generic framework for anisotropic flow analyses with multiparticle azimuthal correlations

Ante Bilandzic,¹ Christian Holm Christensen,¹ Kristjan Gulbrandsen,¹ Alexander Hansen,¹ and You Zhou^{2,3}

¹Niels Bohr Institute, Blegdamsvej 17, 2100 Copenhagen, Denmark

²Nikhef, Science Park 105, 1098 XG Amsterdam, The Netherlands

³Utrecht University, P.O. Box 80000, 3508 TA Utrecht, The Netherlands

Symmetric cumulants:

$$SC(m, n) = \langle v_m^2 v_n^2 \rangle - \langle v_m^2 \rangle \langle v_n^2 \rangle$$

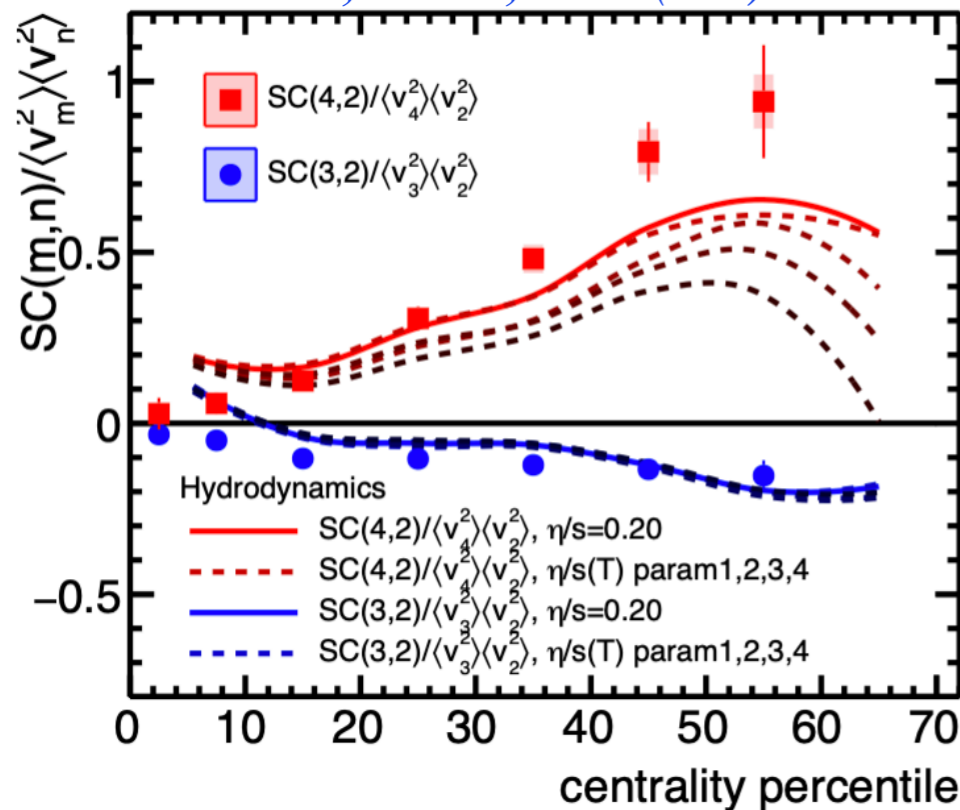
$$\begin{aligned} v_2 &\propto \varepsilon_2 \\ v_3 &\propto \varepsilon_3 \end{aligned}$$



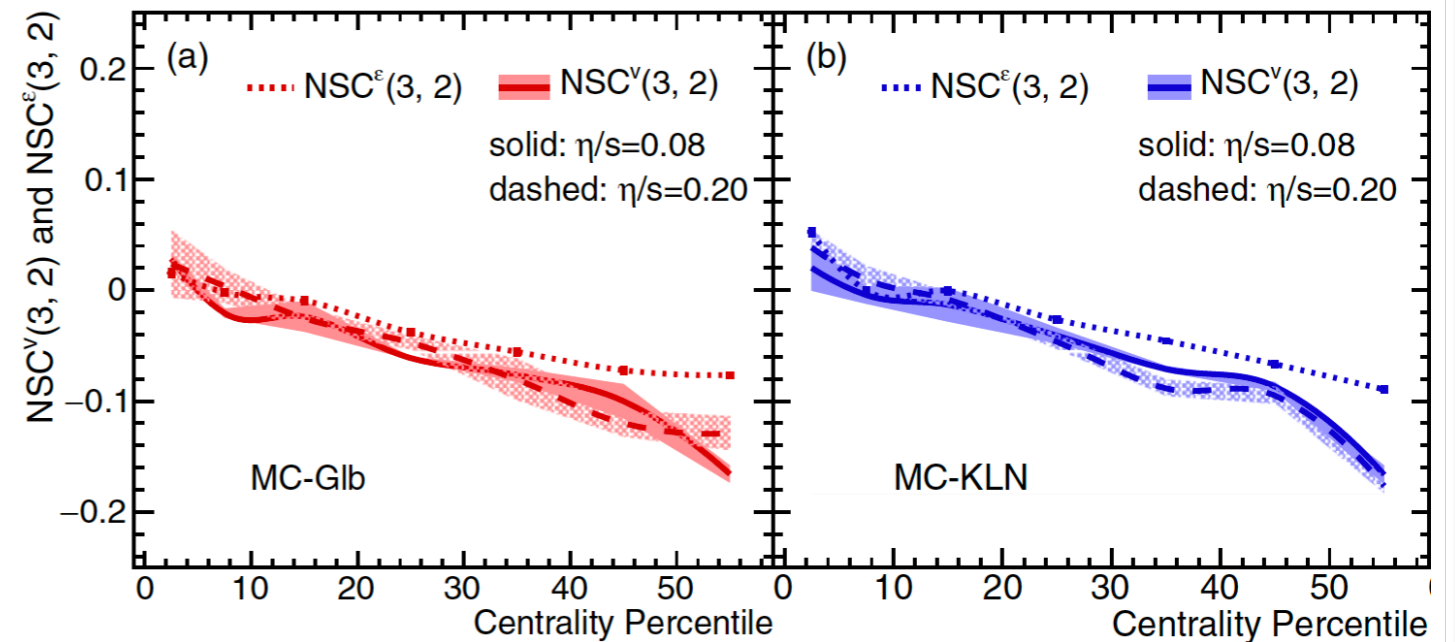
$$\frac{\langle v_2^2 v_3^2 \rangle - \langle v_2^2 \rangle \langle v_3^2 \rangle}{\langle v_2^2 \rangle \langle v_3^2 \rangle} = \frac{\langle \varepsilon_2^2 \varepsilon_3^2 \rangle - \langle \varepsilon_2^2 \rangle \langle \varepsilon_3^2 \rangle}{\langle \varepsilon_2^2 \rangle \langle \varepsilon_3^2 \rangle}$$

