



# TMD Phenomenology and Opportunities at EicC

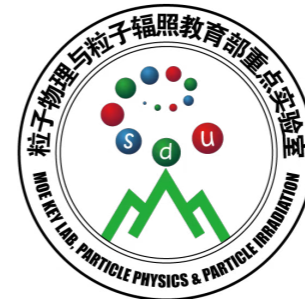
The 1<sup>st</sup> Spicy Gluons Workshop for Young Scientists  
May 15<sup>th</sup>-19<sup>th</sup>, 2024 @ Hefei, Anhui

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Southern Center for Nuclear-Science Theory, IMP, CAS*

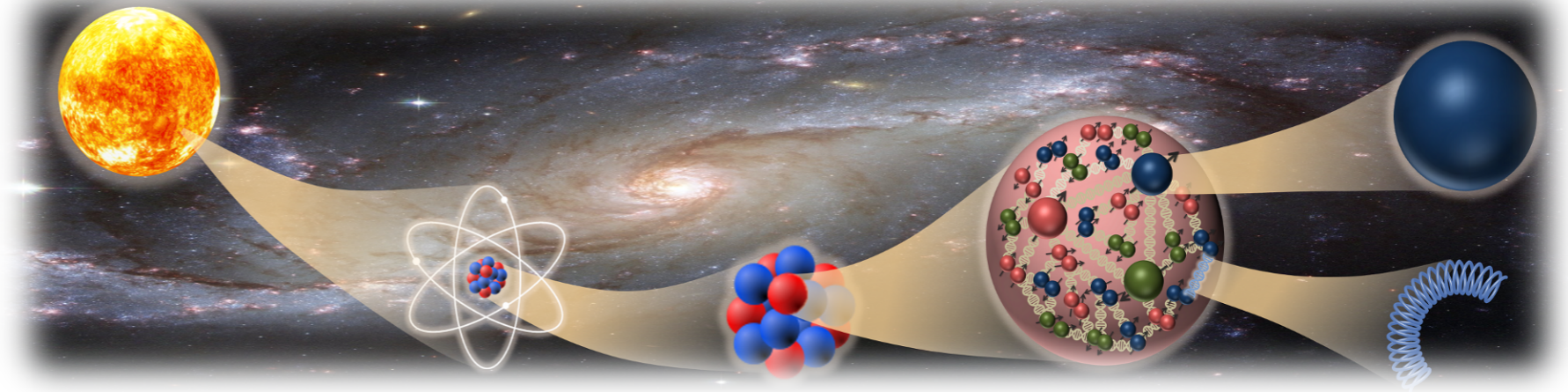
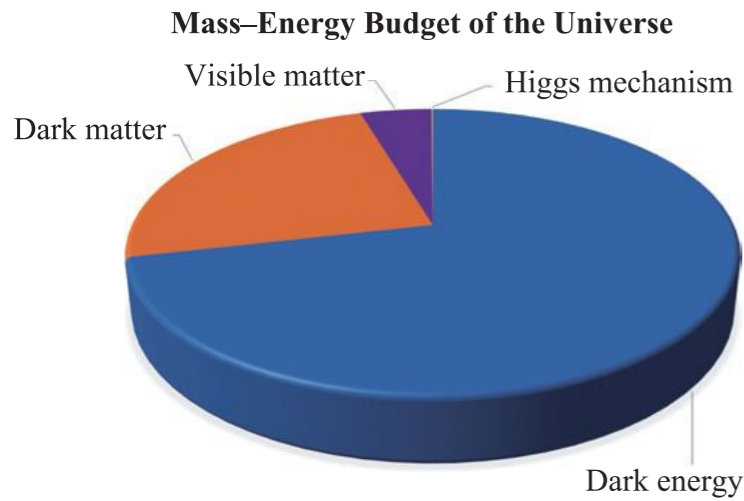


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SHANDONG UNIVERSITY





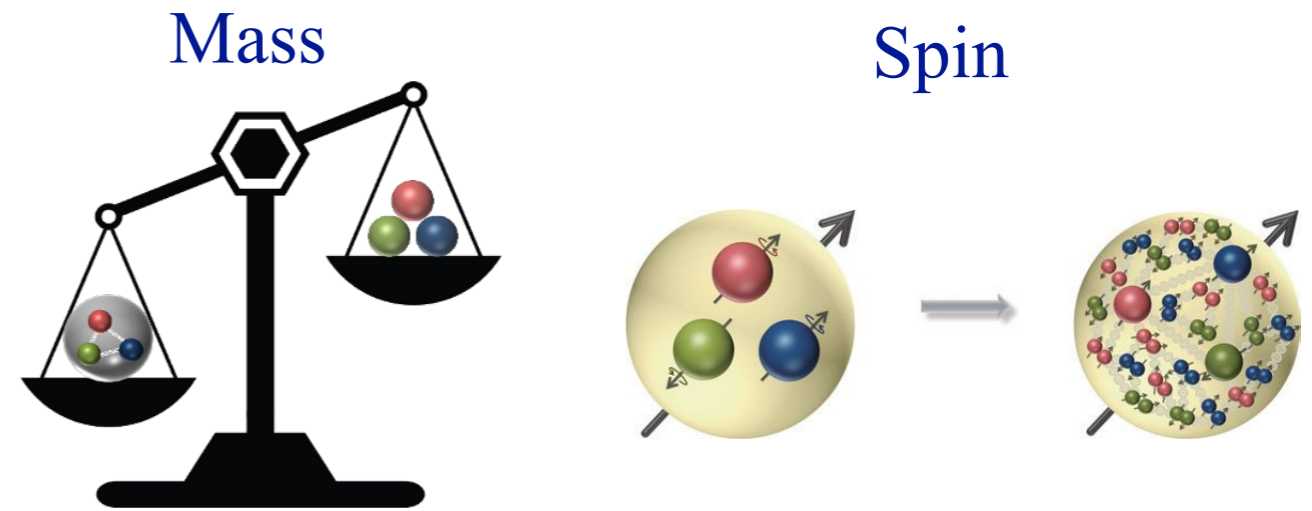
# How much do we understand our world?



**Three generations of matter**

	I	II	III	Force carriers	
Quarks	<b>u</b> Up quark Mass $\approx 2.2$ MeV Charge = $2/3$ Spin = $1/2$	<b>c</b> Charm quark Mass $\approx 1.28$ GeV Charge = $2/3$ Spin = $1/2$	<b>t</b> Top quark Mass $\approx 173.1$ GeV Charge = $2/3$ Spin = $1/2$	<b>g</b> Gluon Mass = 0 Charge = 0 Spin = 1	<b>H</b> Higgs Mass $\approx 124.97$ GeV Charge = 0 Spin = 0
	<b>d</b> Down quark Mass $\approx 4.7$ MeV Charge = $-1/3$ Spin = $1/2$	<b>s</b> Strange quark Mass $\approx 96$ MeV Charge = $-1/3$ Spin = $1/2$	<b>b</b> Bottom quark Mass $\approx 4.18$ GeV Charge = $-1/3$ Spin = $1/2$	<b><math>\gamma</math></b> Photon Mass = 0 Charge = 0 Spin = 1	Scalar bosons
	<b>e</b> Electron Mass $\approx 0.511$ MeV Charge = $-1$ Spin = $1/2$	<b><math>\mu</math></b> Muon Mass $\approx 105.66$ MeV Charge = $-1$ Spin = $1/2$	<b><math>\tau</math></b> Tau Mass $\approx 1.7768$ GeV Charge = $-1$ Spin = $1/2$	<b>Z</b> Z boson Mass $\approx 91.19$ GeV Charge = 0 Spin = 1	
<b><math>\nu_e</math></b> Electron neutrino Mass $< 1$ eV Charge = 0 Spin = $1/2$	<b><math>\nu_\mu</math></b> Muon neutrino Mass $< 0.17$ MeV Charge = 0 Spin = $1/2$	<b><math>\nu_\tau</math></b> Tau neutrino Mass $< 18.2$ MeV Charge = 0 Spin = $1/2$	<b>W</b> W boson Mass $\approx 80.39$ GeV Charge = $\pm 1$ Spin = 1		

Gauge bosons  
Vector bosons



*How do quarks and gluons make up a nucleon?  
How can nucleon properties be explained at quarks and gluons degrees of freedom?*

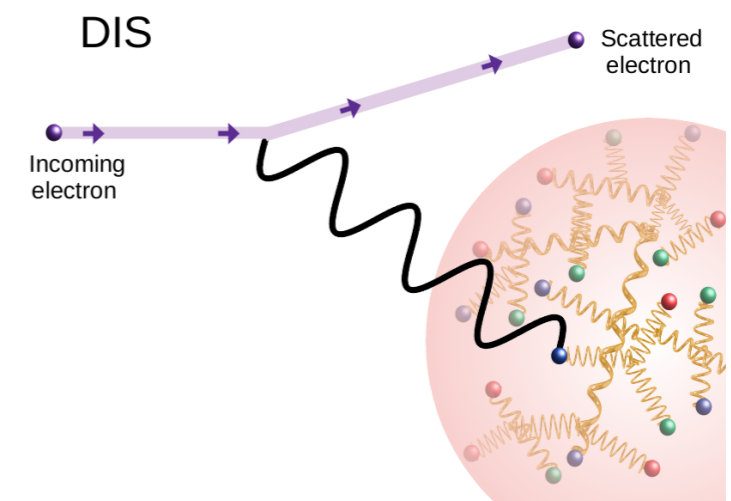
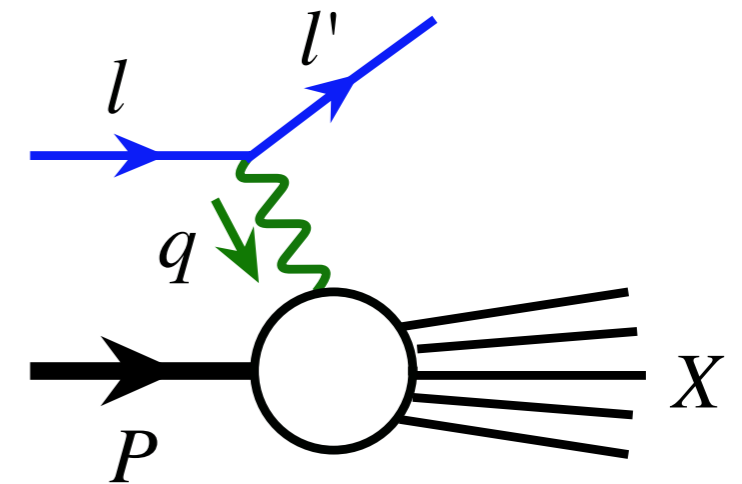


# Lepton-Hadron Deep Inelastic Scattering

Inclusive DIS at a large momentum transfer  $Q \gg \Lambda_{\text{QCD}}$

- dominated by the scattering of the lepton off an active quark/parton
- not sensitive to the dynamics at a hadronic scale  $\sim 1/\text{fm}$
- collinear factorization:  $\sigma \propto H(Q) \otimes \phi_{a/P}(x, \mu^2)$
- overall corrections suppressed by  $1/Q^n$
- indirectly “see” quarks, gluons and their dynamics
- predictive power relies on
  - precision of the probe
  - universality of  $\phi_{a/P}(x, \mu^2)$

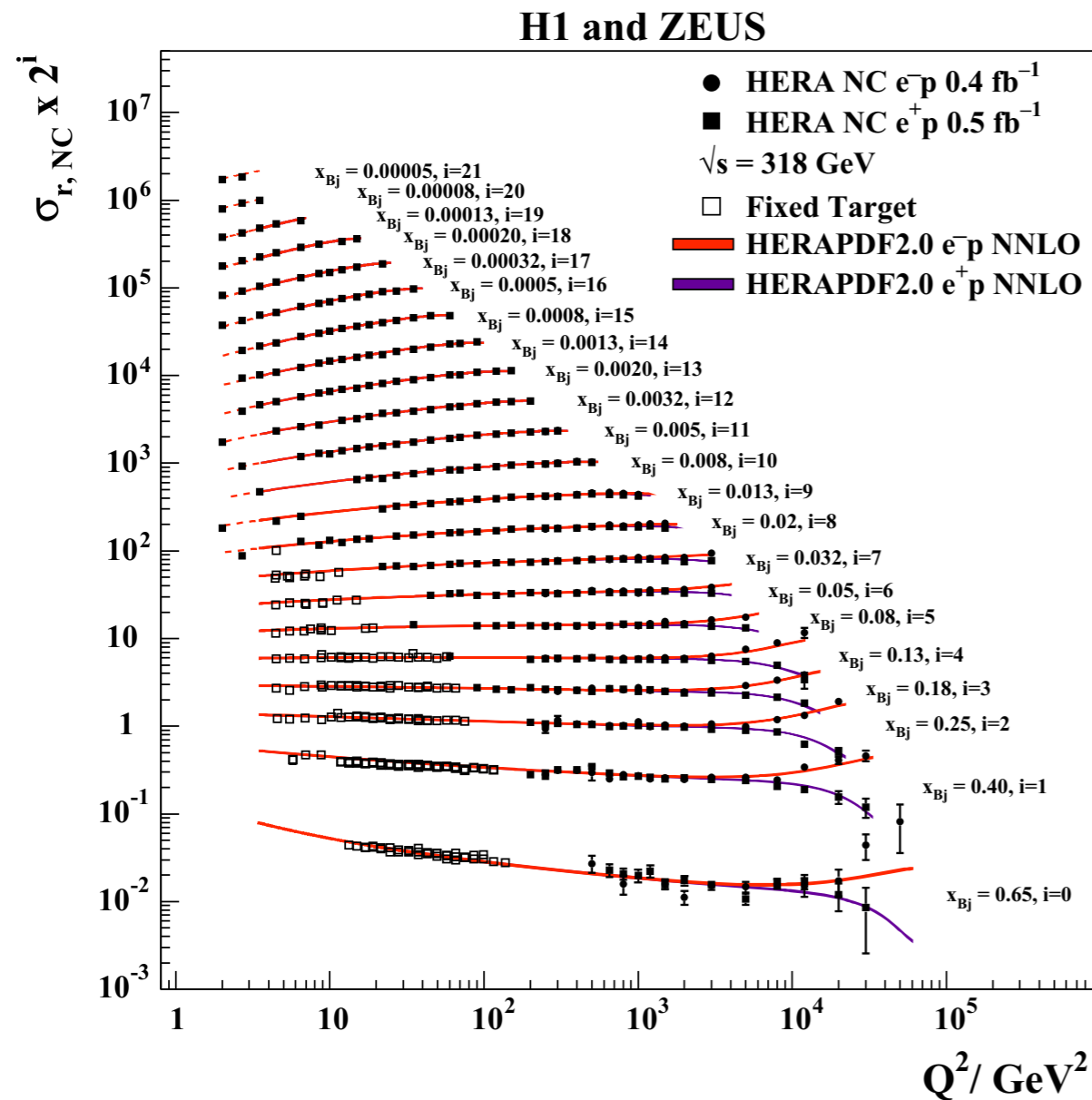
Modern “Rutherford” experiment.



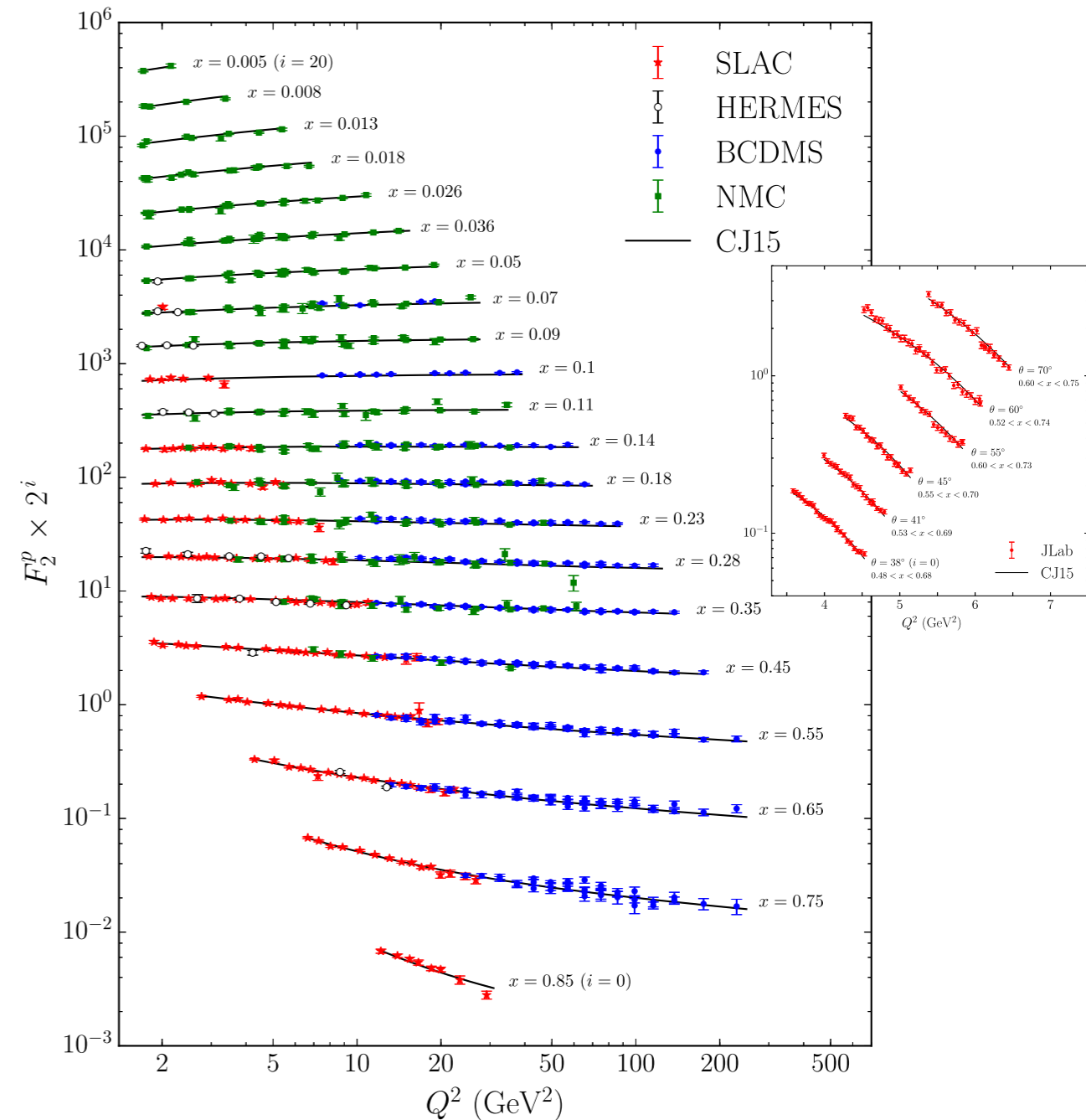
[Figure from DESY-21-099]



# Lepton-Hadron Deep Inelastic Scattering



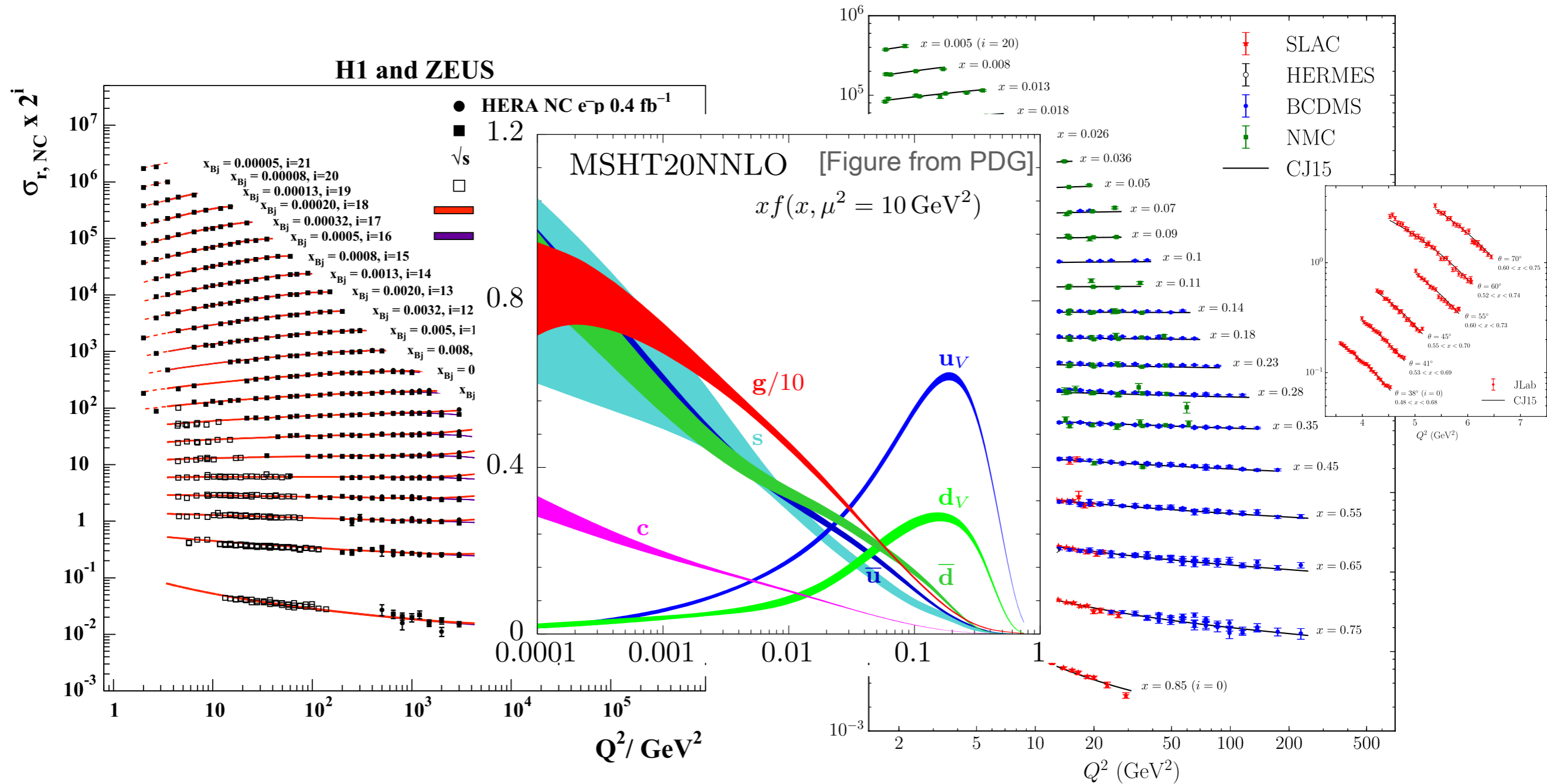
H. Abramowicz *et al.*, EPJC 78, 580 (2015).



A. Accardi *et al.*, PRD 93, 114017 (2016).



# Lepton-Hadron Deep Inelastic Scattering



H. Abramowicz *et al.*, EPJC 78, 580 (2015).

A. Accardi *et al.*, PRD 93, 114017 (2016).

*A successful story of QCD, factorization and evolution!*



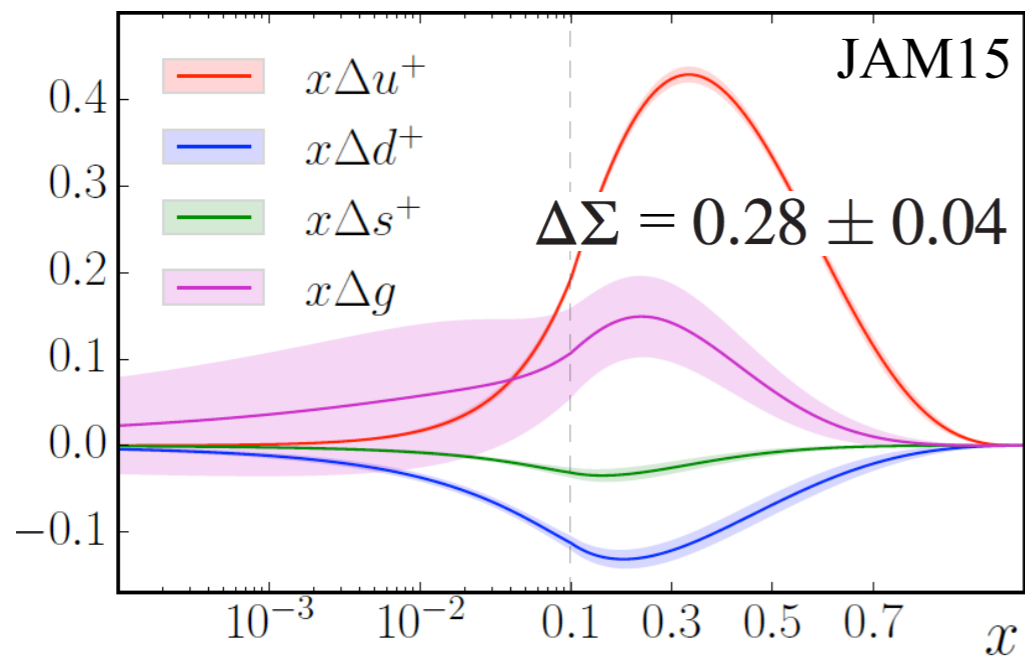
# Nucleon Spin Structure

## Proton spin puzzle

$$\Delta\Sigma = \Delta u + \Delta d + \Delta s \sim 0.3$$

## Spin decomposition

$$J = \frac{1}{2}\Delta\Sigma + \Delta G + L_q + L_g$$



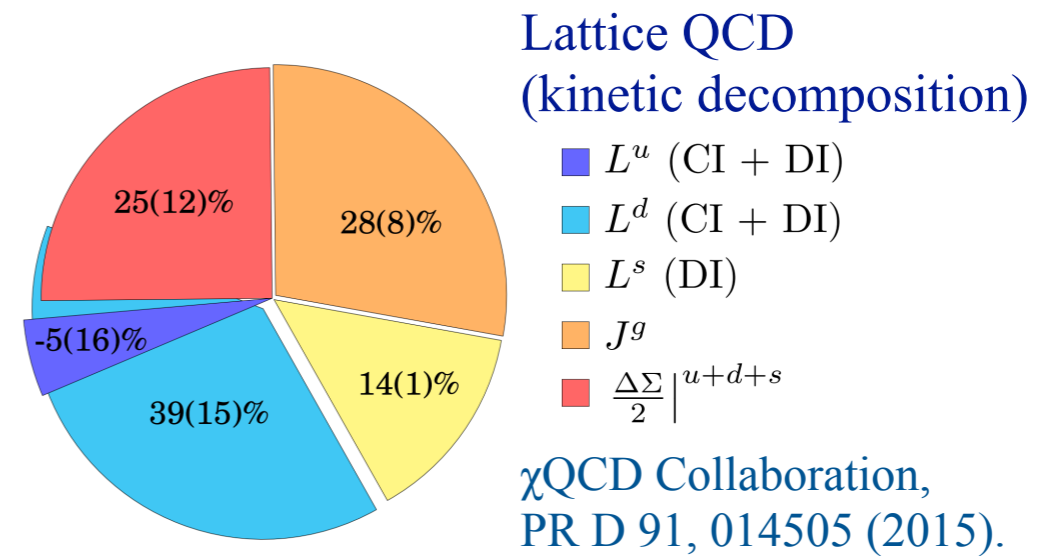
JAM Collaboration, PR D 93, 074005 (2016).

JAM17:  $\Delta\Sigma = 0.36 \pm 0.09$

JAM Collaboration, PRL 119, 132001 (2017).

Quark spin only contributes a small fraction to the nucleon spin.

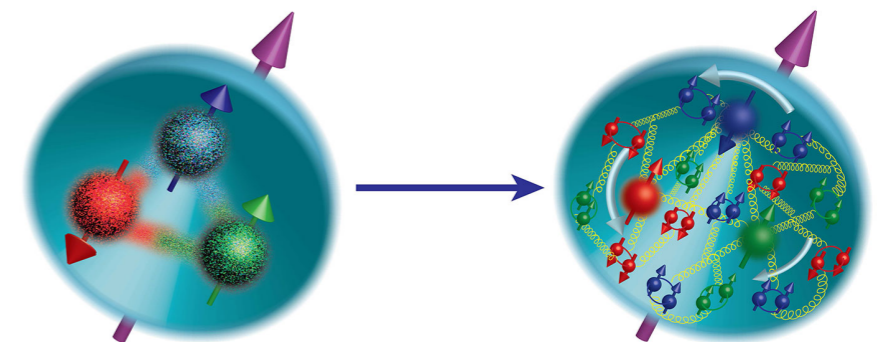
J. Ashman *et al.*, PLB 206, 364 (1988); NP B328, 1 (1989).



Gluon spin from LQCD:  $S_g = 0.251(47)(16)$

50% of total proton spin

Y.-B. Yang *et al.* ( $\chi$ QCD Collaboration), PRL 118, 102001 (2017).

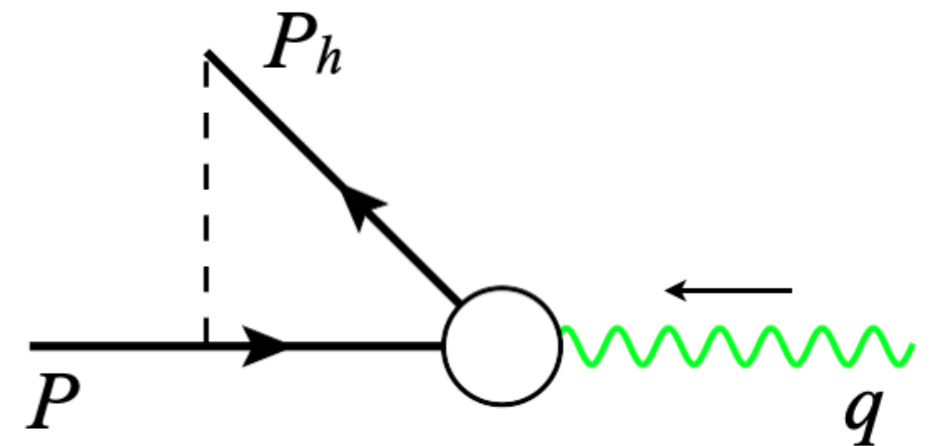
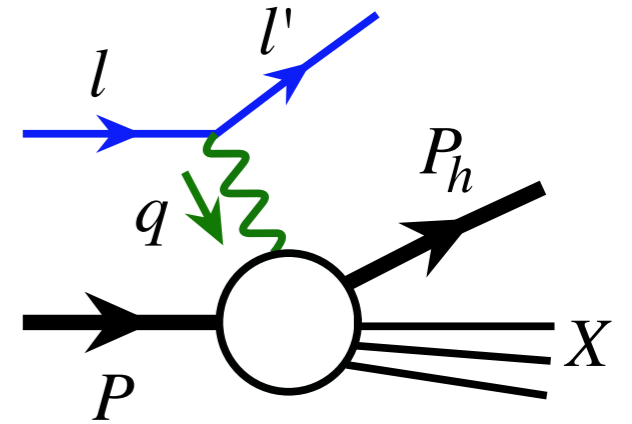




# Semi-inclusive Deep Inelastic Scattering

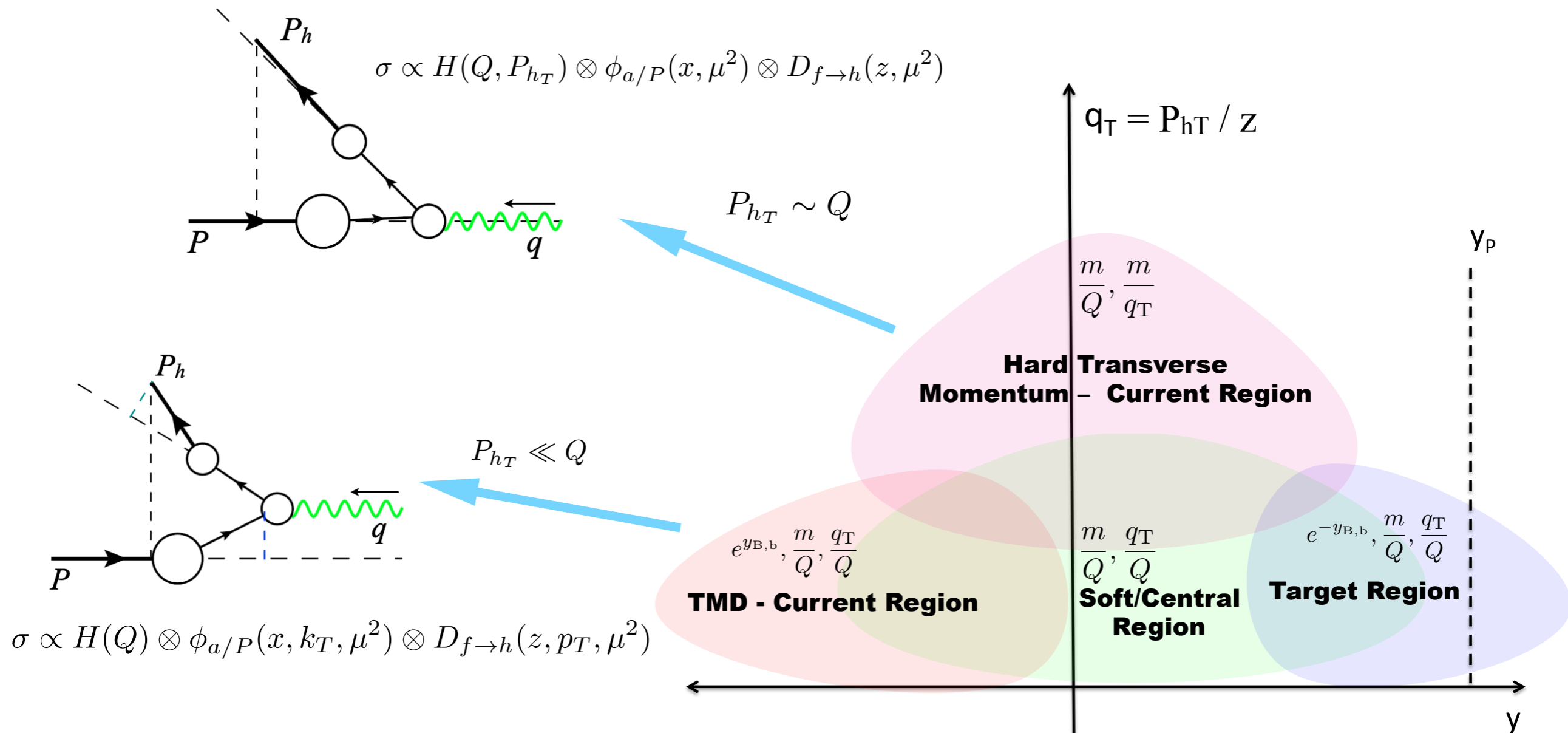
Semi-inclusive DIS: a final state hadron ( $P_h$ ) is identified

- enable us to explore the emergence of color neutral hadrons from colored quarks/gluons
- flavor dependence by selecting different types of observed hadrons: pions, kaons, ...
- a large momentum transfer  $Q$  provides a short-distance probe
- an additional and adjustable momentum scale  $P_{hT}$
- multidimensional imaging of the nucleon