Or: $NSC^v(3, 2) = NSC^\varepsilon(3, 2)$

ALICE, PRL117, 182301 (2016)



X. Zhu etc, PRC95, 044902 (2017)



ALICE, PLB818 (2021) 136354

M. Li, YZ etc, PRC104, 024903 (2021)



Probe Nuclear structure with NSC(3,2)

Normalised Symmetric cumulants:

$$v_2 \propto \varepsilon_2$$

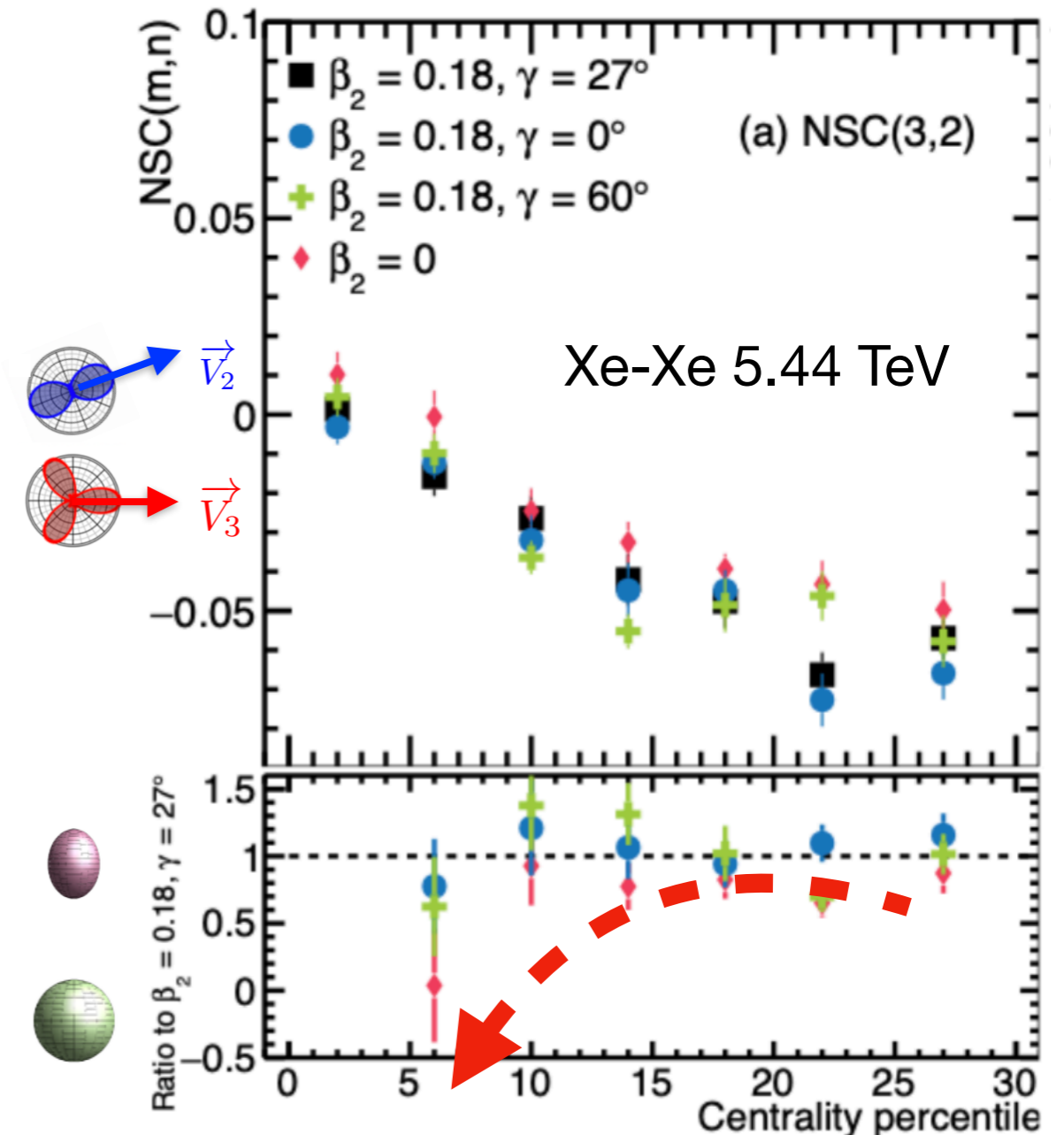
$$v_3 \propto \varepsilon_3$$



$$\frac{\langle v_2^2 v_3^2 \rangle - \langle v_2^2 \rangle \langle v_3^2 \rangle}{\langle v_2^2 \rangle \langle v_3^2 \rangle} = \frac{\langle \varepsilon_2^2 \varepsilon_3^2 \rangle - \langle \varepsilon_2^2 \rangle \langle \varepsilon_3^2 \rangle}{\langle \varepsilon_2^2 \rangle \langle \varepsilon_3^2 \rangle}$$