# SIDIS Kinematic Regions

Sketch of kinematic regions of the produced hadron



$P_{hT}$  is defined in the photon-hadron frame

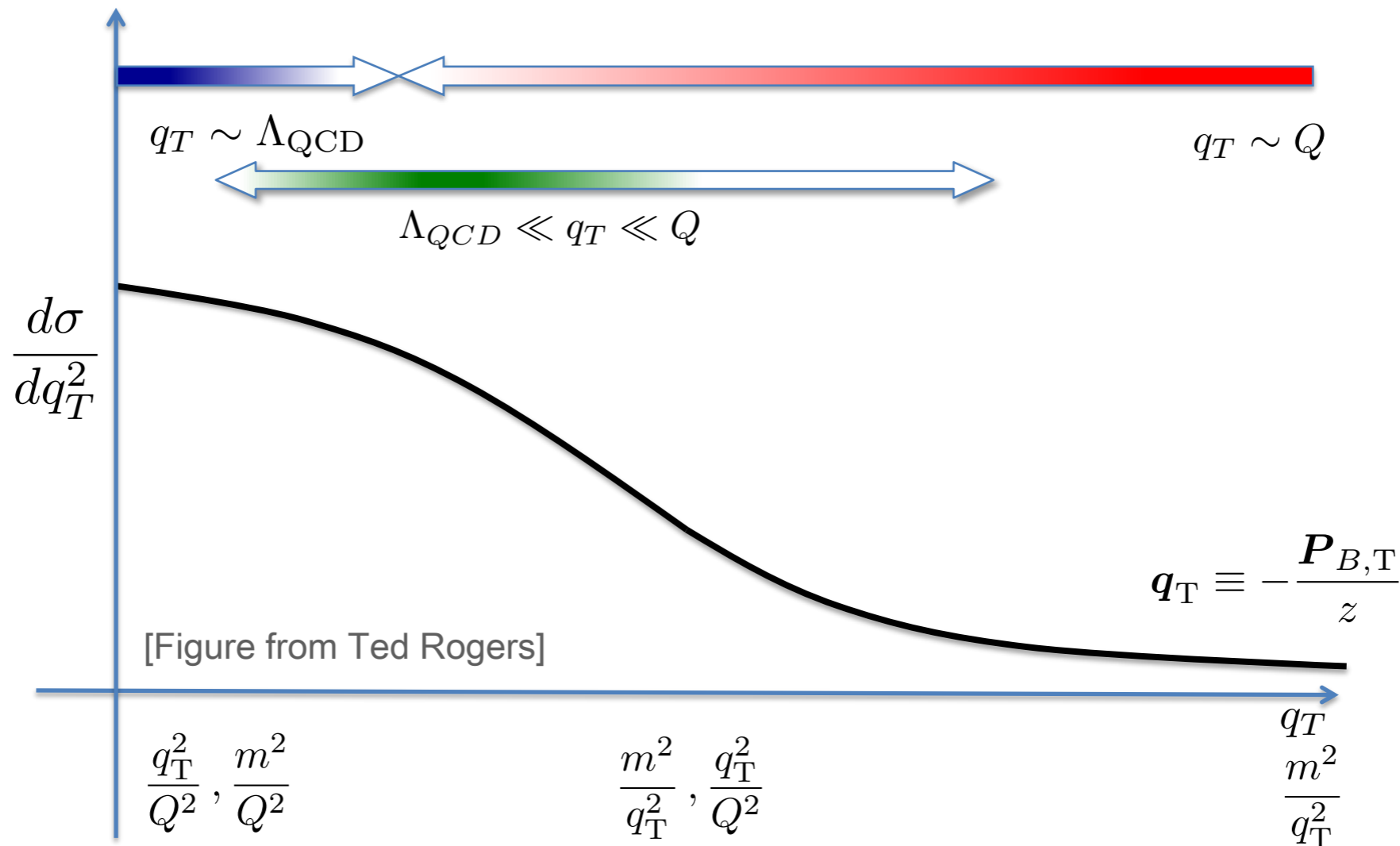
[Figure from JHEP10(2019)122]



# Small and Large Transverse Momentum

W + Y formalism

$$\frac{d\sigma}{d^2q_T dQ \dots} = W(q_T, Q) + Y(q_T, Q) + \mathcal{O}\left(\frac{m}{Q}\right)^n$$

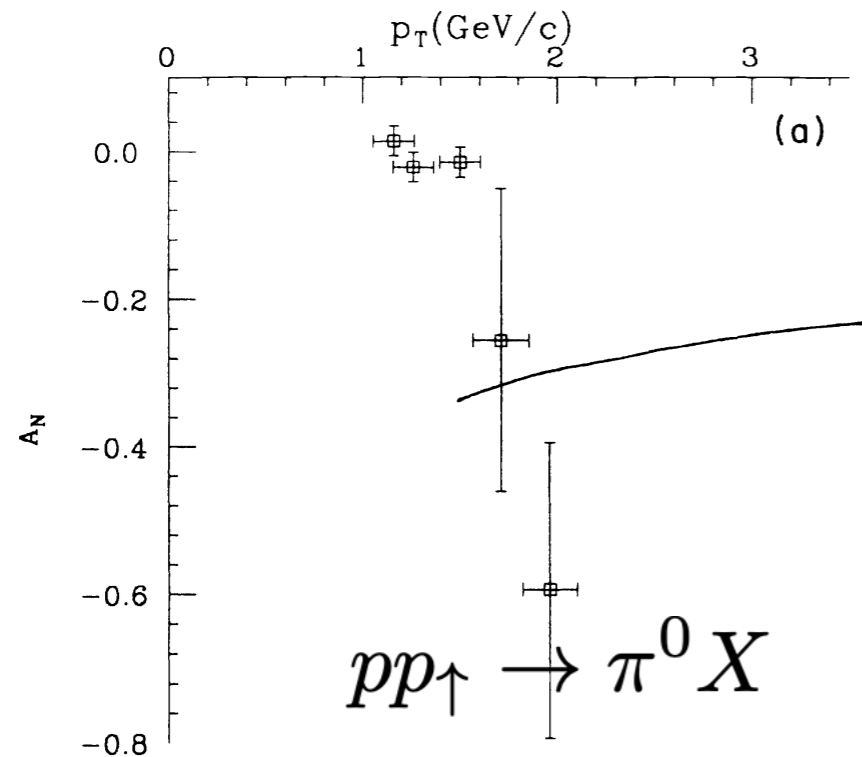


$$W(q_T, Q) = \mathbf{T}_{\text{TMD}} d\sigma$$

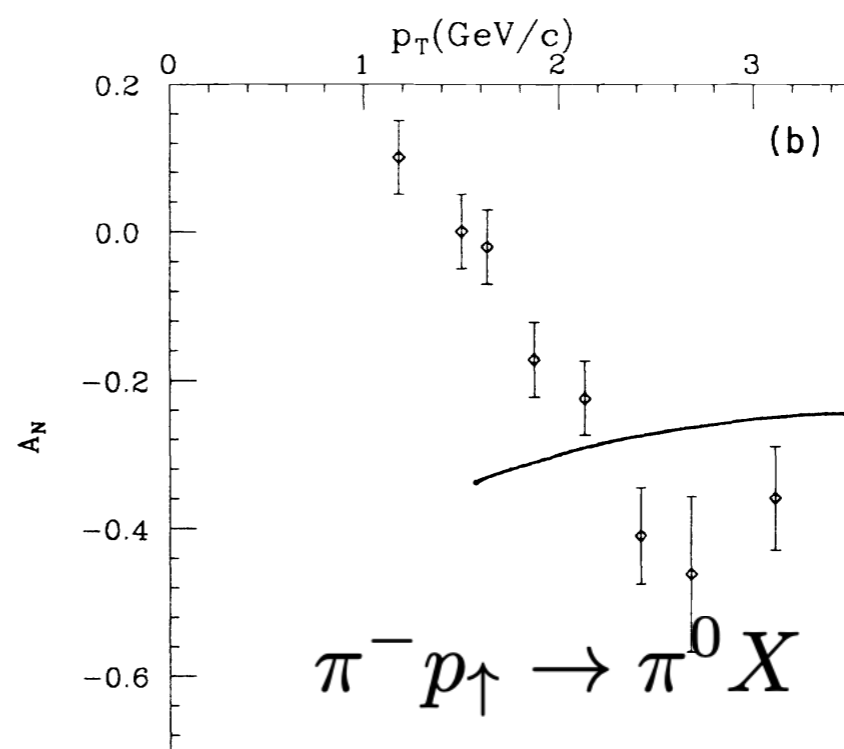
$$Y(q_T, Q) = X(q_T/\lambda) \mathbf{T}_{\text{coll}} (d\sigma - \mathbf{T}_{\text{TMD}} d\sigma) \\ = X(q_T/\lambda) [\text{FO}(q_T, Q) - \text{ASY}(q_T, Q)]$$

# Early Story: the Sivers function

## Transverse single spin asymmetry observed in experiments



Data: J. Antille *et al.*, Phys. Lett B94 (1980) 523.



Data: 7th Symposium on High Energy Spin Physics (1986).

## D. Sivers proposed to explain such SSA a new distribution function

*Sivers function*  $\Delta^N G_{a/p(\uparrow)}(x, \mathbf{k}_T; \mu^2)$

D. Sivers, Phys. Rev. D 41 (1990) 83.

## However it was soon shown this function was T-odd and prohibited by QCD

J. Collins, Nucl. Phys. B 396 (1993) 161.

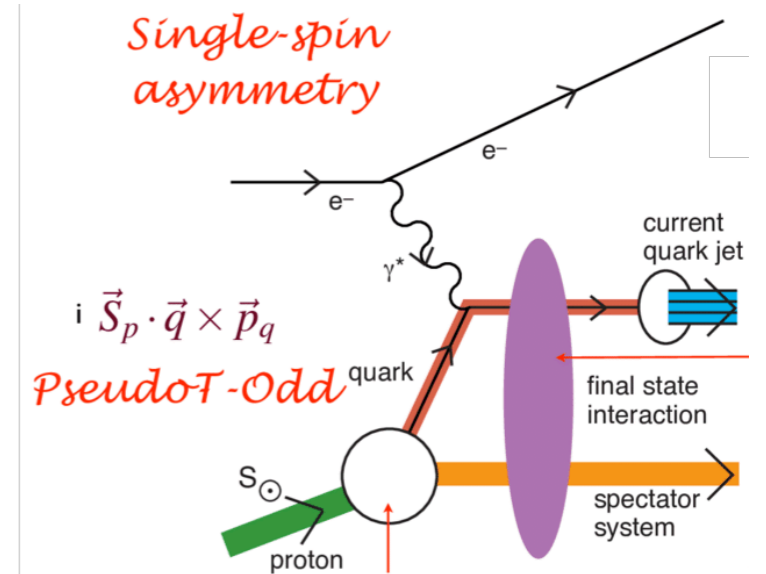
*For the next decade, the “Sivers effect” was thought to vanish.*

# Early Story: the Sivers function

Until an explicit model calculation showing ...

*nonzero Sivers effects exist at leading twist due to final-state interactions*

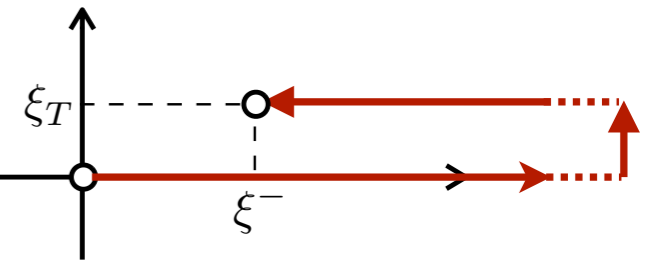
S.J. Brodsky, D.S. Hwang, I. Schmidt, Phys. Lett. B 530 (2002) 99.



**Sivers function can exist due to nontrivial gauge link**

$$\Phi_{ij}(x, p_T) = \int \frac{d\xi^- d^2\xi_T}{(2\pi)^3} e^{ip \cdot \xi} \langle P | \bar{\psi}_j(0) \mathcal{U}_{(0,+\infty)}^{n-} \mathcal{U}_{(+\infty,\xi)}^{n-} \psi_i(\xi) | P \rangle \Big|_{\xi^+=0}$$

J.C. Collins, Phys. Lett. B 536 (2002) 43.



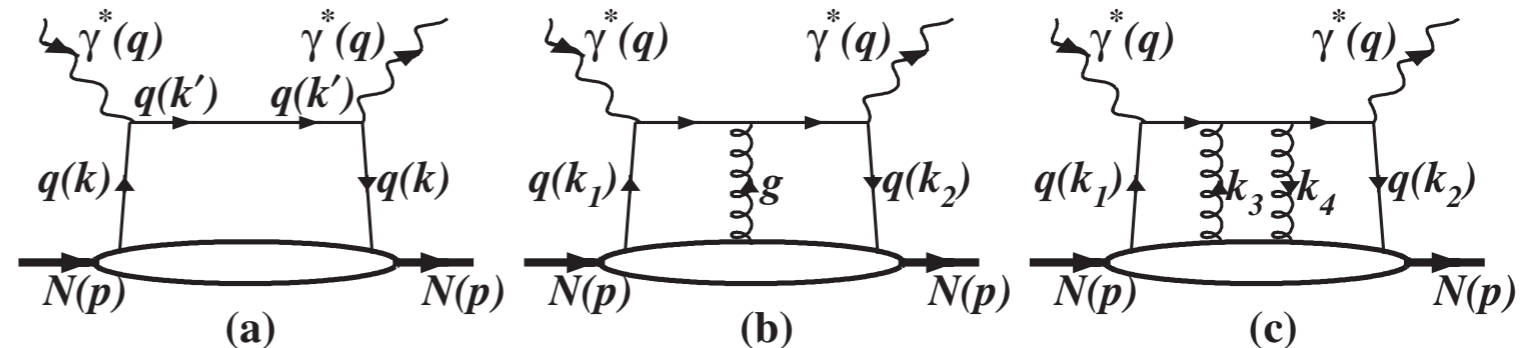
[Figure from A. Bacchetta]

This gauge link effect cannot be removed by choosing light-cone gauge  $A^+ = 0$

X. Ji and F. Yuan, Phys. Lett. B 543 (2002) 66.

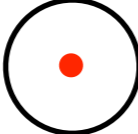
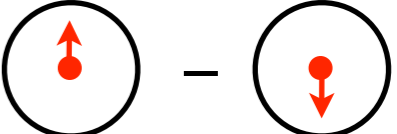
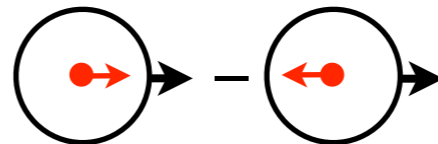
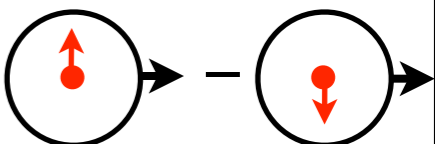
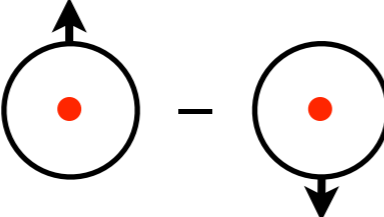
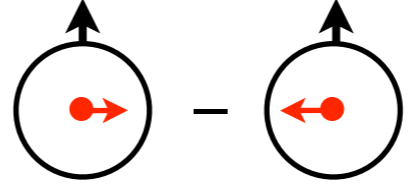
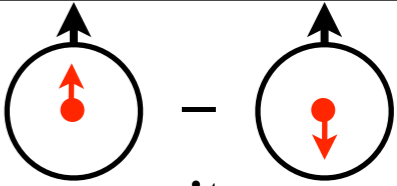
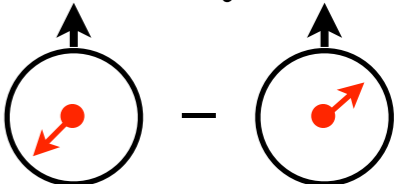
**Collinear expansion**

Z.-t. Liang and X.N. Wang, Phys. Rev. D 75 (2007) 094002.





# Leading Twist TMDs

		Quark Polarization		
		U	L	T
Nucleon Polarization	U	$f_1$  unpolarized		$h_1^\perp$  Boer-Mulders
	L		$g_{1L}$  helicity	$h_{1L}^\perp$  longi-transversity (worm-gear)
	T	$f_{1T}^\perp$  Sivers	$g_{1T}$  trans-helicity (worm-gear)	$h_1$  transversity $h_{1T}^\perp$  pretzelosity

# SIDIS in Trento Convention

## SIDIS differential cross section

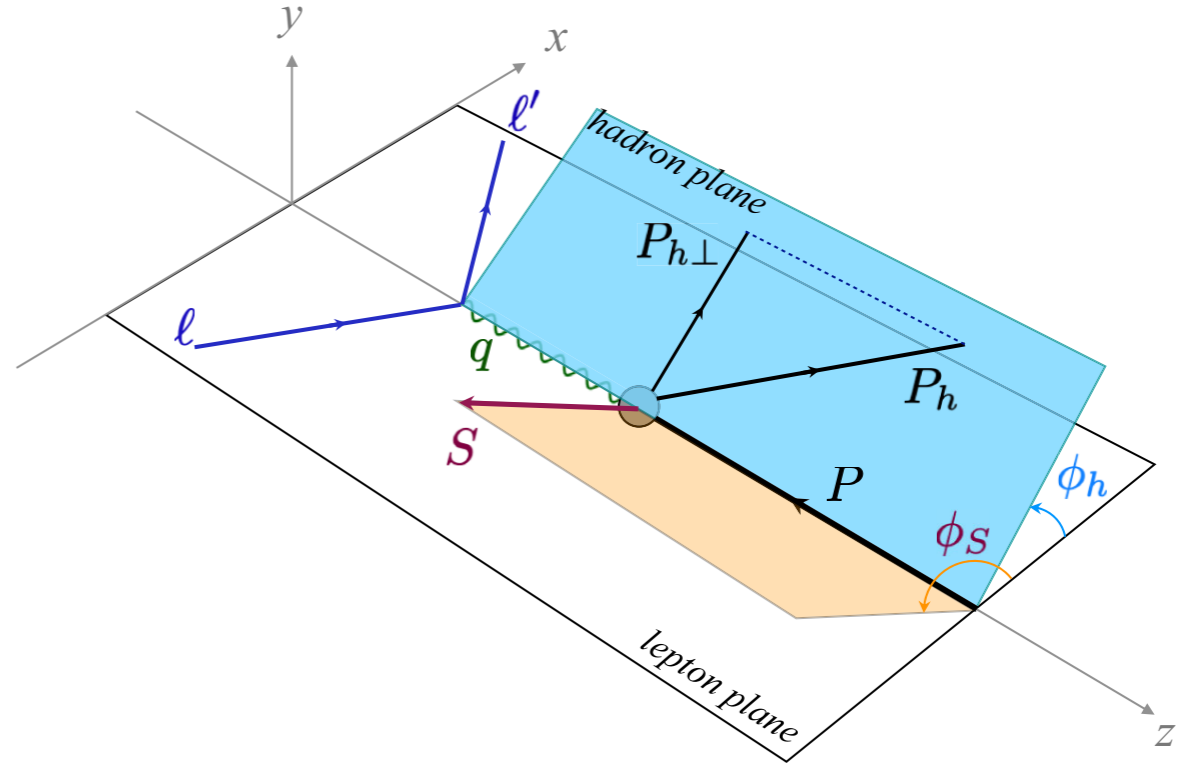
in terms of 18 structure functions

$$F_{AB,C} (x_B, z, Q^2, P_{hT}^2)$$

*A*: lepton polarization

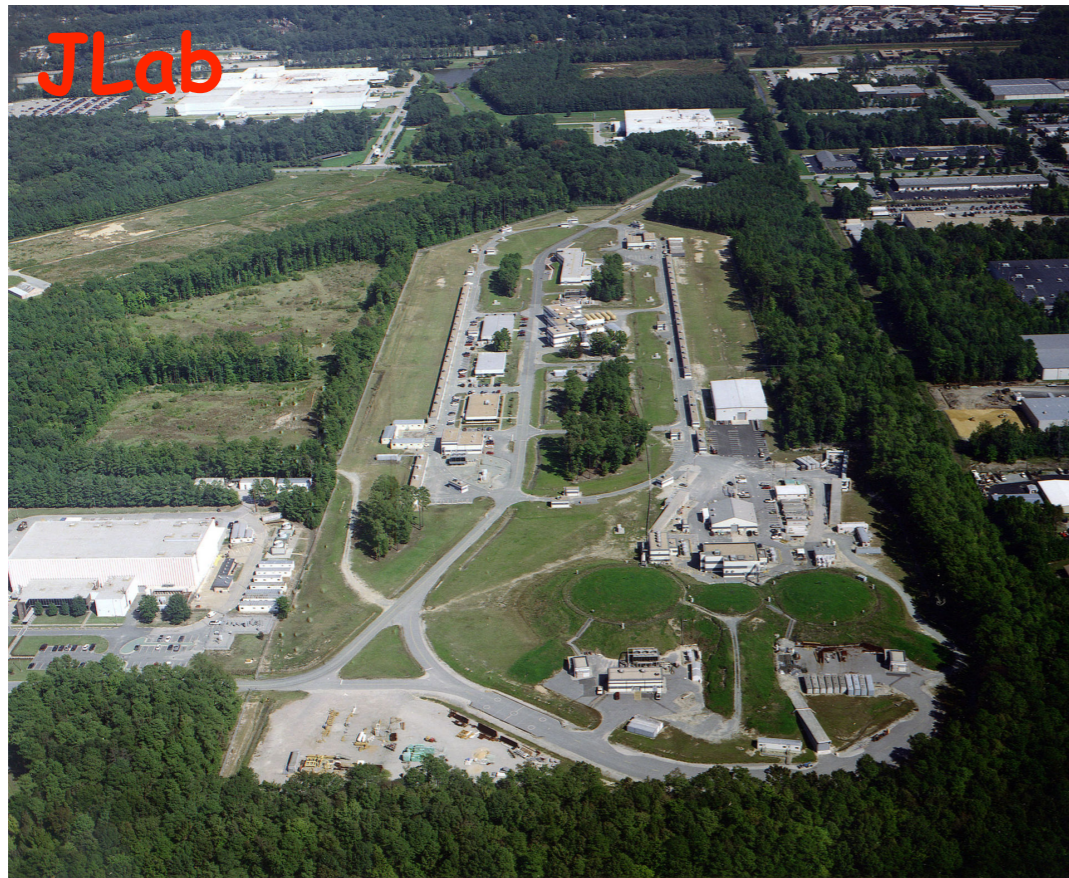
*B*: nucleon polarization

*C*: virtual photon polarization

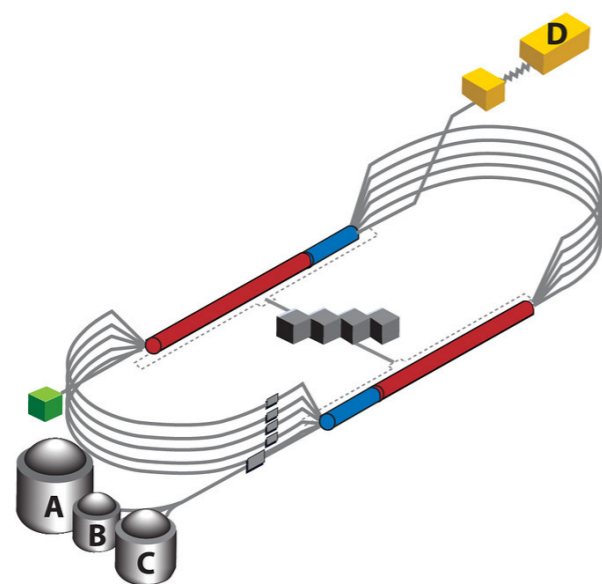


$$\frac{d\sigma}{dx_B dy dz dP_{hT}^2 d\phi_h d\phi_S} = \frac{\alpha^2}{x_B y Q^2} \frac{y^2}{2(1-\epsilon)} \left( 1 + \frac{\gamma^2}{2x_B} \right) \times \left\{ F_{UU,T} + \epsilon F_{UU,L} + \sqrt{2\epsilon(1+\epsilon)} F_{UU}^{\cos \phi_h} \cos \phi_h + \epsilon F_{UU}^{\cos 2\phi_h} \cos 2\phi_h + \lambda_e \sqrt{2\epsilon(1-\epsilon)} F_{LU}^{\sin \phi_h} \sin \phi_h \right. \\ + S_L \left[ \sqrt{2\epsilon(1+\epsilon)} F_{UL}^{\sin \phi_h} \sin \phi_h + \epsilon F_{UL}^{\sin 2\phi_h} \sin 2\phi_h \right] + \lambda_e S_L \left[ \sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} F_{LL}^{\cos \phi_h} \cos \phi_h \right] \\ + S_T \left[ \left( F_{UT,T}^{\sin(\phi_h-\phi_S)} + \epsilon F_{UT,L}^{\sin(\phi_h-\phi_S)} \right) \sin(\phi_h-\phi_S) + \epsilon F_{UT}^{\sin(\phi_h+\phi_S)} \sin(\phi_h+\phi_S) \right. \\ \left. + \epsilon F_{UT}^{\sin(3\phi_h-\phi_S)} \sin(3\phi_h-\phi_S) + \sqrt{2\epsilon(1+\epsilon)} F_{UT}^{\sin \phi_S} \sin \phi_S + \sqrt{2\epsilon(1+\epsilon)} F_{UT}^{\sin(2\phi_h-\phi_S)} \sin(2\phi_h-\phi_S) \right] \\ + \lambda_e S_T \left[ \sqrt{1-\epsilon^2} F_{LT}^{\cos(\phi_h-\phi_S)} \cos(\phi_h-\phi_S) \right. \\ \left. + \sqrt{2\epsilon(1-\epsilon)} F_{LT}^{\cos \phi_S} \cos \phi_S + \sqrt{2\epsilon(1-\epsilon)} F_{LT}^{\cos(2\phi_h-\phi_S)} \cos(2\phi_h-\phi_S) \right] \left. \right\}$$

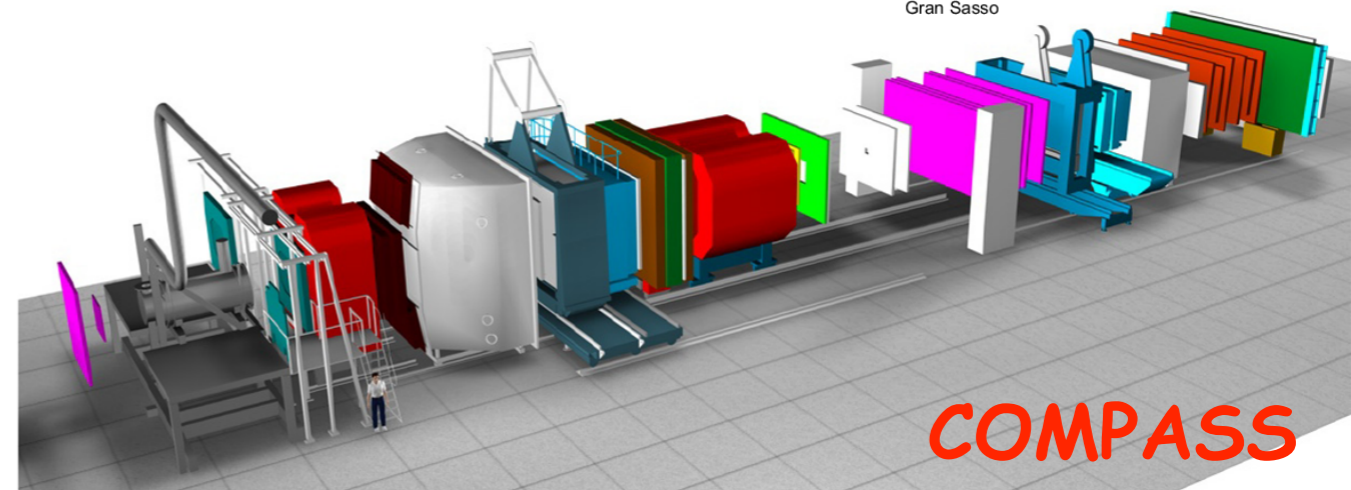
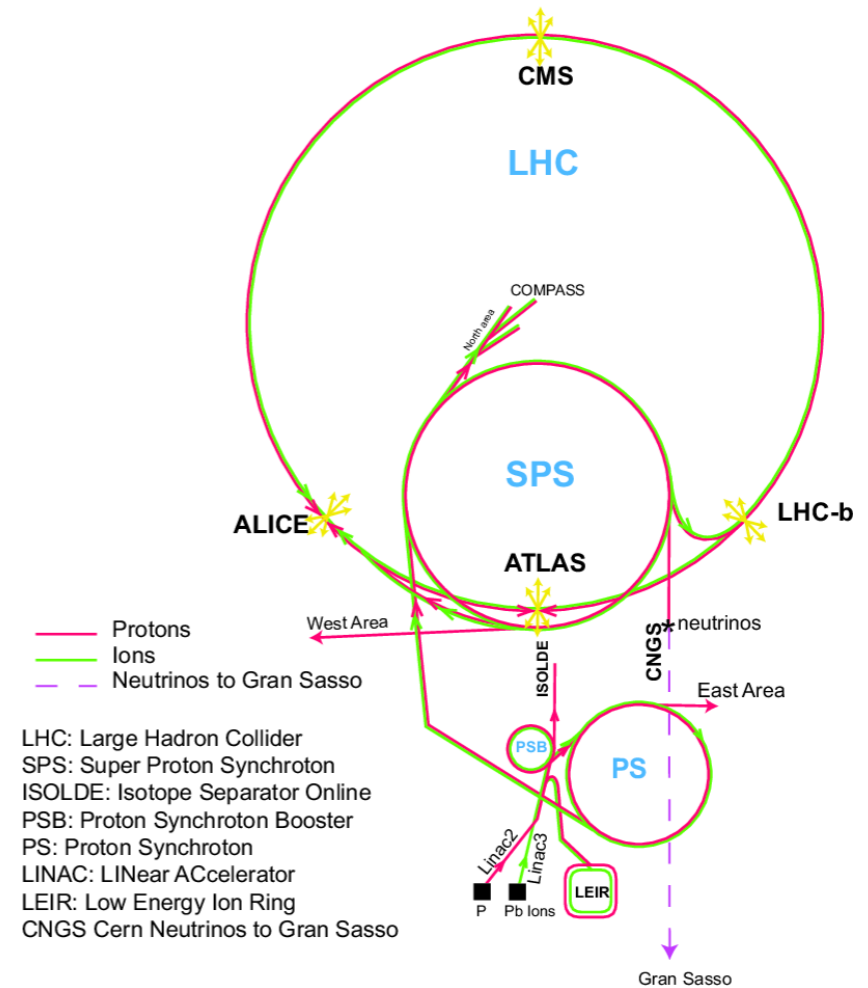
# Fixed Target Experiments (Existing)



JLab

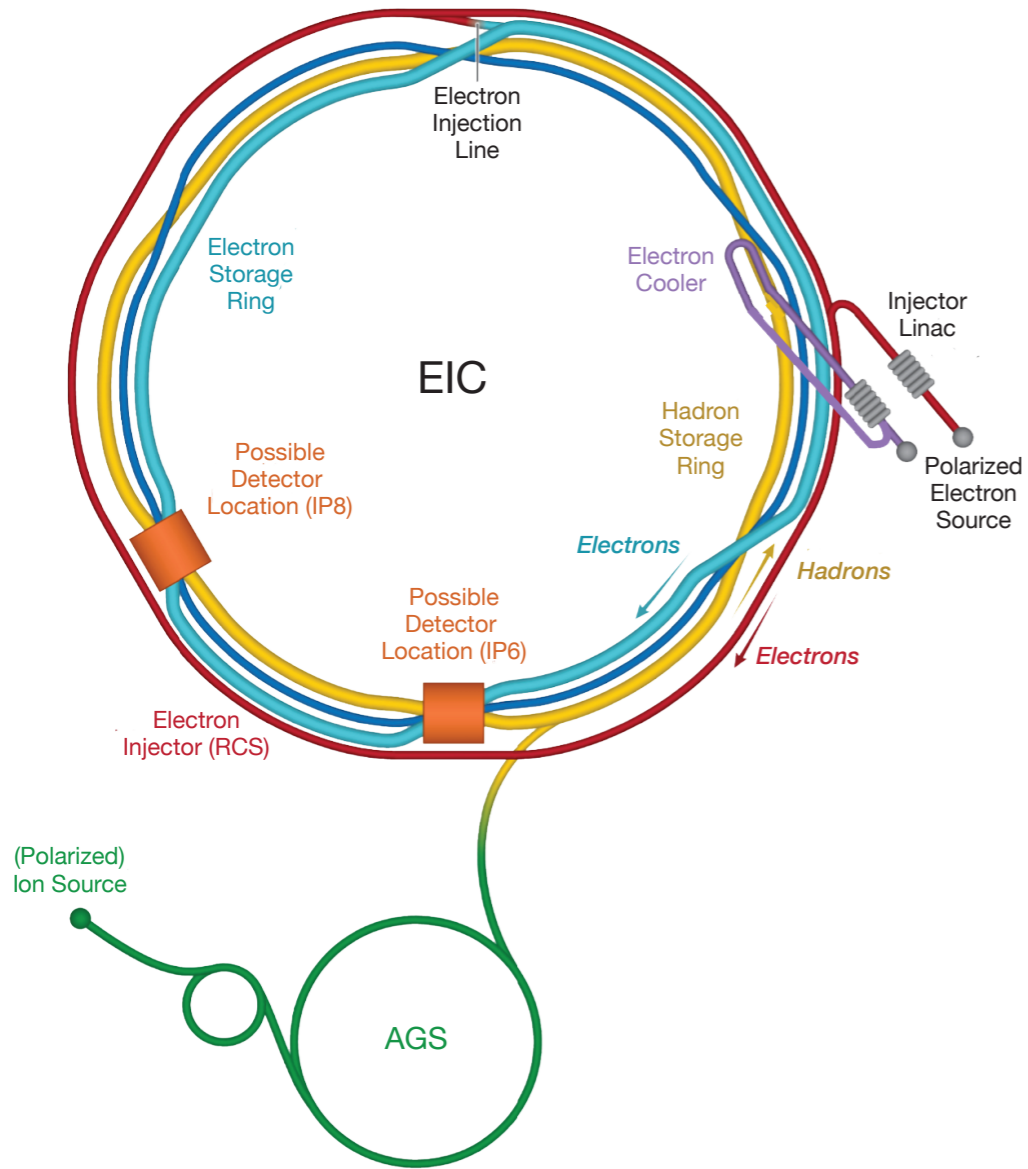


## CERN Accelerators

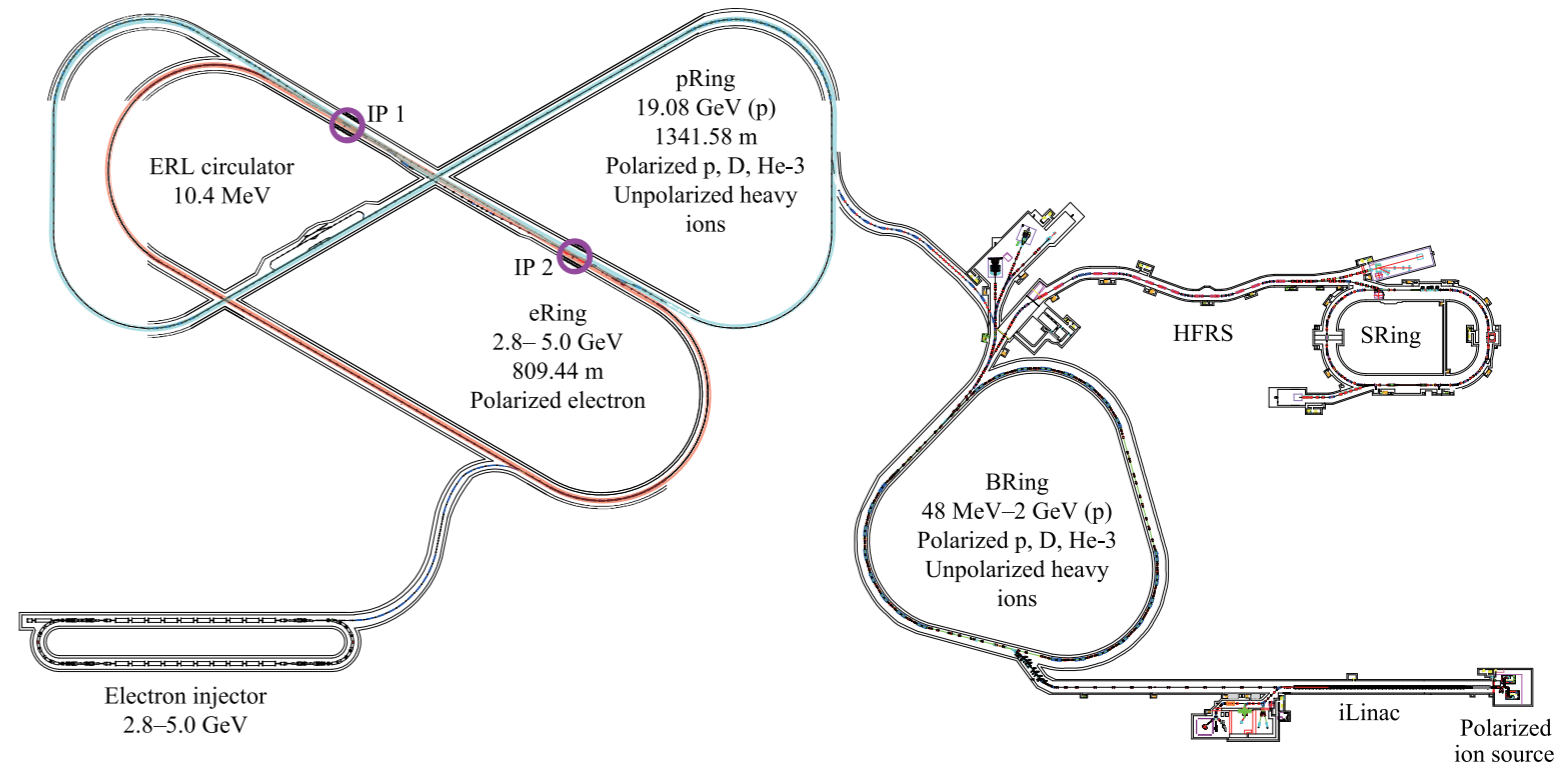




# Electron-Ion Colliders (Future)

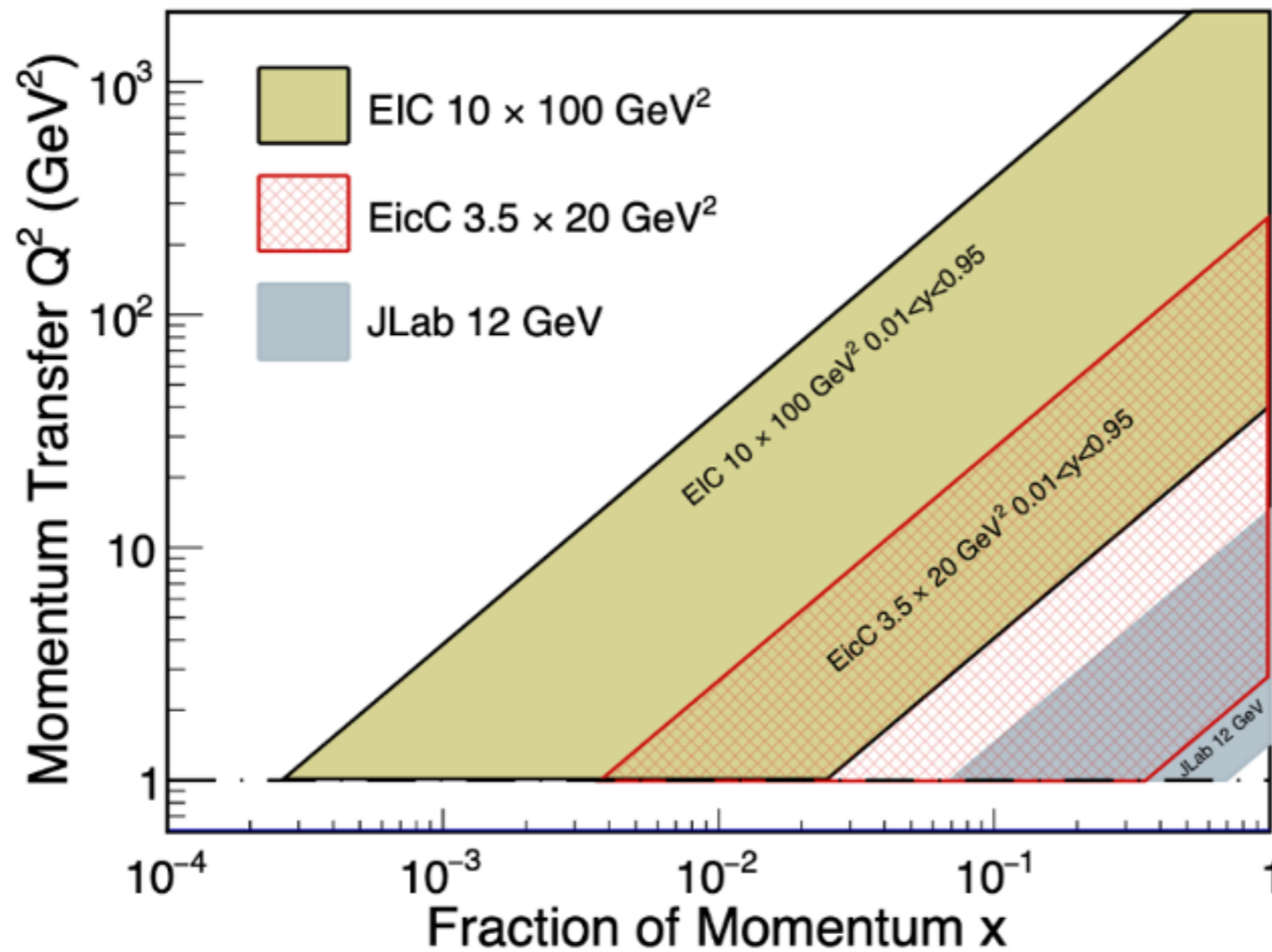


[Figure from EIC Yellow Report]



[Figure from EicC Whitepaper]

# Complementary Kinematic Coverage



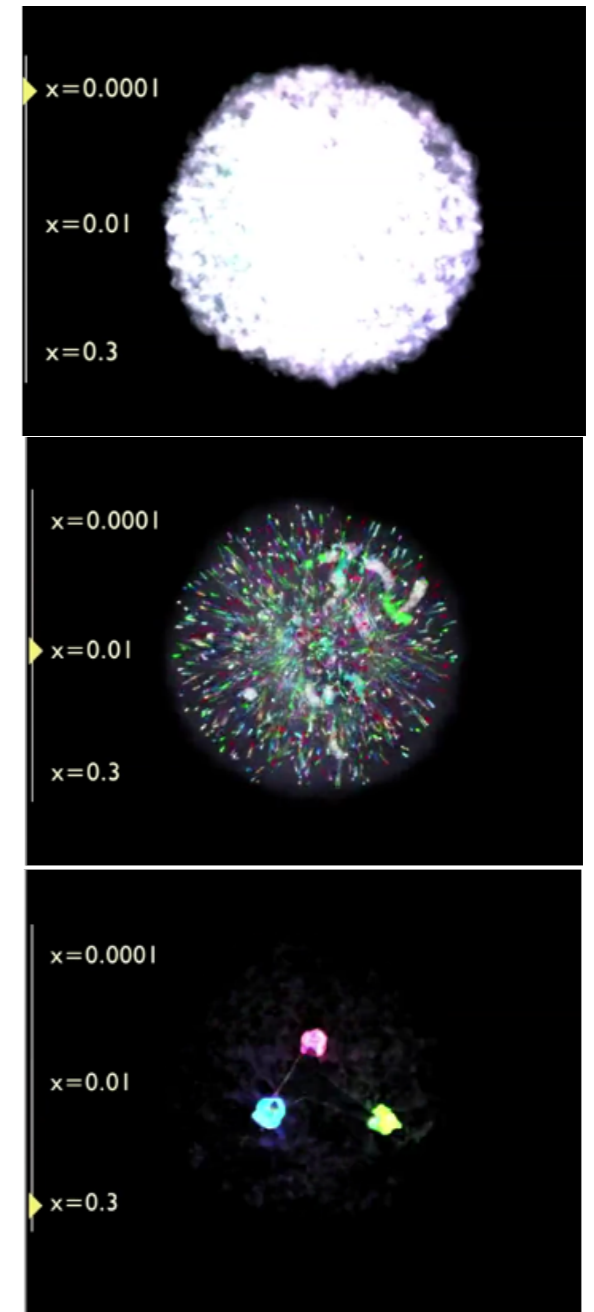
[Figure from EicC White paper]

**EicC** is optimized to systematically explore the gluon and sea quarks in moderate  $x$  regime  
 At a crucial place between JLab and EIC-US

*gluon  
 dominates*

*sea quarks  
 + gluons*

*valence  
 dominates*



R.G. Milner and R. Ent, *Visualizing the proton* 2022

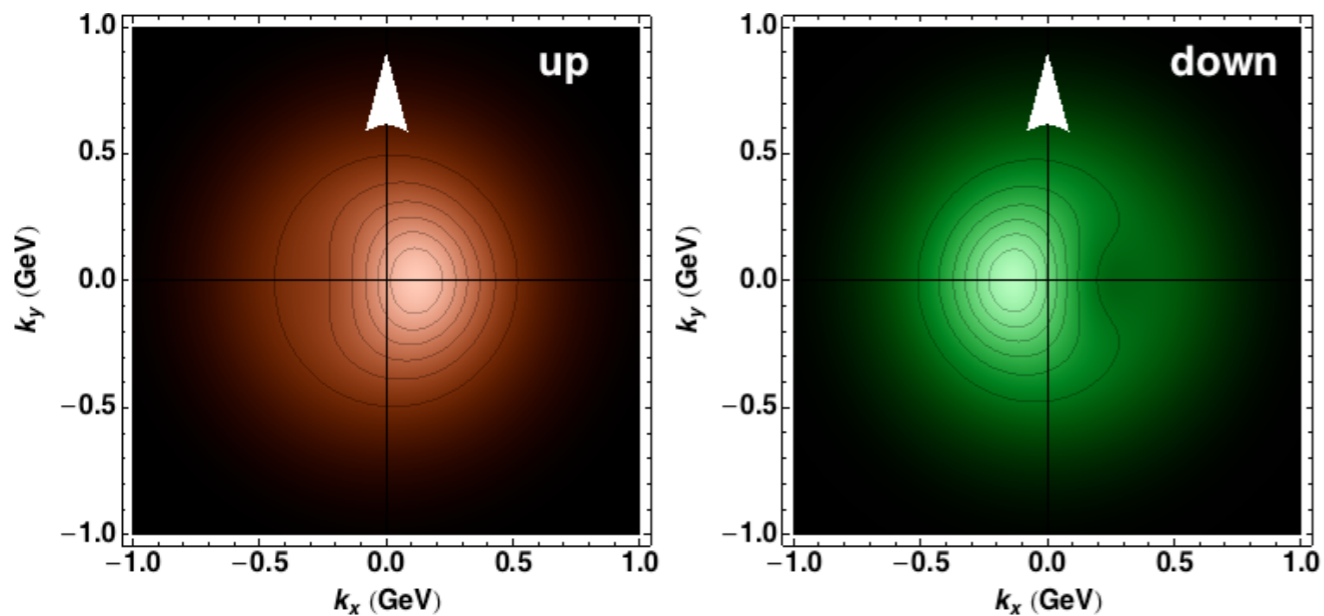
# The Sivers Function

## Sivers TMD distribution function

$$f_{1T}^\perp(x, \mathbf{k}_\perp) \quad \begin{array}{c} \uparrow \\ \circ \\ \downarrow \end{array} - \begin{array}{c} \circ \\ \downarrow \end{array}$$

*A naive T-odd distribution function*

Transverse momentum distribution distorted by nucleon transverse spin



[Figure from A. Bacchetta]

## Effect in SIDIS:

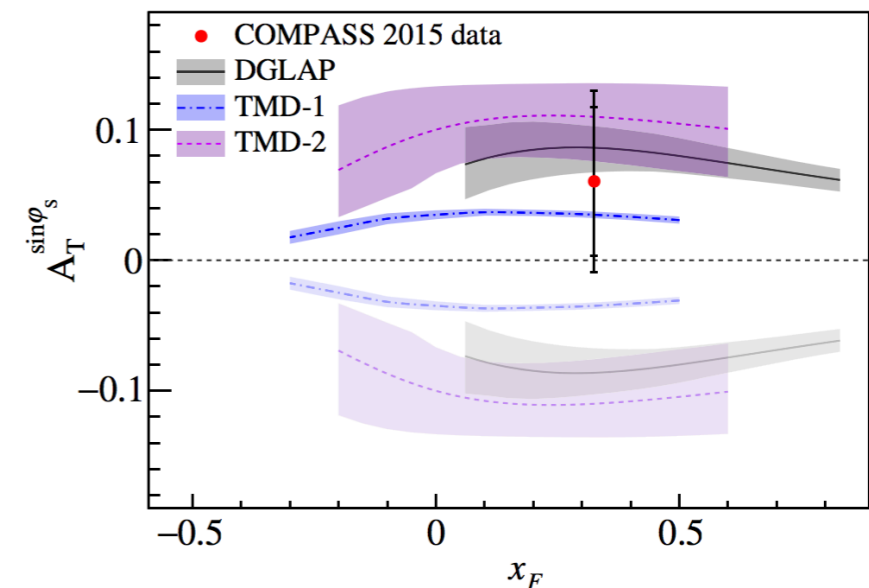
transverse single spin asymmetry  
(Sivers asymmetry)

$$A_{UT}^{\sin(\phi_h - \phi_s)} \sim f_{1T}^\perp \otimes D_1$$

sizable Sivers asymmetry observed by HERMES, COMPASS, JLab

## Sign change prediction:

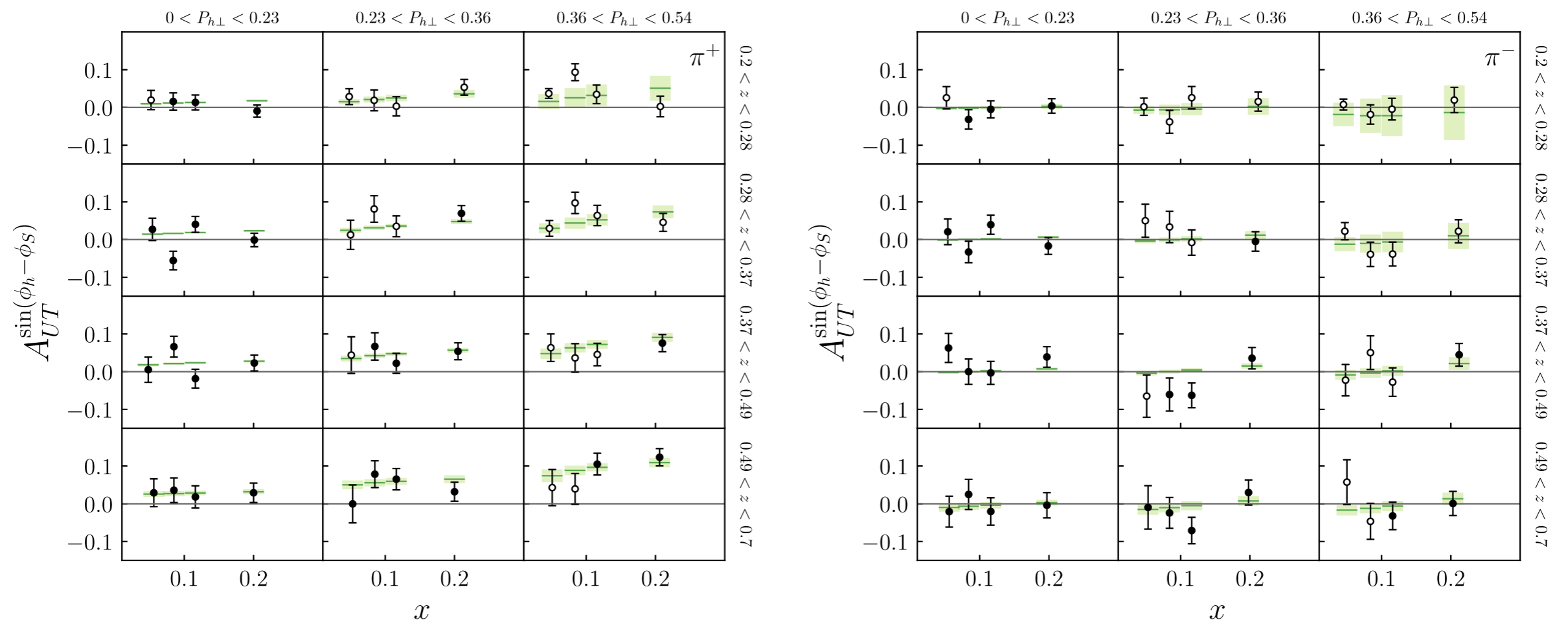
$$f_{1T}^\perp(x, \mathbf{k}_\perp) \Big|_{\text{SIDIS}} = - f_{1T}^\perp(x, \mathbf{k}_\perp) \Big|_{\text{DY}}$$



COMPASS Collaboration, PRL 119, 112002 (2017).

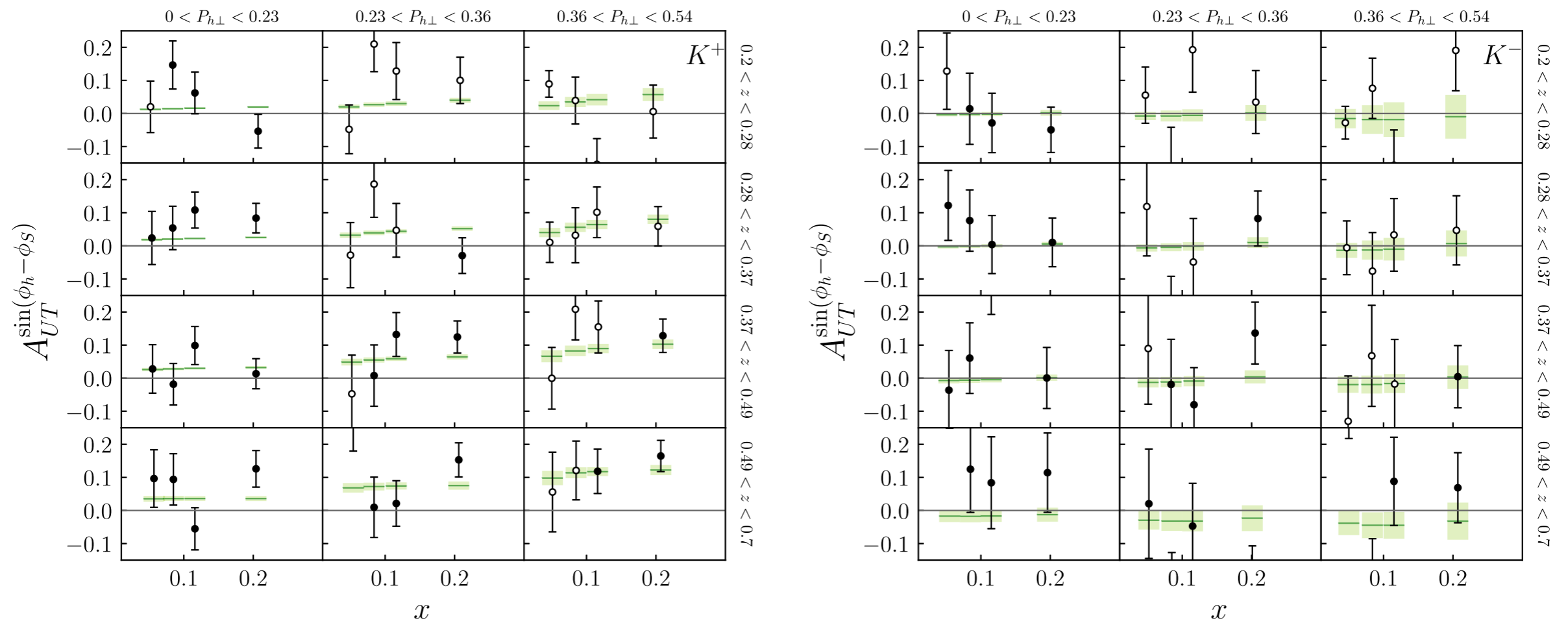


# Measurements of the Sivers Asymmetry



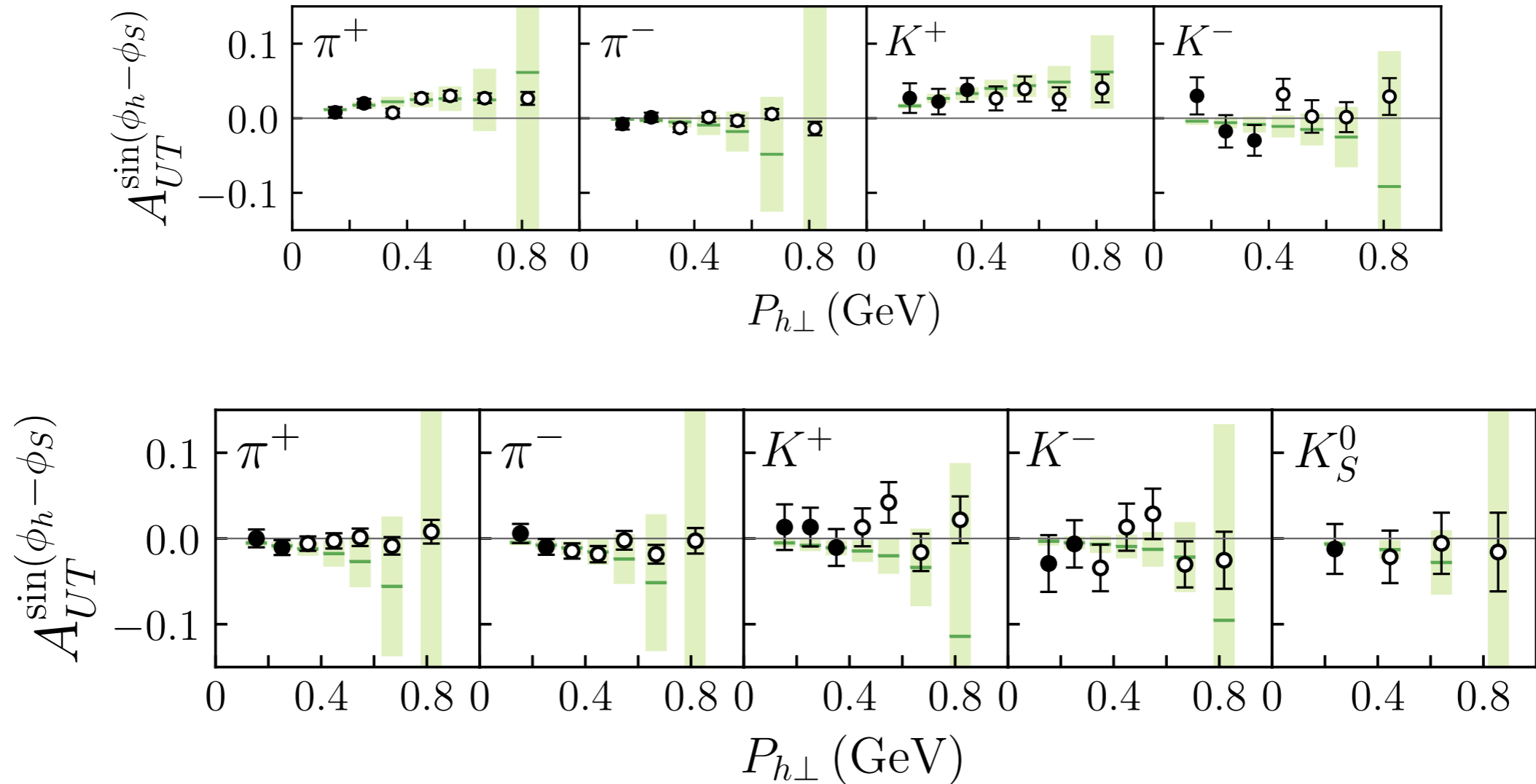
HERMES Collaboration, J. High Energy Phys. 12 (2020) 010. (re-analyzed)

# Measurements of the Sivers Asymmetry



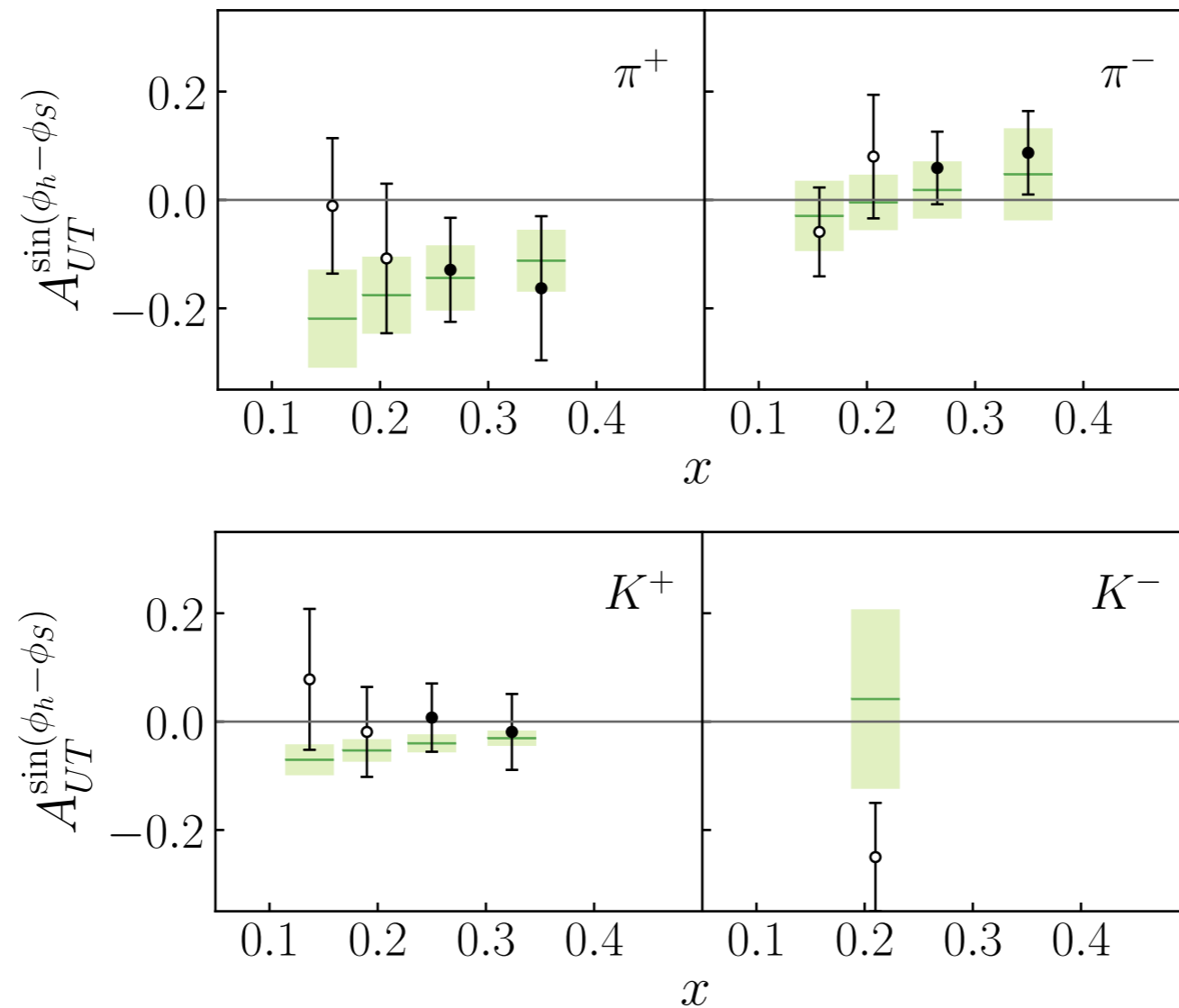
HERMES Collaboration, J. High Energy Phys. 12 (2020) 010. (re-analyzed)

# Measurements of the Sivers Asymmetry



COMPASS Collaboration, Phys. Lett. B 673 (2009) 127; Phys. Lett. B 744 (2015) 250.

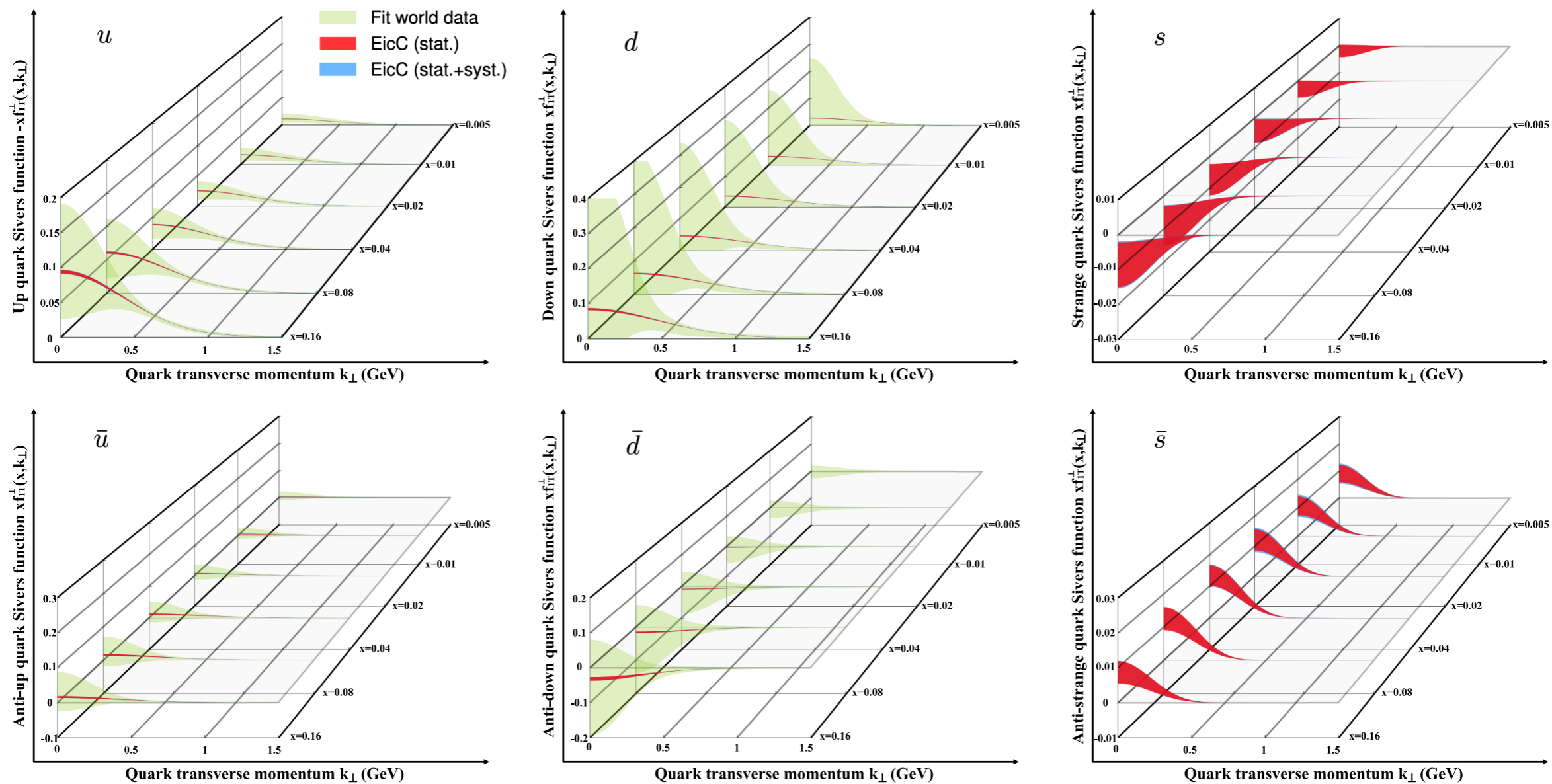
# Measurements of the Sivers Asymmetry



JLab HallA Collaboration, Phys. Rev. Lett. (2011) 072003; Phys. Rev. C 90 (2014) 055201.