Or: $NSC^v(3, 2) = NSC^\varepsilon(3, 2)$

Z. Lu, M. Zhao, J. Jia, YZ, *Eur. Phys. J. A* (2023) 59, 279



❖ Different results due to nuclear deformation observed in NSC(3,2)

❖ New measurements should allow the constrain the β_2 but not γ



Skewness of mean transverse momentum fluctuations in heavy-ion collisions

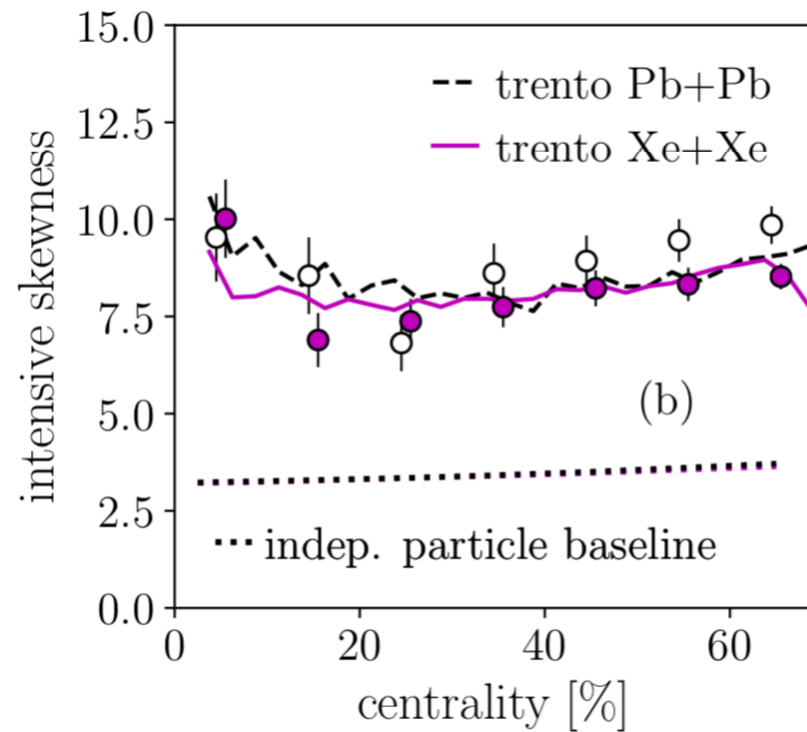
 Giuliano Giacalone^{1,2}, Fernando G. Gardim,³ Jacquelyn Noronha-Hostler,⁴ and Jean-Yves Ollitrault¹
¹Université Paris Saclay, CNRS, CEA, Institut de physique théorique, 91191 Gif-sur-Yvette, France

²Institut für Theoretische Physik, Universität Heidelberg, Philosophenweg 16, 69120 Heidelberg, Germany

³Instituto de Ciência e Tecnologia, Universidade Federal de Alfenas, 37715-400 Poços de Caldas, Minas Gerais, Brazil

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$$\Gamma_{p_t} \equiv \frac{\langle \Delta p_i \Delta p_j \Delta p_k \rangle \langle \langle p_t \rangle \rangle}{\langle \Delta p_i \Delta p_j \rangle^2}$$



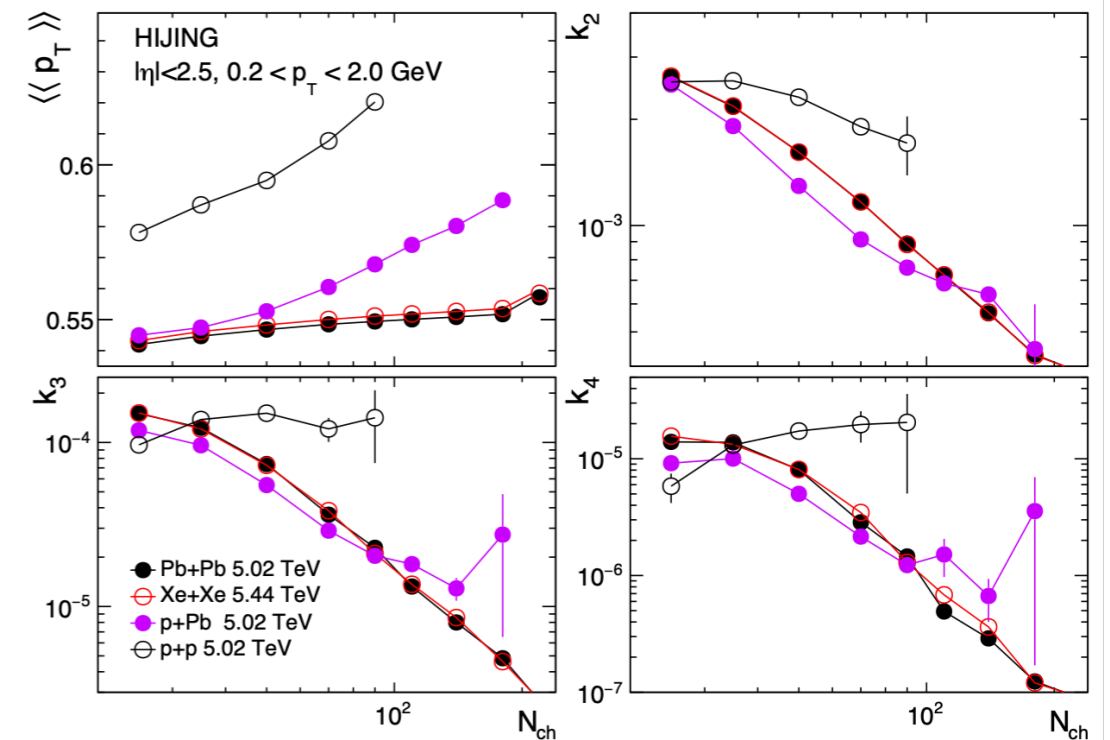
Higher-order transverse momentum fluctuations in heavy-ion collisions