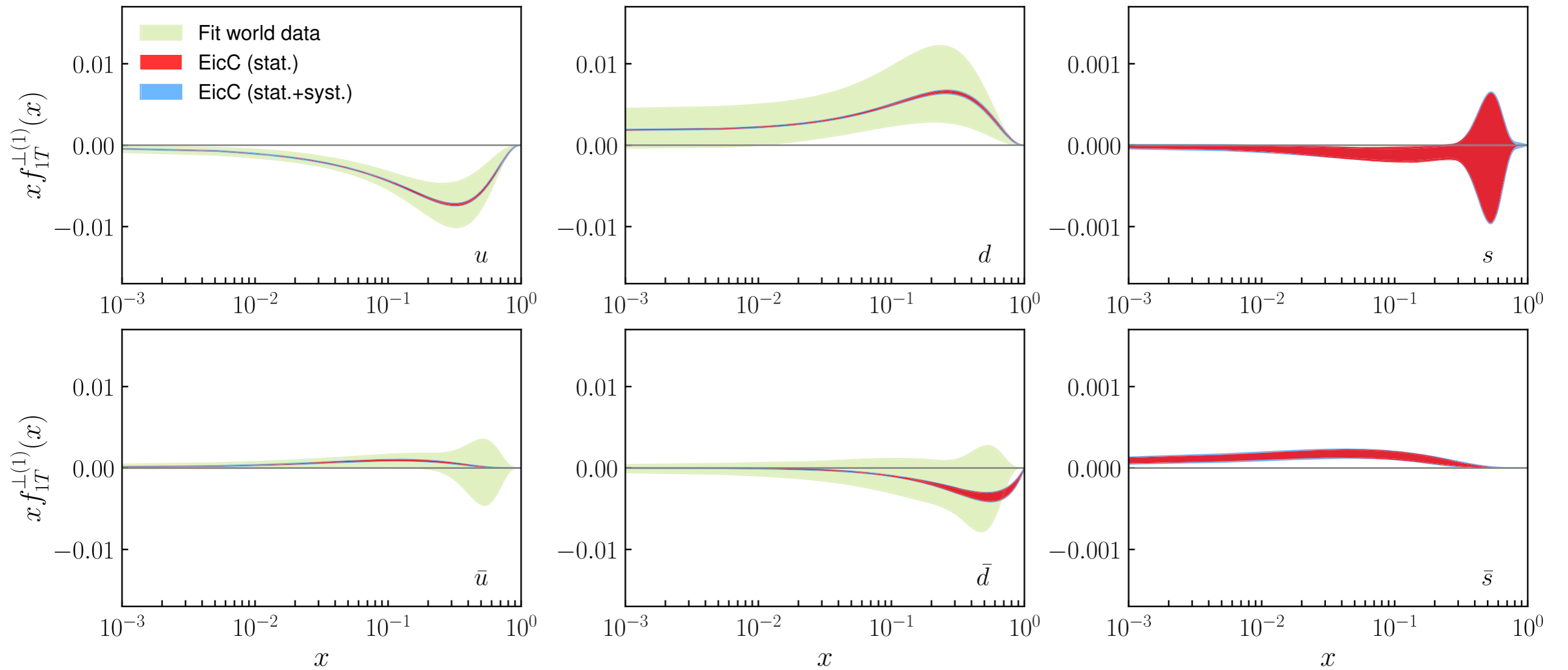


# Extraction of the Sivers function



C. Zeng, T. Liu, P. Sun, Y. Zhao, Phys. Rev. D 106 (2022) 094039.

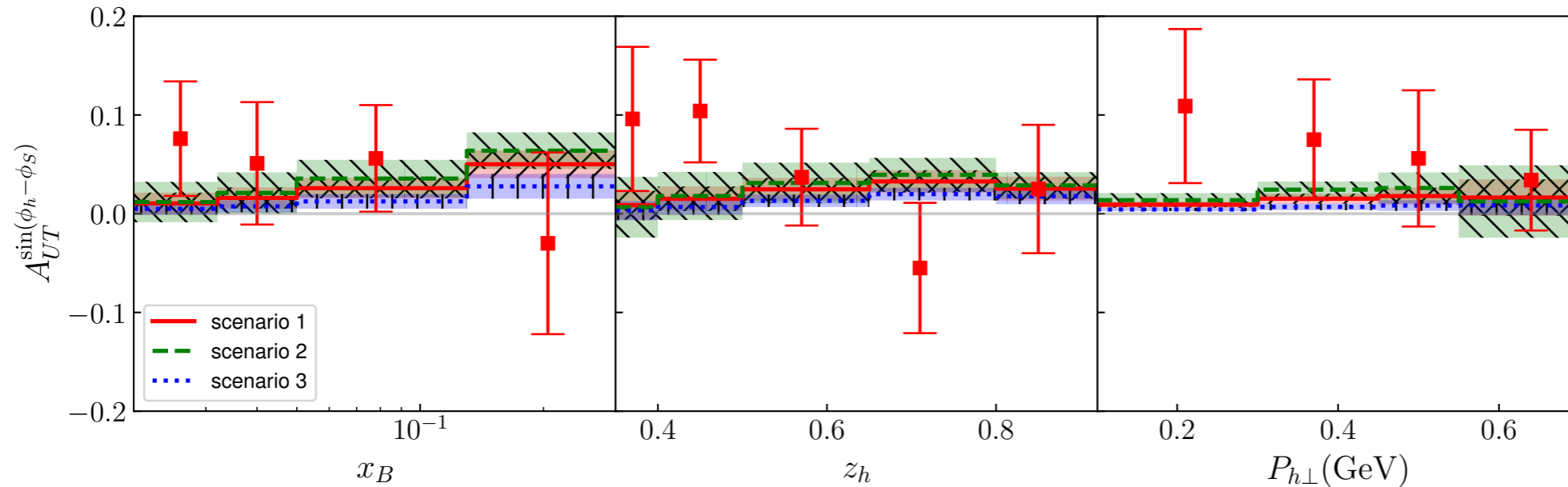
# EicC Impact: Sivers function



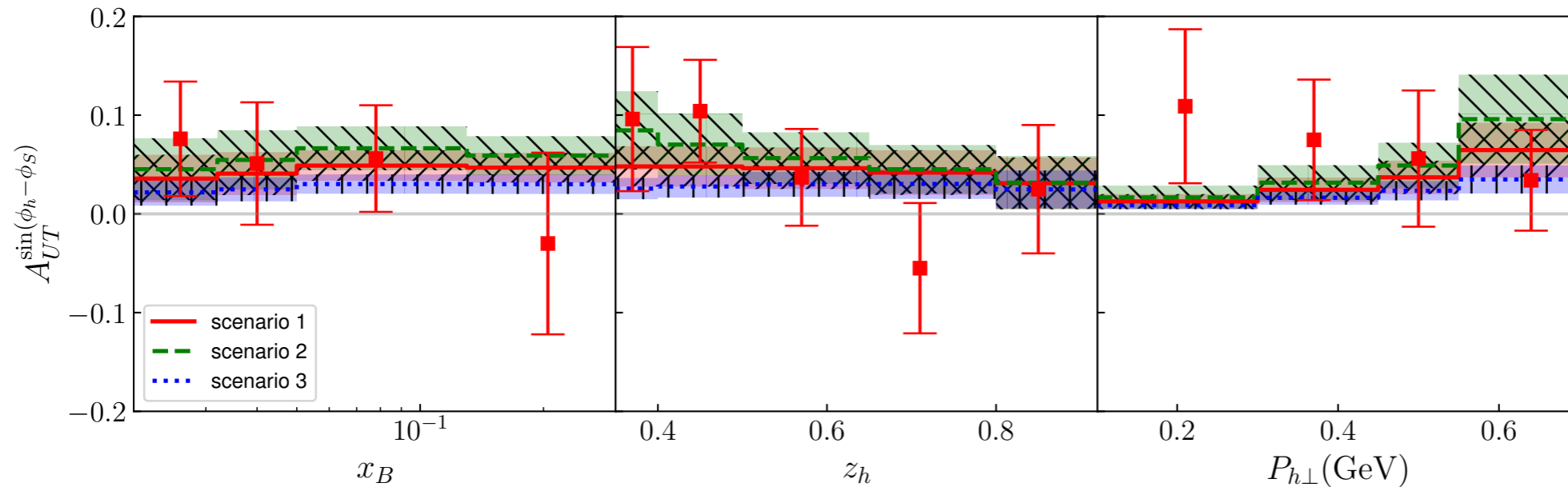
$$f_{1T}^{\perp(1)}(x) = \pi \int d\mathbf{k}_{\perp}^2 \frac{\mathbf{k}_{\perp}^2}{2M^2} f_{1T}^{\perp}(x, \mathbf{k}_{\perp}^2)$$

C. Zeng, T. Liu, P. Sun, Y. Zhao, Phys. Rev. D 106 (2022) 094039.

# Sivers Asymmetry of $\rho^0$ Production



Sivers functions from  
C. Zeng, TL, P. Sun, Y. Zhao,  
PRD 106 (2022) 094039.



Sivers functions from  
M. Bury, A. Prokudin, A.  
Vladmirov,  
JHEP 05 (2021) 151.

Data from COMPASS Collaboration, PLB 843 (2023) 137950.

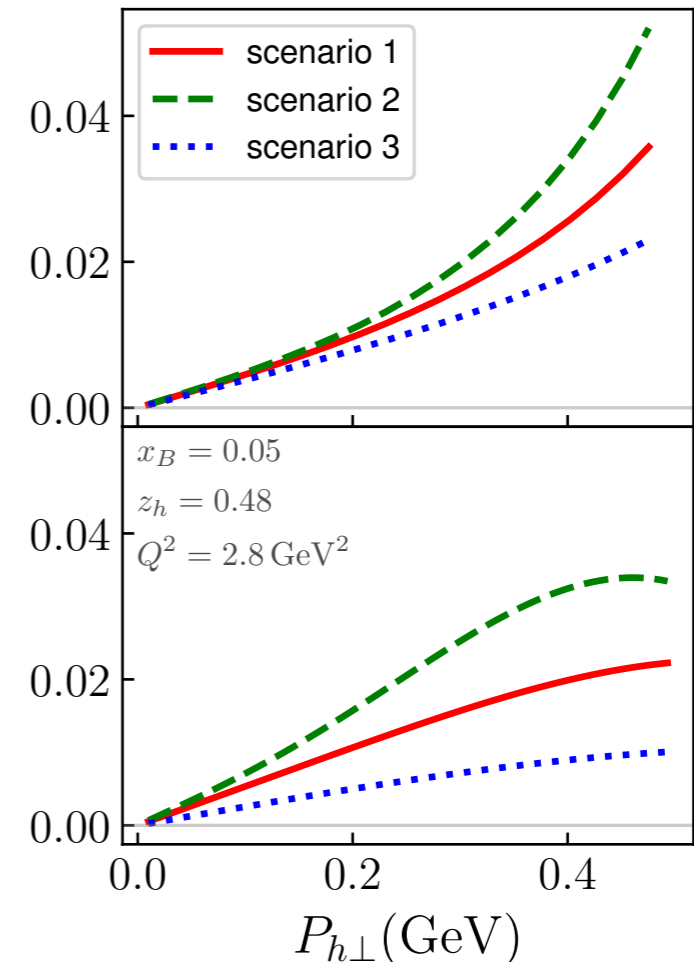
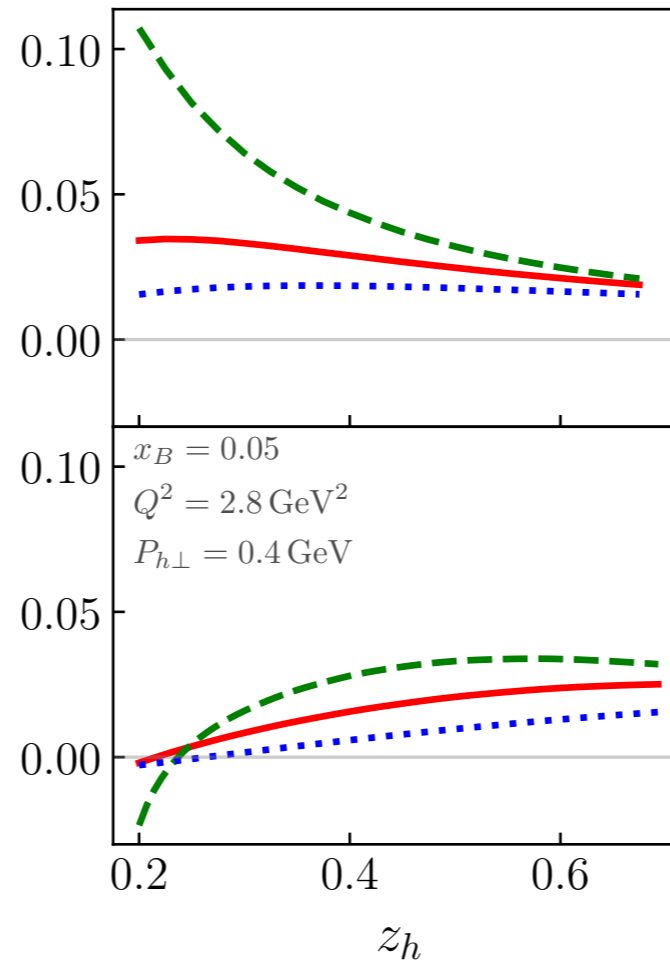
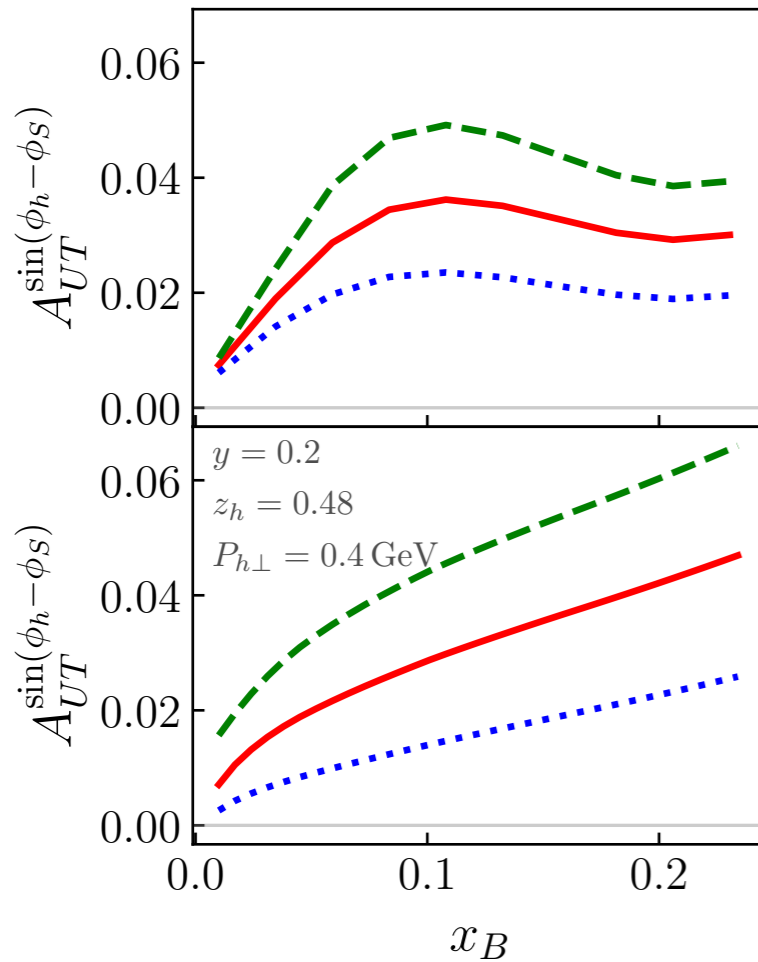
Scenarios: different transverse momentum dependences of  $\rho^0$  fragmentation functions

Y. Deng, TL, Y.-j. Zhou, 2024

# Sivers Asymmetry of $\rho^0$ Production

Predictions at EicC kinematics:

$$\sqrt{s} = 16.7 \text{ GeV}$$



ZLSZ 2022

BPV 2021

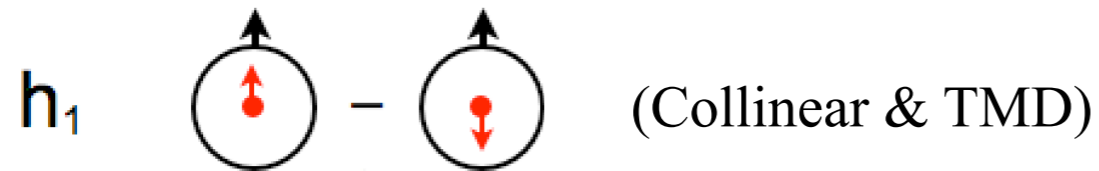
Different predictions to be tested at EicC kinematics

Y. Deng, TL, Y.-j. Zhou, 2024



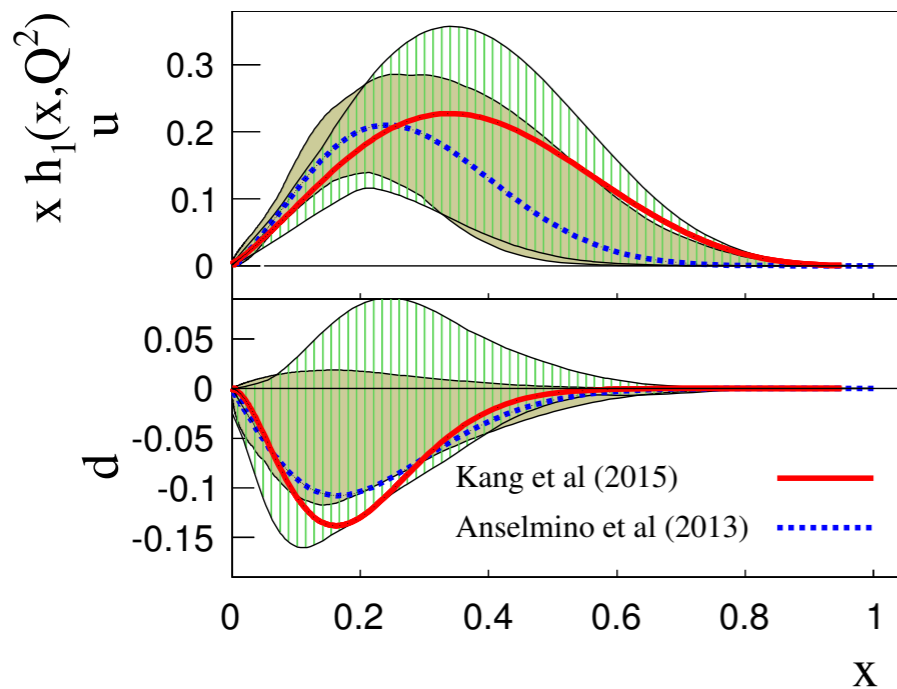
# Transversity Distribution

## Transversity distribution



A transverse counter part to the longitudinal spin structure: helicity  $g_{1L}$ , but NOT the same.

## Phenomenological extractions



Z.-B. Kang, A. Prokudin, P. Sun, F. Yuan, PRD 93, 014009 (2016).

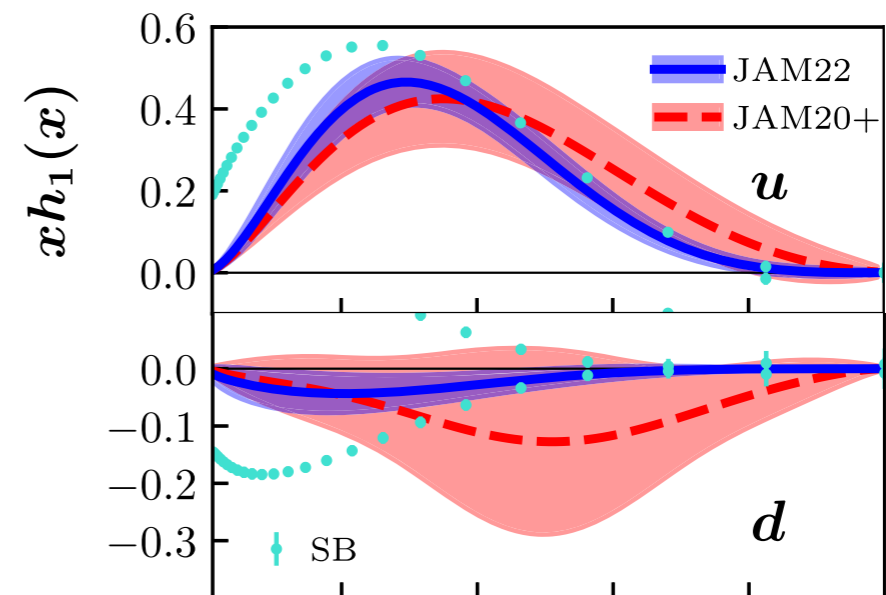
## Chiral-odd:

- No mixing with gluons
- Valence dominant
- Couple to another chiral-odd function.

## Effect in SIDIS:

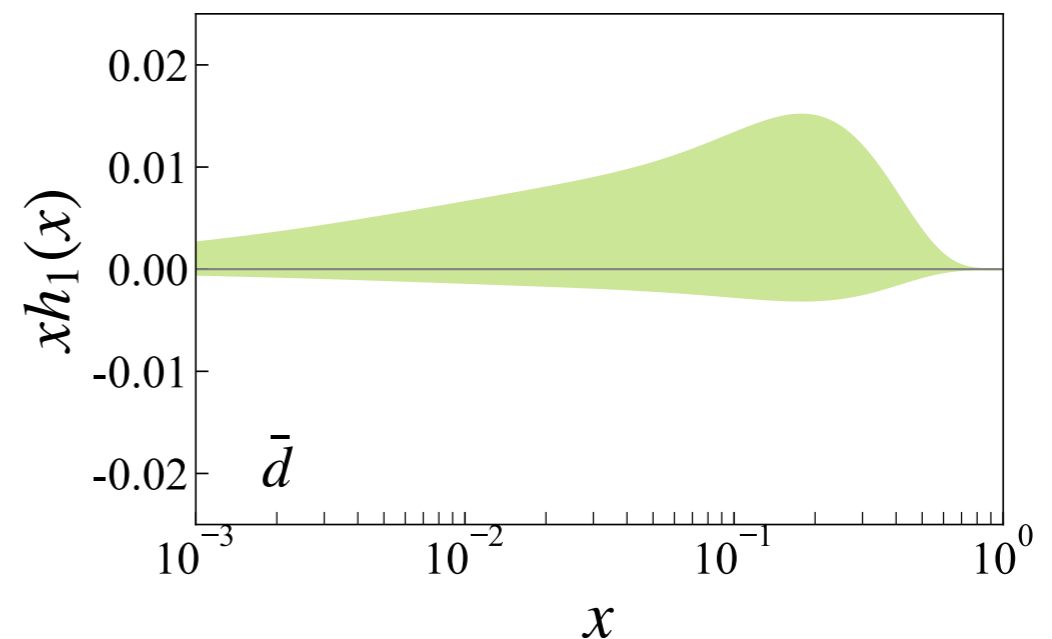
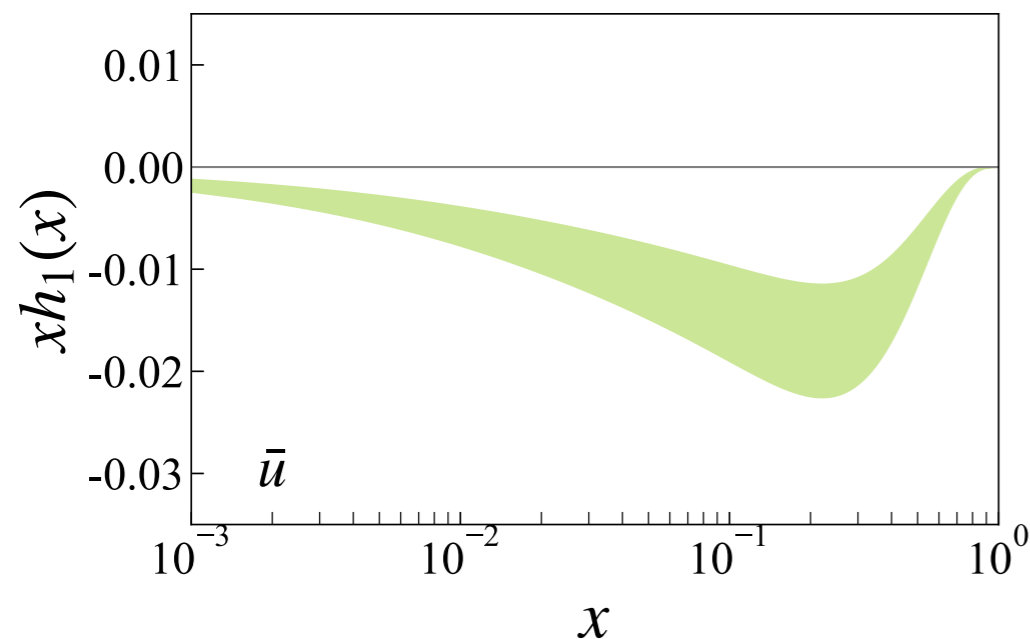
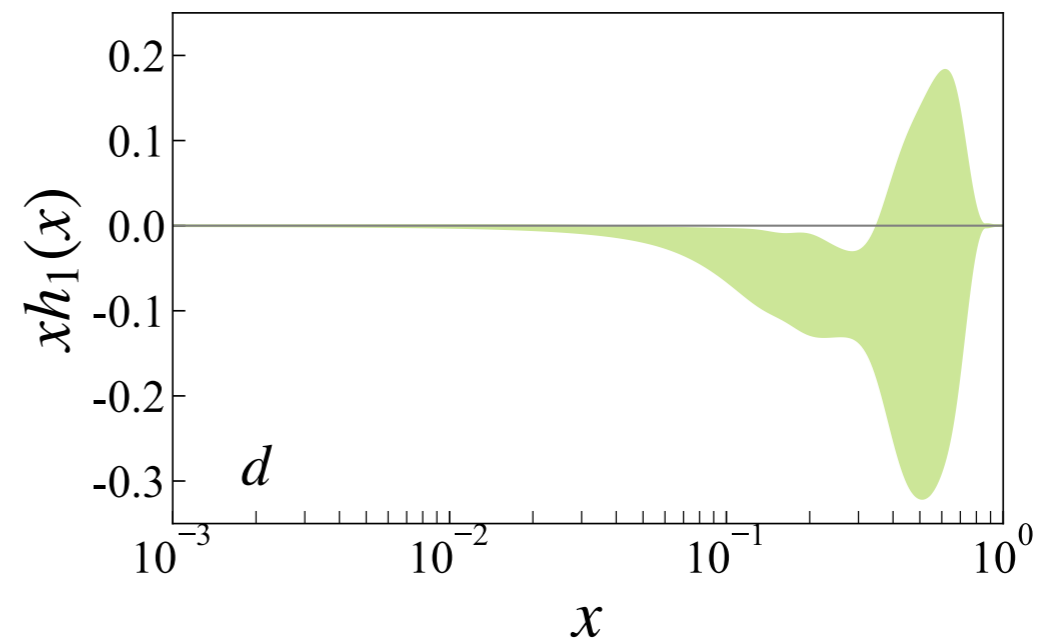
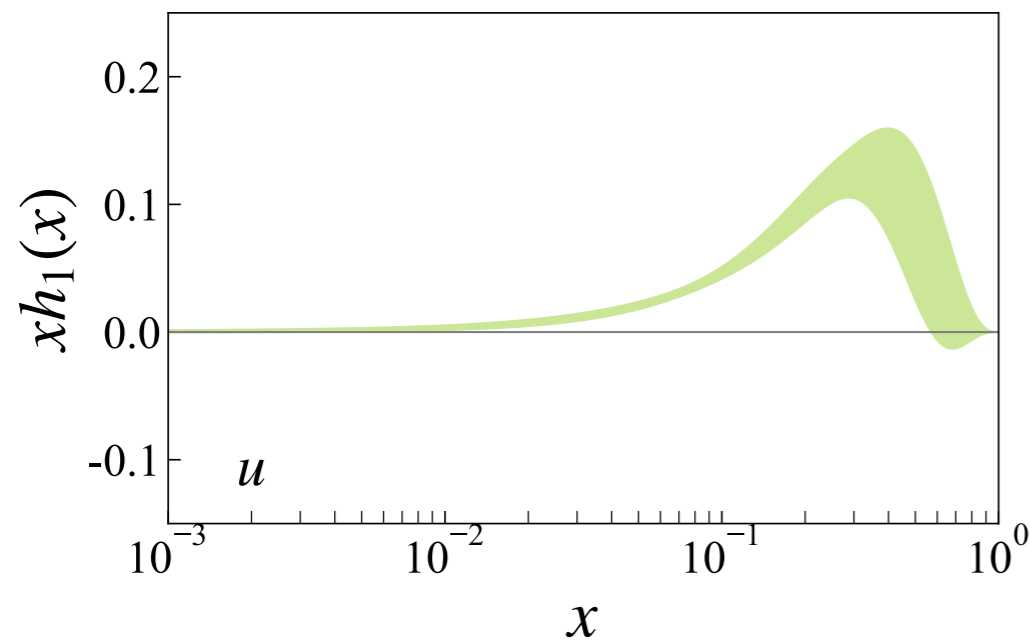
transverse single spin asymmetry  
(Collins asymmetry)

$$h_1(x, \mathbf{k}_\perp^2) \otimes H_1^\perp(z, \mathbf{p}_\perp^2)$$



JAM Collaboration, PRD 104, 034014 (2022).

# Sea Quark Transversity

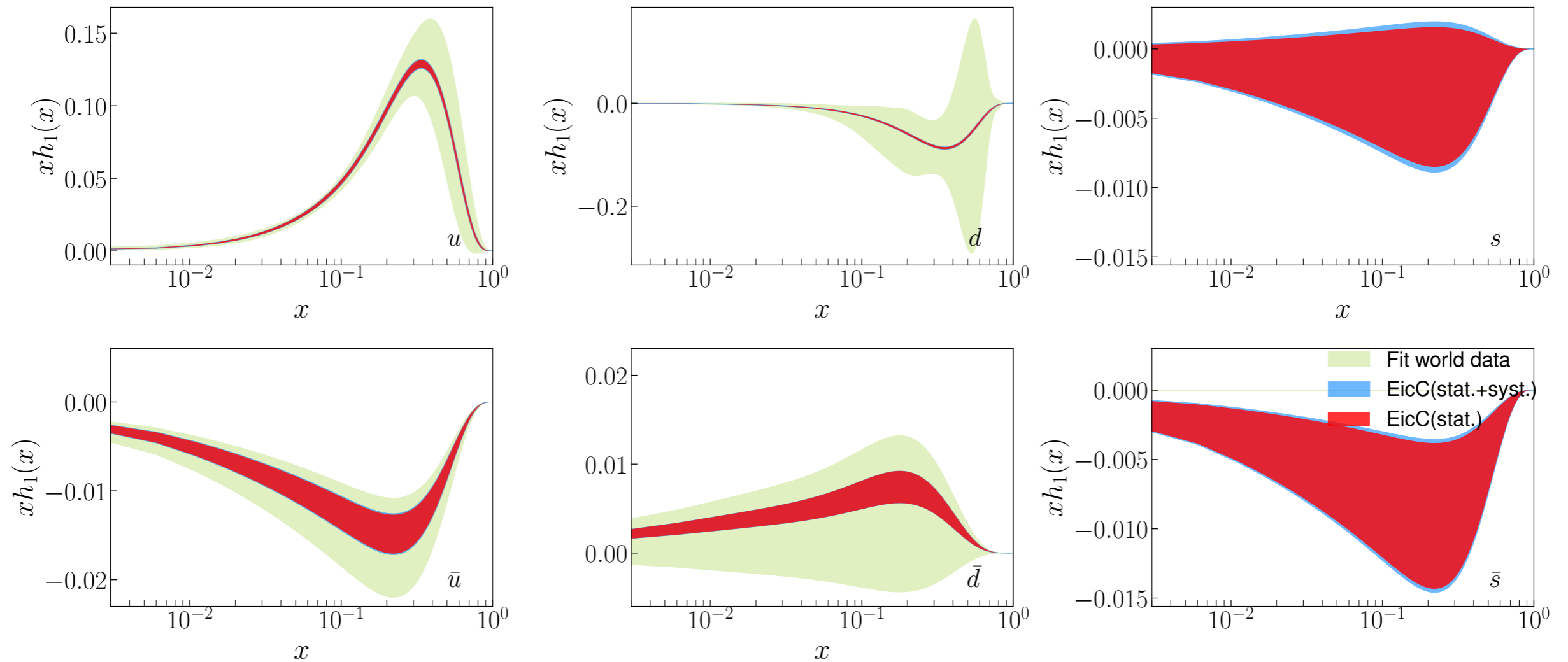


Anti-u quark favors negative distribution

Anti-d quark consistent with zero with current precision

C. Zeng, H. Dong, TL, P. Sun, Y. Zhao, PRD 109 (2024) 056002.

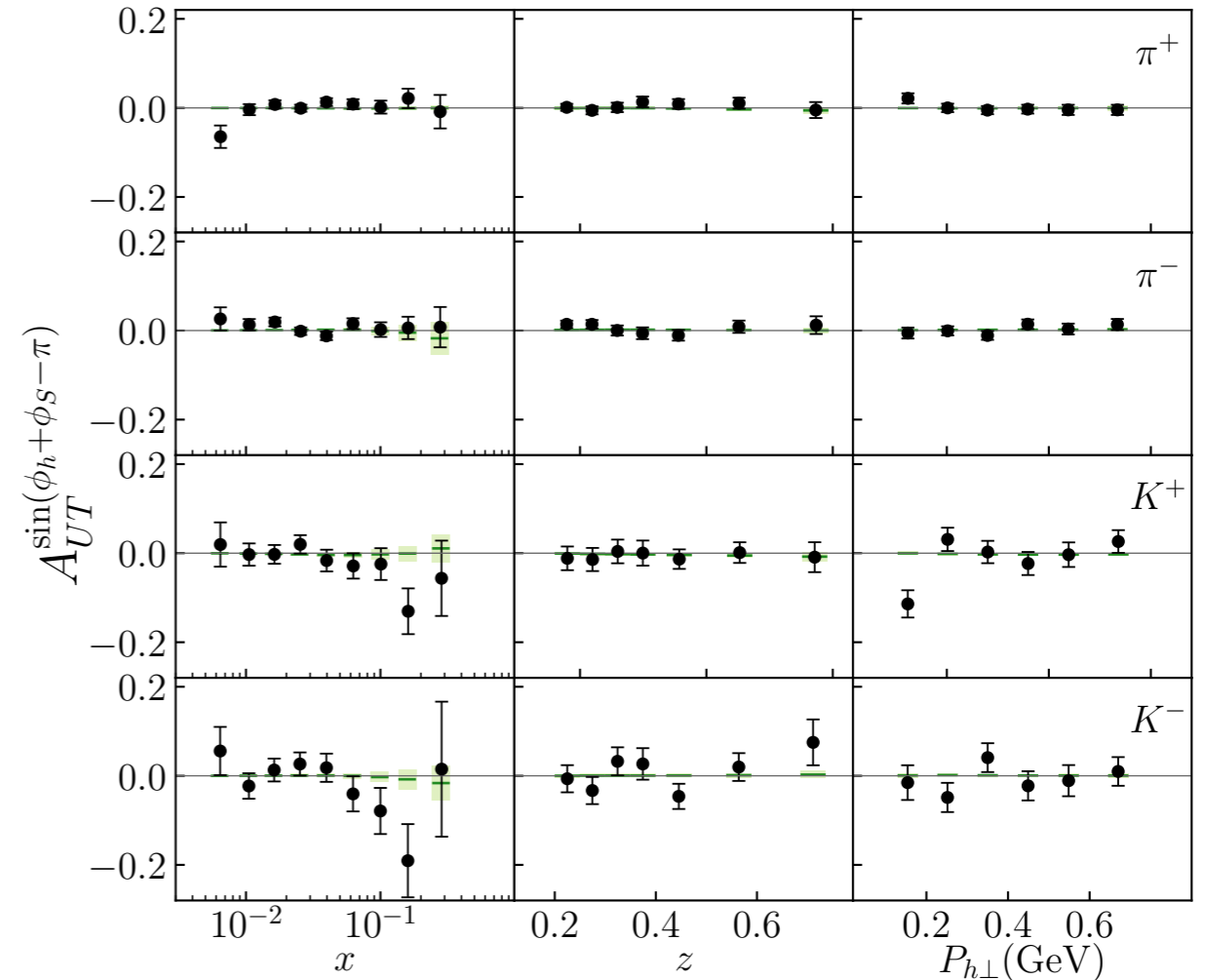
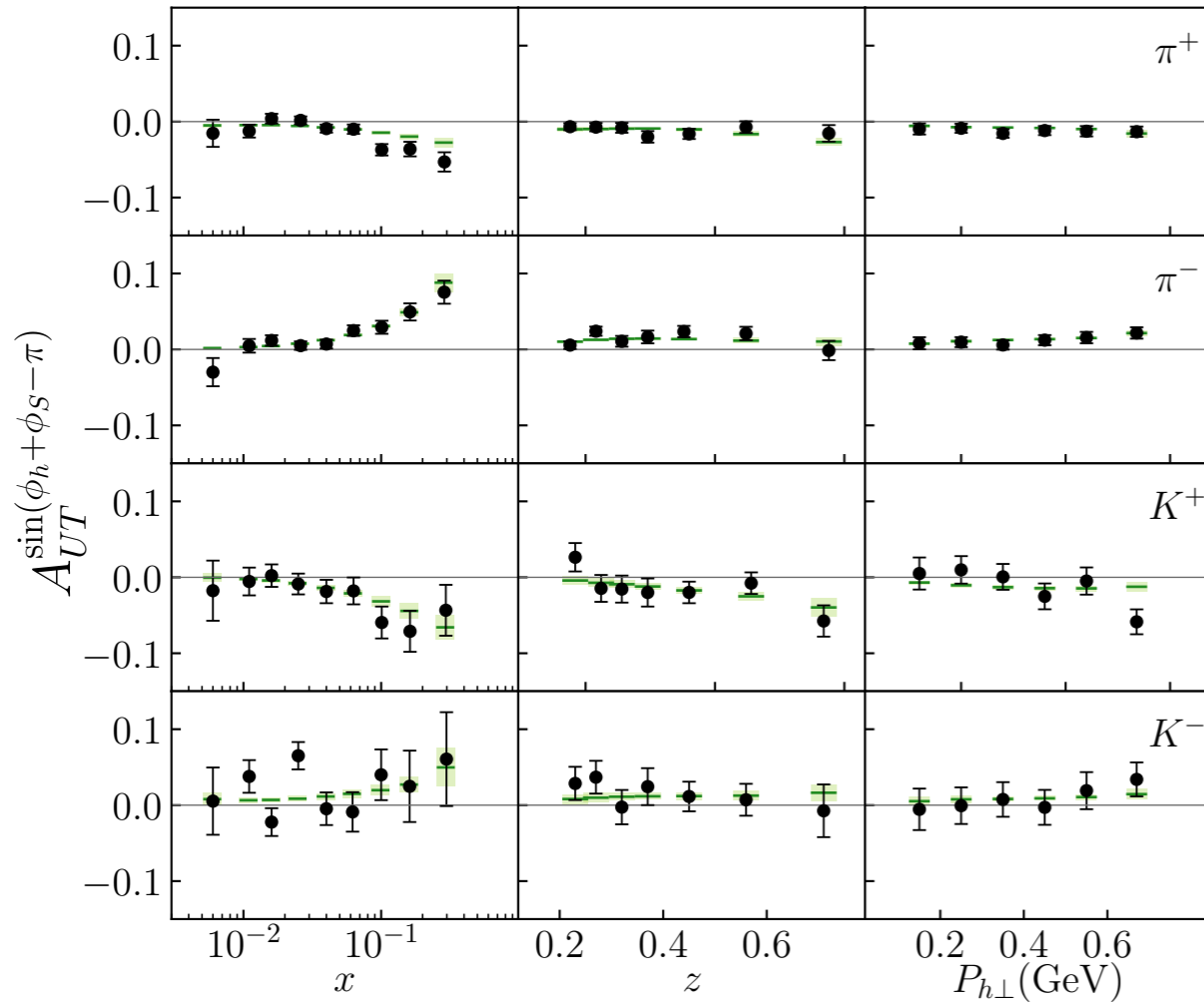
# EicC Impact on Transversity



EicC can significantly improve the precision of transversity distributions, especially for sea quarks.

C. Zeng, H. Dong, TL, P. Sun, Y. Zhao, PRD 109 (2024) 056002.

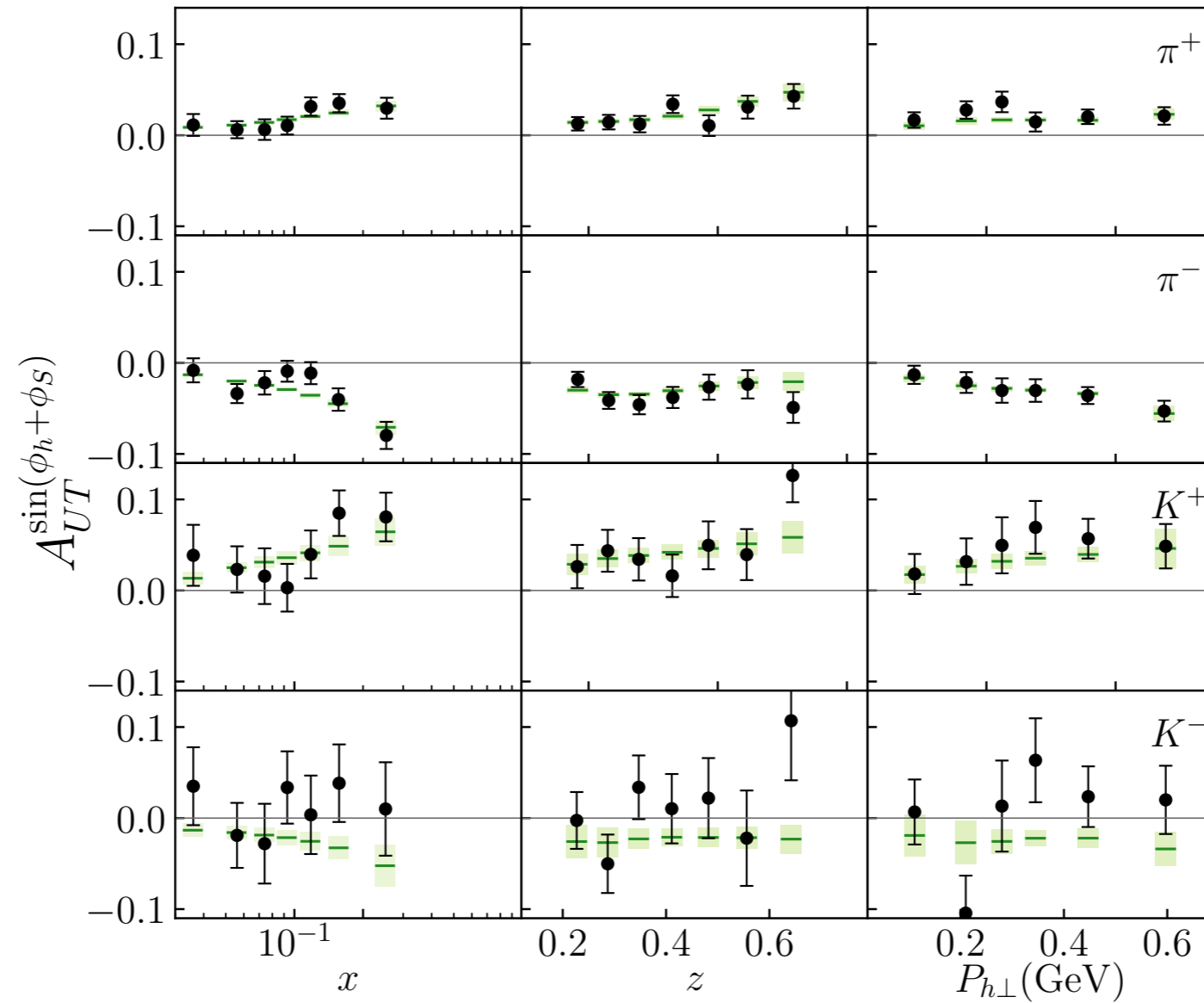
# Comparison with Data



COMPASS Collaboration, Phys. Lett. B 673 (2009) 127; Phys. Lett. B 744 (2015) 250.

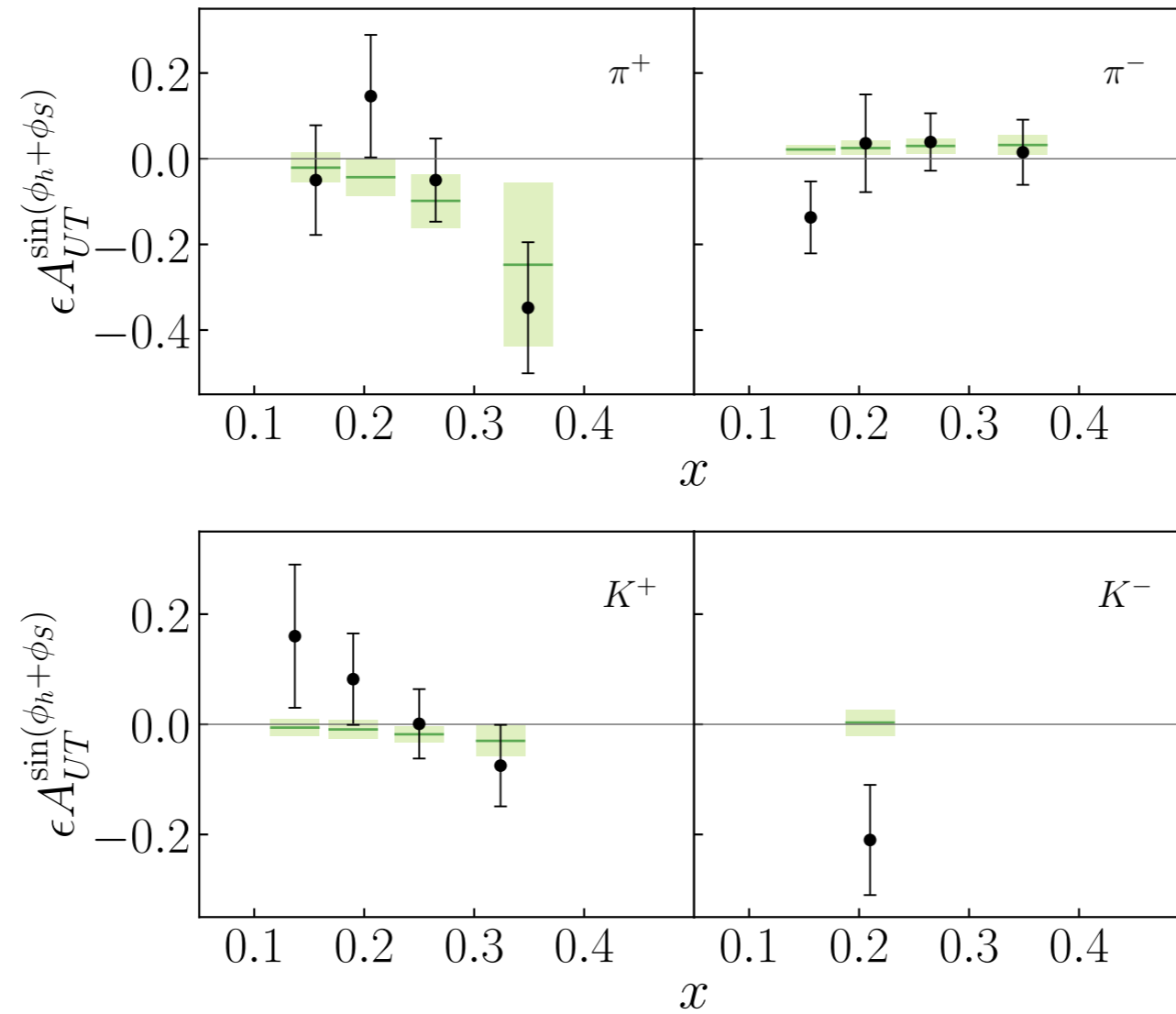


# Comparison with Data



HERMES Collaboration, J. High Energy Phys. 12 (2020) 010. (re-analyzed)

# Comparison with Data



JLab HallA Collaboration, Phys. Rev. Lett. (2011) 072003; Phys. Rev. C 90 (2014) 055201.

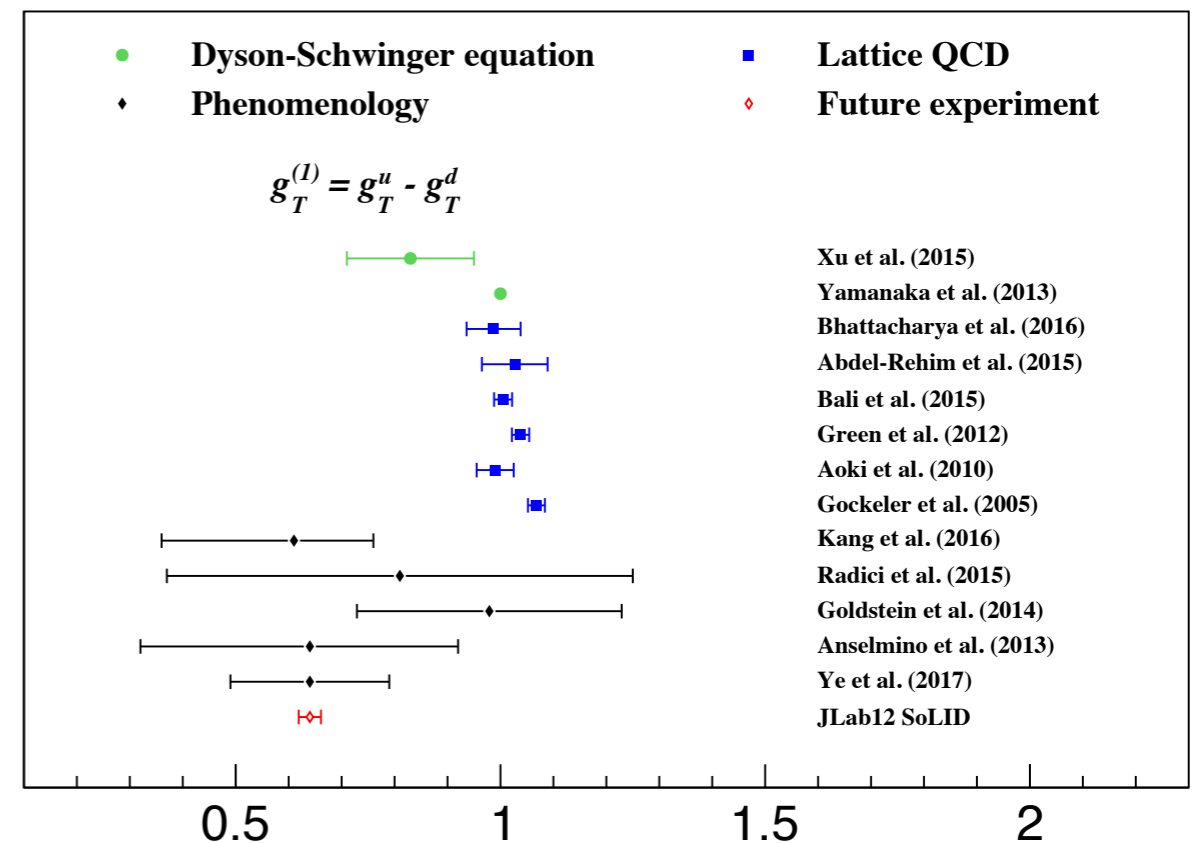
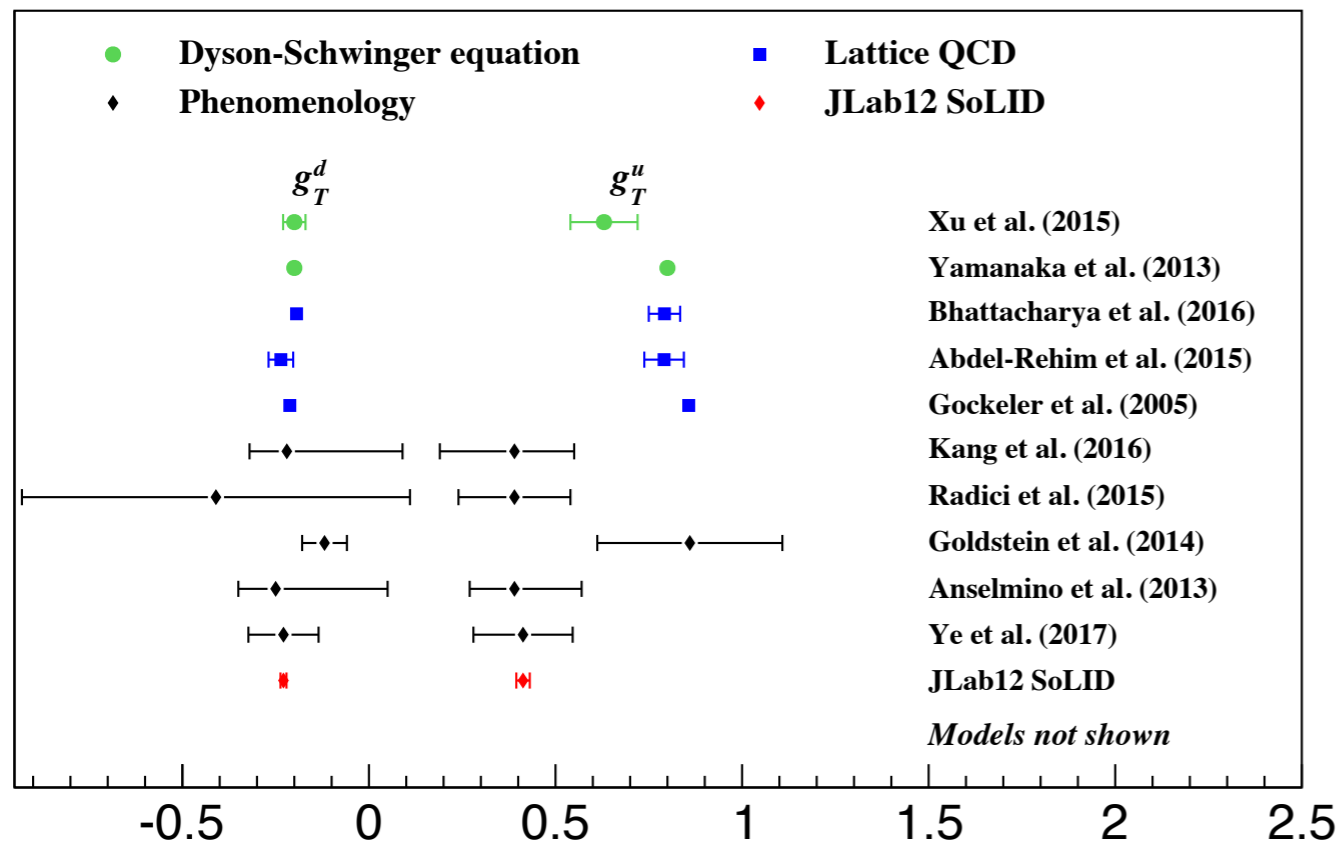
# Tensor Charge

## Tensor charge

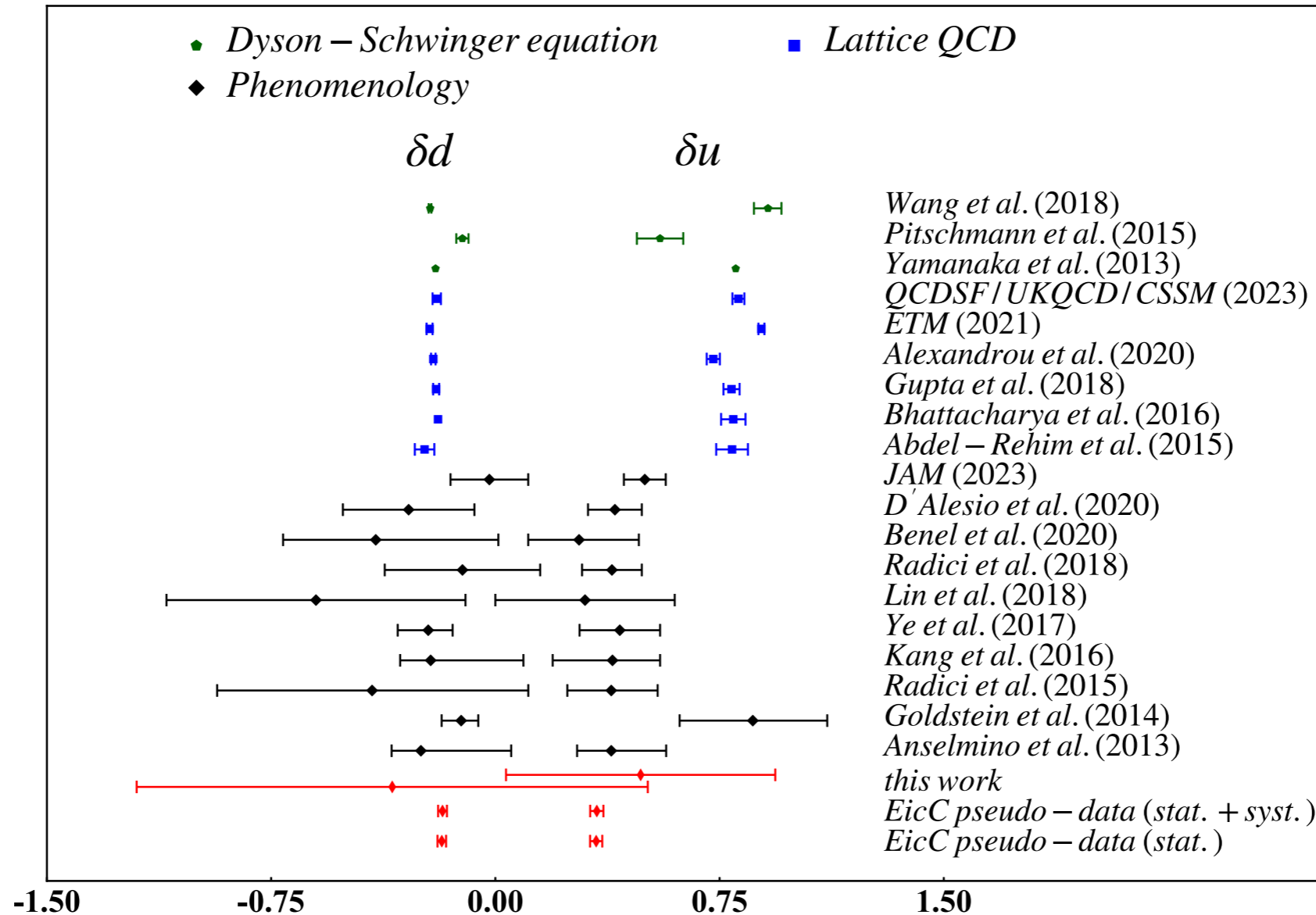
$$\langle P, S | \bar{\psi}^q i\sigma^{\mu\nu} \gamma_5 \psi^q | P, S \rangle = g_T^q \bar{u}(P, S) i\sigma^{\mu\nu} \gamma_5 u(P, S)$$

$$g_T^q = \int_0^1 [h_1^q(x) - h_1^{\bar{q}}(x)] dx$$

- A fundamental QCD quantity: matrix element of local operators.
- Moment of the transversity distribution: valence quark dominant.
- Calculable in lattice QCD.



# Tensor Charge

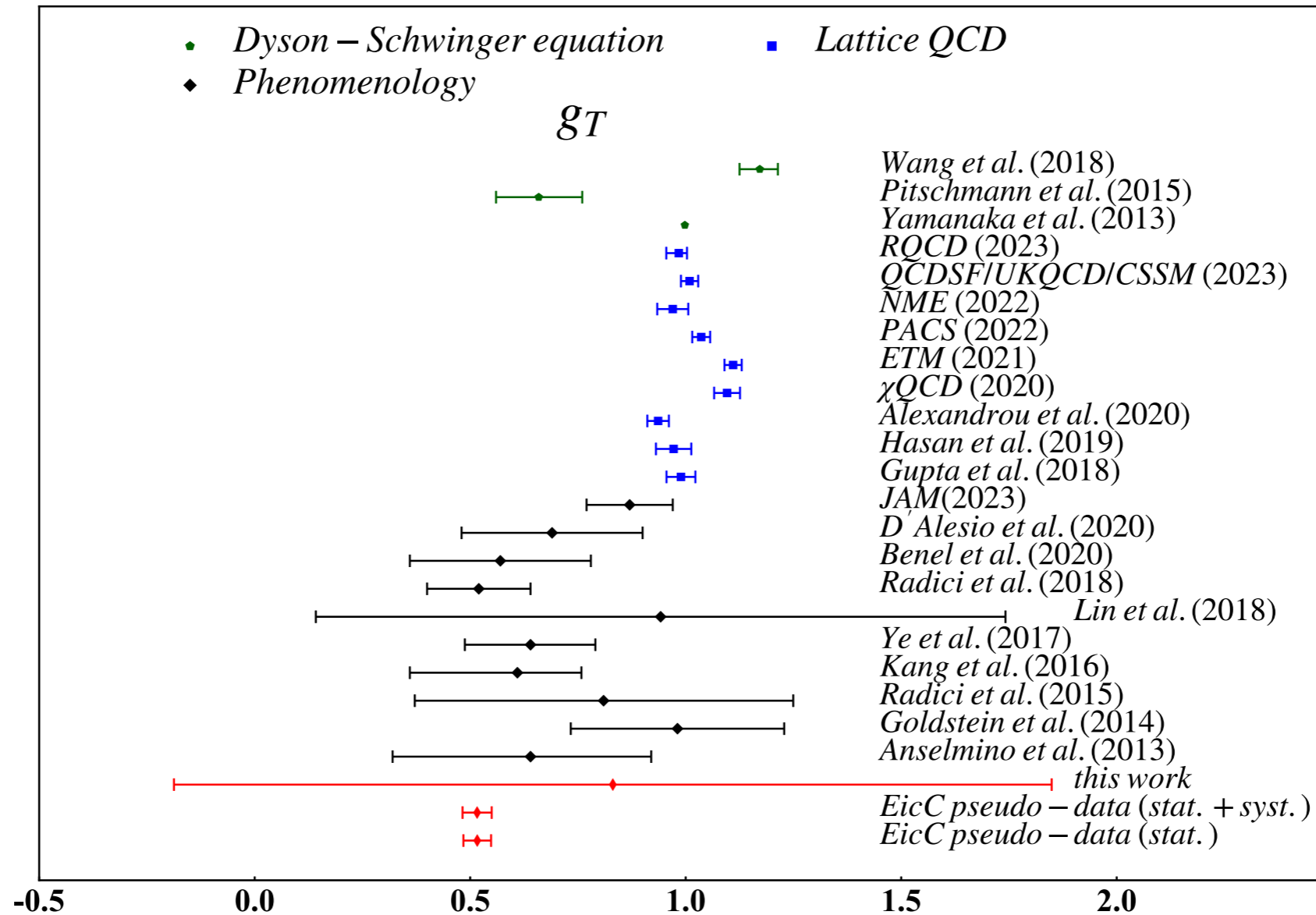


Larger uncertainties when including anti-quarks (less biased)  
 Compatible with lattice QCD calculations

C. Zeng, H. Dong, TL, P. Sun, Y. Zhao, PRD 109 (2024) 056002.



# Tensor Charge



Larger uncertainties when including anti-quarks (less biased)  
 Compatible with lattice QCD calculations

C. Zeng, H. Dong, TL, P. Sun, Y. Zhao, PRD 109 (2024) 056002.

# Double Spin Asymmetry and Worm-gear

## Trans-helicity worm-gear distribution

$$g_{1T}^\perp(x, k_T) \quad \begin{array}{c} \uparrow \\ \circ \rightarrow \\ \uparrow \end{array} - \begin{array}{c} \uparrow \\ \circ \leftarrow \\ \uparrow \end{array}$$

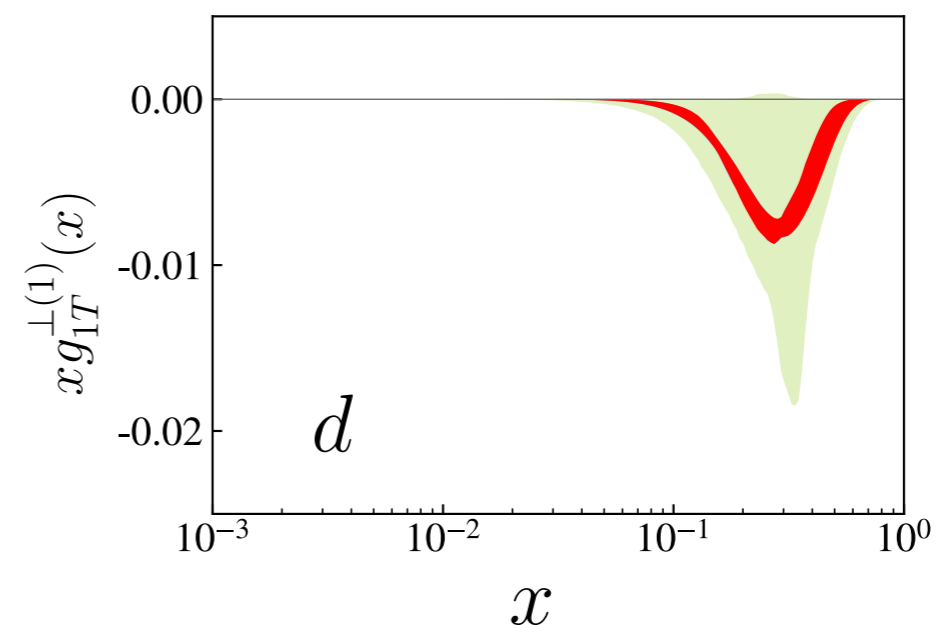
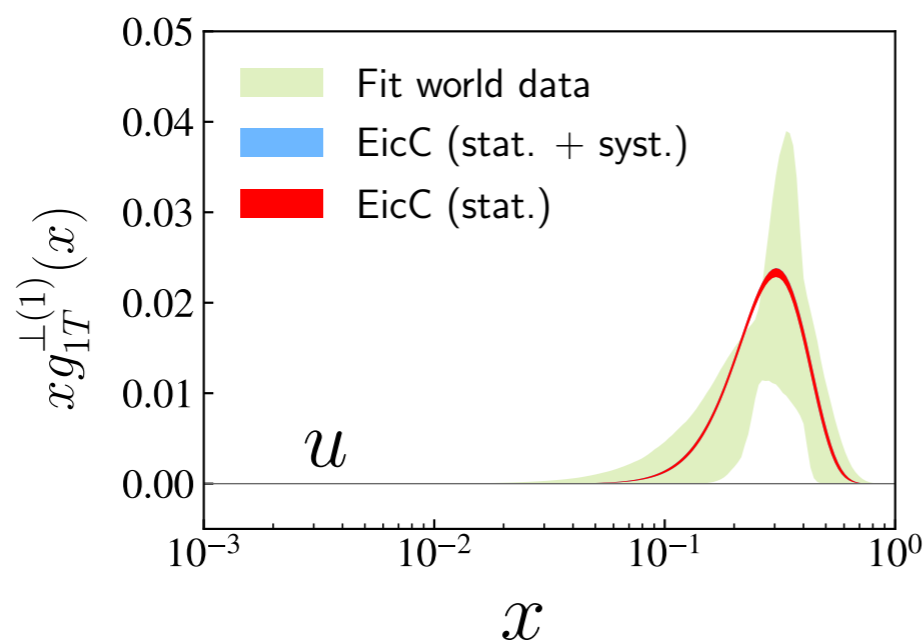
- Longitudinally polarized quark density in a transversely polarized nucleon
- Overlap between wave functions differing by one unit of orbital angular momentum

### Effect in SIDIS:

A longitudinal-transverse double spin asymmetry

$$A_{LT}^{\cos(\phi_h - \phi_s)} \sim g_{1T}^\perp \otimes D_1$$

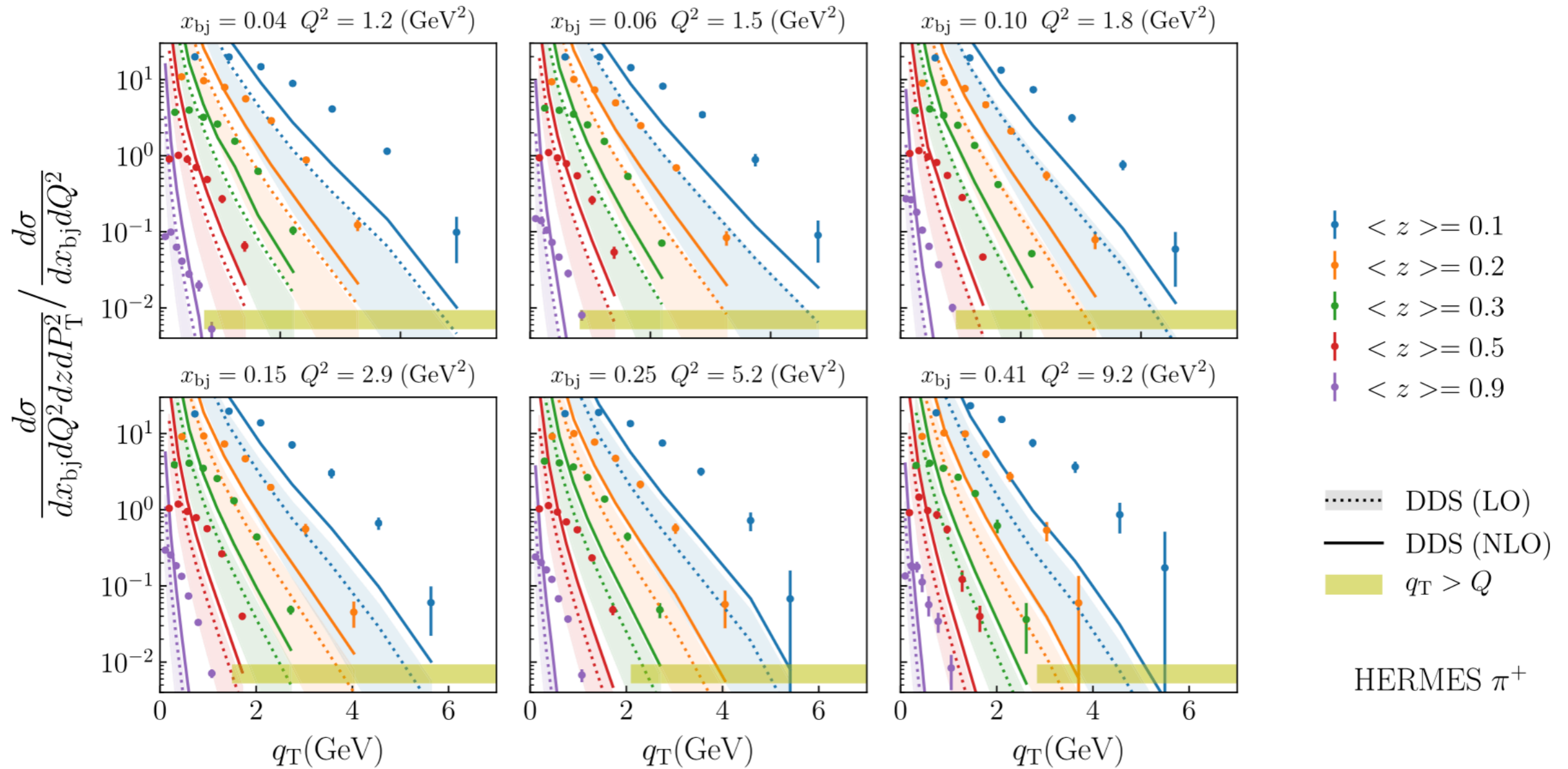
## Phenomenological extraction



K. Yang, TL, P. Sun, Y. Zhao, B.-Q. Ma, arXiv:2403.12795

*The story is not ending ...*

# Challenge at Large Transverse Momentum



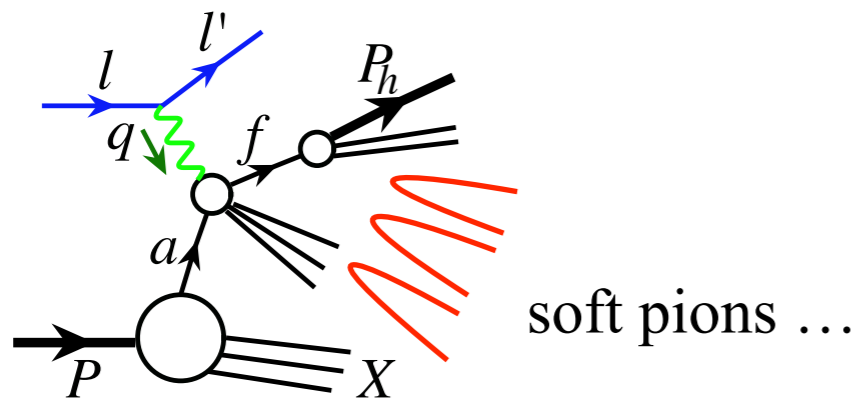
J.O. Gonzalez-Hernandez, T.C. Rogers, N. Sato, B. Wang, Phys. Rev. D 98 114005 (2018).