 Somadutta Bhatta¹, Chunjian Zhang¹ and Jianguong Jia^{1,2,*}
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²Physics Department, Brookhaven National Laboratory, Upton, New York 11976, USA

$$k_2 = \frac{\langle c_2 \rangle}{\langle \langle p_T \rangle \rangle^2}, \quad k_3 = \frac{\langle c_3 \rangle}{\langle \langle p_T \rangle \rangle^3},$$

$$k_4 = \frac{\langle c_4 \rangle - 3\langle c_2 \rangle^2}{\langle \langle p_T \rangle \rangle^4}, \quad k_{2,2\text{sub}} = \frac{\langle c_{2,2\text{sub}} \rangle}{\langle \langle p_T \rangle \rangle_a \langle \langle p_T \rangle \rangle_c},$$



$$d_{\perp} = \sqrt{N_{\text{part}} / \langle r_{\perp}^2 \rangle}$$

$$\frac{\delta d_{\perp}}{d_{\perp}} = \sqrt{\frac{5}{16\pi}} \beta_2 \left(\cos(\gamma) D_{0,0}^2(\Omega) + \frac{\sin(\gamma)}{\sqrt{2}} [D_{0,2}^2(\Omega) + D_{0,-2}^2(\Omega)] \right)$$

Final state cumulant	Initial state cumulant	Liquid-drop model
κ_2	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle$	$\frac{1}{32\pi} \langle \beta_2^2 \rangle$
κ_3	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle$	$\frac{\sqrt{5}}{896\pi^{3/2}} \langle \cos(3\gamma) \beta_2^3 \rangle$
κ_4	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^4 \right\rangle - 3 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle^2$	$-\frac{3}{14336\pi^2} (7\langle \beta_2^2 \rangle - 5\langle \beta_2^4 \rangle)$
κ_5	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^5 \right\rangle - 10 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle$	$-\frac{5\sqrt{5}}{315392\pi^{5/2}} (11\langle \cos(3\gamma) \beta_2^3 \rangle \langle \beta_2^2 \rangle - 5\langle \beta_2^5 \rangle)$
κ_6	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^6 \right\rangle - 15 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^4 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle + 30 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle^3 - 10 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle^2$	$\frac{5}{918412504\pi^3} (42042\langle \beta_2^2 \rangle^3 - 5720\langle \cos(3\gamma) \beta_2^3 \rangle^2 - 45045\langle \beta_2^2 \rangle \langle \beta_2^4 \rangle + 8575\langle \beta_2^6 \rangle + 700\langle \cos(6\gamma) \beta_2^6 \rangle)$
κ_7	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^7 \right\rangle - 21 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^5 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle + 210 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle^2 - 35 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^4 \right\rangle$	$-\frac{15\sqrt{5}}{524812288} (2002\langle \beta_2^2 \rangle^2 \langle \cos(3\gamma) \beta_2^3 \rangle + 715\langle \cos(3\gamma) \beta_2^3 \rangle \langle \beta_2^4 \rangle + 910\langle \cos(3\gamma) \beta_2^5 \rangle \langle \beta_2^2 \rangle - 175 \cos(3\gamma) \beta_2^7)$
κ_8	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^8 \right\rangle - 28 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^6 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle + 420 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^4 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle^2 - 35 \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^4 \right\rangle^2 - 630 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle^4 + 560 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle^2 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle - 56 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^5 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}} \right)^3 \right\rangle$	$\frac{5}{142748942336\pi^4} (2144142\langle \beta_2^2 \rangle^4 - 3063060\langle \beta_2^2 \rangle^2 \langle \beta_2^4 \rangle - 340\langle \beta_2^2 \rangle (2288\langle \cos(3\gamma) \beta_2^3 \rangle^2 - 35(49\langle \beta_2^6 \rangle + 4\langle \cos(6\gamma) \beta_2^6 \rangle)) + 25(21879\langle \beta_2^4 \rangle^2 + 14144\langle \cos(3\gamma) \beta_2^3 \rangle \langle \cos(3\gamma) \beta_2^5 \rangle - 35(79\langle \beta_2^8 \rangle + 16\langle \cos(6\gamma) \beta_2^8 \rangle))$



Multi-particle p_T correlations

PHYSICAL REVIEW C **103**, 024910 (2021)

Skewness of mean transverse momentum fluctuations in heavy-ion collisions

Giuliano Giacalone^{1,2}, Fernando G. Gardim,³ Jacquelyn Noronha-Hostler,⁴ and Jean-Yves Ollitrault¹

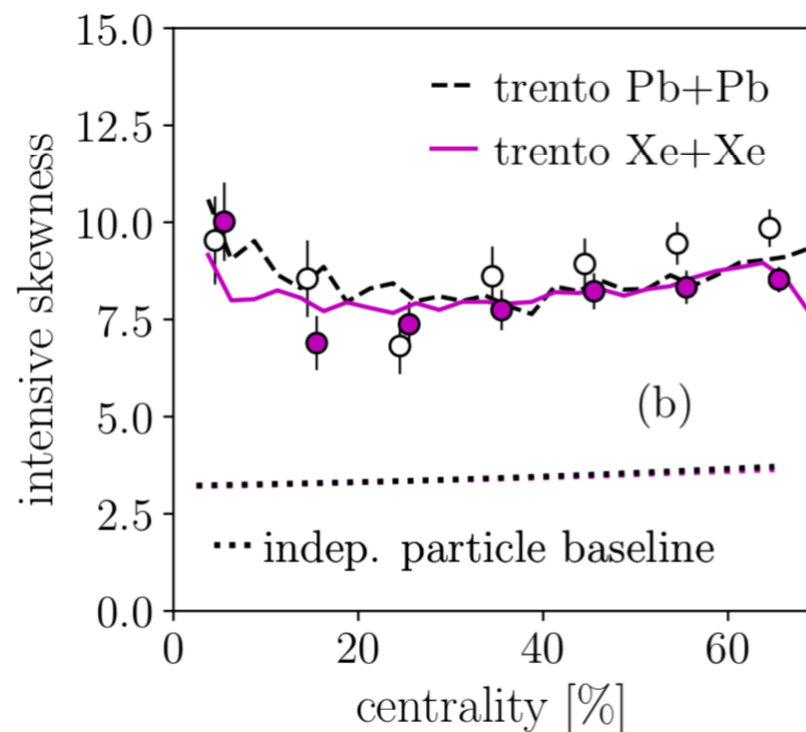
¹Université Paris Saclay, CNRS, CEA, Institut de physique théorique, 91191 Gif-sur-Yvette, France

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PHYSICAL REVIEW C **105**, 024904 (2022)

Higher-order transverse momentum fluctuations in heavy-ion collisions

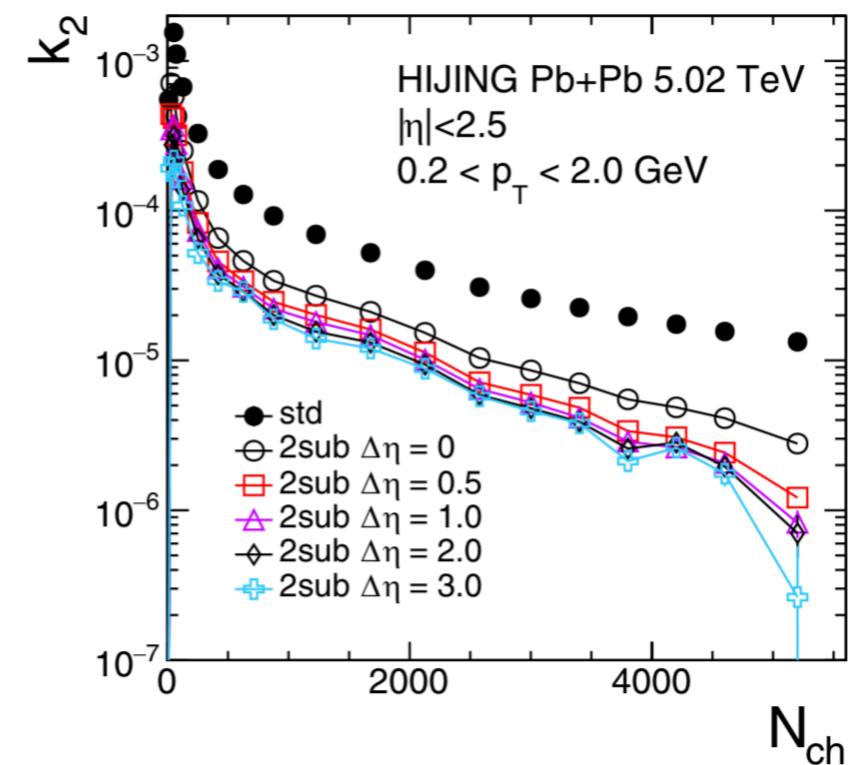
Somadutta Bhatta¹, Chunjian Zhang¹ and Jiangyong Jia^{1,2,*}