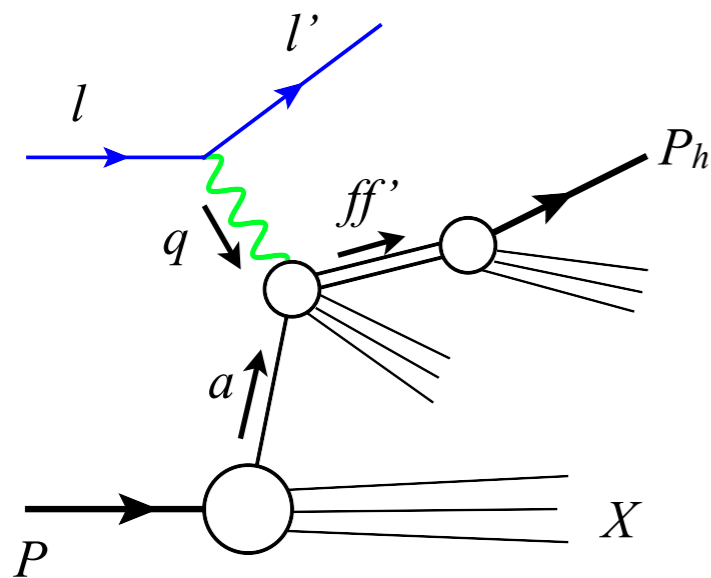
# Challenge at Large Transverse Momentum

Our proposal: power correction



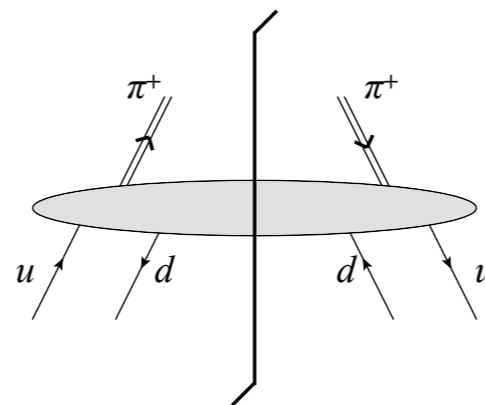
Need large enough phase space to shower  
 $\Rightarrow$  sufficiently high multiplicity

Near the edge of phase space: large  $P_{hT}$  or  $z_h$   
 $\Rightarrow$  low multiplicity



## NLP contribution:

Hard part is formally suppressed by  $1/Q^2$  or  $1/P_{hT}^2$   
 Its contribution is not necessarily small,  
 if it gets enhancement from hadronization



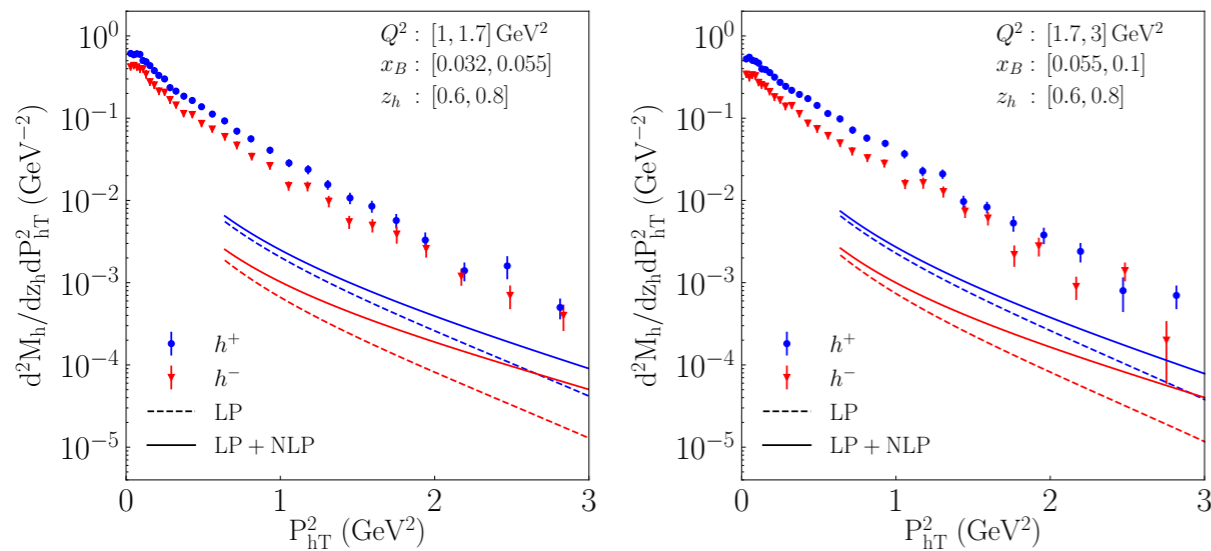
*Parton pair with the right quantum number  
 has better chance to form the hadron.*

TL and J.W. Qiu, 2020

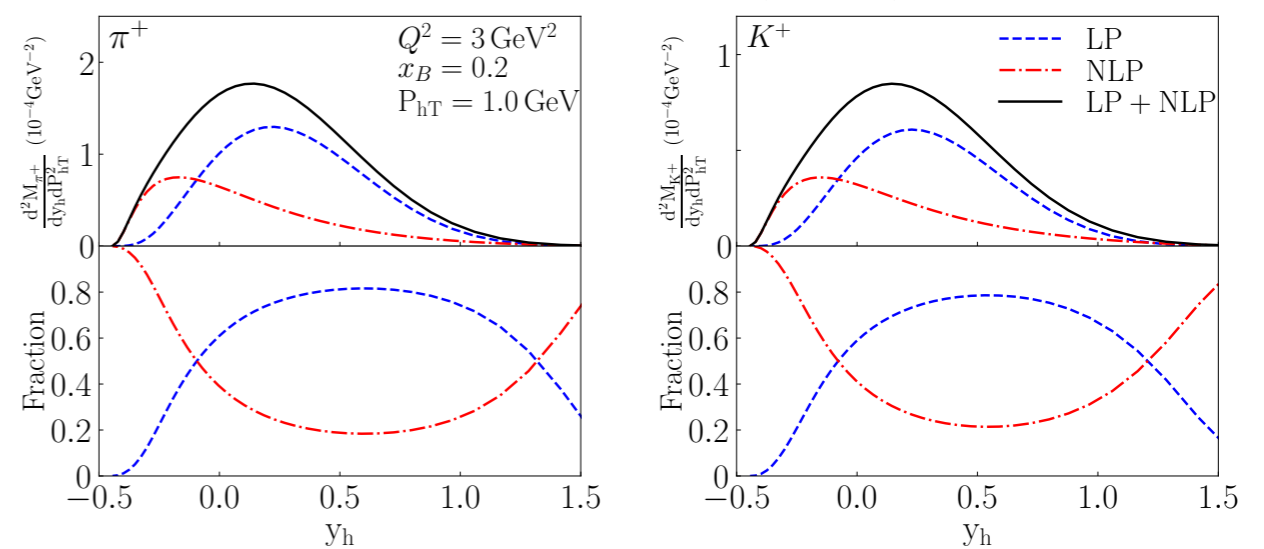
# Challenge at Large Transverse Momentum

## Numerical estimation

$E_{\text{beam}} = 160 \text{ GeV}$  (COMPASS)



$E_{\text{beam}} = 11 \text{ GeV}$  (JLab)



Only consider the leading term — *lower limit of NLP contribution*.  
NLP contribution is more significant at lower collision energy.

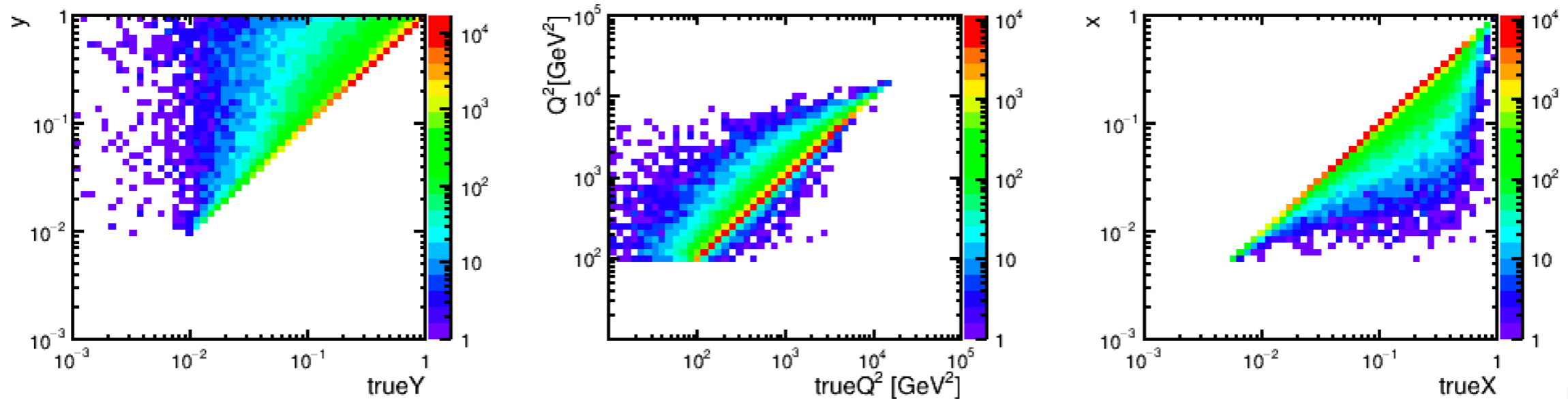
## Evolution should be modified accordingly

$$\frac{\partial}{\partial \ln \mu^2} D_{[ff'(\kappa)] \rightarrow h} = \sum_{[\tilde{f}\tilde{f}'(\kappa)']} D_{[\tilde{f}\tilde{f}'(\kappa')] \rightarrow h} \otimes \Gamma_{[ff'(\kappa)] \rightarrow [\tilde{f}\tilde{f}'(\kappa)]}$$

$$\frac{\partial}{\partial \ln \mu^2} D_{f \rightarrow h} = \sum_{f'} D_{f' \rightarrow h} \otimes \gamma_{f \rightarrow f'} + \frac{1}{\mu^2} \sum_{[ff'(\kappa)]} D_{[ff'(\kappa)] \rightarrow h} \otimes \tilde{\gamma}_{f \rightarrow [ff'(\kappa)]}$$

TL and J.W. Qiu, 2020

# Radiative Corrections



[Figures from X. Chu at 2nd EIC YR workshop]

*kinematic experienced by the parton*  $\neq$  *kinematic reconstructed from observed momenta*

## Challenges in traditional approach:

- The determination of the RC factor usually relies on MC simulation, requiring the physics we want to extract or beyond the experimental acceptance.
- The extraction of the Born cross section is an inverse problem.
- Increasingly difficult for reactions beyond inclusive DIS, e.g. SIDIS.

*“In many nuclear physics experiments, radiative corrections quickly become a dominant source of systematics. In fact, the uncertainty on the corrections might be the dominant source for high-statistics experiment”*

*— EIC Yellow Report*

# Radiative Corrections

## Our proposal:

- Do not try to invent any scheme to treat QED radiation to match Born kinematics.  
— No radiative correction!
- Generalize the QCD factorization to include electroweak theory, treat QED radiation in the same way as QCD radiation is treated.
- Same systematically improvable treatment of QED contributions for both inclusive DIS and SIDIS.

## From radiative correction to radiation contribution:

$$\sigma_{\text{Measured}}(x_B, Q^2) = \sigma_{\text{lep}}^{\text{univ}}(\mu^2; m_e^2) \otimes \sigma_{\text{had}}^{\text{univ}}(\mu^2; \Lambda_{\text{QCD}}^2) \otimes \hat{\sigma}_{\text{IR-safe}}(\hat{x}_B, \hat{Q}^2, \mu^2) + \mathcal{O}\left(\frac{\Lambda_{\text{QCD}}^2}{Q^2}, \frac{m_e^2}{Q^2}\right)$$

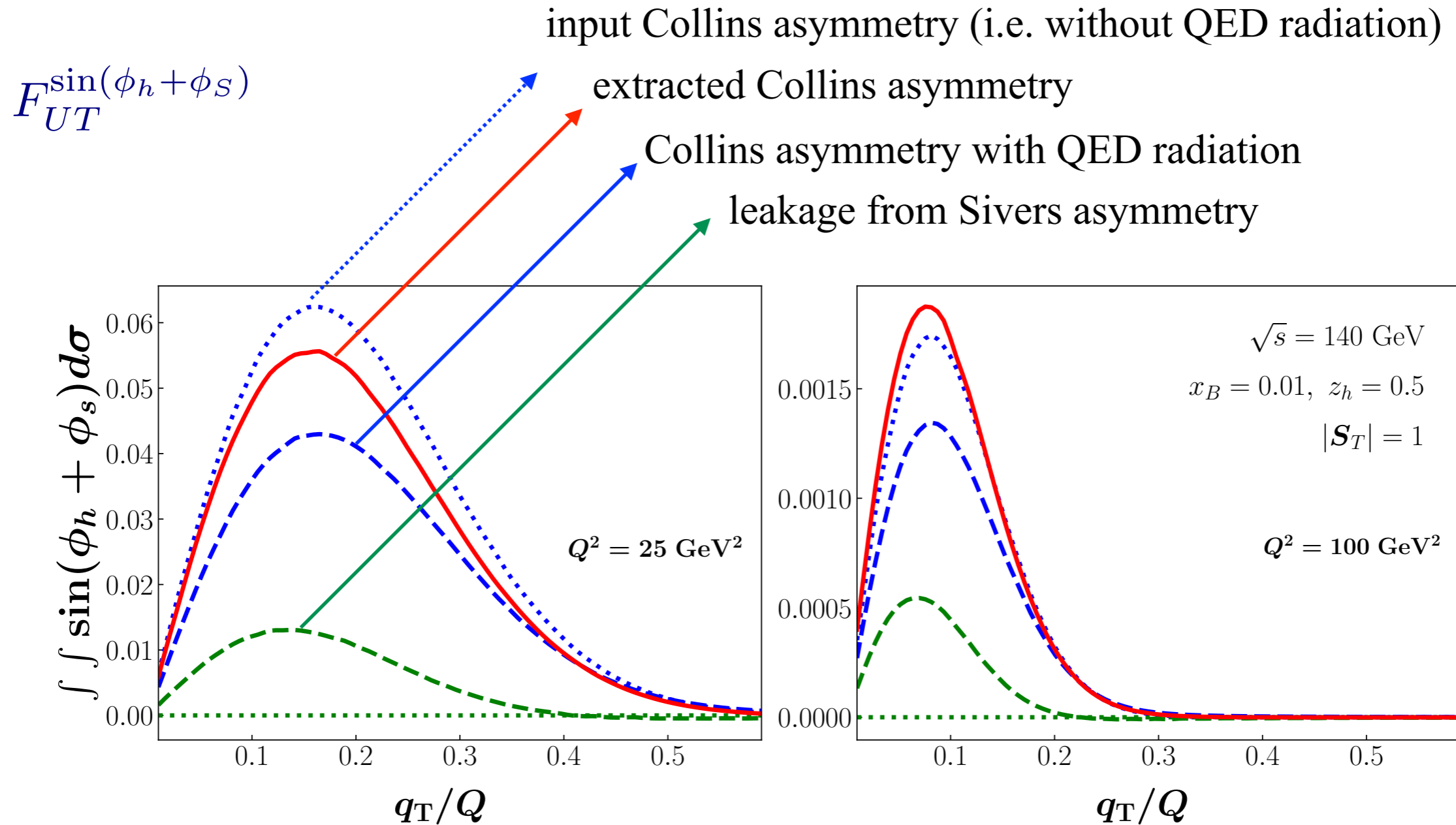
- IR sensitive QED contributions are absorbed into LDF and LFF.
- IR safe QED contributions are calculated order-by-order in power of  $\alpha$ .
- Neglect power suppressed contributions.

TL, W. Melnitchouk, J.W. Qiu, N. Sato, 2021



# Radiative Correction

Numerical estimation: Collins asymmetry



TL, W. Melnitchouk, J.W. Qiu, N. Sato, 2021

# Summary

- Spin always surprises since its discovery nearly 100 years ago
- Nucleon spin structure is still not well understood
- Rich information is contained in TMDs
  - quark transverse momentum distorted by nucleon spin;
  - correlation between quark longitudinal/transverse spin and nucleon spin;
  - ...
- SIDIS with polarized beam and target is a main process to study polarized TMDs
- Also an important approach to test/develop the theories/models
- EicC can significantly improve the precision of the determination of TMDs, especially for sea quarks, complementary to JLab12 and EIC-US.
- There are still challenges on the theoretical side
  - power corrections, higher twist effects
  - radiative corrections
  - target fragmentation
  - ...

*Thank you!*

*Backup*

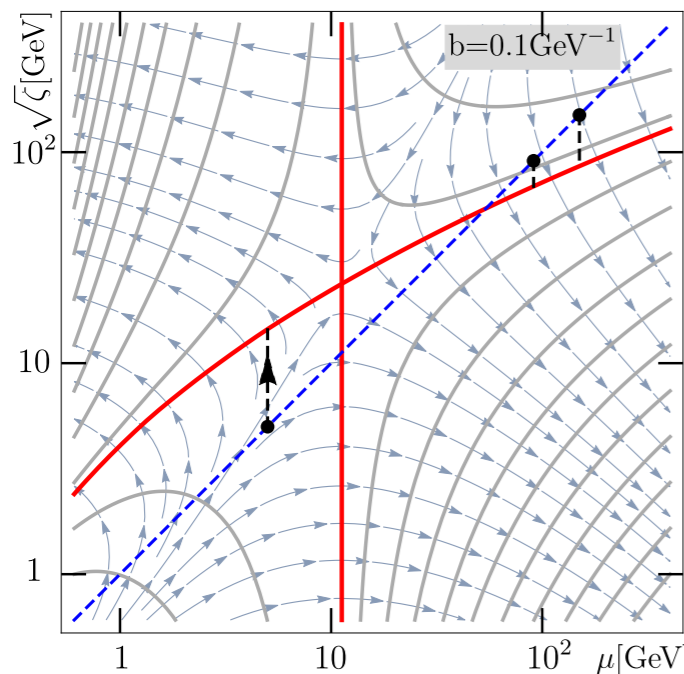
# TMD Evolution

## Evolution equations

$$\begin{aligned} \mu^2 \frac{dF(x, b; \mu, \zeta)}{d\mu^2} &= \frac{\gamma_F(\mu, \zeta)}{2} F(x, b; \mu, \zeta) & -\zeta \frac{d\gamma_F(\mu, \zeta)}{d\zeta} &= \mu \frac{d\mathcal{D}(\mu, b)}{d\mu} = \Gamma_{\text{cusp}}(\mu) \\ \zeta \frac{dF(x, b; \mu, \zeta)}{d\zeta} &= -\mathcal{D}(b, \mu) F(x, b; \mu, \zeta) & \gamma_F(\mu, \zeta) &= \Gamma_{\text{cusp}}(\mu) \ln\left(\frac{\mu^2}{\zeta}\right) - \gamma_V(\mu) \end{aligned}$$

$$F(x, b; \mu_f, \zeta_f) = \exp \left[ \int_P \left( \gamma_F(\mu, \zeta) \frac{d\mu}{\mu} - \mathcal{D}(\mu, b) \frac{d\zeta}{\zeta} \right) \right] F(x, b; \mu_i, \zeta_i)$$

## $\zeta$ -prescription



$$\mu^2 = \zeta = Q^2 \quad R[b; (\mu_i, \zeta_i) \rightarrow (Q, Q^2)] = \left( \frac{Q^2}{\zeta_\mu(Q, b)} \right)^{-\mathcal{D}(Q, b)}$$

$$\frac{d \ln \zeta_\mu(\mu, b)}{d \ln \mu^2} = \frac{\gamma_F(\mu, \zeta_\mu(\mu, b))}{2\mathcal{D}(\mu, b)}$$

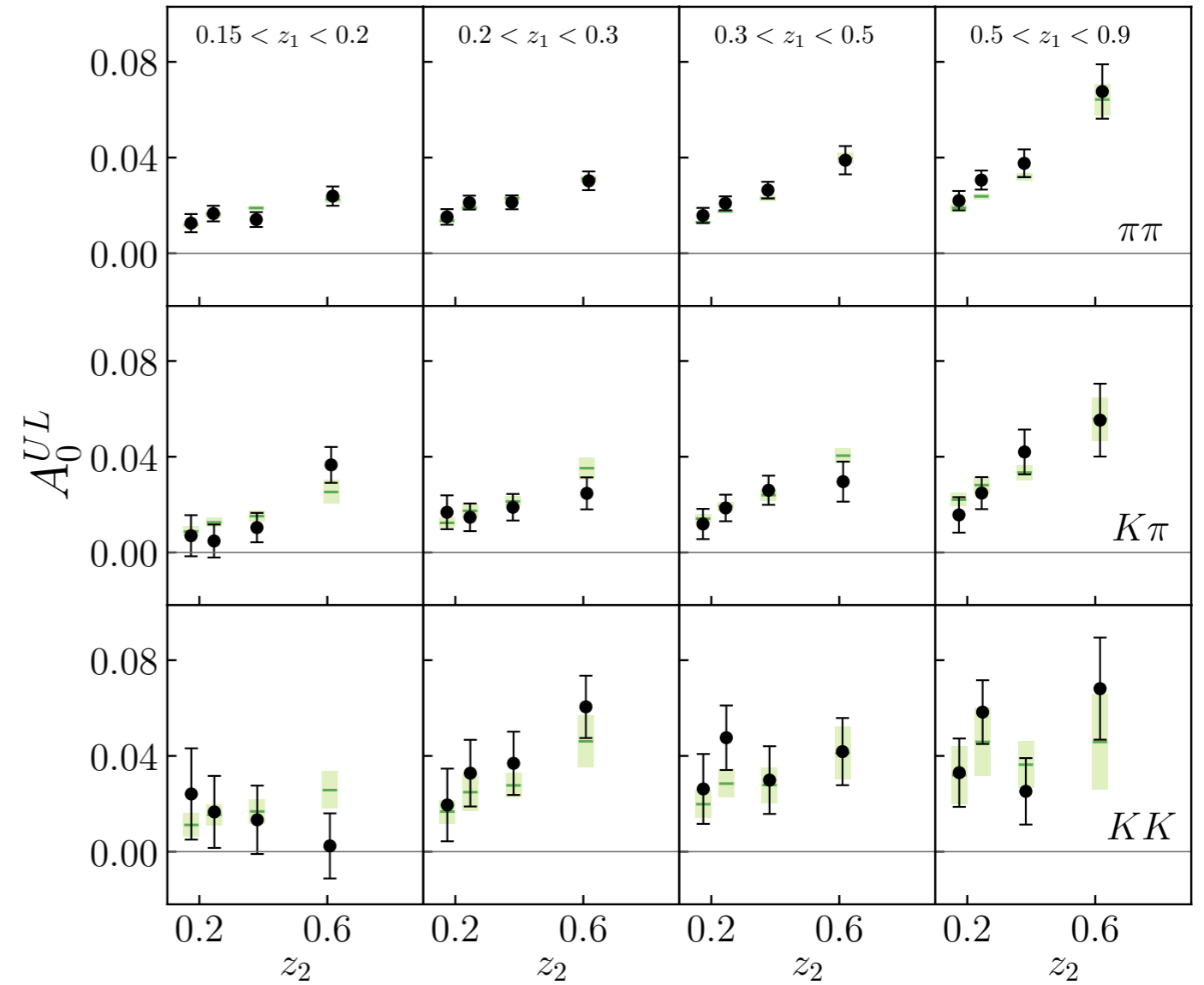
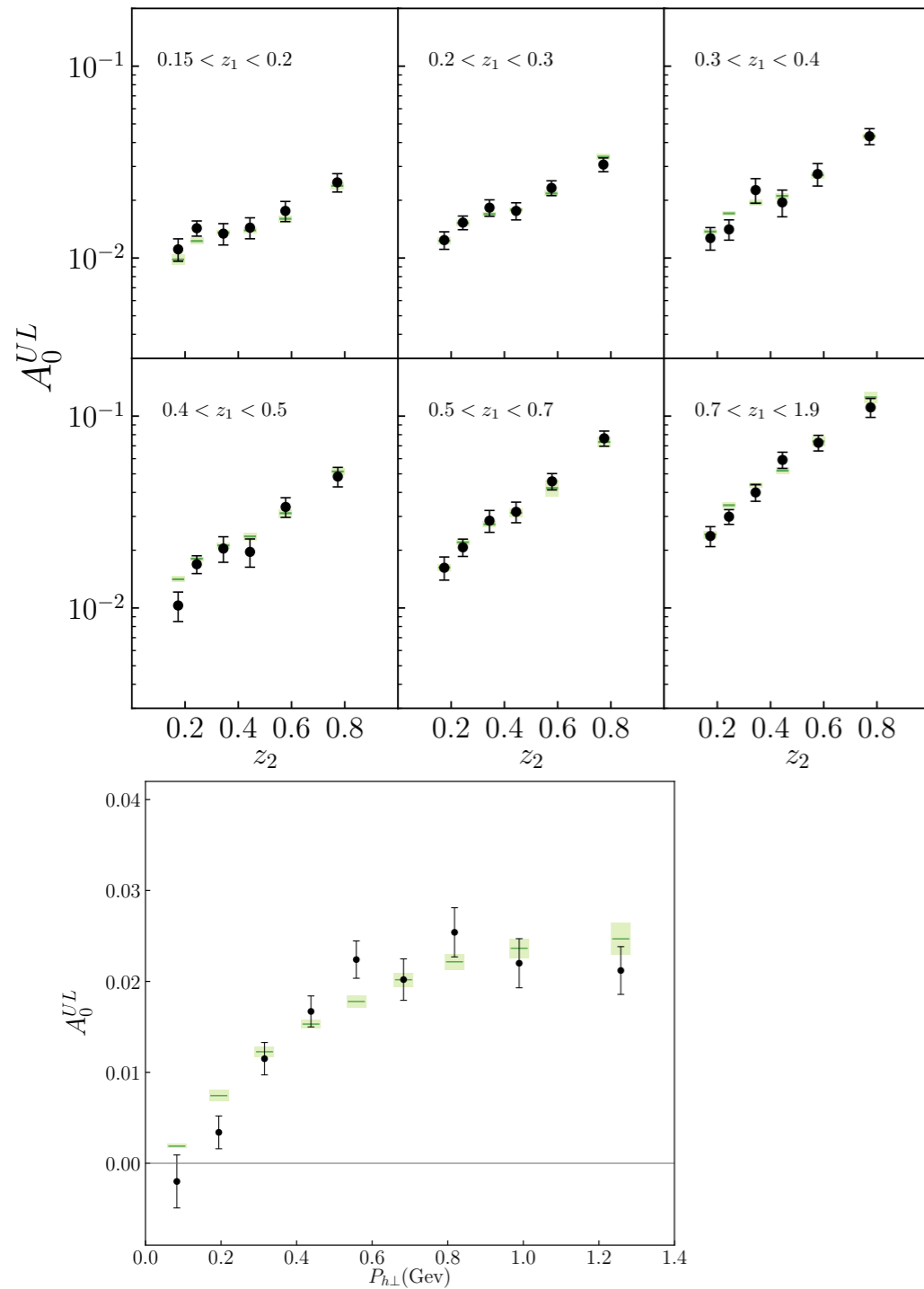
$$\mathcal{D}(\mu_0, b) = 0, \quad \gamma_F(\mu_0, \zeta_\mu(\mu_0, b)) = 0$$

$$F(x, b; Q, Q^2) = \left( \frac{Q^2}{\zeta_Q(b)} \right)^{-\mathcal{D}(b, Q)} F(x, b)$$

# Comparison with Data

BaBar (2014)

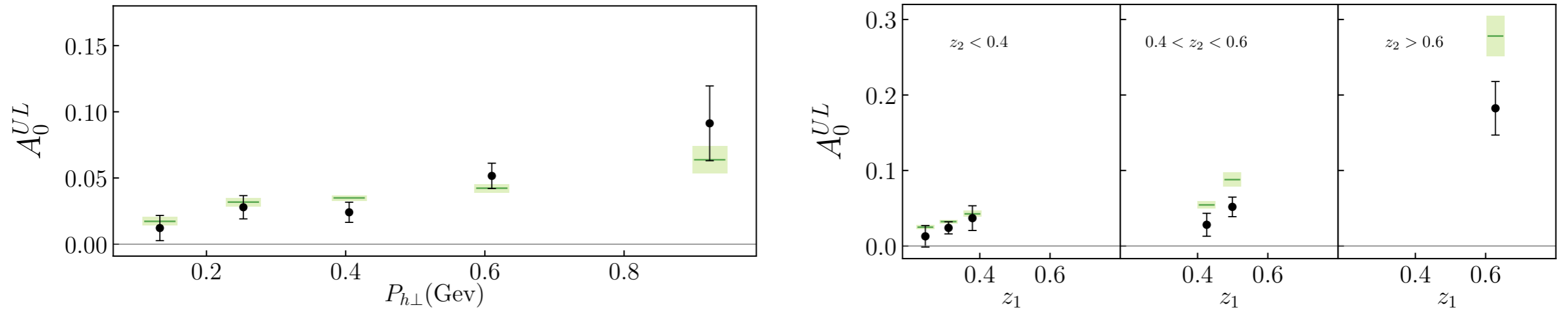
BaBar (2016)