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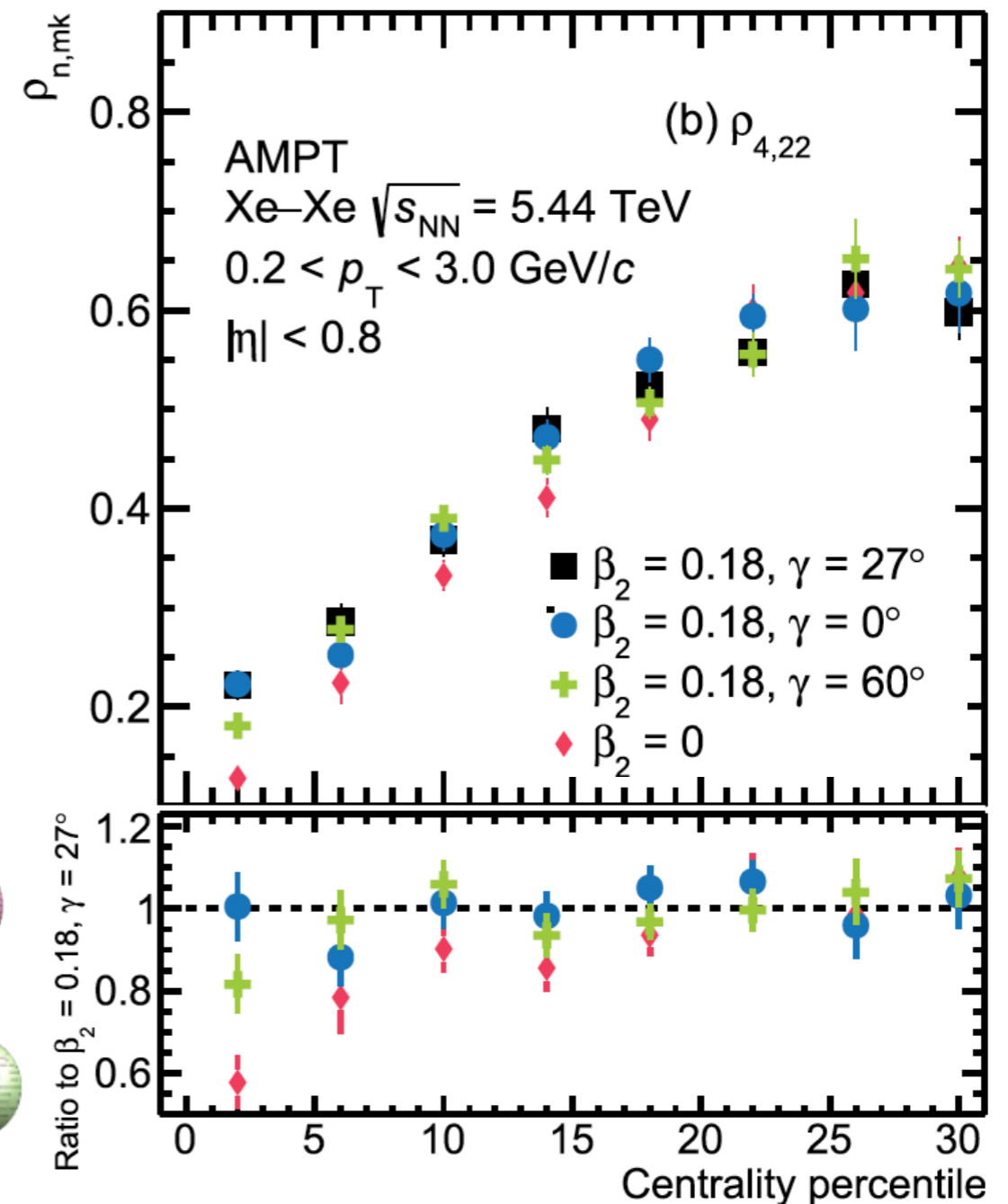
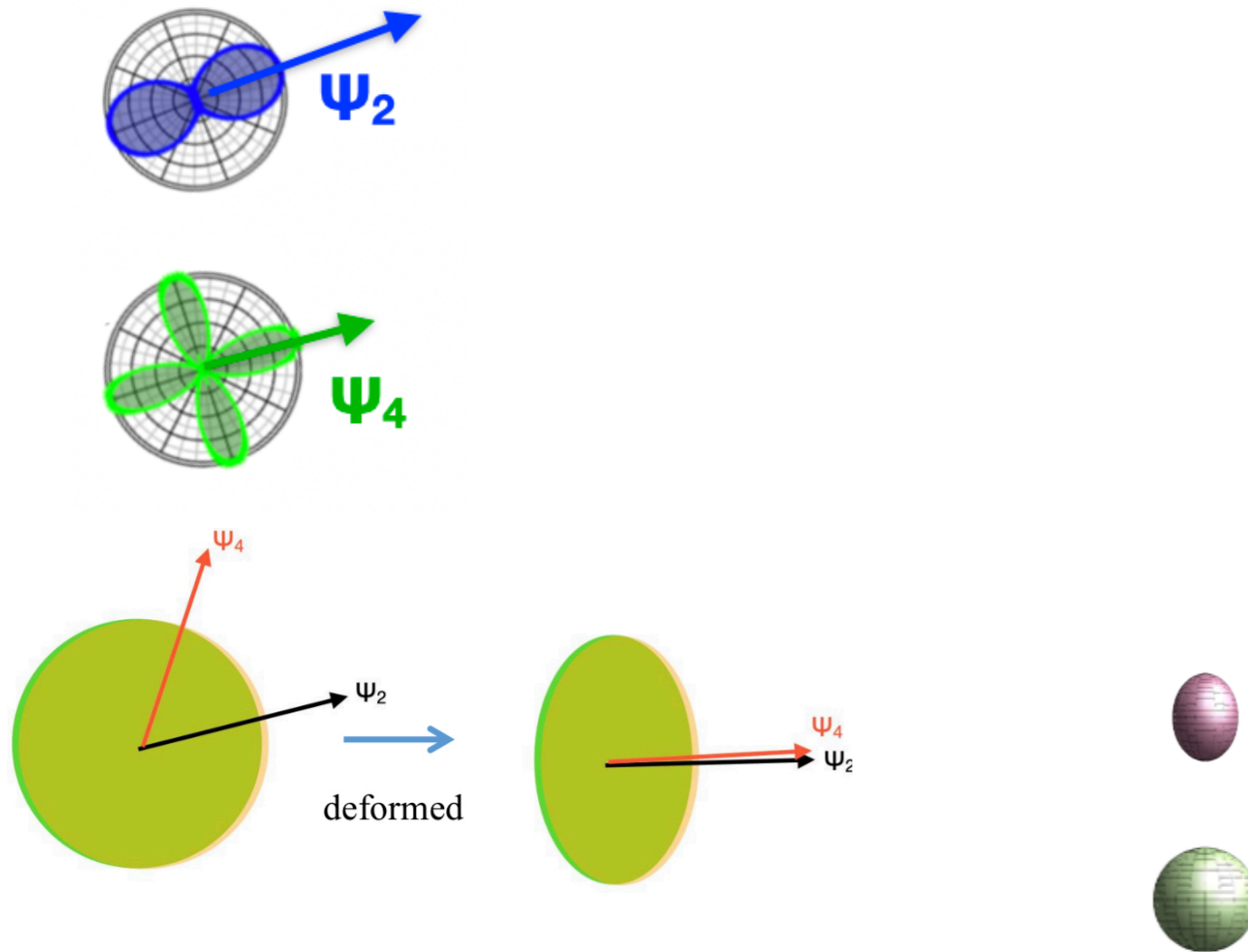
- $[P_T]$ and its event-by-event fluctuations measured in heavy-ion collisions at the LHC -> probe initial **size** and **size fluctuations**



Enhanced ψ_n correlations in models

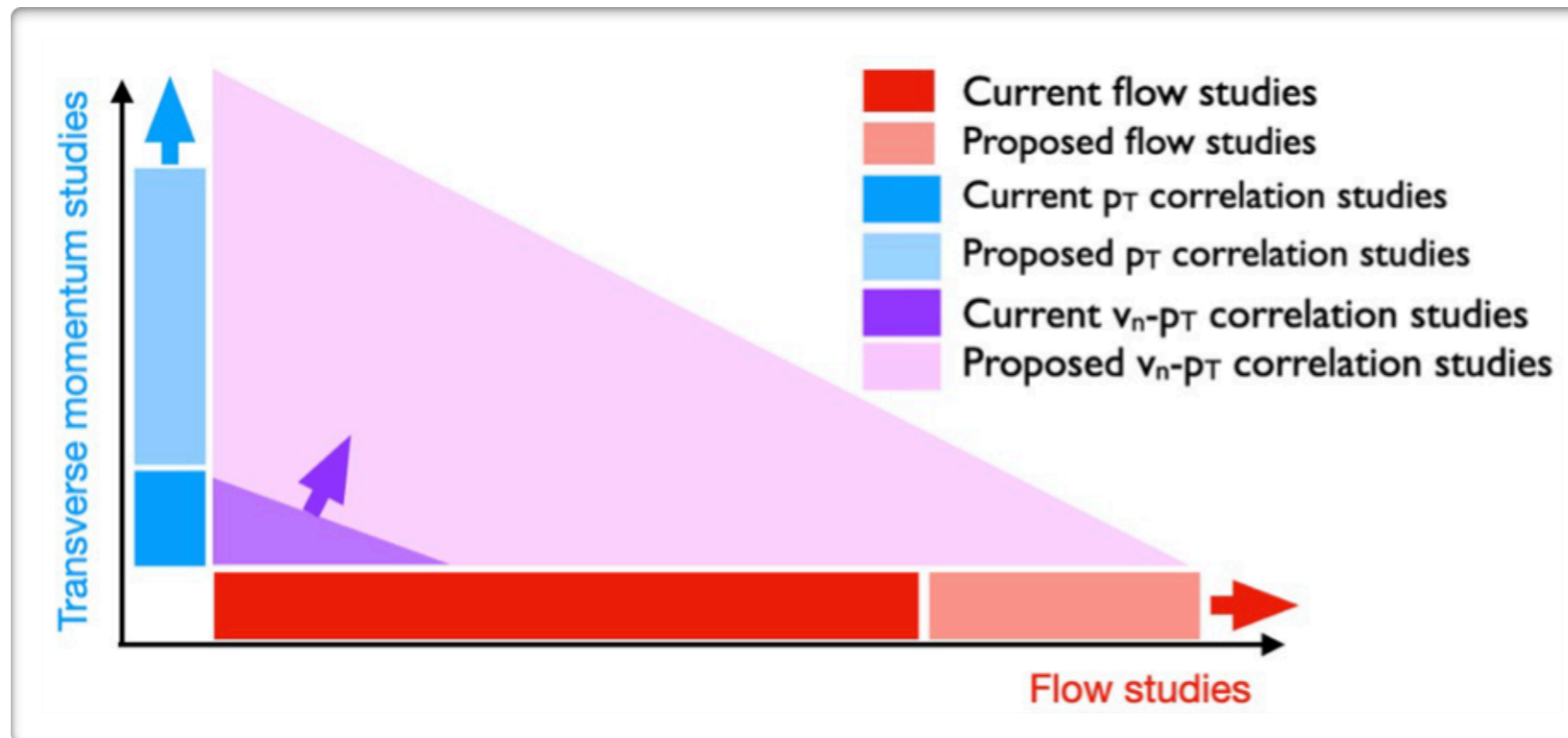
Z. Lu, M. Zhao, J. Jia, YZ, *Eur. Phys. J. A* (2023) 59, 279

- ❖ $\rho_{4,22}$ probes correlations between Ψ_2 and Ψ_4
 $\sim \langle \cos 4(\Psi_2 - \Psi_4) \rangle$



- ❖ A stronger correlation is well explained by the transport model using deformed ^{129}Xe nuclei using transport model

$[p_T]$ - v_n correlations



❖ **Shape** of the fireball: **Anisotropic flow**

❖ **Size** of the fireball: radial flow $[p_T]$

❖ Final state: correlation between v_n and p_T

$$\rho(v_n^2, [p_T]) = \frac{\text{cov}(v_n^2, [p_T])}{\sqrt{\text{var}(v_n^2)}\sqrt{\text{var}([p_T])}}$$