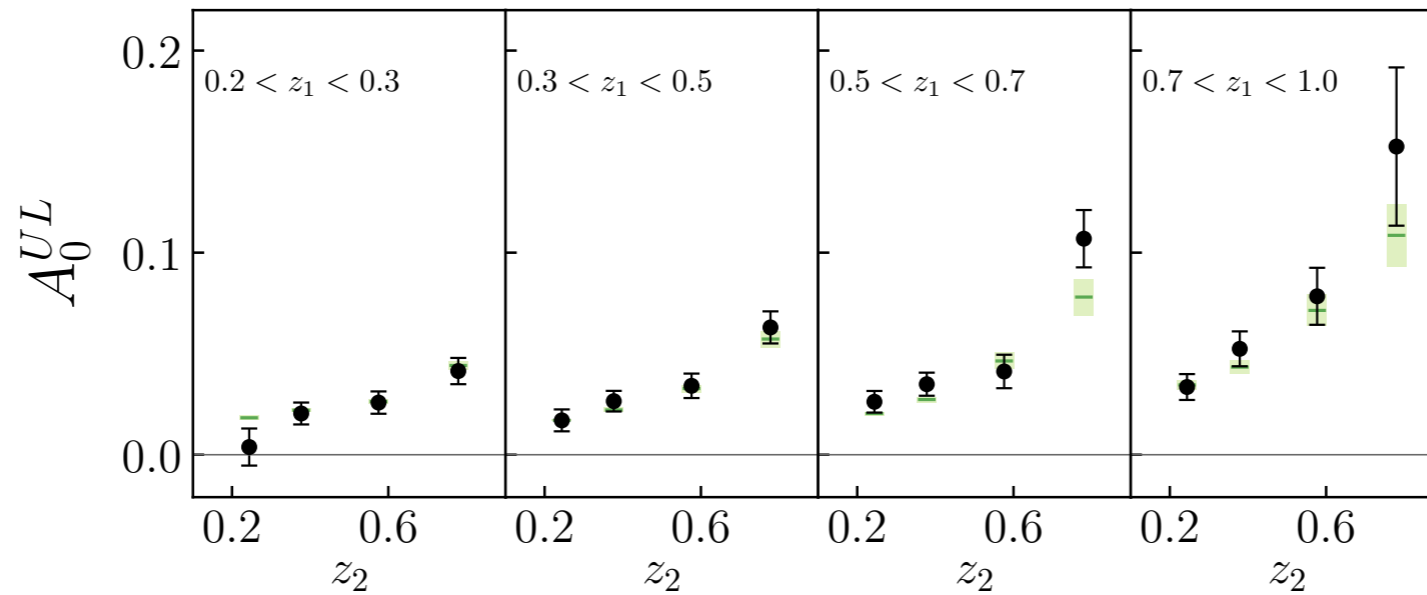


# Comparison with Data

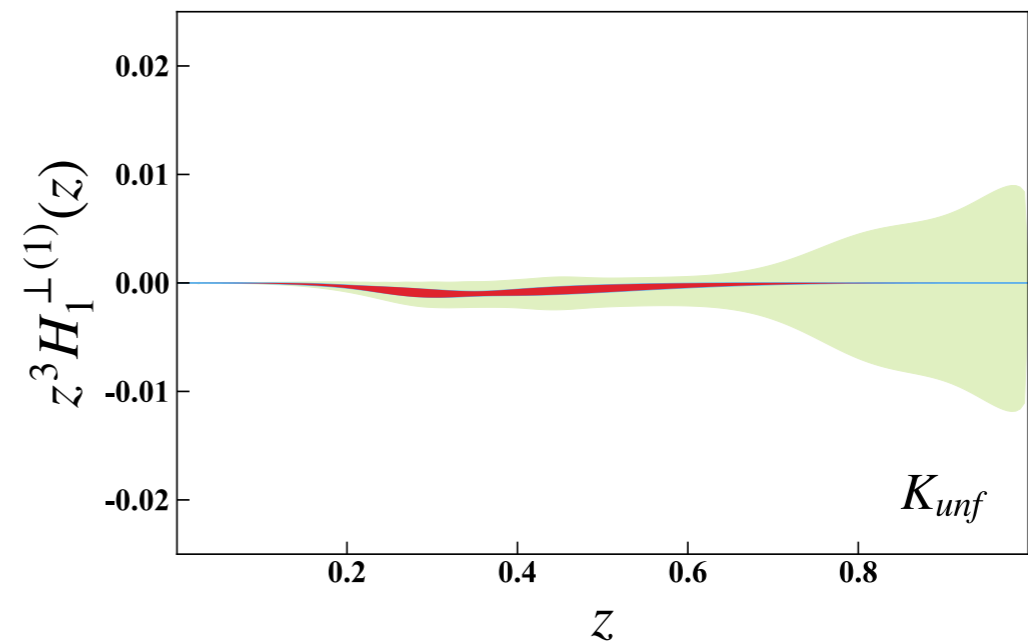
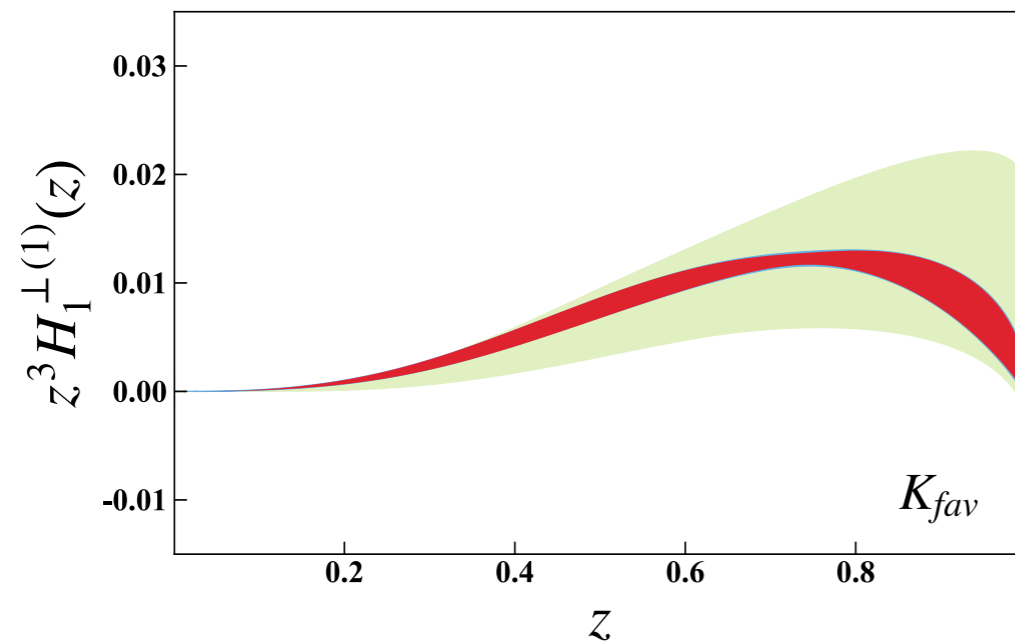
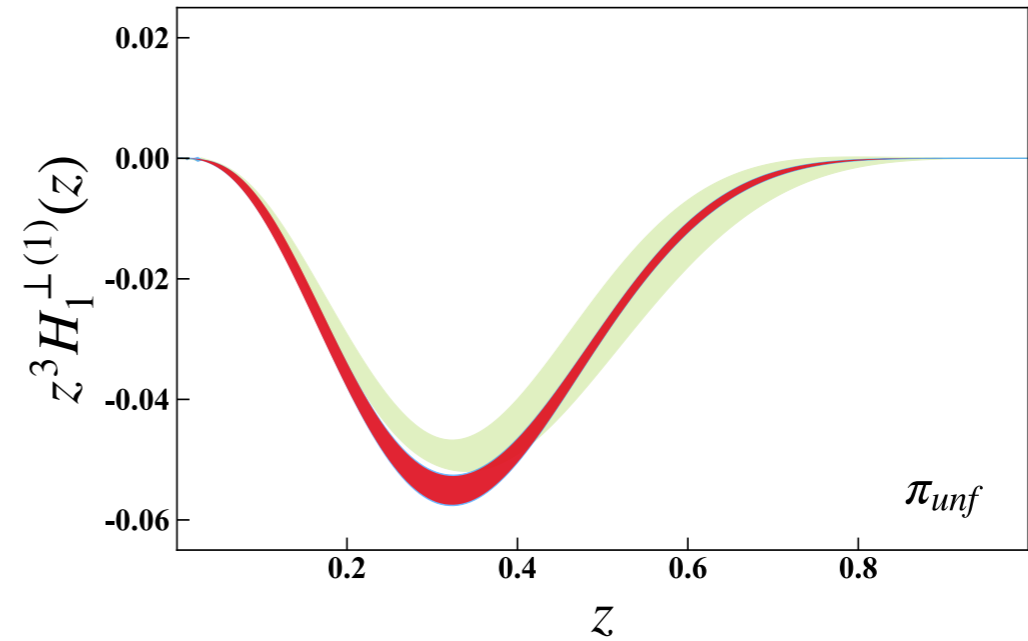
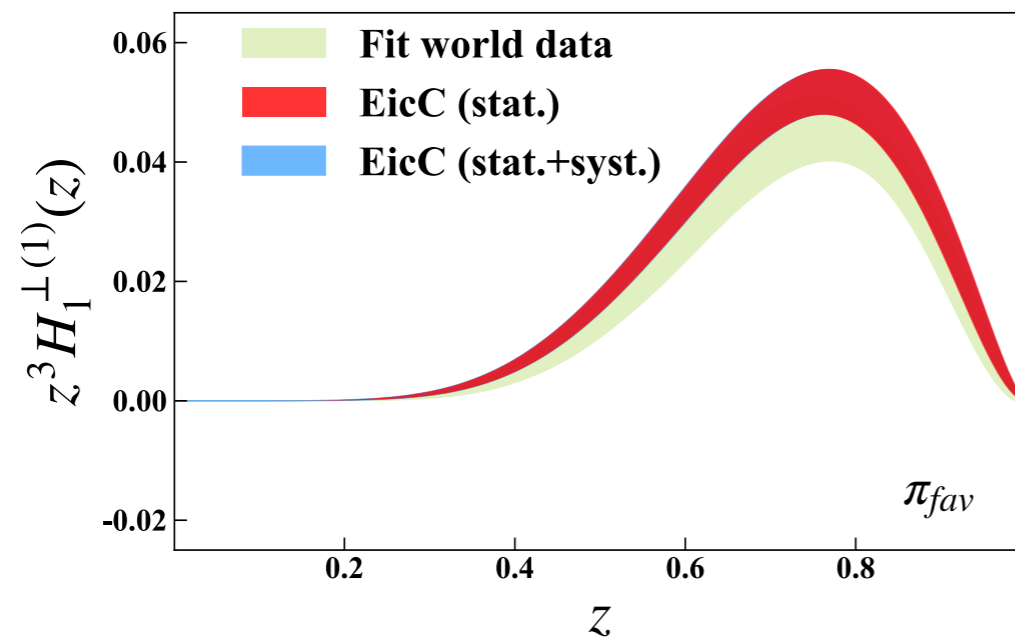
## BESIII



## Belle

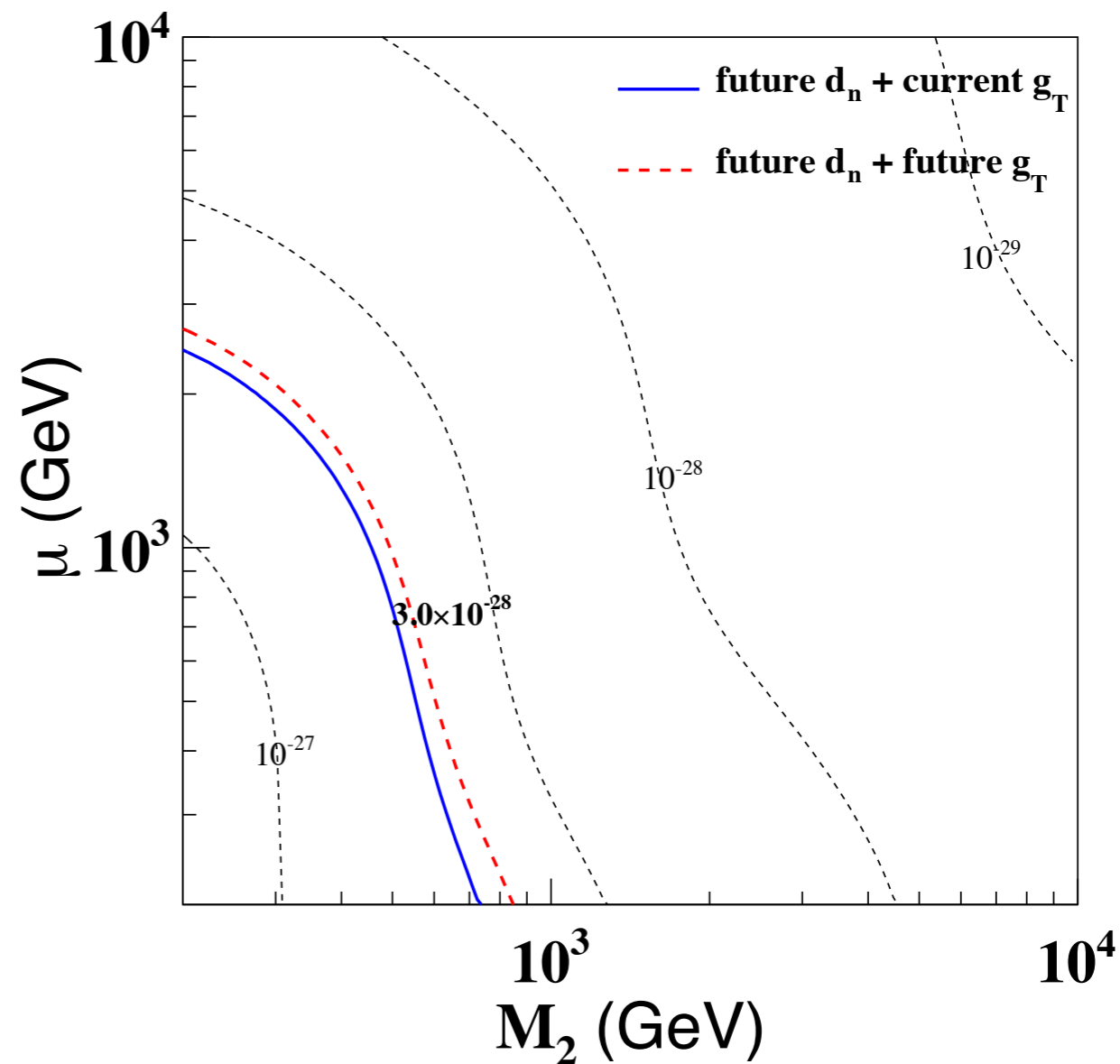
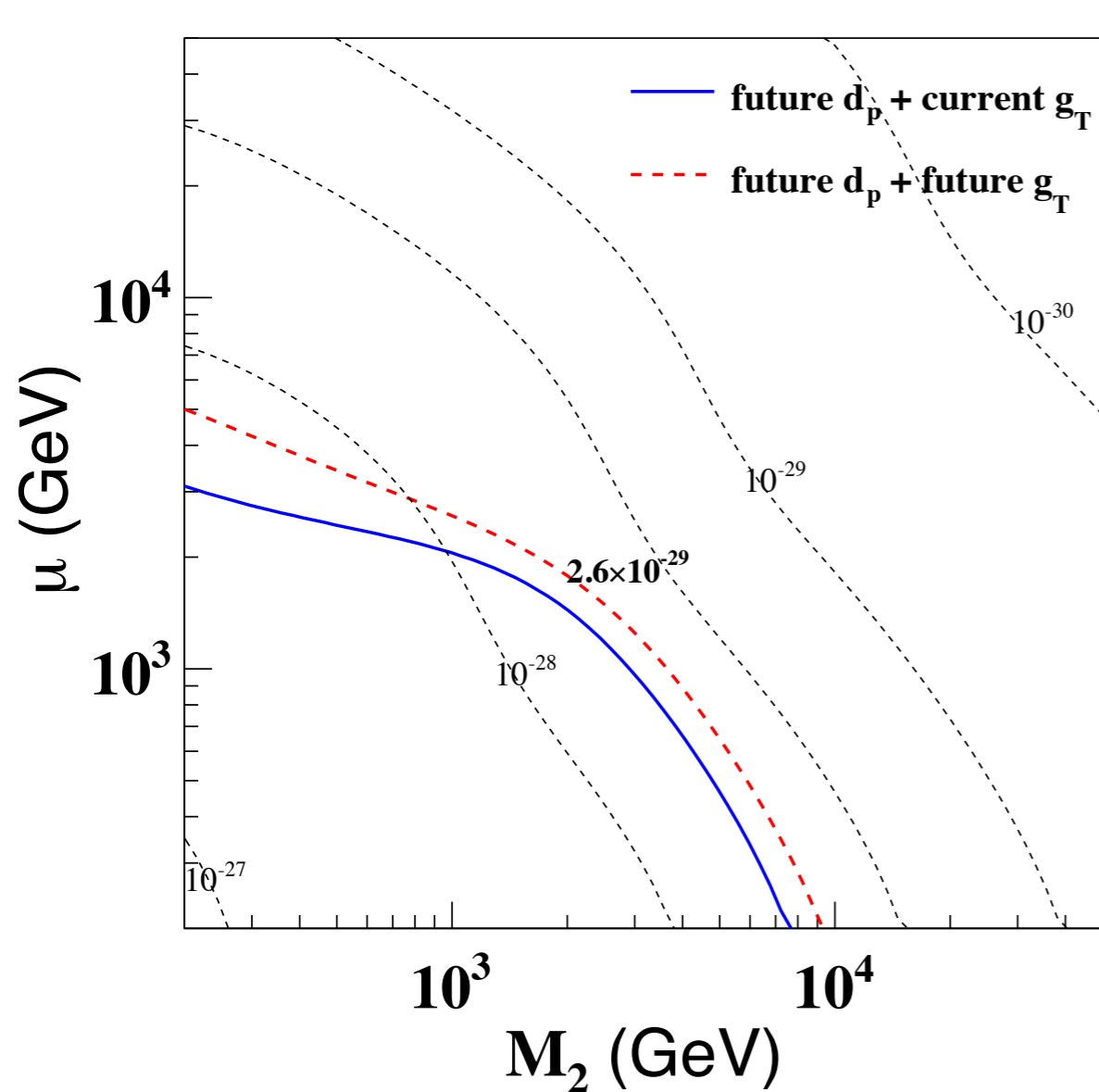


# Result: Collins Fragmentation Function



C. Zeng, H. Dong, TL, P. Sun, Y. Zhao, arXiv:2310.15532

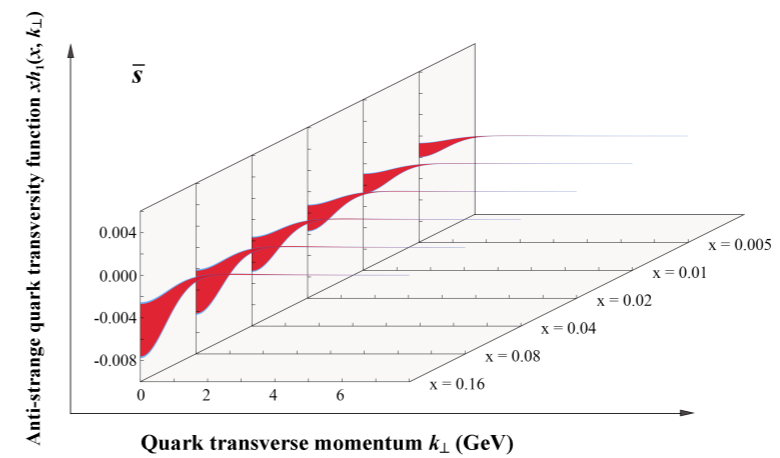
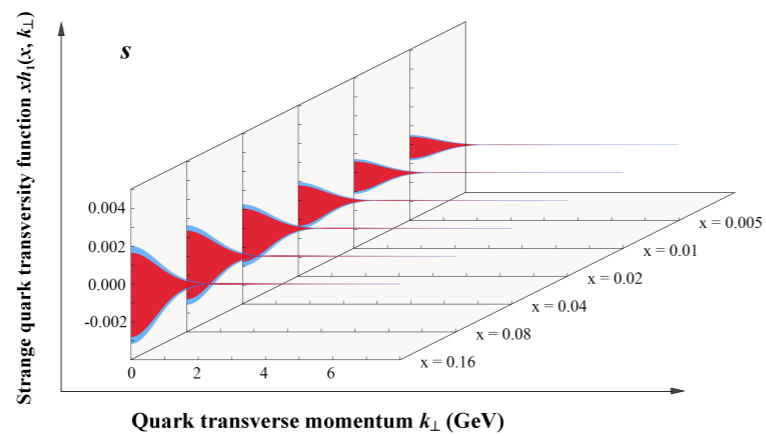
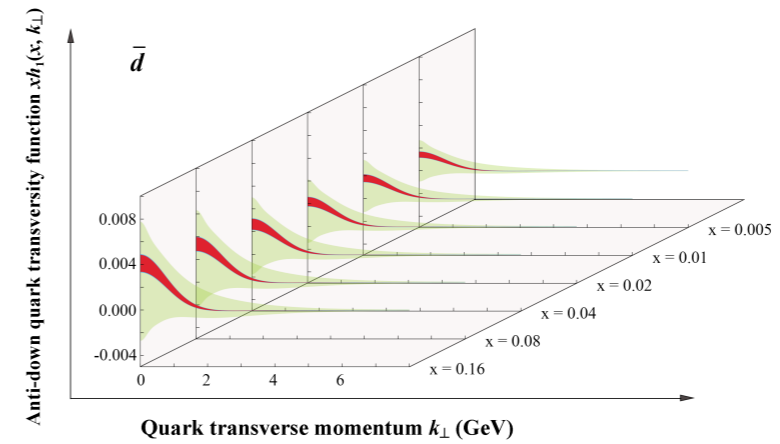
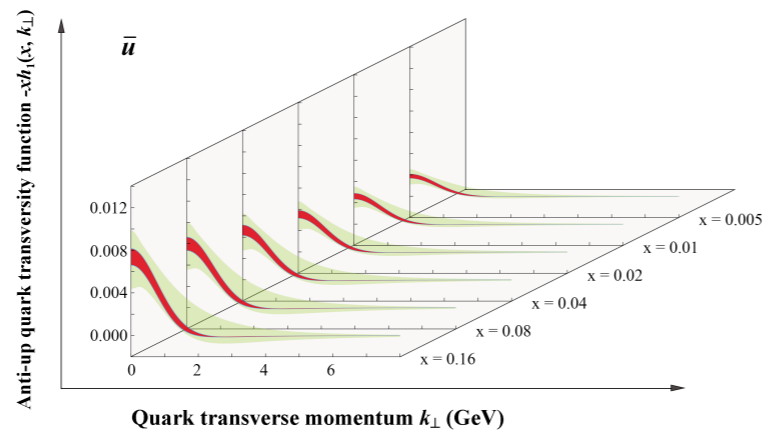
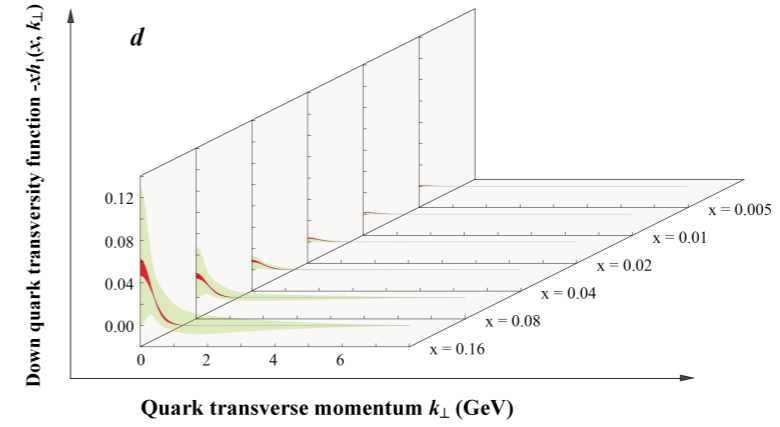
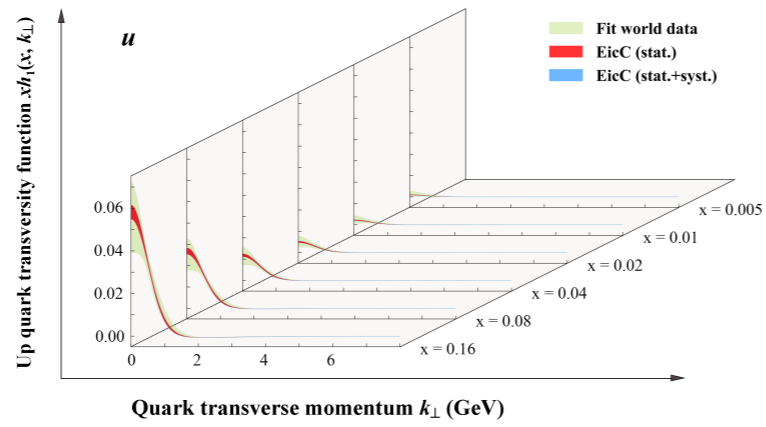
# Test New Physics Model: Split-supersymmetry



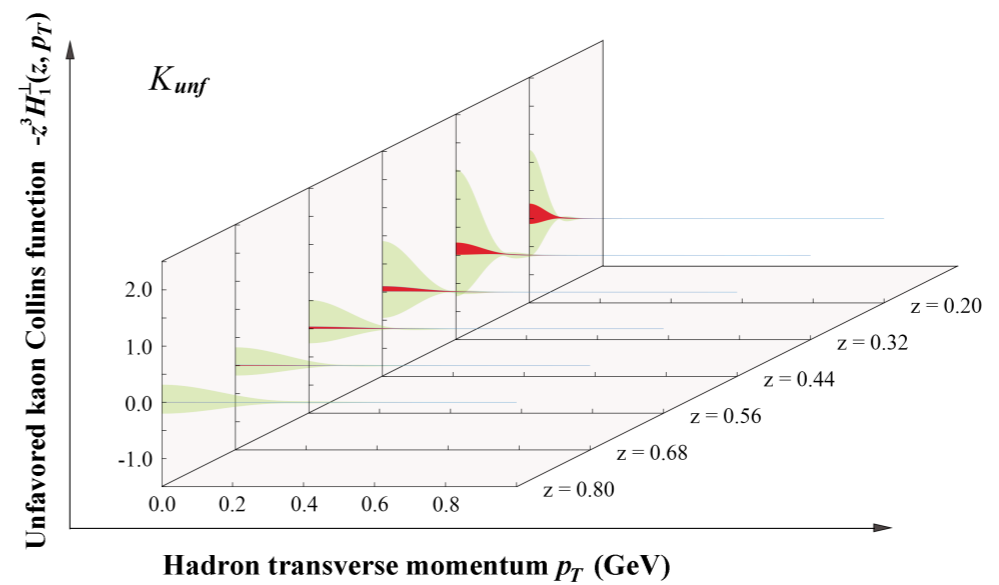
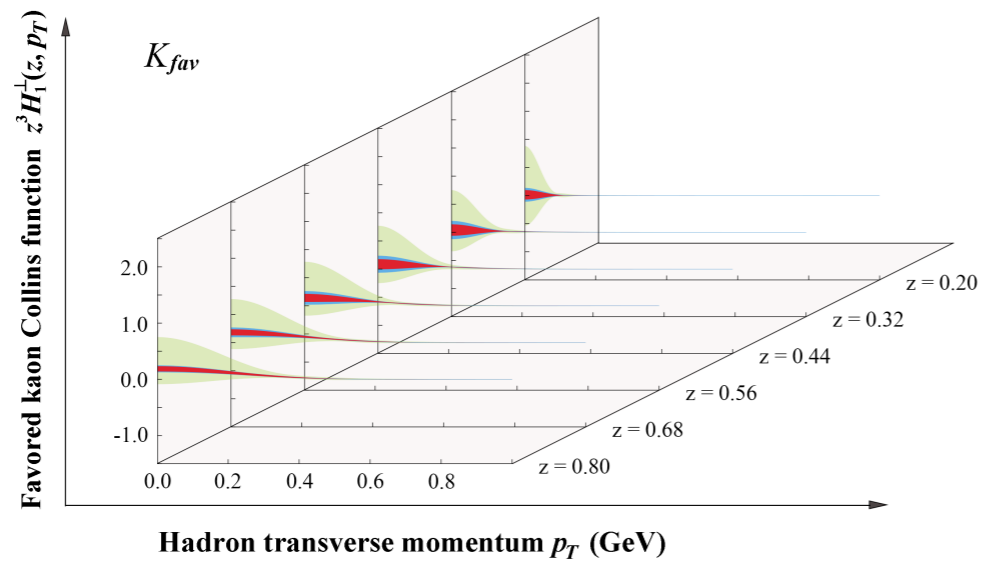
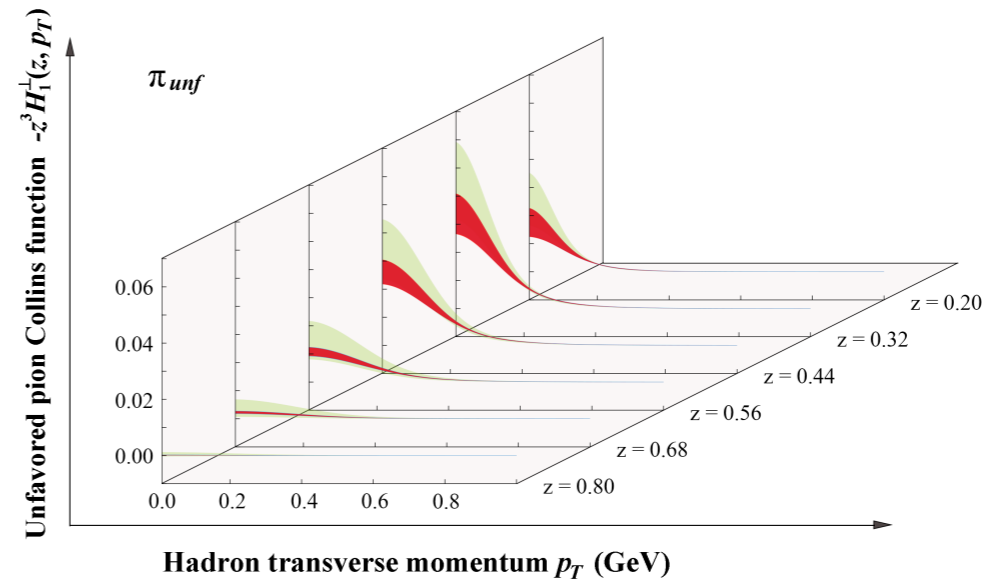
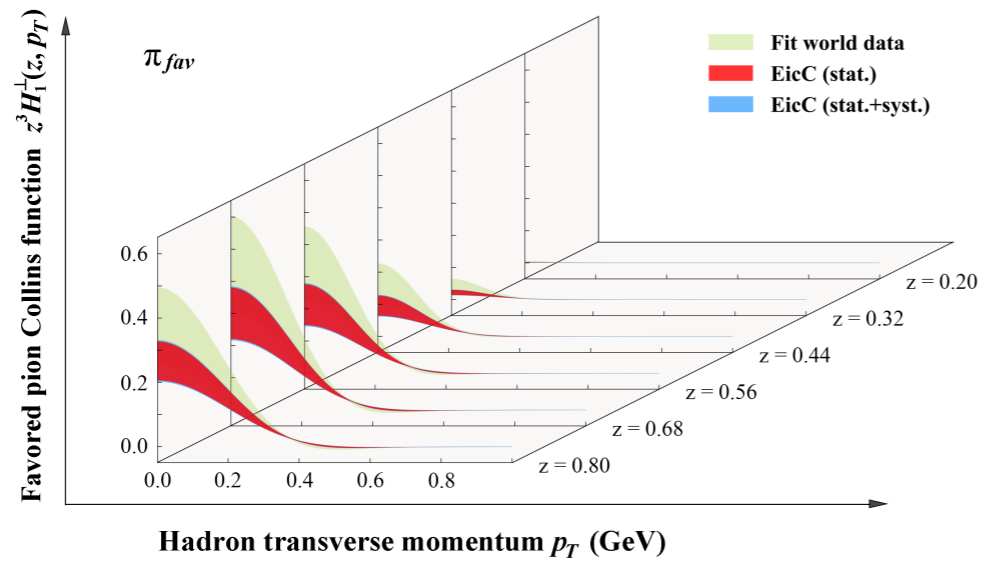
- In the unified framework of gaugino masses, sfermion mass at  $10^9$  GeV,  $\tan\beta=1$ ,  $\sin\varphi=1$

TL, Z. Zhao, H. Gao, Phys. Rev. D 97, 074018 (2018).