P. Bozek etc, PRC96 (2017) 014904

❖ Assuming $v_n \propto \epsilon_n$, $[p_T] \propto E_0$

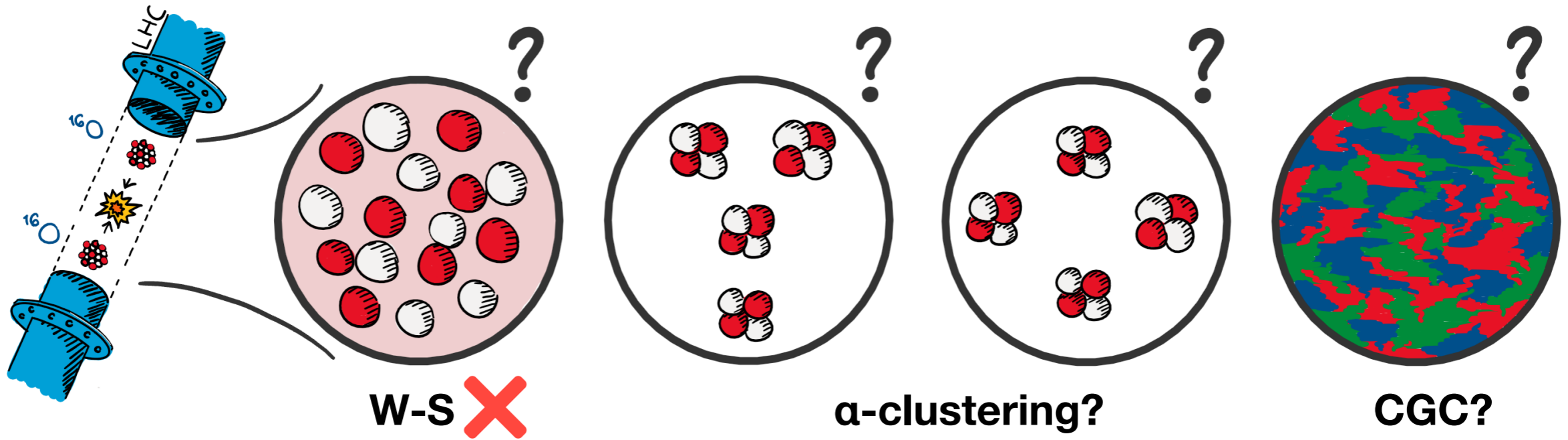
$$\rho(v_n^2, [p_T]) = \rho(\epsilon_n^2, [E_0])$$

final-state model
calculation

Initial-state model
estimation



❖ One can compare $\rho(v_n^2, [p_T])$ measurements to $\rho(\epsilon_n^2, [E_0])$ calculations, to constrain the initial state model

O-O collisions at RHIC and the LHC



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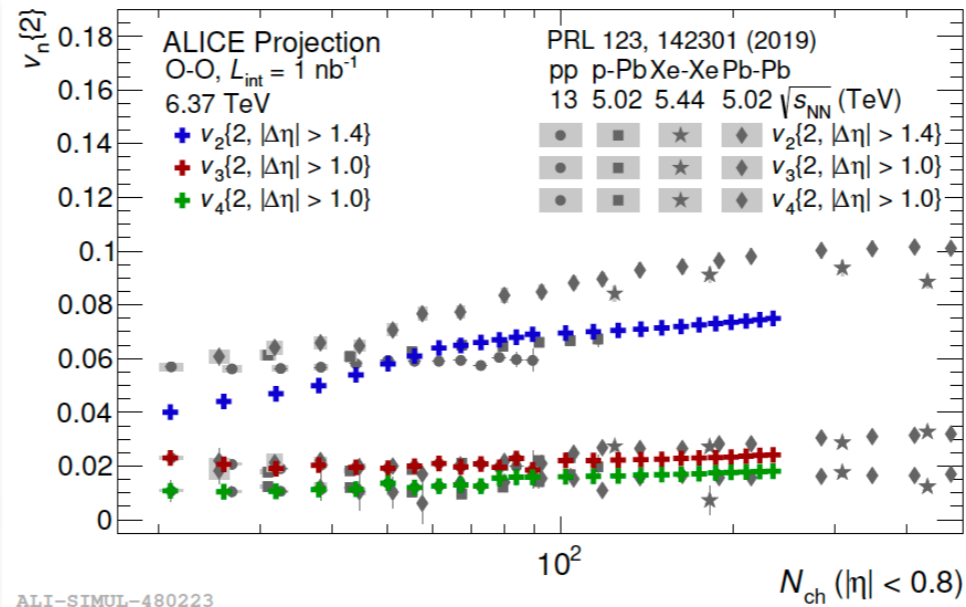



ALICE Collaboration

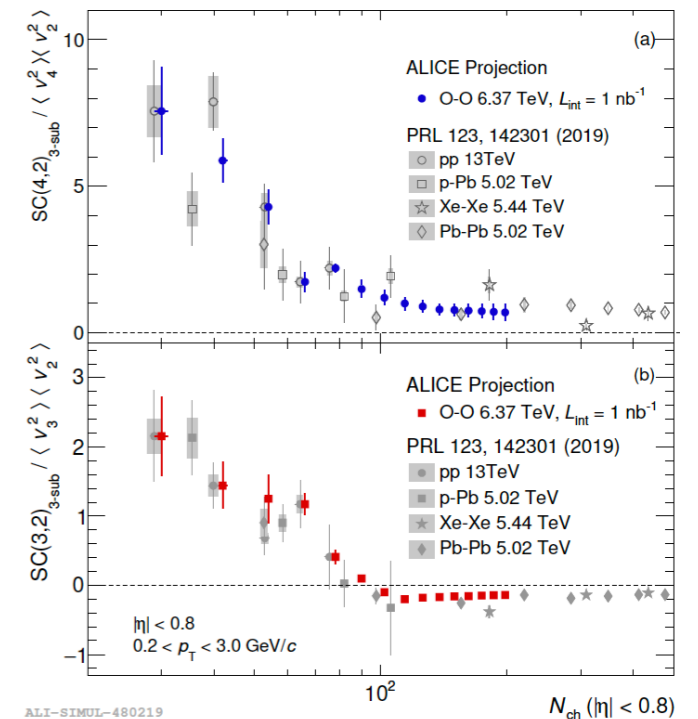
ALICE physics projections for a short oxygen-beam run at the LHC

Abstract

This document collects performance projections for a selection of measurements that can be carried out with a short O-O run during the LHC Run 3. The baseline centre-of-mass energy per nucleon-nucleon collision is $\sqrt{s_{NN}} = 6.37$ TeV and measurement uncertainties are given for the integrated luminosity $L_{int} = 1 \text{ nb}^{-1}$. Some projections for p-O collisions are also included. These studies were presented at the CERN workshop on Opportunities of O-O and p-O collisions at the LHC [1,2].



ALI-SIMUL-480223



ALI-SIMUL-480219