# Transversity TMDs



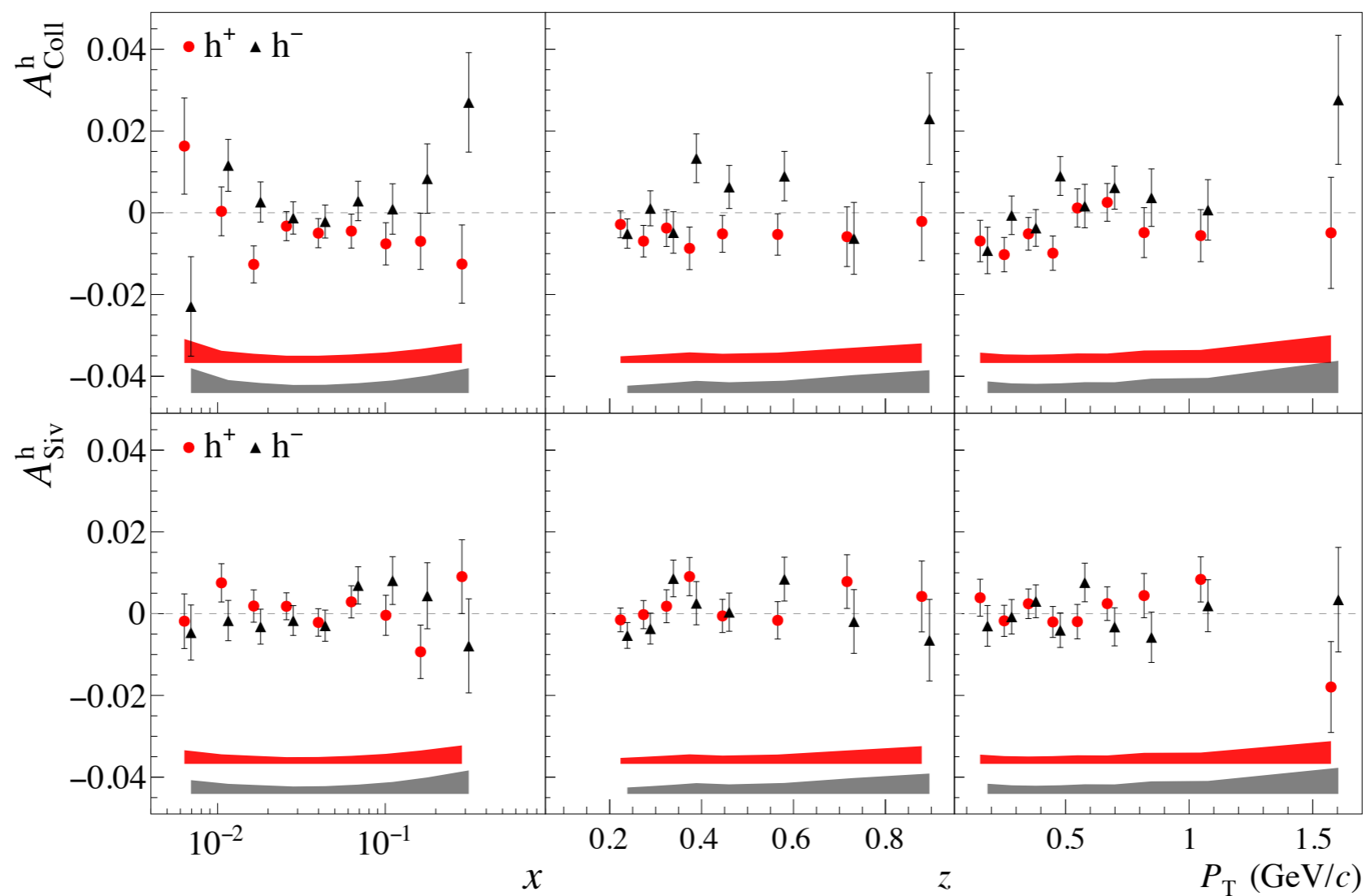
# Collins TMD FFs



# Some More on Transversity

New data released by COMPASS

SIDIS on transversely polarized deuteron target

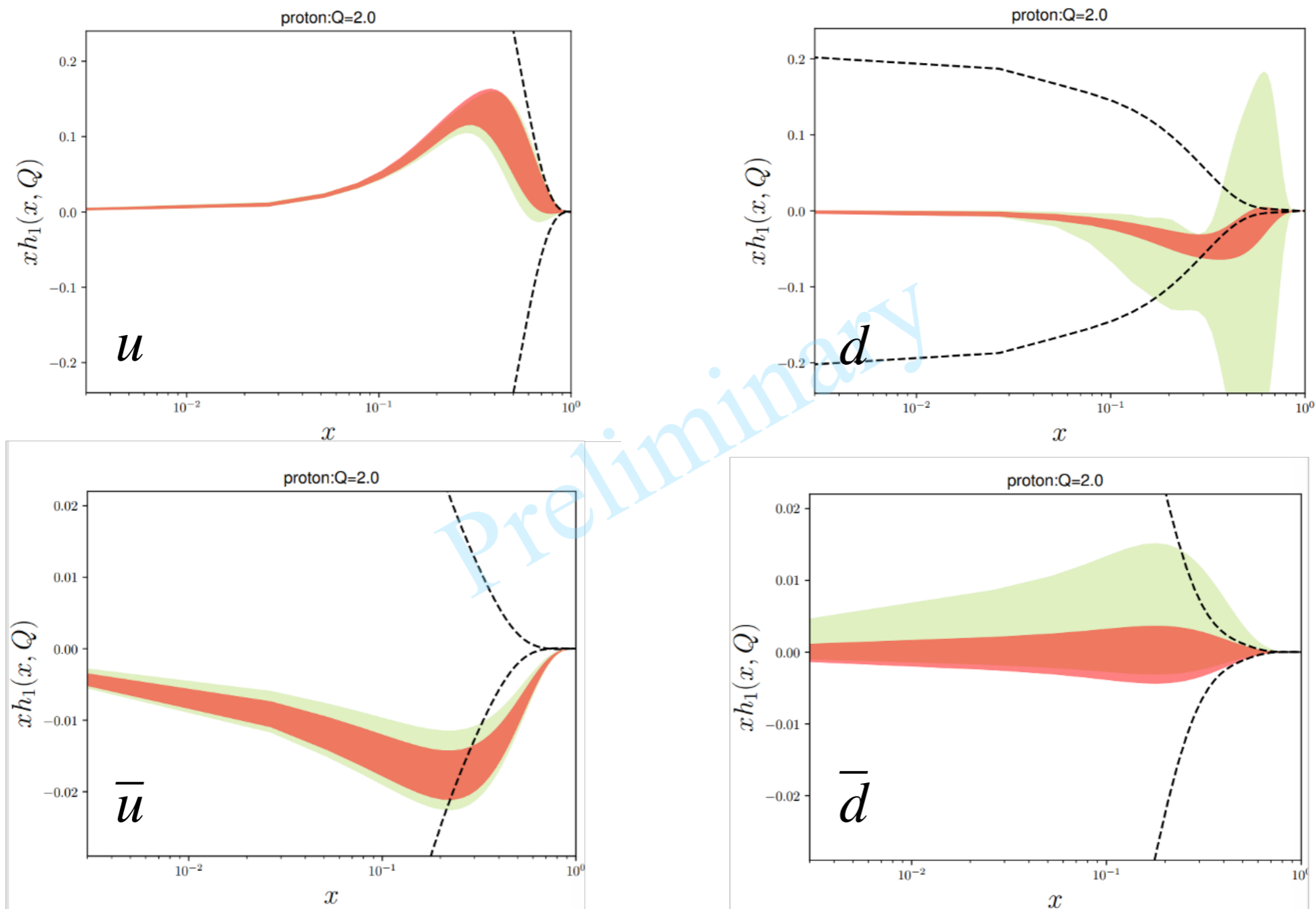


G.D. Alexeev *et al.*, COMPASS Collaboration, arXiv:2401.00309



# Some More on Transversity

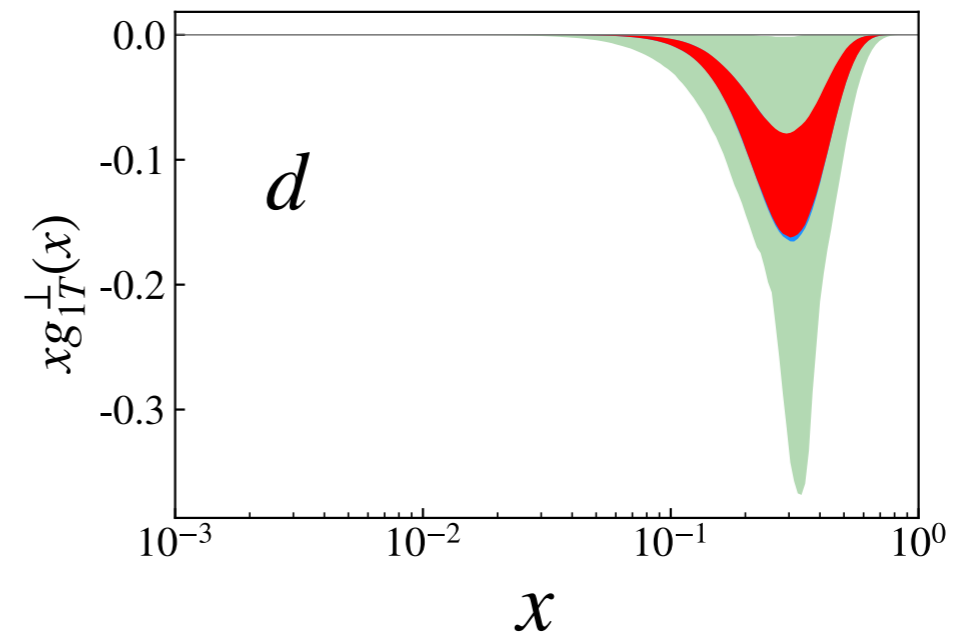
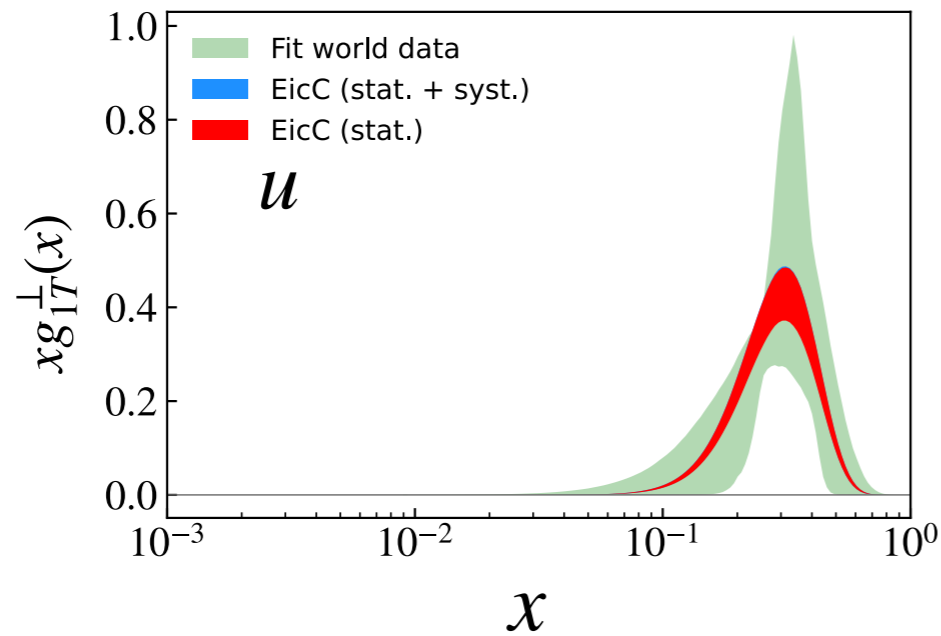
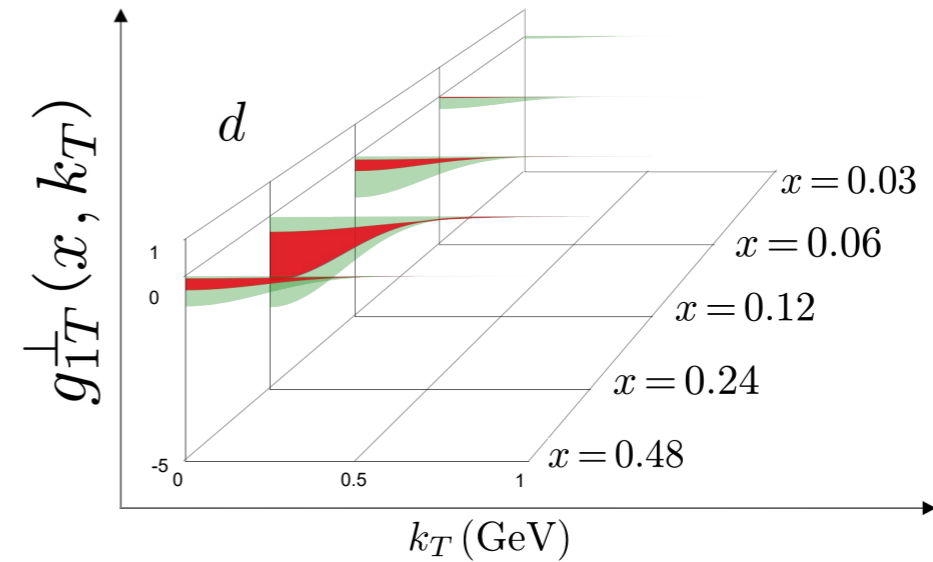
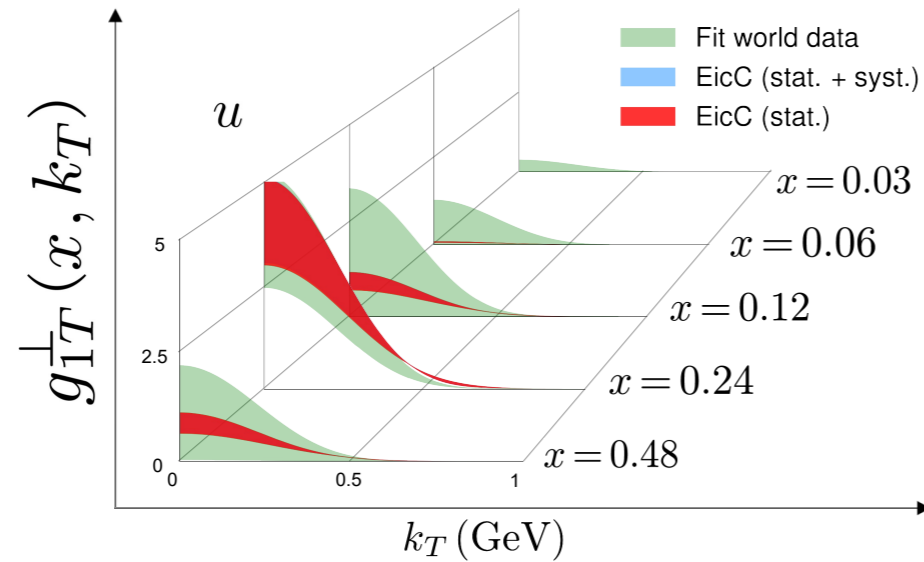
Preliminary results (without systematic uncertainties)



C. Zeng, H. Dong, TL, P. Sun, Y. Zhao

# Double Spin Asymmetry and Worm-gear

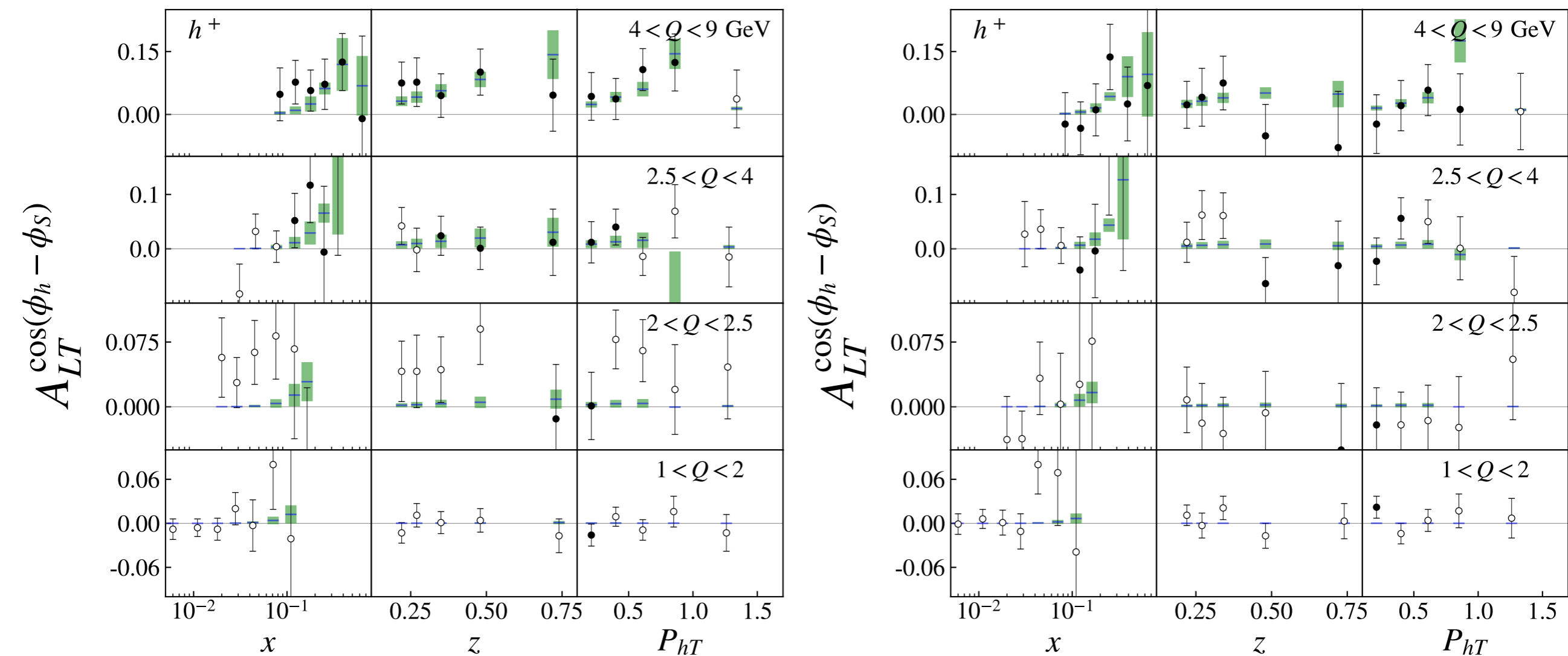
## Phenomenological extraction



$$g_{1T}^{\perp(1)}(x) = \int d^2\mathbf{k}_T \left( \frac{k_T^2}{2M} \right) g_{1T}^\perp(x, \mathbf{k}_T^2)$$

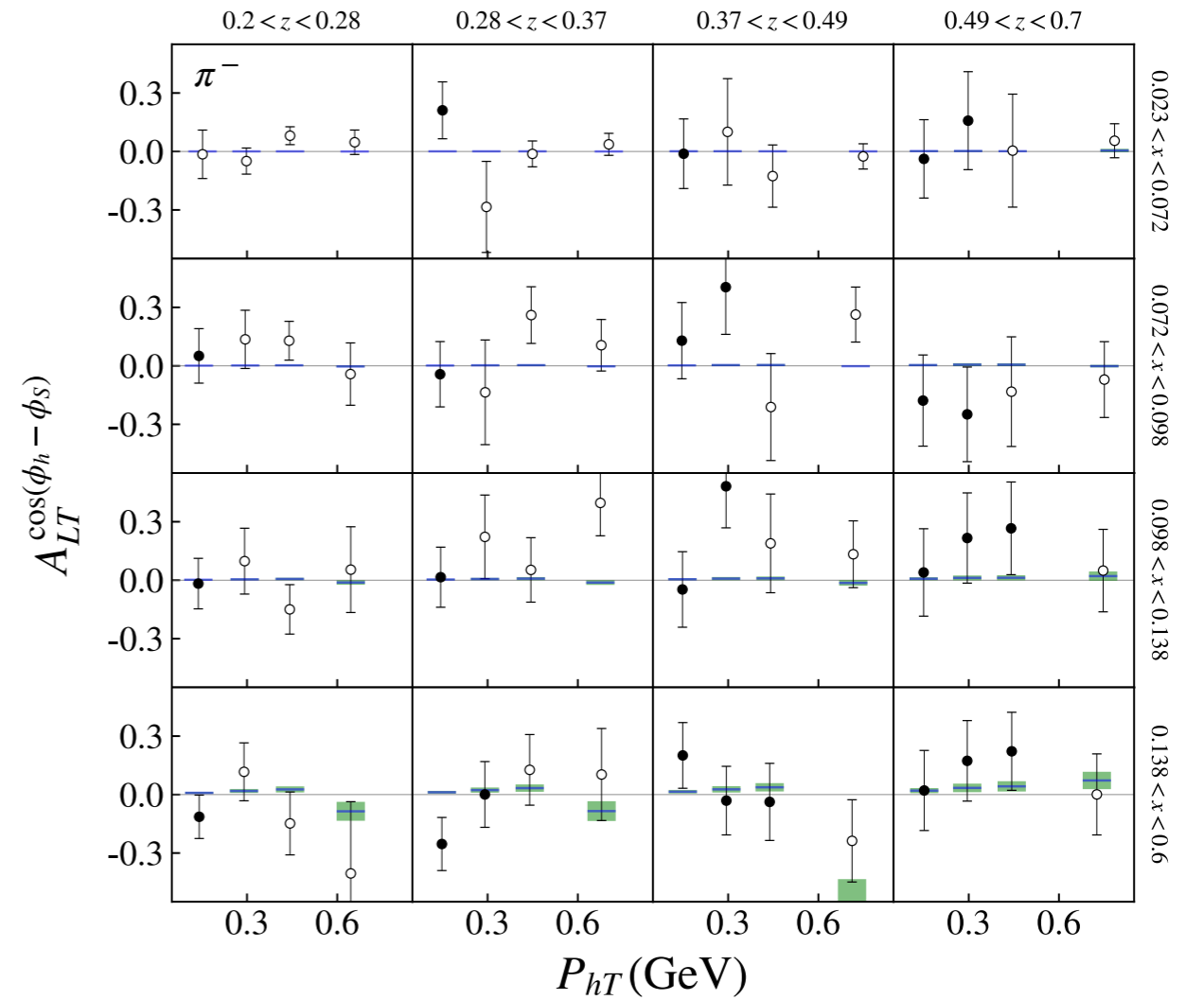
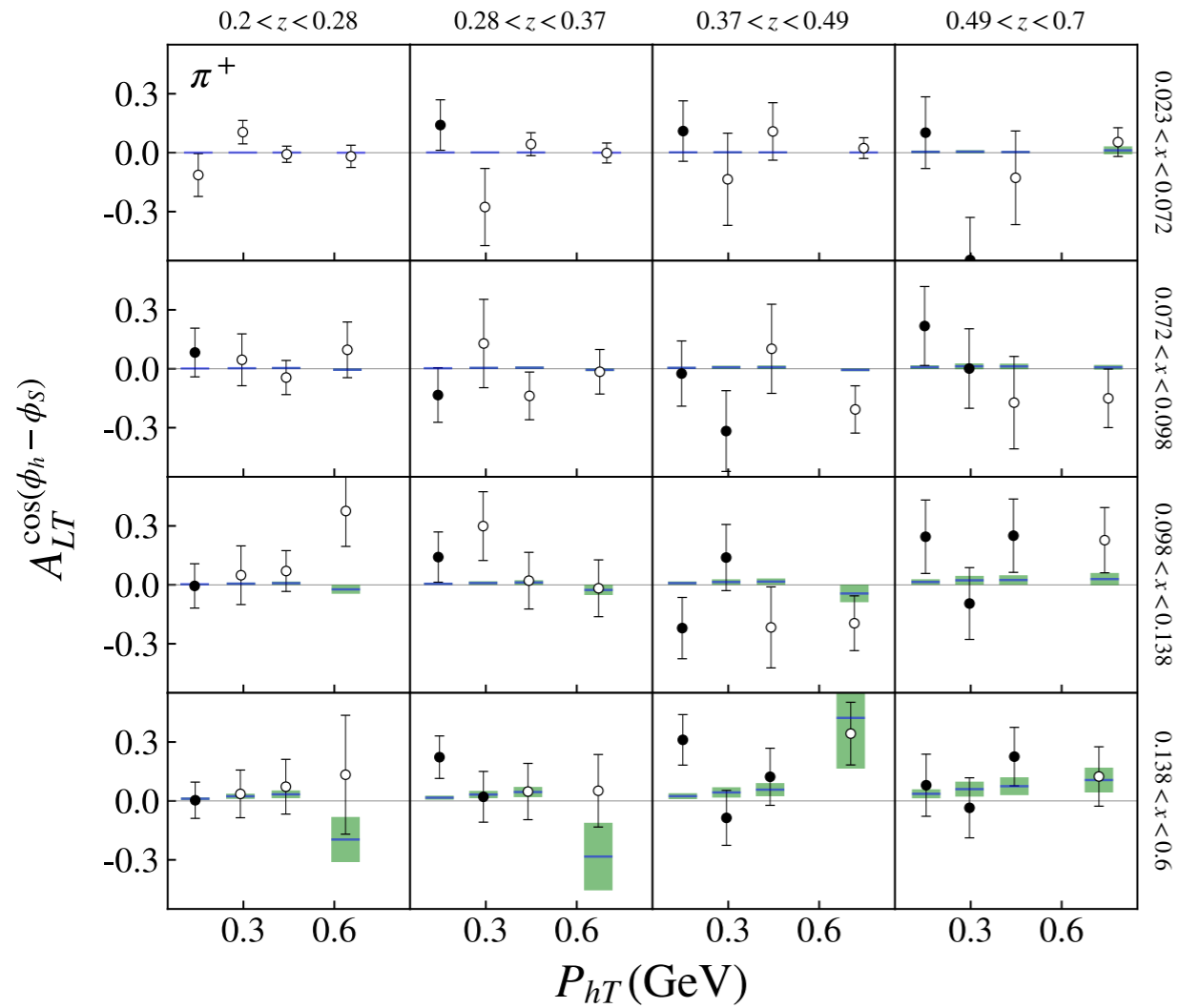
K. Yang, TL, P. Sun, Y. Zhao, B.-Q. Ma, arXiv:2403.12795

# Comparison with Data



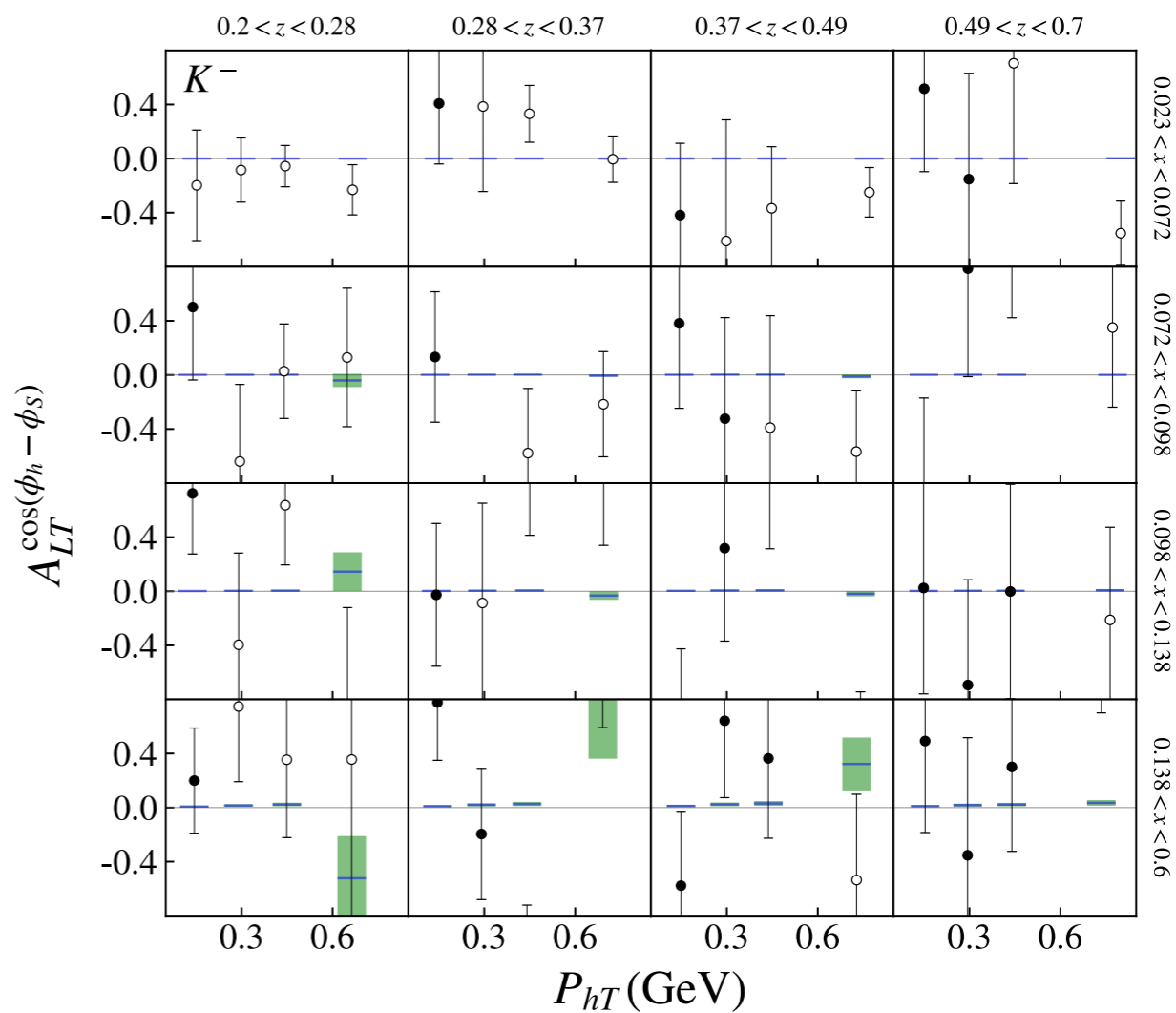
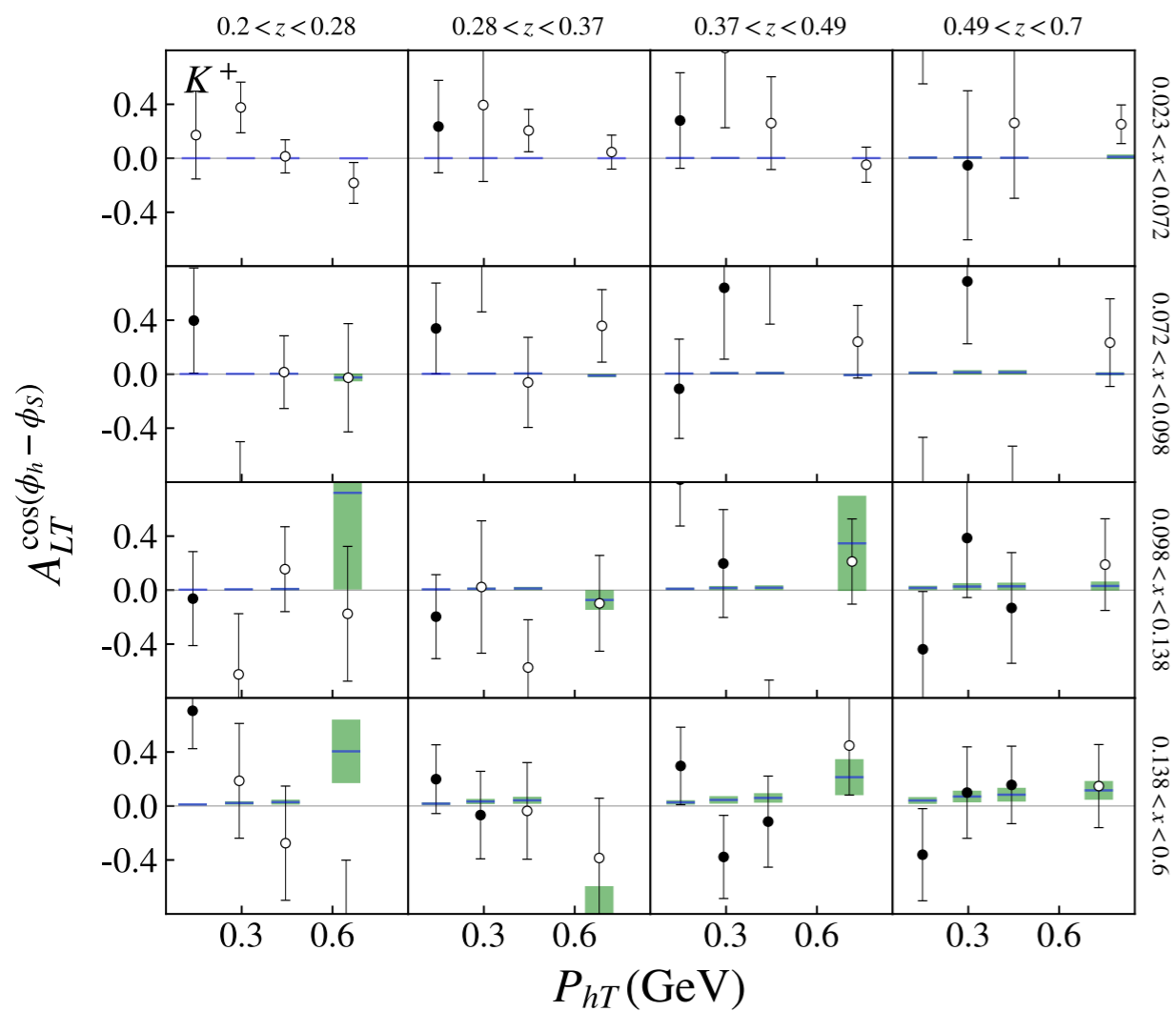
COMPASS Collaboration, Phys. Lett. B 770 (2017) 138.

# Comparison with Data



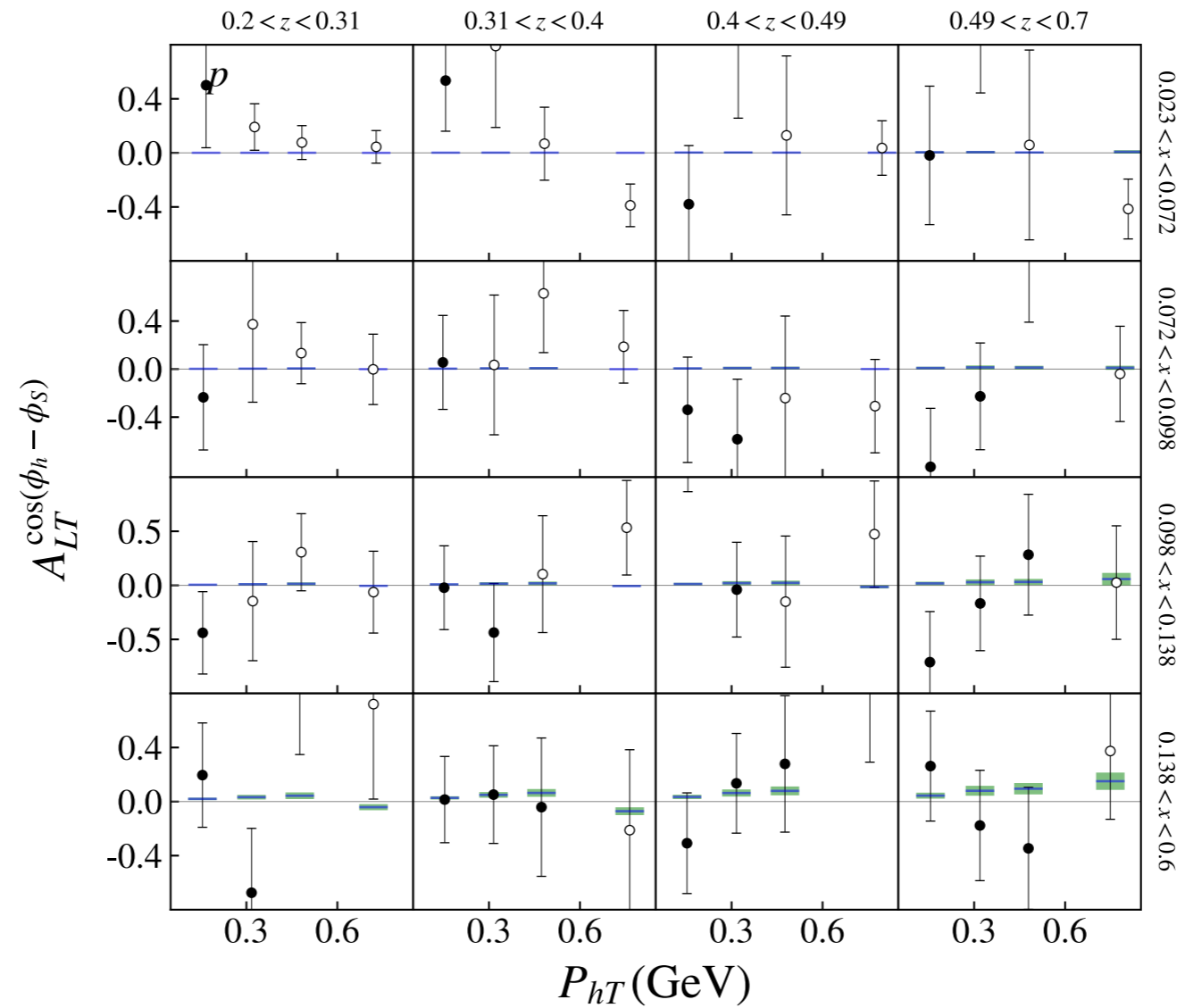
HERMES Collaboration, J. High Energy Phys. 12 (2020) 010. (re-analyzed)

# Comparison with Data



HERMES Collaboration, J. High Energy Phys. 12 (2020) 010. (re-analyzed)

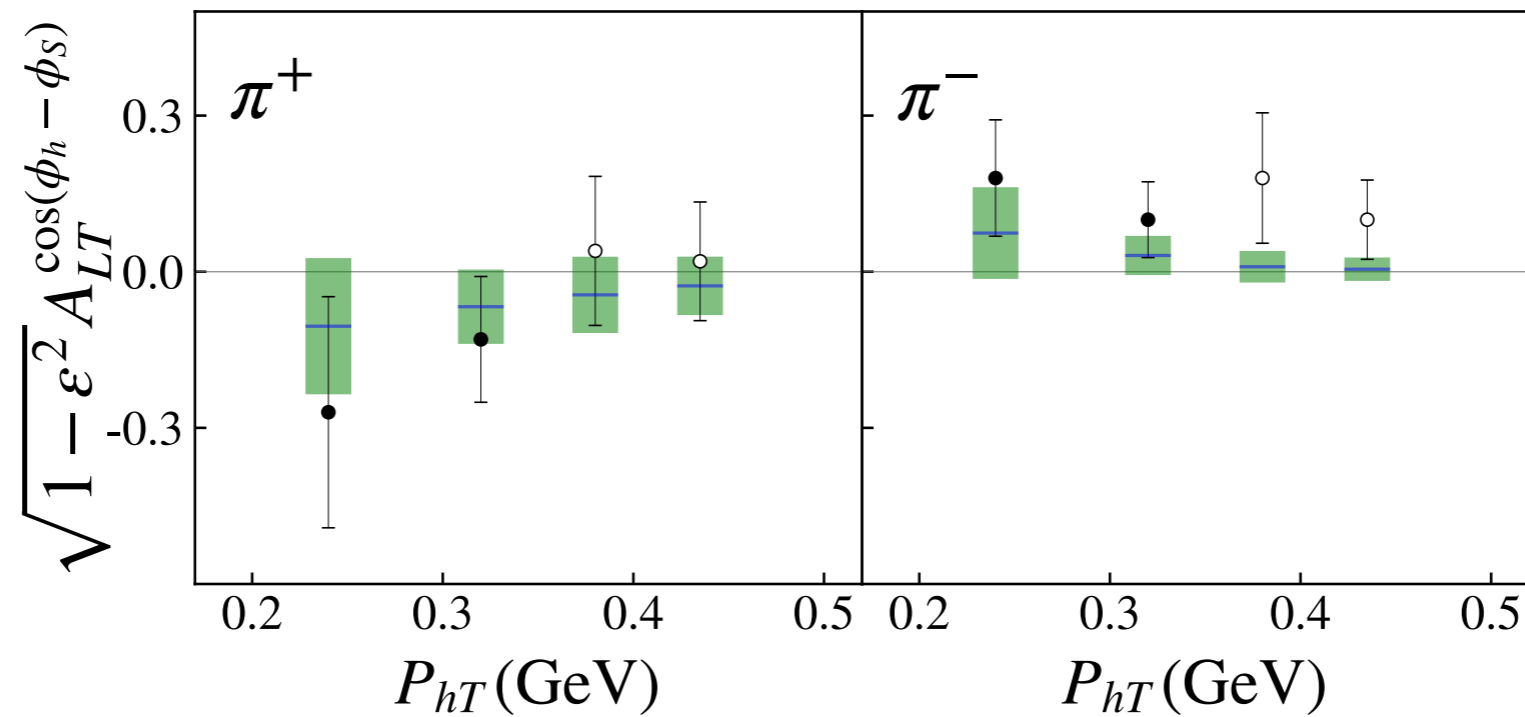
# Comparison with Data



HERMES Collaboration, J. High Energy Phys. 12 (2020) 010. (re-analyzed)



# Comparison with Data



JLab HallA Collaboration, Phys. Rev. Lett. 108 (2012) 052001.

# Connection to New Physics

Current upper limit on the neutron EDM (electric dipole moment)

$$d_n < 1.8 \times 10^{-26} e \text{ cm} \quad (90\% \text{ CL})$$

C. Abel *et al.*, Phys. Rev. Lett. 124, 081803 (2020)

Current upper limit on the proton EDM

$$d(^{199}\text{Hg}) < 7.4 \times 10^{-30} e \text{ cm} \quad (95\% \text{ CL})$$

B. Graner *et al.*, Phys. Rev. Lett. 116, 161601 (2016).

$$d_p < 2.1 \times 10^{-25} e \text{ cm}$$

B.K. Sahoo *et al.*, Phys. Rev. D 95, 012002 (2017).

Constraint on quark EDMs

$$d_p = g_T^u d_u + g_T^d d_d + g_T^s d_s \quad d_n = g_T^d d_u + g_T^u d_d + g_T^s d_s$$

$$d_u < 1.27 \times 10^{-24} e \text{ cm} \quad d_d < 1.17 \times 10^{-24} e \text{ cm}$$

sensitivity to new physics:  $d_q \sim e m_q / (4\pi\Lambda^2)$    $\Lambda \sim 1 \text{ TeV}$

TL, Z. Zhao, H. Gao, Phys. Rev. D 97, 074018 (2018).